

# Selected QCD Results from Tevatron

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Representing  
DØ and CDF

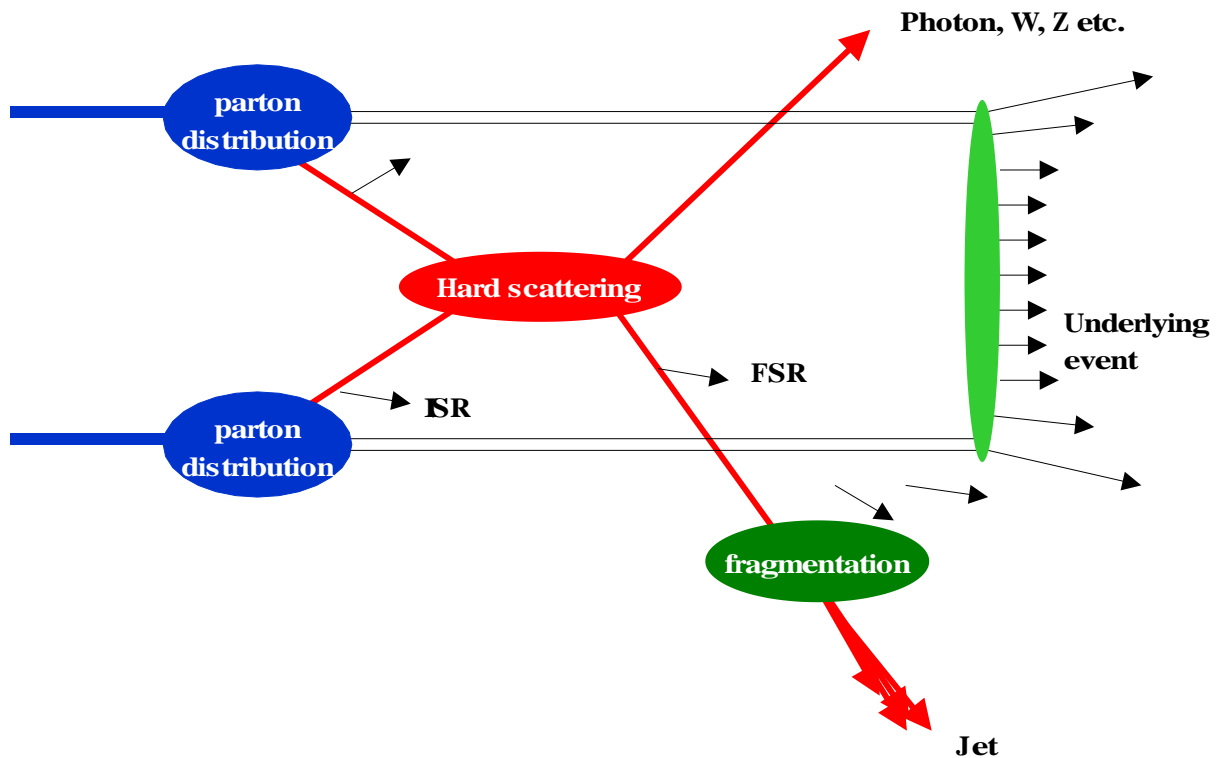
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Datong, 4<sup>th</sup> September 2001

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- multiple jet production
  - ▷ ratios of multijet inclusive cross-sections
  - ▷ studies of  $E_T$  and relative azimuthal angles
- jet structure
  - ▷ transverse energy distributions within jets
  - ▷ subjet/charged particle multiplicities

# Topics in QCD at Tevatron

Generic hadron-hadron collision:



QCD topics in Run I:

- inclusive jet cross-sections and dijet mass distributions
- direct photon production
- vector boson production
- $b\bar{b}$  production
- hard diffraction, BFKL studies
- multiple jet production (covered here)
- jet structure, multiplicities (covered here)

# Data Sets and Event Kinematics

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## Data sets:

- $p\bar{p}$  collisions at  $\sqrt{s} = 1.8$  TeV (and  $\sqrt{s} = 630$  GeV) collected by DØ and CDF
- Run I (1992-95):  $\sim 110$  pb $^{-1}$  (each experiment) ( $\sim 0.5$  pb $^{-1}$  at  $\sqrt{s} = 630$  GeV)
- Run II (since 3/2001, not yet fully operational):  $\sim (2 - 15)$  fb $^{-1}$  (each experiment)

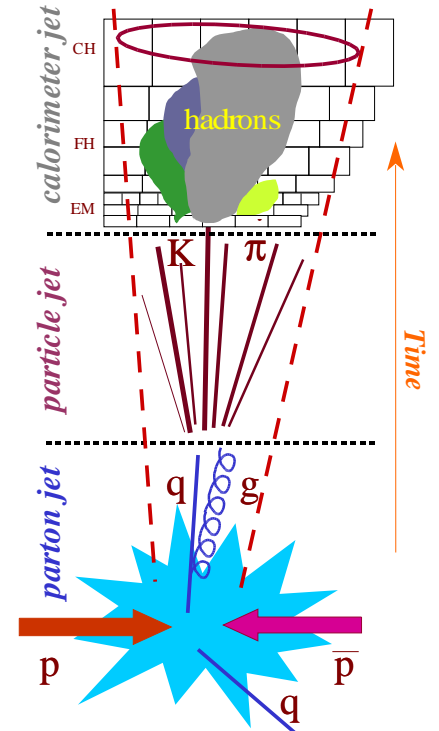
## Measured event variables:

- transverse momentum:  $E_T$
- azimuthal angle:  $\phi$
- pseudo-rapidity:  $\eta = -\ln(\tan(\theta/2))$   
with polar angle:  $\theta$

# Jets at the Tevatron

## Jet algorithms:

- fixed cone size (most common)
  - ▷ clustering of calorimeter cells within  $R = \sqrt{\eta^2 + \phi^2} \leq R_0$  (usually  $R_0 = 0.7$ )
- $k_T$  algorithm
  - ▷ successive combination algorithm based on relative transverse momenta of cells (particles)



## Correction to particle level:

- correct for finite energy resolution
- subtract underlying event (modeled by minimum bias data)

⇒ 'hermetic' calorimeter with fine segmentation and excellent energy resolution

- DØ:
- ▷ coverage:  $|\eta| < 4.1$
  - ▷ segmentation:  $\Delta\eta \times \Delta\phi = 0.1 \times 0.1$   
( $\Delta\eta \times \Delta\phi = 0.05 \times 0.05$  in EM shower maximum)
  - ▷ single particle energy resolution:
    - electromagnetic:  $\Delta E/E \sim 15\% / \sqrt{E[\text{GeV}]}$
    - hadronic:  $\Delta E/E \sim 50\% / \sqrt{E[\text{GeV}]}$

# Ratios of Multijet Cross Sections (I)

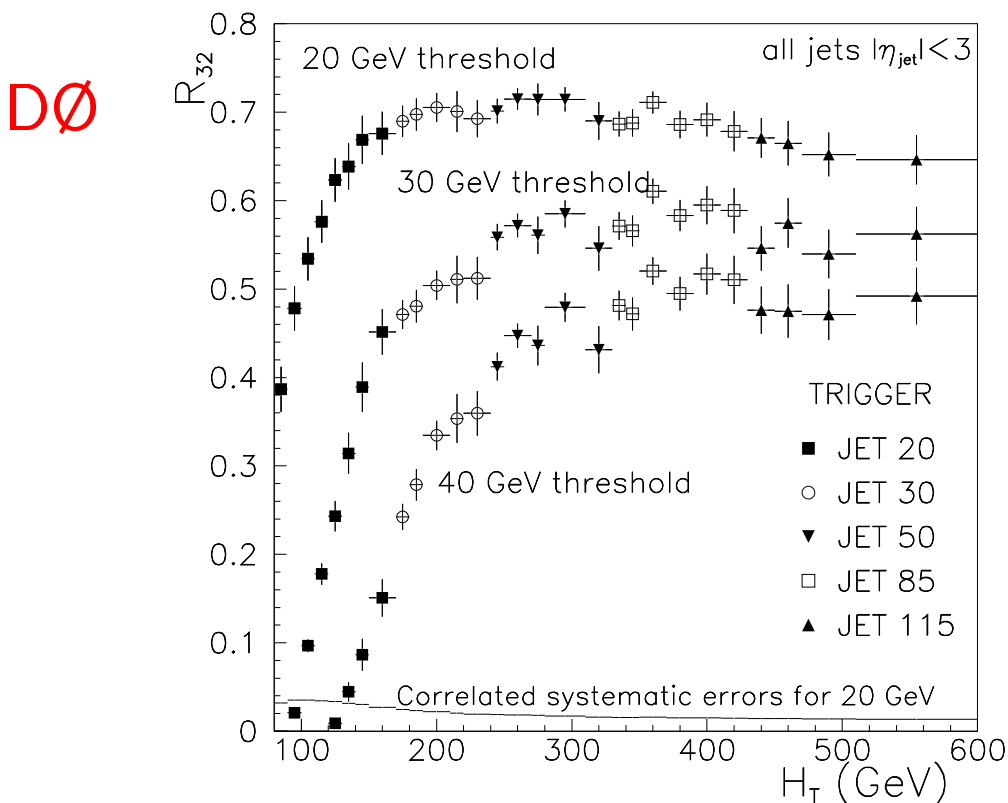
Measurement of the ratio of inclusive three-jet to inclusive two-jet cross section:

$$R_{32} = \frac{\sigma_3}{\sigma_2} = \frac{\sigma(p\bar{p} \rightarrow \geq 3 \text{ jets} + X)}{\sigma(p\bar{p} \rightarrow \geq 2 \text{ jets} + X)}$$

as a function of scalar sum of transv. energies  $H_T = \sum E_T^{\text{jet}}$   
DØ: PRL 86, 1955 (2001)

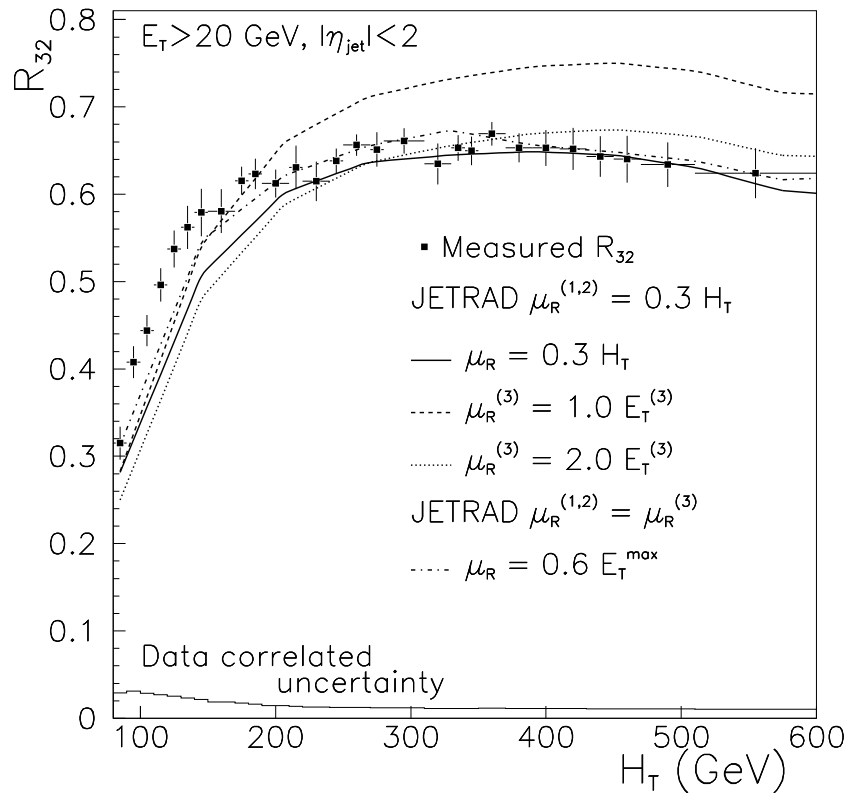
Motivation:

- probing the rate of gluon emission in QCD  
( $R_{32} \sim \alpha_s$ , c.f. measurements at PETRA)
- prediction is sensitive to choice of renormalization scales



# Ratios of Multijet Cross Sections (II)

DØ



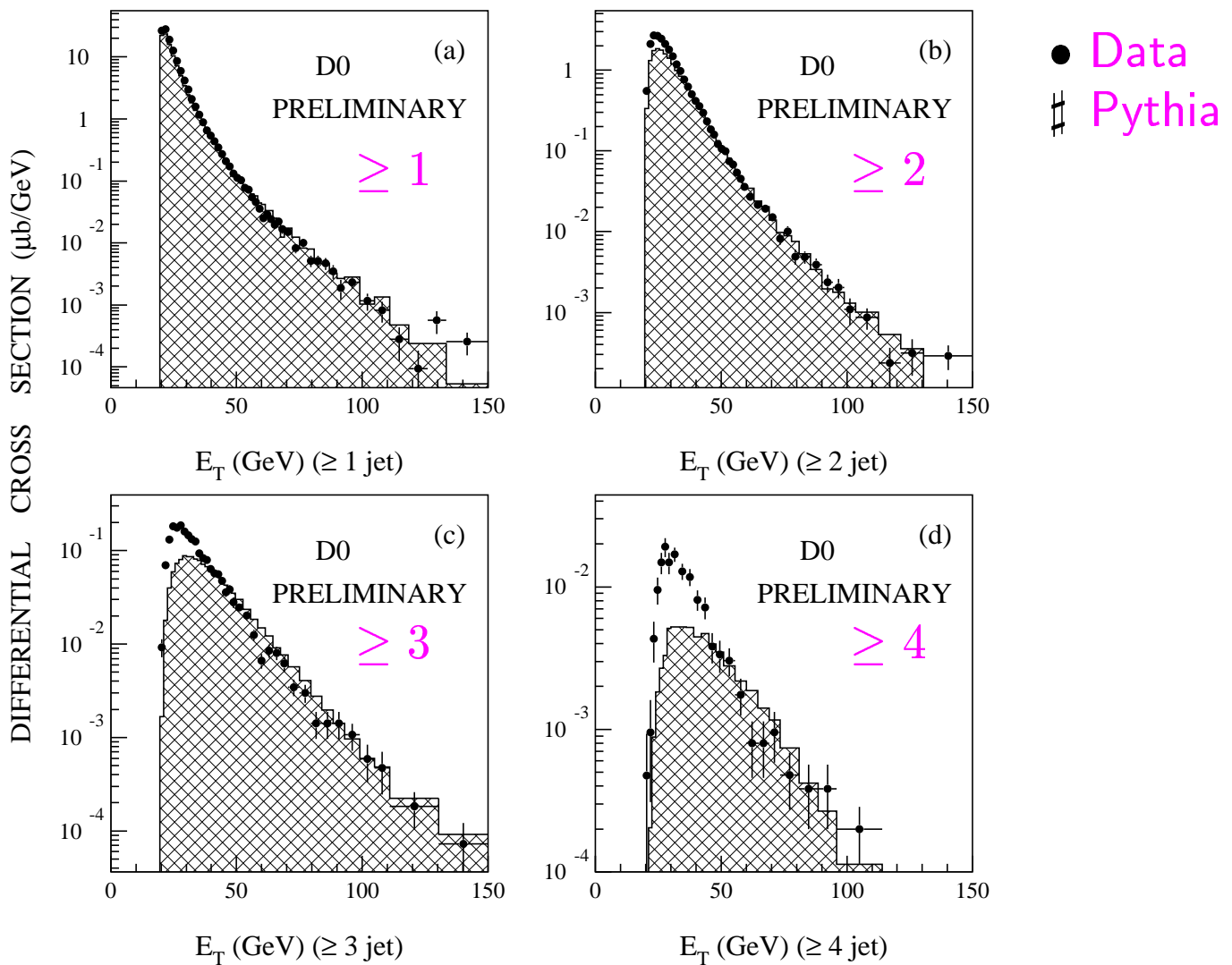
- Jetrad: MC simulation of parton-level jets in NLO
- factorization scale  $\mu_F$  set equal to renormal. scale  $\mu_R$
- a. choose  $\mu_R^{(1,2)}$  for two leading jets proportional to  $H_T$ , vary  $\mu_R^{(3)}$  of 3<sup>rd</sup> jet (same as  $\mu_R^{(1,2)}$ , proportional to  $E_T^{(3)}$ )
- b. choose all  $\mu_R$  proportional to  $E_T^{\max}$
- $\Rightarrow$  within errors (correlated) data can be described by:
  - a.  $\mu_R^{(1,2,3)} \sim 0.3 H_T$
  - b.  $\mu_R^{(1,2,3)} \sim 0.6 E_T^{\max}$
- $\hookrightarrow$  need for different scale for 3<sup>rd</sup> jet not supported

# Multiple Jet Production at low $E_T$ (I)

Study of transverse momentum distributions and relative azimuthal angles in multiple jet production with  $E_T > 20$  GeV

DØ: [hep-ex/0106072](http://hep-ex/0106072)

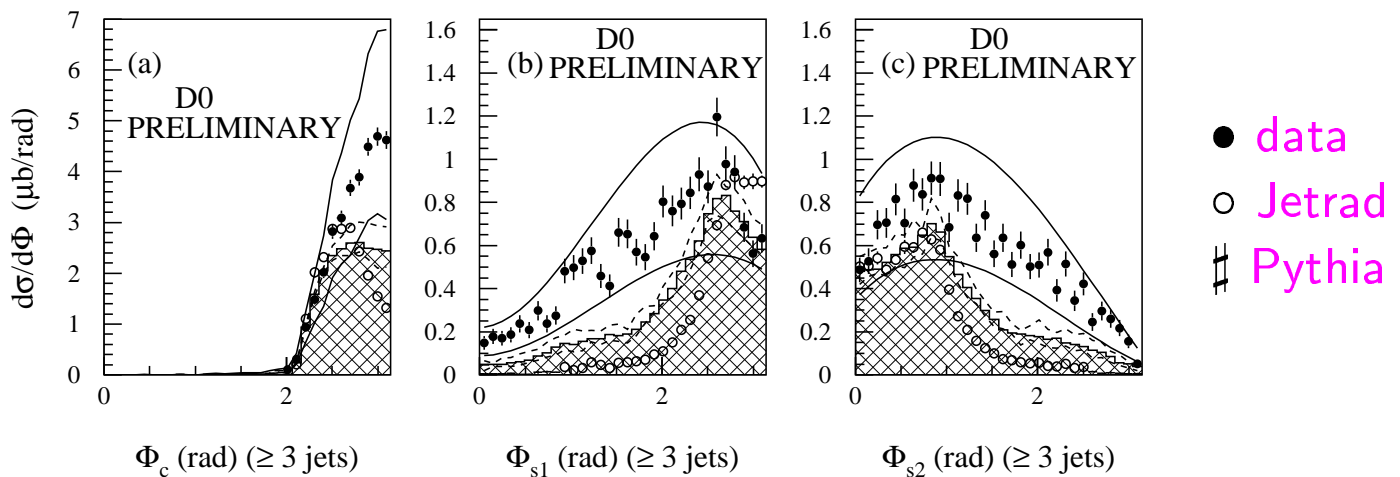
Large discrepancies between data and Pythia for 3 and 4 jet production for  $E_T$  of leading jet below  $\sim (30 - 40)$  GeV



# Multiple Jet Production at low $E_T$ (II)

Relative azimuthal angle in  $\geq 3$ -jet events:

- a. between pair with minimal  $q_{ij} = (\mathbf{E}_{T_i} + \mathbf{E}_{T_j}) / (E_{T_i} + E_{T_j})$  ( $\Phi_c = \Phi_{ij}$ )
- b.+c. between 3<sup>rd</sup> jet and the 1<sup>st</sup> and 2<sup>nd</sup> leading jet in pair (cut on  $\pi - \Phi_c < 0.4$ )



- Leading jets are more back-to-back in data.
- Correlation of 3<sup>rd</sup> jet with axis of 2<sup>nd</sup> jet much less pronounced in data.
- c.f. good description of angular distributions for  $E_T > 50\text{GeV}$ , [DØ: PRD 53, 6000 \(1996\)](#)
- Observed differences cannot be explained by variations in the modeling of underlying event or multiple-parton scattering.
- BFKL dynamics in low  $Q^2/s$  regime?

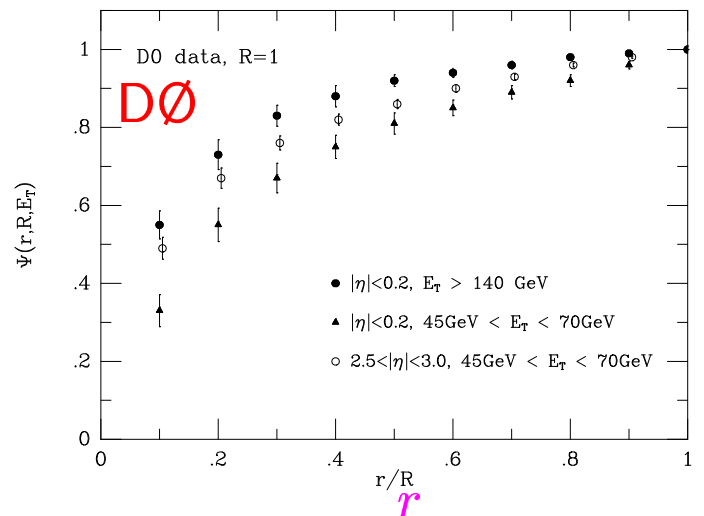
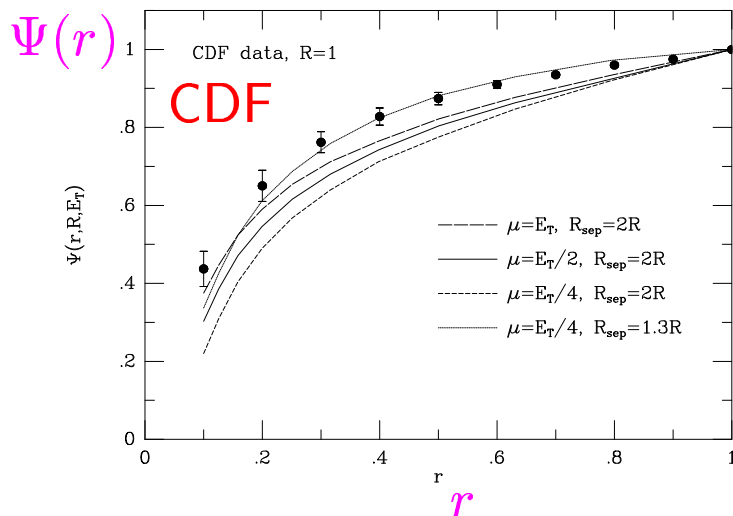


# Jet Profiles, Transverse Energy Distributions

Early studies by CDF and DØ of jet profiles as measured by the transverse energy flow within the cone

CDF: PRL 70, 713 (1993); DØ: PL B357, 500 (1995);  
(now textbook knowledge)

$\Psi(r)$ : average fraction of the jet  $E_T$  in a sub-cone of radius  $r \leq R = 1$



Learned:

- Large scale dependence in  $\mathcal{O}(\alpha_s^3)$ .
- Jets become narrower with increasing  $E_T$
- Jets have narrower profile in forward region (high  $x$ : larger quark contribution in hard scattering)

# Multiplicities in Quark and Gluon Jets

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## Motivation:

- test of QCD: ratio of number of particles within gluon jets to quark jets expected to be approximately ratio of color charges:  $C_A/C_F = 9/4$
- separation of q and g jets (e.g. for top, W + jet)

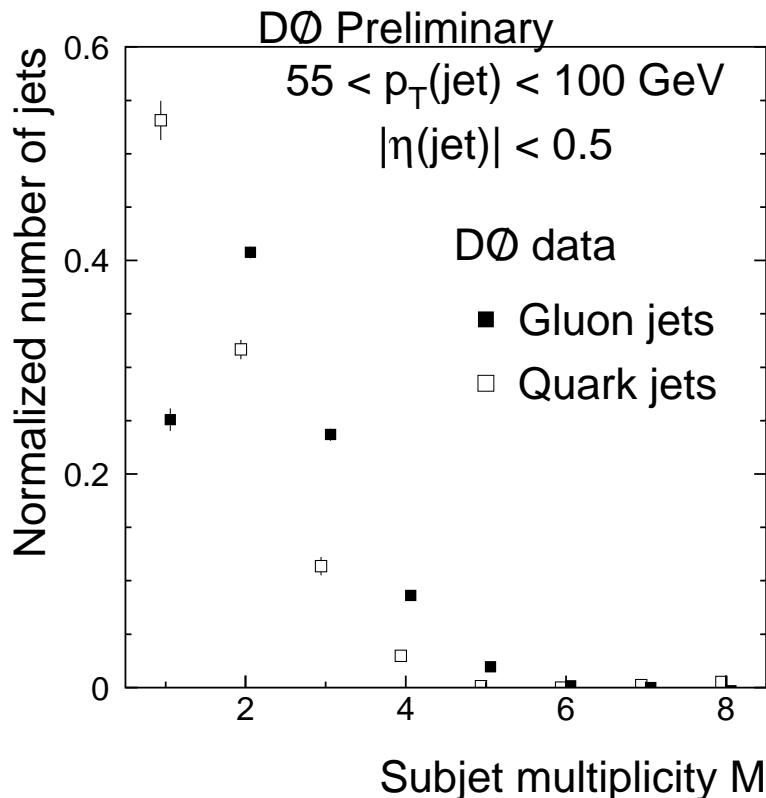
## Method:

- select quark and gluon enriched jet samples using average momentum fraction of parton  $x$ 
  - ▷ low  $x$ : gluon dominance
  - ▷ high  $x$ : valence quarks
- $D\emptyset$ : compare jets at same  $(E_T, \eta)$  produced at different  $\sqrt{s}$
- CDF: study dependence of multiplicity on dijet mass ( $\sim x_1 x_2$ ) at fixed  $\sqrt{s}$
- both experiments: obtain relative q/g content from MC simulations (Herwig) and parton distribution functions (PDFs, based on DIS and other data)

## Subjet Multiplicity in q and g Jets

- DØ compares 630 GeV and 1800 GeV data at same  $E_T$  and  $\eta$  and infers q and g jet differences using Herwig 5.9 and CTEQ4M PDF. [hep-ex/0106040](http://hep-ex/0106040)
- Jets and subjets are defined with  $k_T$  algorithm. Objects are merged into subjets if

$$d_{ij} = \min(p_{T_i}^2, p_{T_j}^2) \cdot \frac{\Delta R_{ij}^2}{D^2} < 10^{-3} p_T^{jet}$$



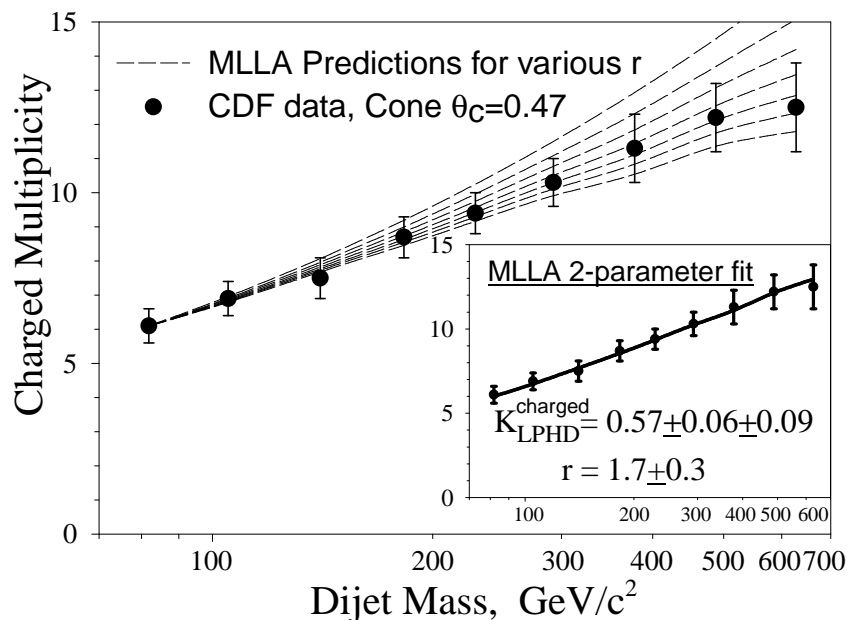
$$\Rightarrow R = \frac{\langle M_g \rangle - 1}{\langle M_q \rangle - 1} = 1.84 \pm 0.15(\text{stat})_{-0.18}^{+0.22}(\text{sys})$$

c.f. Herwig:  $R = 1.91 \pm 0.16$

in accordance with naive expect. from color factors ( $\frac{C_A}{C_F} = \frac{9}{4}$ )

# Charged Particle Multiplicity in Jets

- CDF measures mean charged particle multiplicity in dijet prod. as a function of dijet masses between 80 and 630  $\text{GeV}/c^2$ .  
[FERMILAB-PUB-01-106-E](#)
- Relative quark/gluon jet contributions are inferred from Herwig and CTEQ4M and CTEQ4HJ PDFs.
- Data are fit within framework of Modified Leading Log Approximation (MLLA) and Local Parton Hadron Duality (LPHD,  $\rightarrow$  # partons to # hadrons independent of  $E_T$ )



- Within MLLA+LPHD scheme:

$$N_{\text{partons}}^{\text{g-jets}} / N_{\text{partons}}^{\text{q-jets}} = 1.7 \pm 0.3$$

$$N_{\text{hadrons}}^{\text{charged}} / N_{\text{partons}} = 0.57 \pm 0.11$$

- ▷ multiplicity ratio consistent with naive expect. and Herwig
- ▷  $N_{\text{hadrons}} \sim N_{\text{partons}}$

# Summary and Outlook

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- Tevatron contributes to qualitative and quantitative understanding of higher order effects in QCD.
- Parton Shower MC and NLO calculations can describe most data except in the low  $E_T$  region of multijet production.
- Additional  $D\bar{D}$  event shape study (transverse thrust) available soon.
- Run II offers good opportunities for QCD measurements, especially at **large**  $E_T$ .