



Final  
02-0233



**Using Inertial Measurements for the  
Reconstruction Of 6-DOF  
Entry, Descent, and Landing Trajectory and  
Attitude Profiles (AAS 02-164)**

*Geoffrey G. Wawrzyniak and Michael E. Lisano  
Jet Propulsion Laboratory, California Institute of Technology*

*Space Flight Mechanics Meeting  
San Antonio, Texas  
Tuesday, January 29, 2002*



# *Outline*



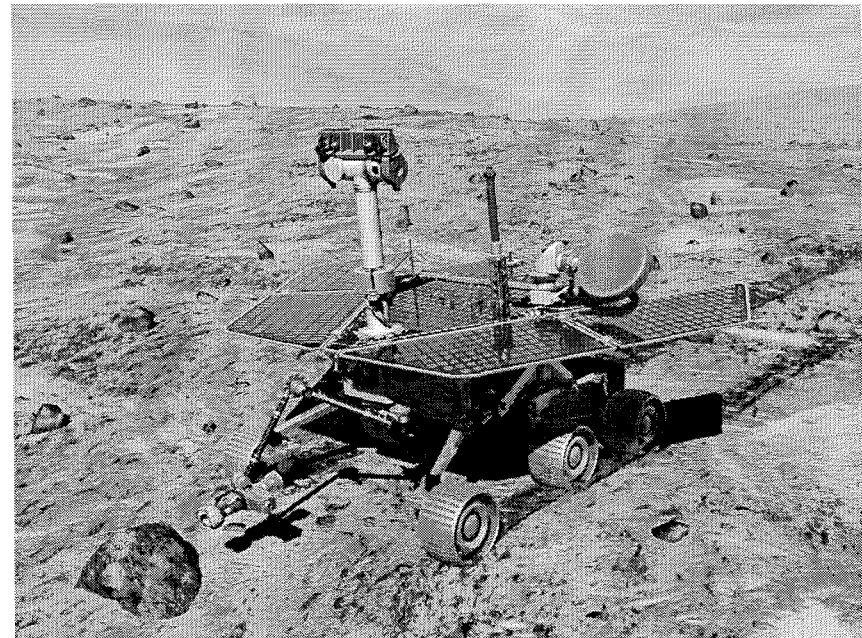
- **Introduction**
- **Motivation**
- **Mars Exploration Rover Entry, Descent, and Landing (MER EDL)**
- **Airbag Testing**
  - Objectives
  - Facilities
  - Equipment and Instrumentation
  - Video of Drop Test (facilities permitting)
- **Trajectory Reconstruction (REDLand)**
  - Objectives
  - Algorithm and Method
  - Results
- **Conclusions and Future Work**
- **Questions**



# Introduction



- **MER missions to Mars**
  - Two identical space vehicles and rovers
  - Doubles scientific return for minimal added effort
  - Launching summer of 2003
  - Arriving 21 days apart on Mars at different locations
- **Similar to Mars Pathfinder (not the same, though)**
  - Rover concept
  - Parachute -- retrorocket -- airbag EDL
- **Rovers expected to travel up to 1 km**
- **Determine history of climate and water in two areas that may once have been favorable for life**
- **Instruments will help give better understanding of Martian geology**
  - 360° panorama
  - Rock and soil samples
  - RAT (Rock Abrasion Tool) exposes fresh surfaces of rock





# *Motivation for Trajectory Reconstruction* **JPL**

- **Need to determine the “stroke” of the airbags at impact to within 10 cm ( $3\sigma$ ) from airbag drop tests**
  - Airbag physics is a black art
  - Stroke is the amount of airbag compression
  - No direct measurement exists for measuring stroke
  - Bottoming out, or “full stroke” is caused by inadequate pressure in the airbags
  - Too high of a pressure, and the airbags could pop on impact
- **Need to reconstruct EDL trajectory of 1st MER within seven days of its arrival**
  - 2nd MER will arrive 21 days later
- **REDLand (Reconstruction of Entry, Descent, and Landing) software developed by authors to accomplish first objective**
- **REDLand is prototype for IPANEMA (Interim Planetary Atmosphere Navigation for Estimation and Mission Analysis)**
- **IPANEMA, also written by the authors, will be used to reconstruct the EDL of the MER mission**



# MER-A EDL Sequence



## MER-A Sequence

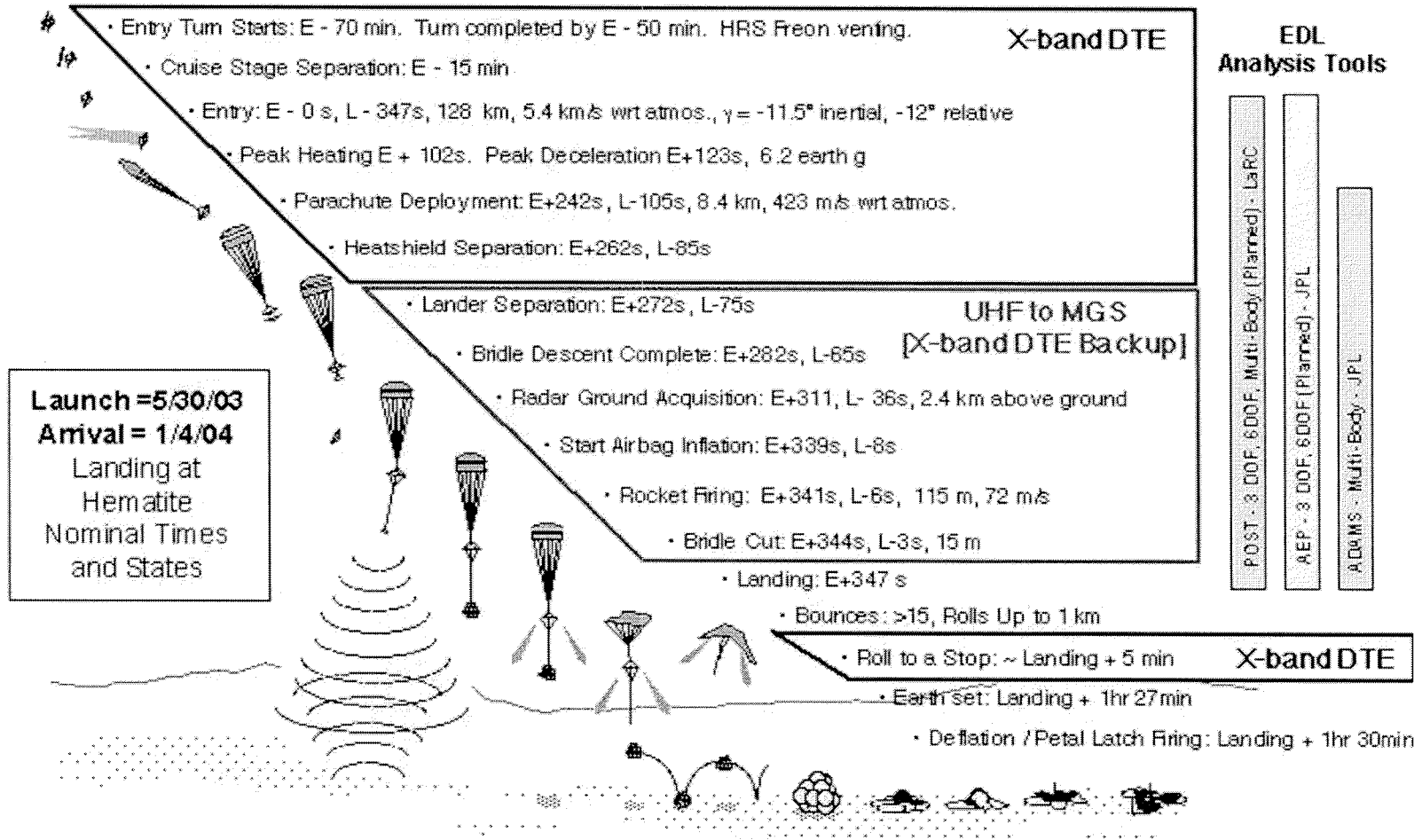


Illustration courtesy of Phil Knocke, JPL



# MER-B EDL Sequence



## MER-B Sequence

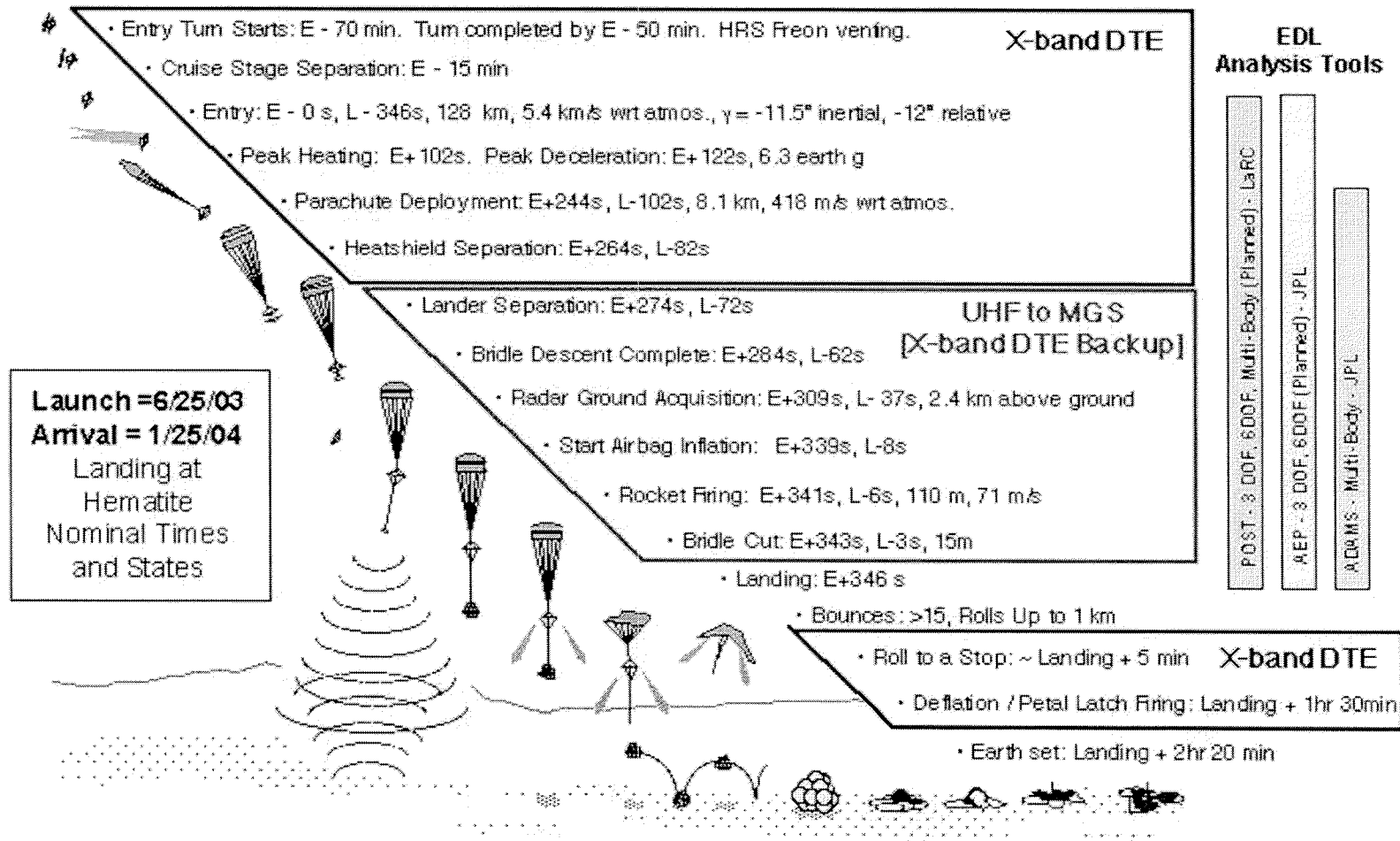


Illustration courtesy of Phil Knocke, JPL



# *Airbag Drop Test Objectives*



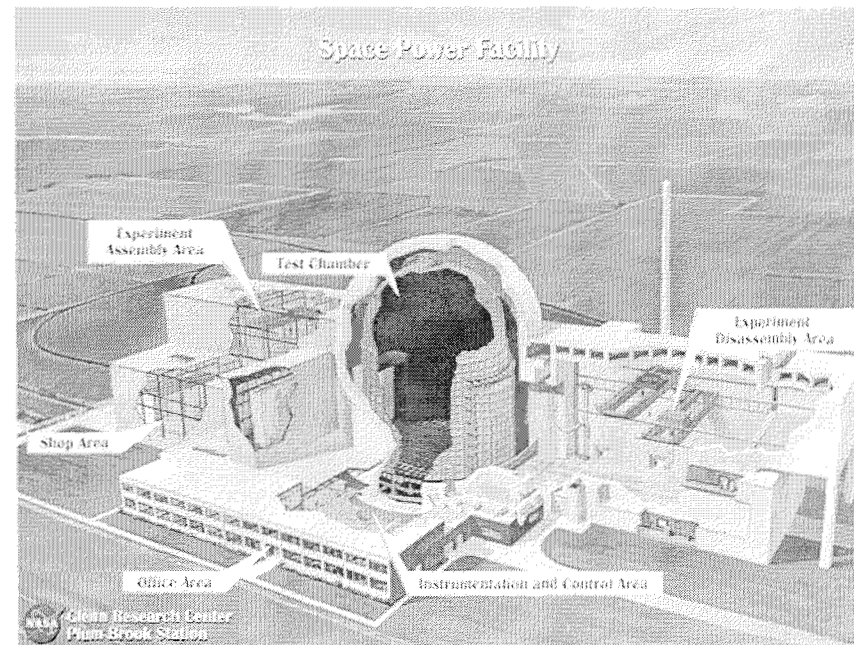
- **Evaluate the performance of MPF heritage airbag design under the higher landing mass conditions**
  - MPF mass was 385 kg
  - MER drop test mass is 535 kg
- **Evaluate the relative performance between abrasion layers constructed from 100 denier and 200 denier fabrics**
  - Denier is a thread count (or fabric thickness)
  - Trade-off is between number of layers and denier of airbag
- **Evaluate the MER petal to airbag interface**
- **Measure tendon loads, acceleration and stroke**



# Airbag Drop Test Facilities



- Drop tests are conducted at the Space Power Facility (SPF) at NASA Glenn Research Center, Plum Brook Station, Sandusky, Ohio
- Only place in the world that can simulate Martian landing environment and conduct drop tests of scale models
  - Largest vacuum chamber on Earth
- Chamber is 100 feet in diameter, 122 feet high
- Center of the chamber is a ramp with a rock field to simulate the Martian surface



*From "World Class Facilities CD-ROM", NASA Glenn Research Center at Lewis Field Productions, Cleveland, OH, 2000*

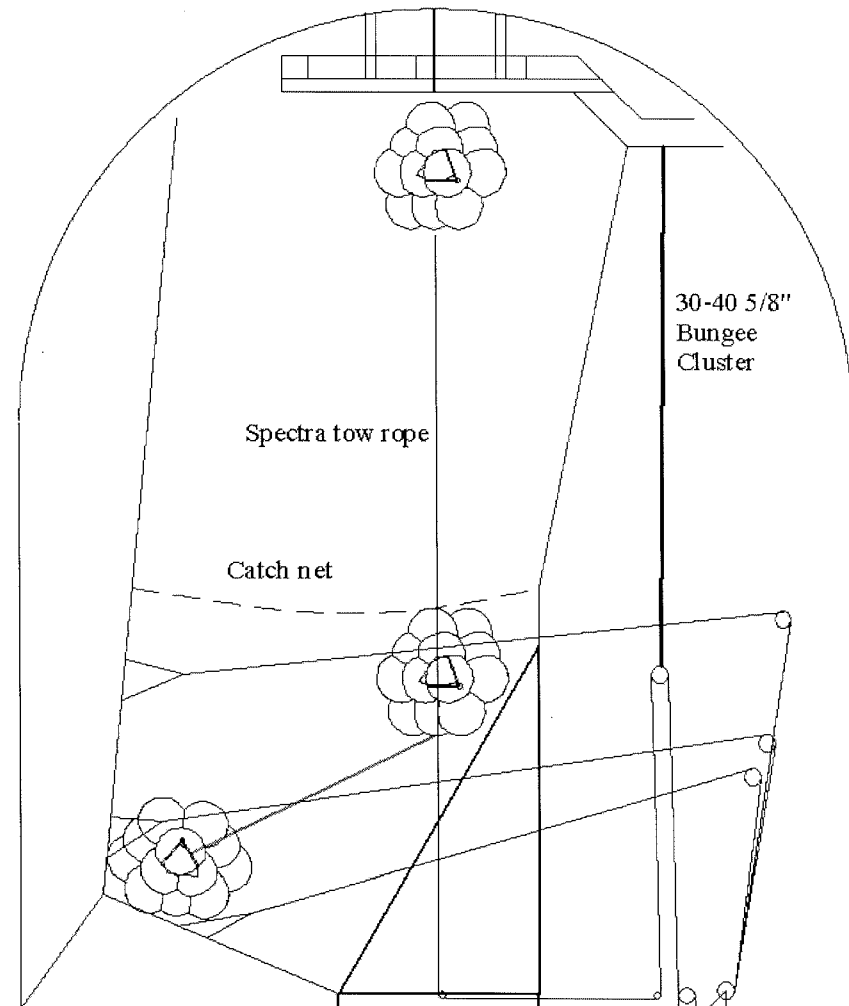




# Airbag Drop Test Facilities



- At right is a figure of the drop test chamber
  - Z-axis is up
  - Y-axis is right
  - X-axis is out of page
- Pyro is fired to release lander from the hanging sling
- Bungee accelerates lander towards the 60° ramp
  - Simulate Mars EDL horizontal velocity component from the wind
- Airbags encounter the ramp and compress
- Airbags and lander bounce off the ramp into catch net
- Entire sequence from release to net takes less than 2 seconds
- Drop captured by numerous cameras situated around the chamber



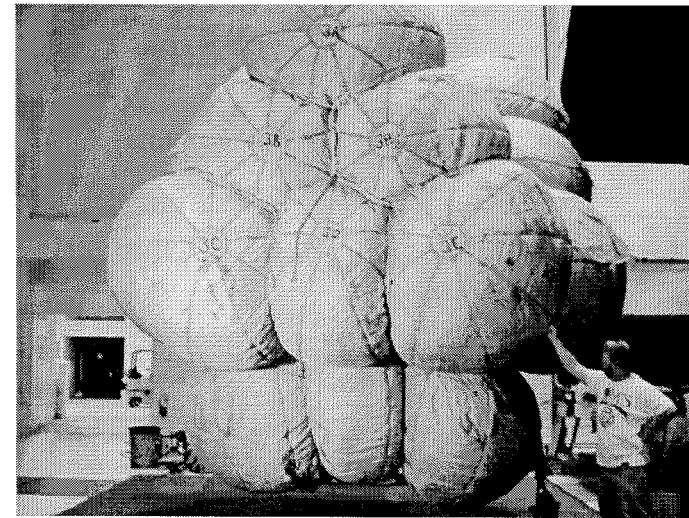
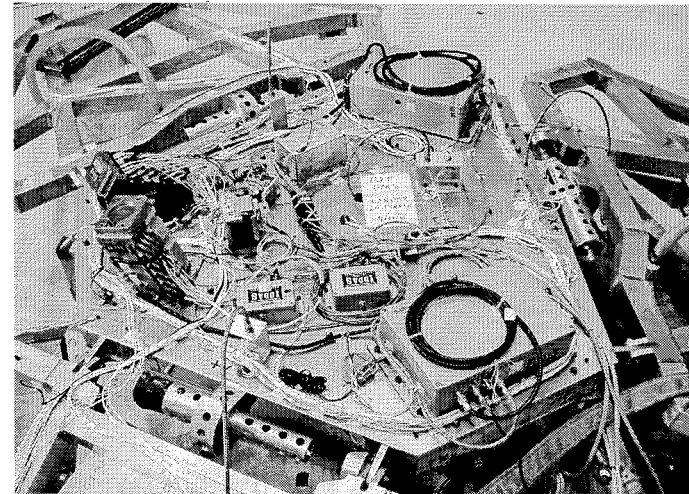
*Drawing courtesy of Tom Rivellini, JPL*



# Equipment and Instrumentation



- Drop test lander is similar in size, shape and mass of flight lander
- Base petal of test lander holds instrument panel
  - IDDAS (Intelligent Dummy Data Acquisition System)
  - Accelerometers
  - Rate gyroscopes
  - Pressure transducers
  - Tendon load cells
  - Latch pin load cells
  - String potentiometers
  - Orientation Sensor
- Ballast mass added to side petals
- Lander is approximately 1 meter tall
- Inflated airbags on lander are 4 meters tall



*Photos courtesy of ILC Dover, Inc.*



*(movie)*

**JPL**

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QuickTime™ and a  
Sorenson Video decompressor  
are needed to see this picture.



# *REDLand Trajectory Reconstruction*



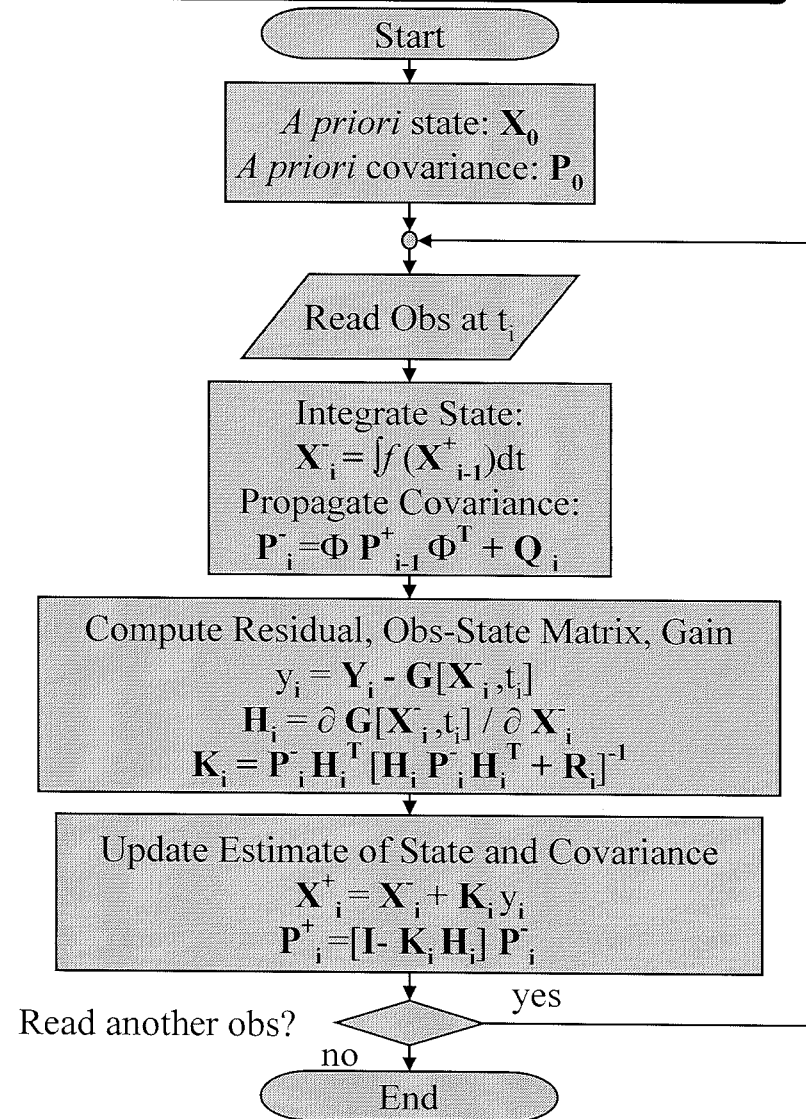
- **Objectives**
  - Determine acceleration environment of lander
  - Indirectly determine airbag stroke
  - Learn how to model IMU measurements for MER EDL using IPANEMA (Interim Planetary Atmosphere Navigation for Estimation and Mission Analysis)
- **REDLand uses IMU data as measurements in EKF**
  - Traditional route of dead reckoning integrates IMU data
- **REDLand estimates (of the CG and as functions of time):**
  - Position (SPF reference frame)
  - Velocity (SPF reference frame)
  - Translational Acceleration (Body frame)
  - Quaternion (SPF to Body)
  - Rotational Rate (Body frame)
  - Rotational Acceleration (Body frame)
- **Quaternion relates SPF and Body reference frames**
- **The rotation to the Mars frame from the SPF frame is a  $-60^\circ$  about the SPF X-axis**



# Extended Kalman Filter



- The trajectory and attitude reconstruction will be performed using an Extended Kalman Filter (EKF)
- At right is a flowchart of a typical EKF
- *A priori* values are from the initial conditions
- $\Phi$  is the state transition matrix
- $Q$  is the process noise matrix
- $Y$  is the observed measurement,  $G$  is the modeled measurement. Their difference is the residual,  $y$
- $H$  is the state-observation matrix
- $R$  is the measurement noise matrix
- $K$  is the gain
- The next slides discuss each of these elements of an EKF in more depth





## Measurement Types (*Y* in EKF)



- **Accelerations from a number of three-axis accelerometers positioned in the lander**
  - Current  $1\sigma$  noise assumption is 0.1 g
  - DC offsets are averaged and removed
  - 1 g is added to unbiased accelerometer tri-axis
    - This will lead to a propagated error if initial orientation is miscalculated
  - **Modeled kinematics (G in EKF) of acceleration at a point “a” relative to a reference point “o” is:**
$$a_a = a_o + \omega \times \omega \times r_{a/o} + \alpha \times r_{a/o}$$
  - **Small error may arrive from  $\Delta r_{a/o}$  uncertainty (most apparent during max rotation rate and acceleration)**
    - $\text{Max}(\omega) \sim 12 \text{ r/s}$ ,  $\text{Max}(\alpha) \sim 140 \text{ r/s}^2$ , Set  $a_o = 0$
    - $a_a(r_{a/o} = 50\text{cm}) = 142 \text{ m/s}^2$ ,  $a_a(r_{a/o} = 51\text{cm}) = 144.84 \text{ m/s}^2$
    - Difference of 0.3 g
  - **Small errors may also arrive from orientation of accelerometers wrt lander axes**
    - $20\text{g} * \sin(1^\circ) = 0.35 \text{ g}$
- **Rotational rates from a three-axis gyroscope in the lander**
  - Current  $1\sigma$  noise assumption is 0.4 mV
  - 1 mV  $\sim$  1 deg/sec



## *Process Noise Matrix (Q) Assumptions*



- The propagated covariance matrix is:

$$P_i^- = \Phi P_{i-1}^+ \Phi^T + Q_i$$

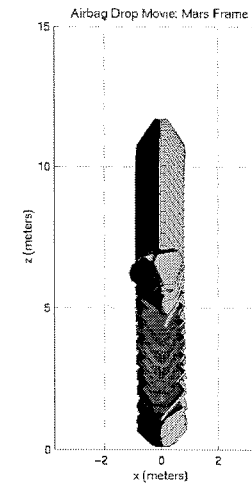
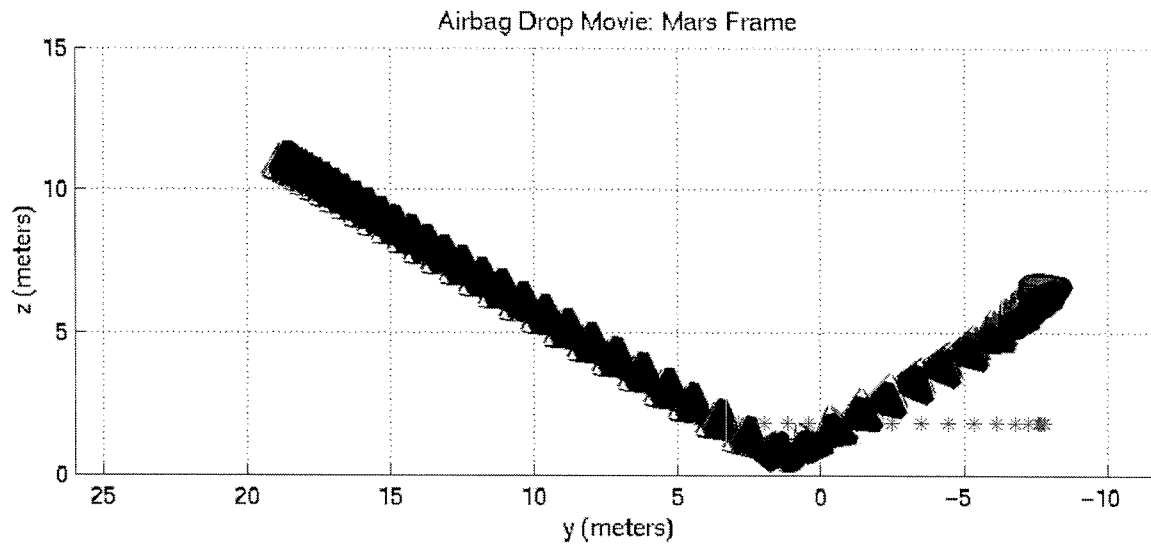
- Q is a diagonal matrix that can be thought of as a lower bound on the propagated covariance matrix
- Non-zero Q prevents the estimator from converging
- Tuning of an EKF is the black art of balancing the uncertainty of the dynamics model and the uncertainty of the measurements, or Q/R
- Q should only be applied to states where and when there are dynamics uncertainties
  - Release and impact
  - Velocities predicted using a constant value for g
  - Translation and rotation accelerations
  - Rotation rates
- The measurement update to the covariance matrix,

$$P_i^+ = [I - K_i H_i] P_i^-$$

will correct for the added process noise (Q)



# Results: Mars view animation frames

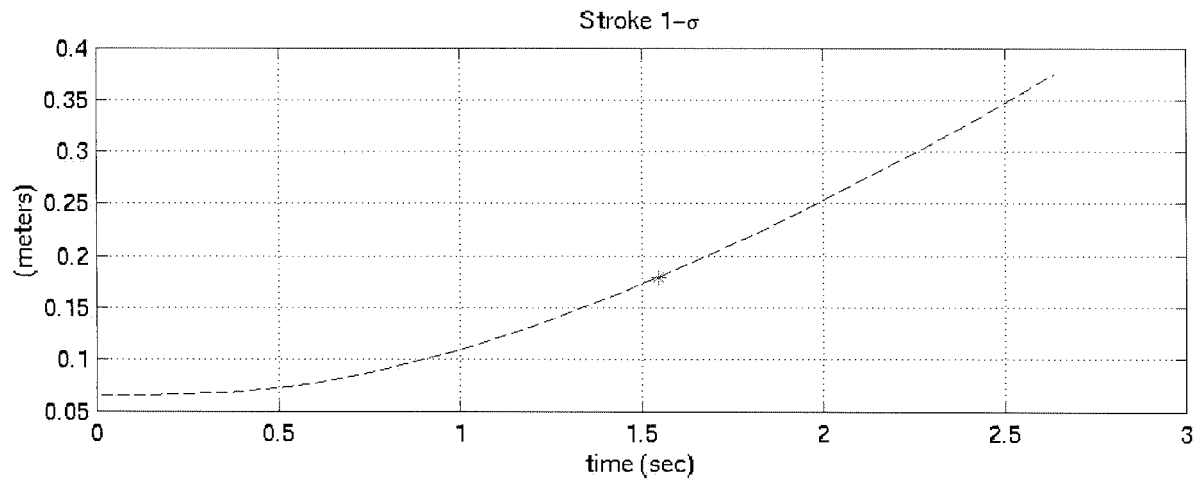
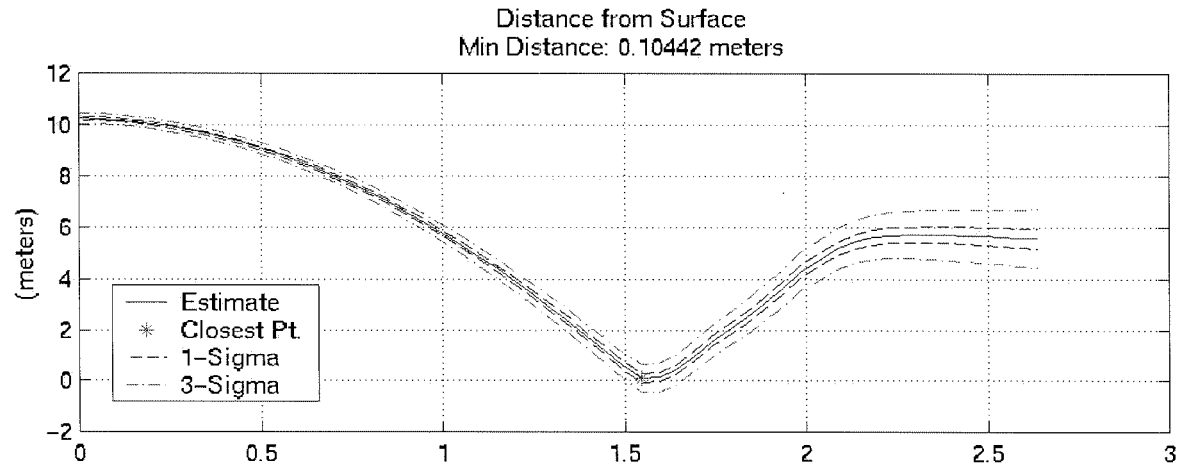


\* Roll Line. This movie was played at 20 frames per second.



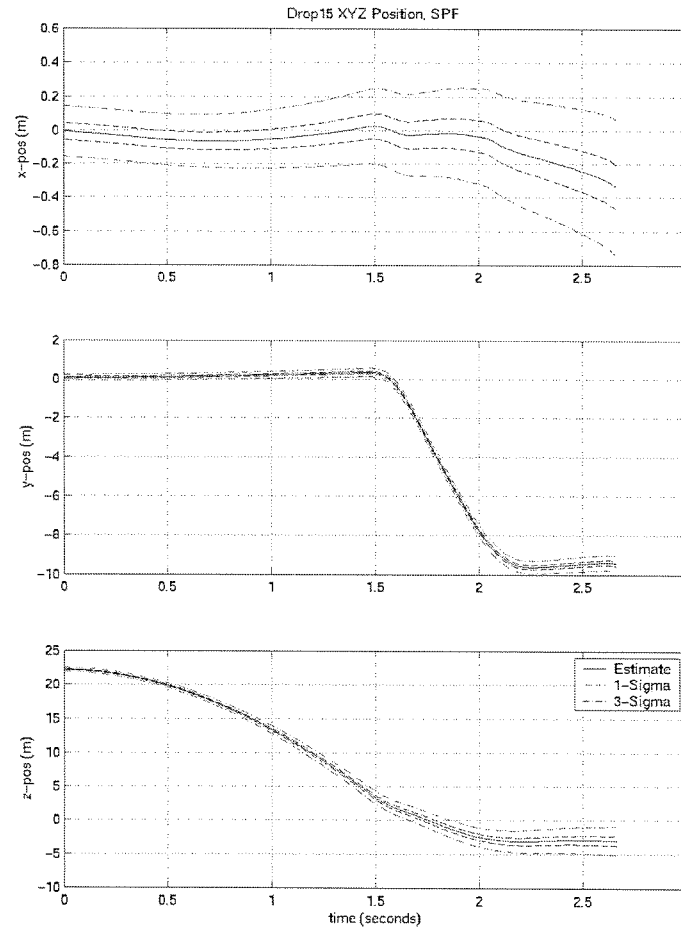


# Stroke Estimate





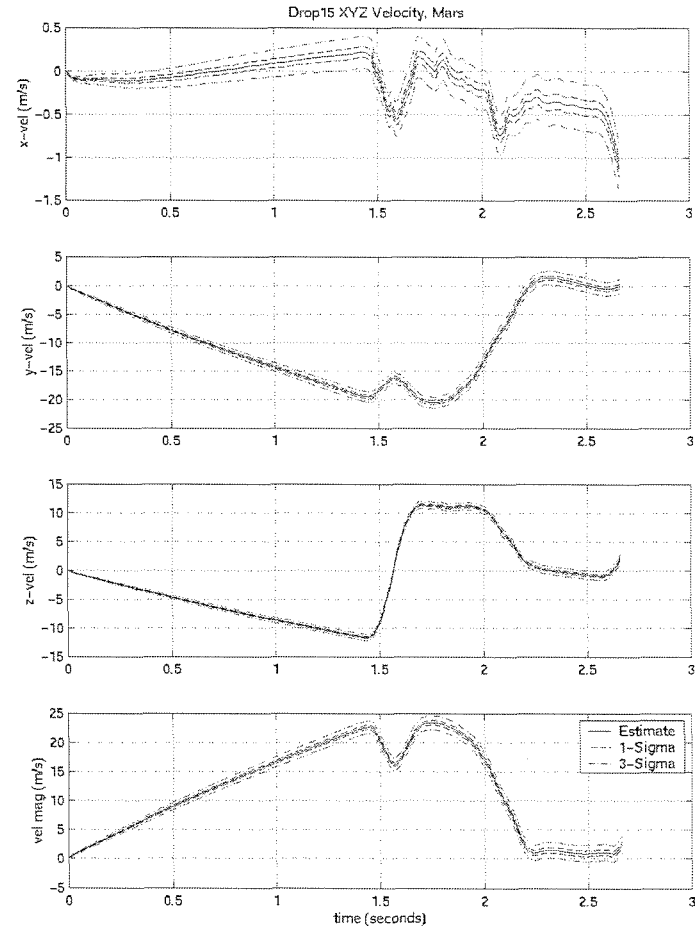
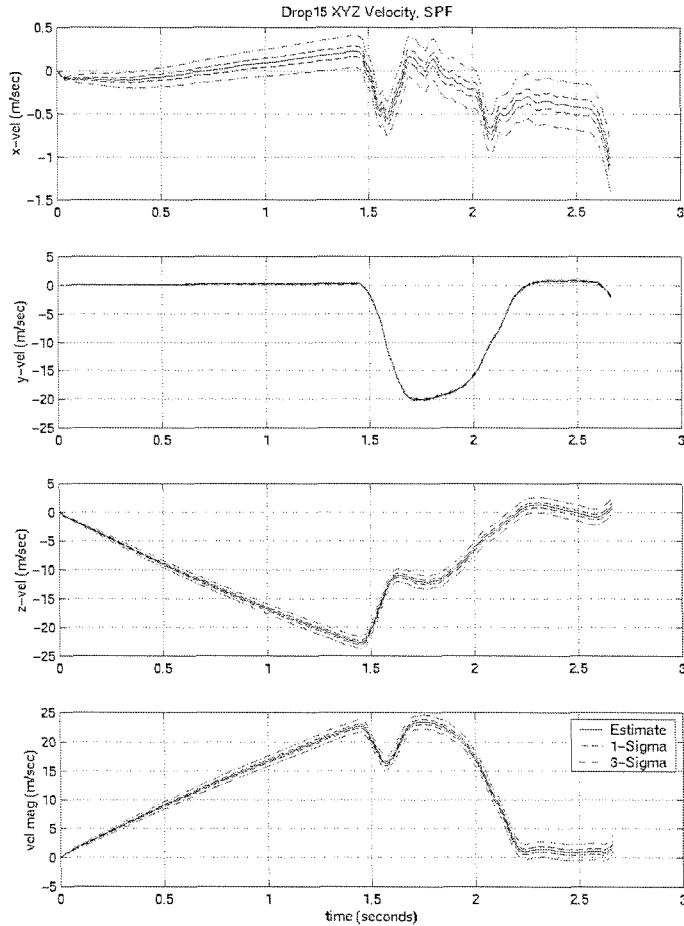
# Results: Position (SPF frame)



XYZ Positions in the SPF frame



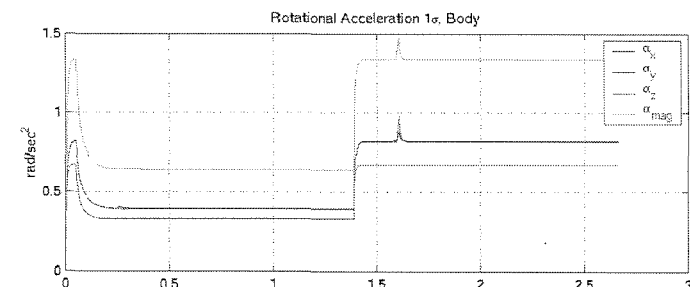
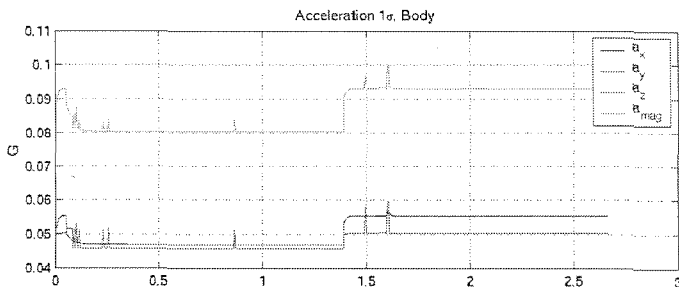
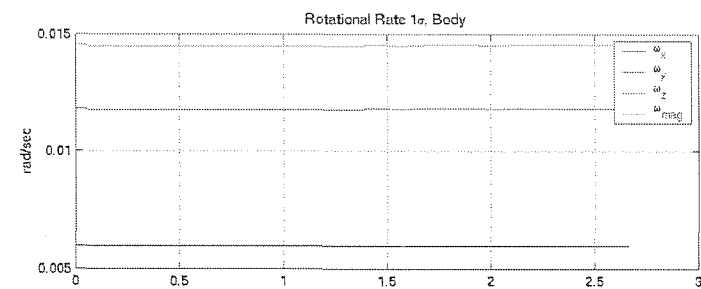
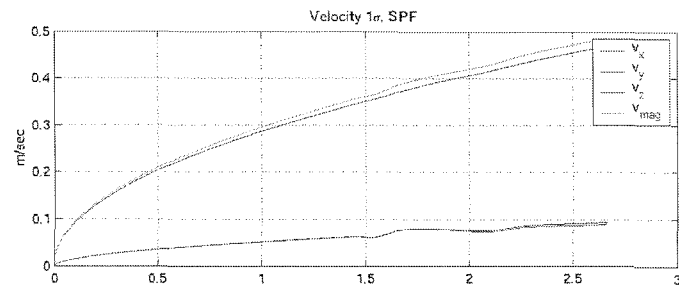
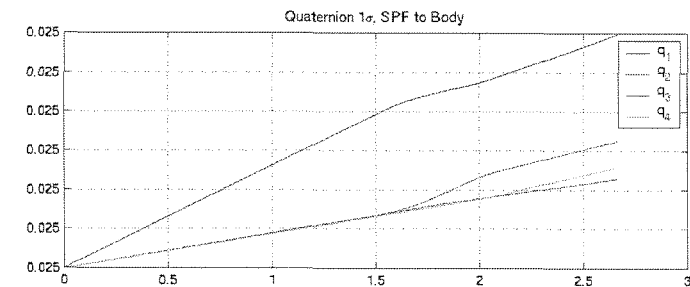
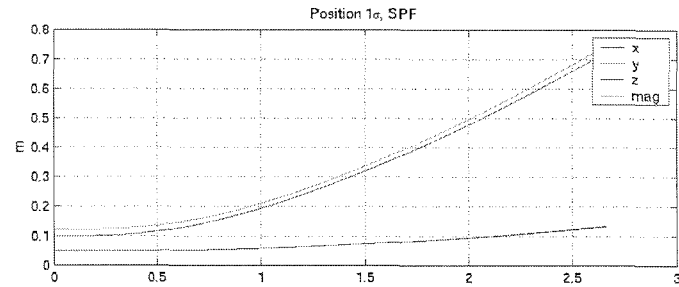
# Results: Velocity (SPF and Mars frames) **JPL**



XYZ Velocities in the SPF (left) and Mars (right) frames



# Uncertainties: Translational & Rotational **JPL**



Translational (left) and Rotational (right) Uncertainties



# *Initial Conditions*



- Previous slide of estimate  $1\sigma$  uncertainties illustrates need for accurate initial conditions
- Uncertainties of unmeasured states grows as a value of its derivative state
  - Position uncertainty grows at a rate equal to the value of the velocity uncertainty, etc.
- If stroke measurement is needed to be know to within 10 cm ( $3\sigma$ ), initial conditions must be an order of magnitude more accurate
- Initial position and initial attitude are important since no measurements of height or attitude are made during the drop (only acceleration and rotation rate are measured)
- Navigators are involved in precision measurements of the SPF chamber's layout and magnetic field
  - We (navigators) are dealing with hardware and getting our hands dirty!



## *Conclusions and Future Work*



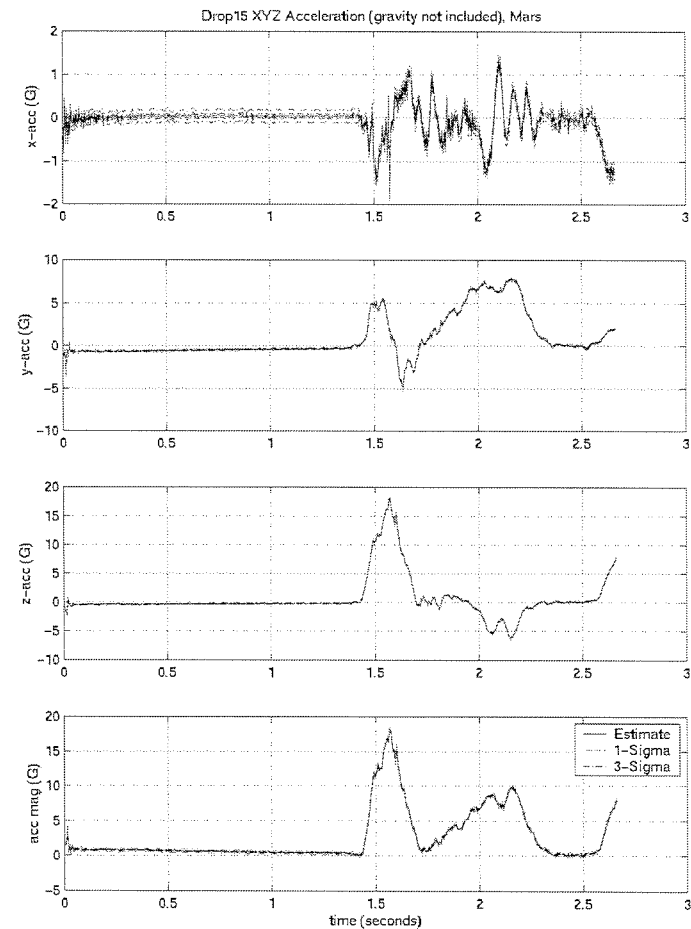
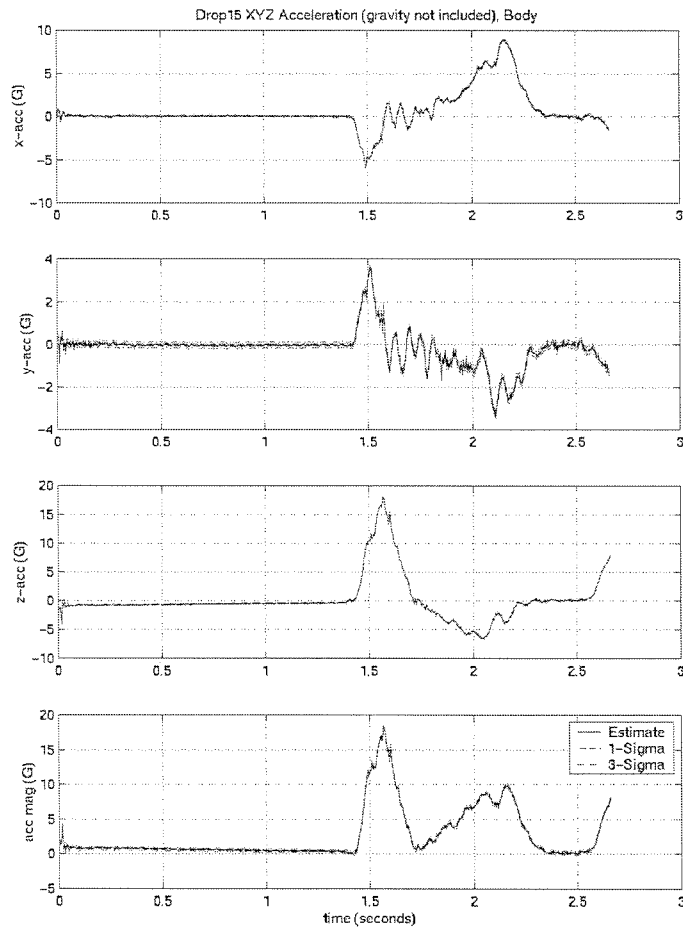
- REDLand demonstrates that IMU data can be used as measurements in a Kalman filter
- JPL is on course to have a high-fidelity EDL reconstruction application for the MER missions
- Must get better estimate of stroke
- Must get accurate measurements of the initial conditions
- Future drop tests will include distance measurement



# *Backup Slides*



# Results: Acceleration (Body and Mars)

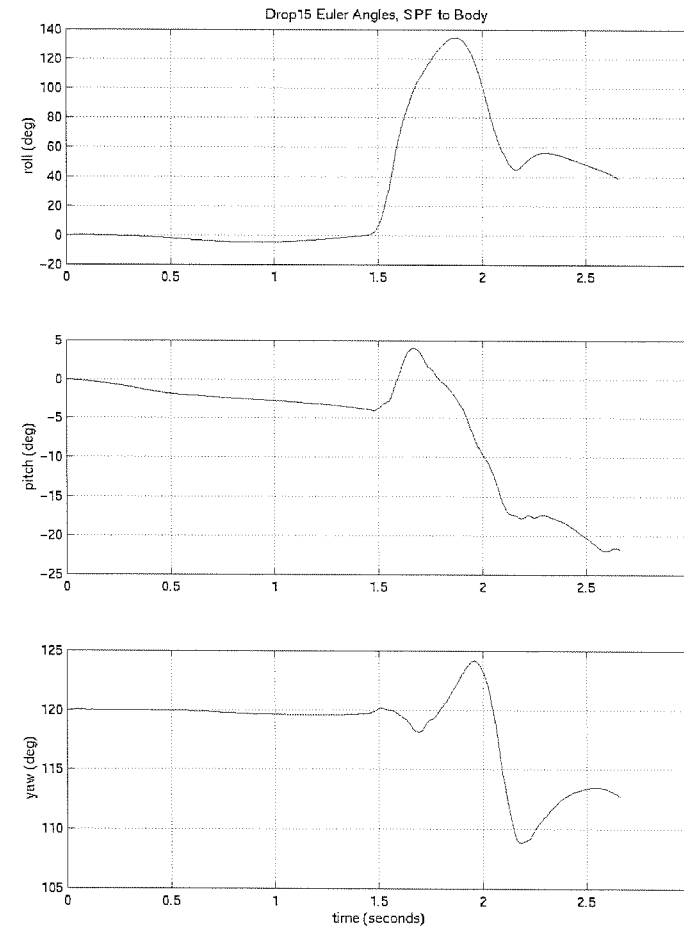
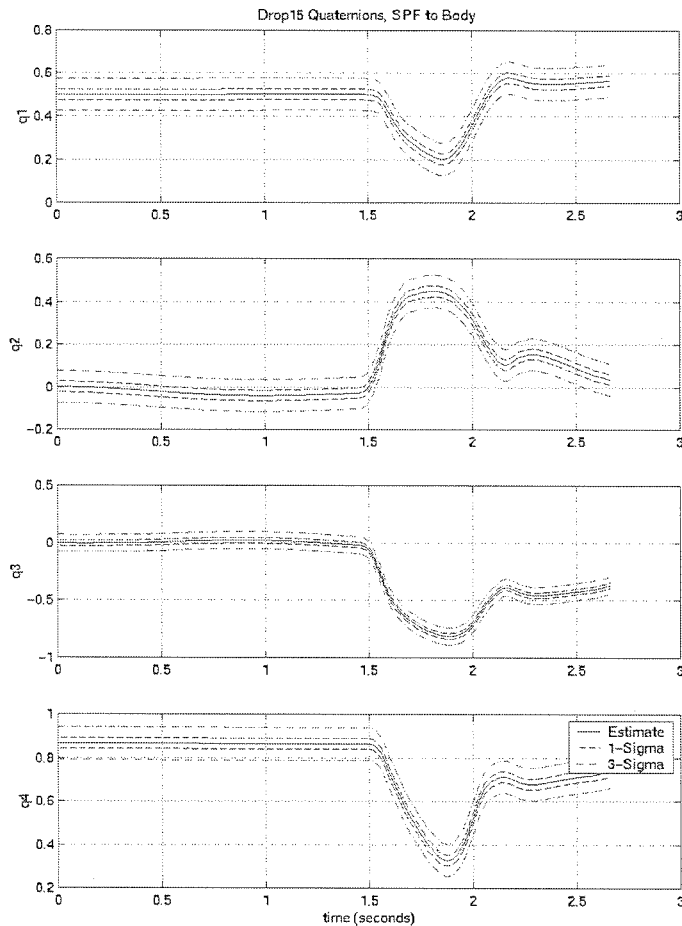


XYZ Accelerations in the Body (left) and Mars (right) frames





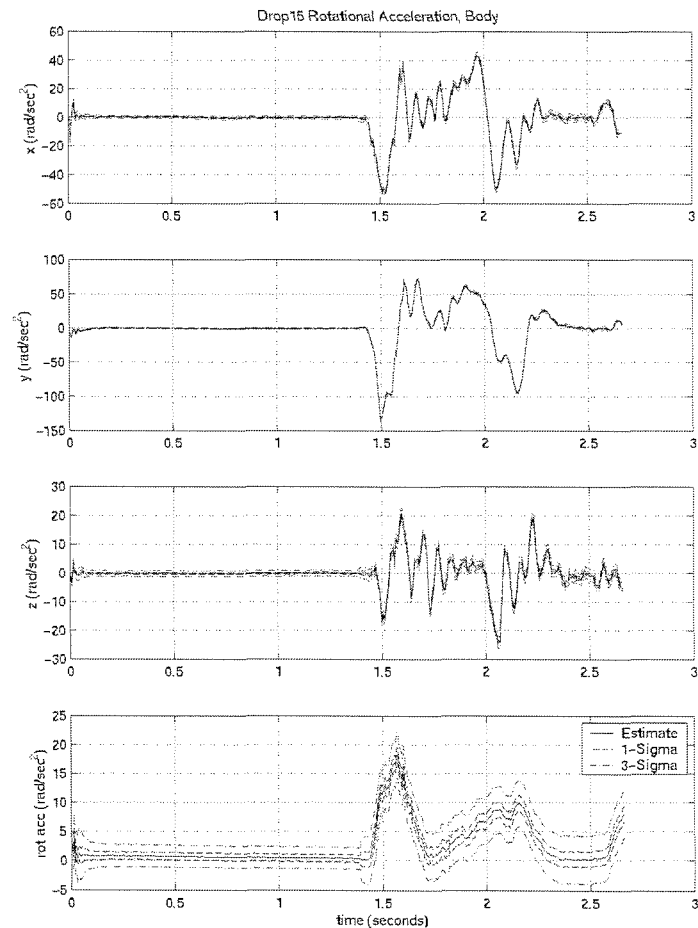
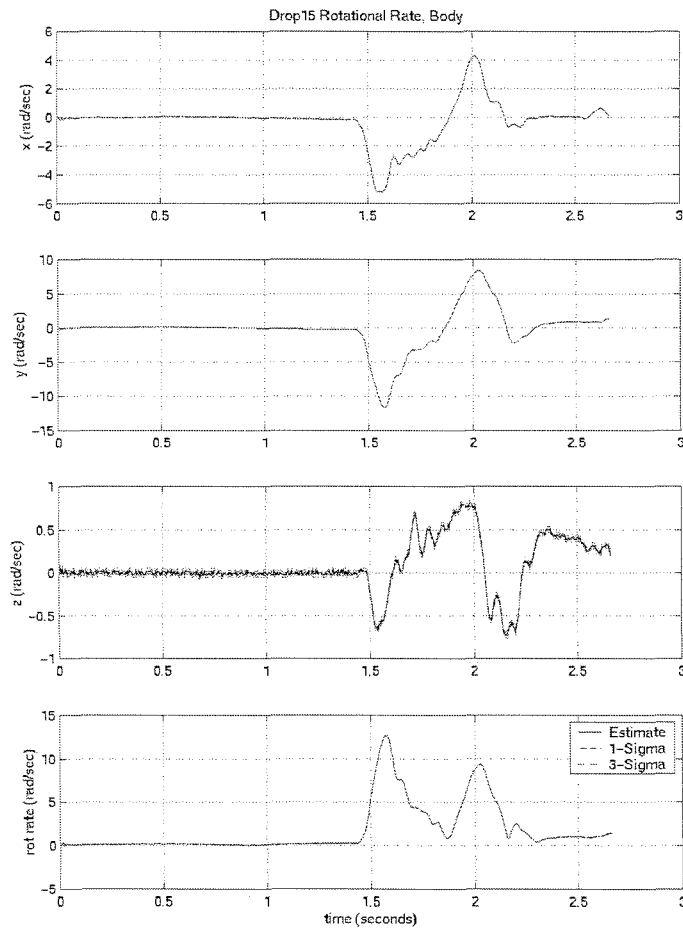
# Results: Quaternion and Euler Angles



SPF to Body rotations: Quaternion (left) and 1-2-3 Euler Angles (right)



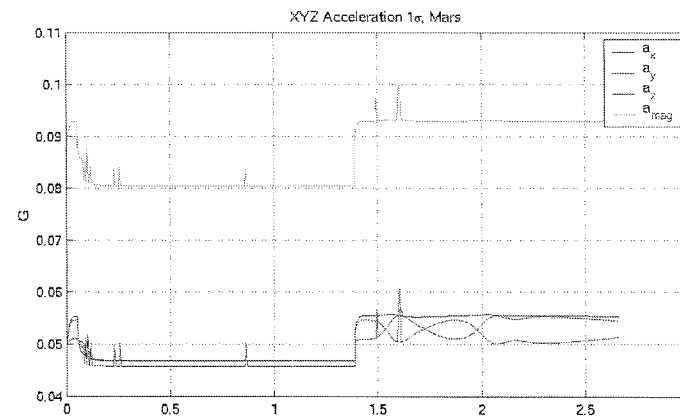
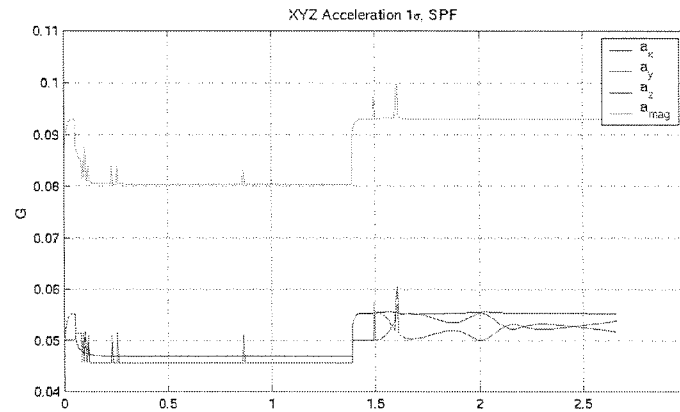
# Results: Rotational Rate and Acceleration **JPL**



XYZ Rotational Rate (left) and Rotational Acceleration (right)



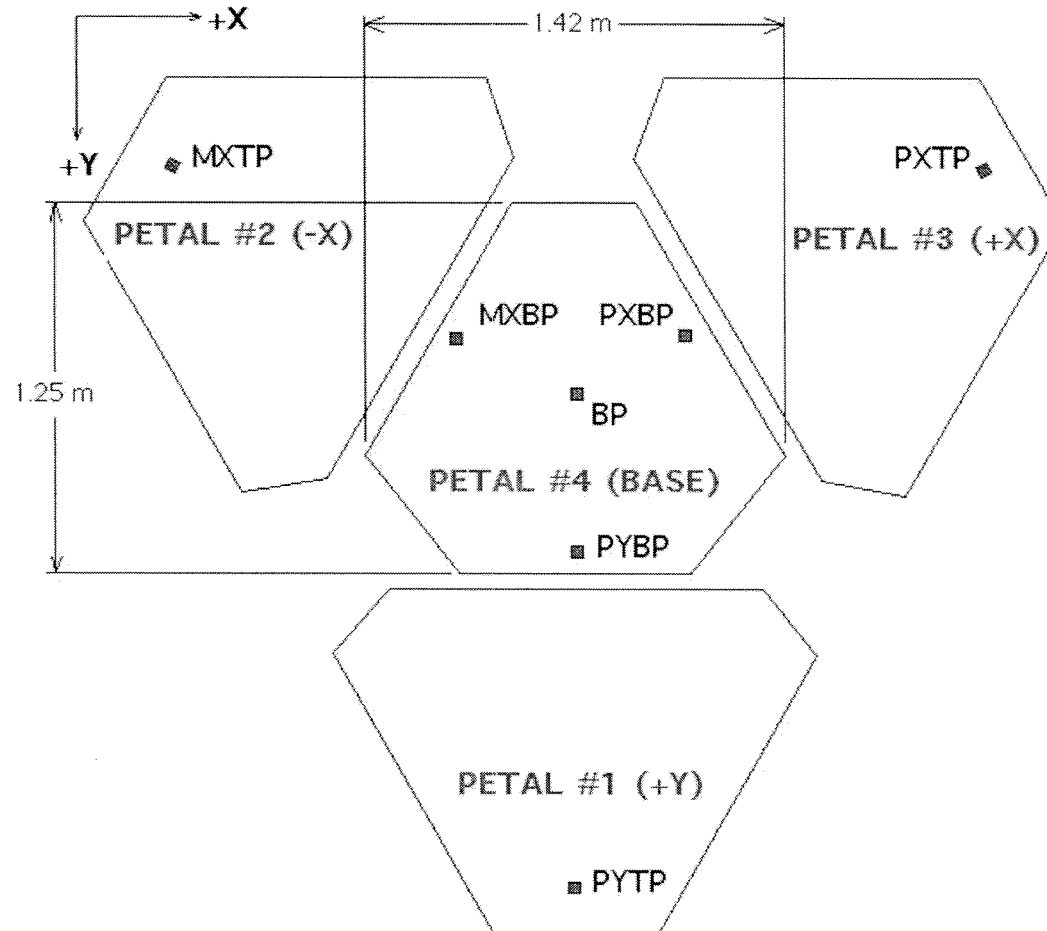
# Acceleration Uncertainty (SPF & Mars)



Translational Acceleration Uncertainties in the SPF (top) and Mars (bottom) frames



# Accelerometer Layout





# *Accelerometers on Tri-axial Block*

**JPL**

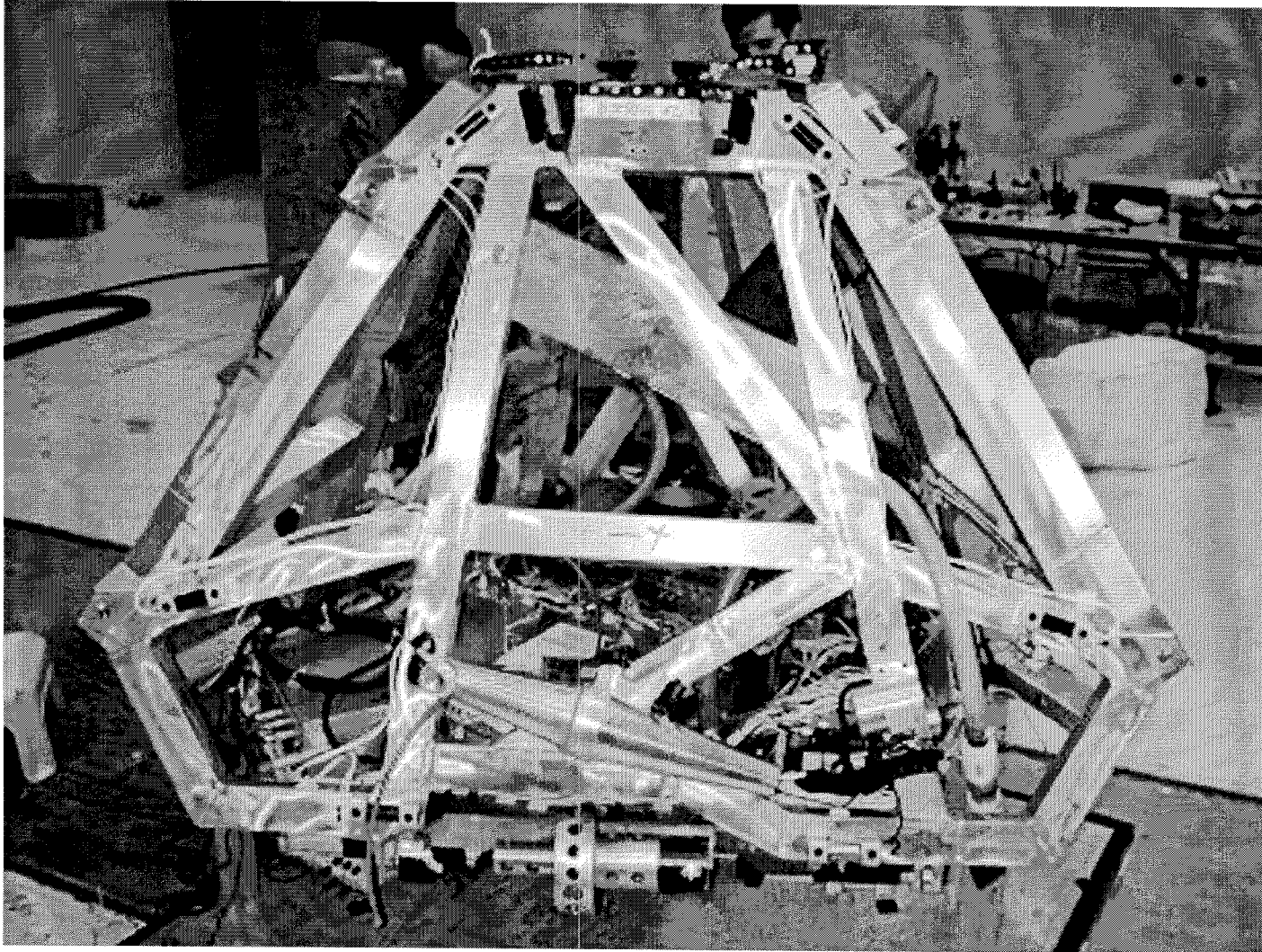


*Photo courtesy of ILC Dover, Inc.*



# *Closed Lander*

**JPL**



*Photo courtesy of ILC Dover, Inc.*