Learning and the Adaptive Management of Fisheries Resources

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Overview

- When is learning worth the trouble?
- Adapting in a fully observable world
- Adapting in a partially observable world
- Application to habitat management

When Is Learning Worth The Trouble?

- Adaptive Management
 - different things to different people
 - new information or situation
 - stochastic dynamic optimization:
 - action* = f(situation, information)
 - trade-offs between present and future
- Learning vs doing:
 - Is it worth acting suboptimally now to be able, by virtue of better info, to do better later?
 - In general, what's the best mix of learning and doing?

When Is Learning Worth The Trouble?



When Is Learning Worth The Trouble?

- Optimal control, Markov decision processes
 no learning or passive learning
- Dual control
 - control engineers and a few ecologists
 - 'active adaptive mgt'
- Partially observable Markov decision processes
 - AI and robotics
 - similar spirit to dual control, but different math

Markov Decision Processes (MDPs):

Adapting in an Observable World

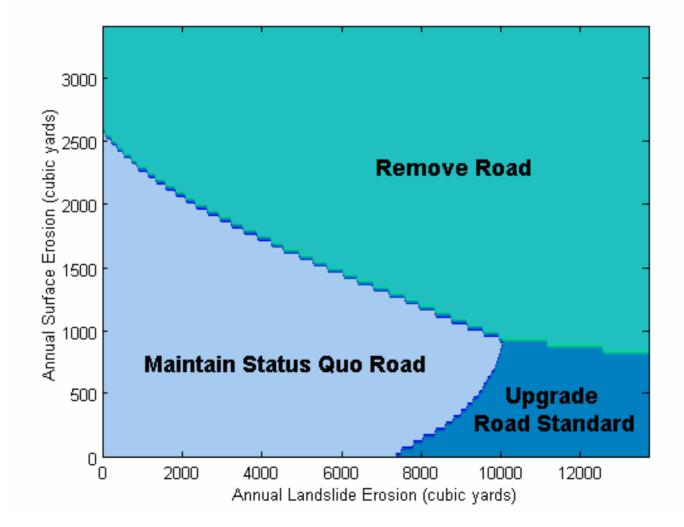
•Dynamic + Stochastic: future = f(present, error)

•Solution:
$$\delta_i^*(x_i) = \underset{a \in A}{\operatorname{argmax}} \left[q_i^a(x_i) + \beta \sum_j p_{ij}^a q_j^a(x_j) \right]$$

•Process uncertainty, but not observational or model uncertainty

•Nothing about gathering info on state variables*

MDPs: adapting in an observable world





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Partially Observable MDPs (POMDPs): Adapting in a Noisy World

- Stochastic + dynamic + noisy
- Belief becomes a state variable
 - beliefs from priors and observations
 - uncountably infinite
- MDP: state → action
 POMDP: belief → action
- Solution: $\delta_i^*(\pi_i) = \arg\max_{a \in A} \left[\sum_i \pi_i q_i^a + \beta \sum_{i,j,\theta} \pi_i p_{ij}^a r_{j\theta}^a q_j^a \right]$

POMDP Example



North Fork Caspar Cr., plugged culvert Rd 5



When is erosion monitoring worth the expense?

Problem Setup

- When is erosion monitoring worth the trouble?
- States = {Good Road, Bad Road}
- Decisions = {Do Nothing, Monitor, Treat}
- Observations = {Good Road, Bad Road}

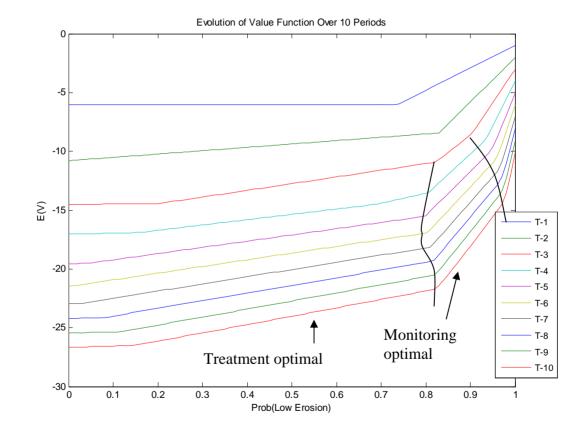
Problem Setup

$$P_{ij}^{1} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad P_{ij}^{2} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad P_{ij}^{3} = \begin{bmatrix} 0.95 & 0.05 \\ 0.80 & 0.20 \end{bmatrix}$$

$$R_{j\theta}^{1} = \begin{bmatrix} 0.6 & 0.4 \\ 0.4 & 0.6 \end{bmatrix} \quad R_{j\theta}^{2} = \begin{bmatrix} 0.9 & 0.1 \\ 0.1 & 0.9 \end{bmatrix} \quad R_{j\theta}^{3} = \begin{bmatrix} 0.5 & 0.5 \\ 0.5 & 0.5 \end{bmatrix}$$

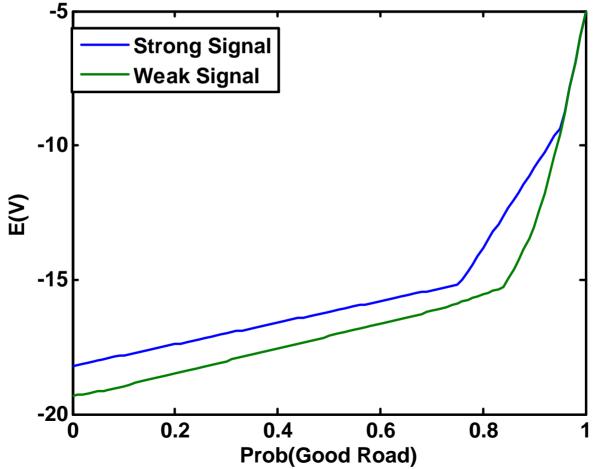
$$W_{ij\theta}^{1} = \begin{bmatrix} -1 & -20 \\ -1 & -20 \end{bmatrix} \quad W_{ij\theta}^{2} = \begin{bmatrix} -3 & -22 \\ -3 & -22 \end{bmatrix} \quad W_{ij\theta}^{3} = \begin{bmatrix} -6 & -6 \\ -6 & -6 \end{bmatrix}$$

Results for a 10-period problem



Results (cont)

Value Function at T-5 Under Different Observation Models



POMDP Assessment

- POMDP may be a good tool for fisheries mgt
 - partial observability is central in fisheries
 - monitoring funds are scarce
 - applicable to planning and behavioral models
- Drawbacks
 - computation
 - assumes (stochastic) dynamics are known
- Need to
 - increase state and decision space \rightarrow heuristics
 - try state augmentation for parameter uncertainty

Odds & Ends

- POMDP and state augmentation (Fernandez-Rao)
- Reinforcement Learning (Bertsekas)
- Sequential hypothesis testing (Wald)
- [Behavioral & cognitive modeling:
 - neural basis of learning (Ishii et al.)
 - behavioral psychology (Bearden)
 - location choice (Lane)



POMDPs: Adapting in a Noisy World

- MDP = {S, P, A, W}
 POMDP = {S, P, Θ, R, A, W}
- MDP maps state → action
 POMDP maps beliefs → action
- Unknown state variables, known parameters*

POMDP Value Function

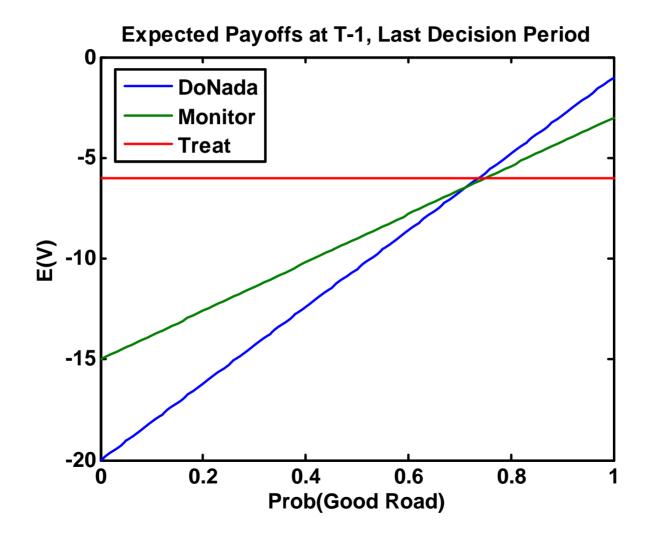
$$V_{t}(\pi) = \max_{a} \left[\sum_{i} \pi_{i} q_{i}^{a} + \sum_{i,j,\theta} \pi_{i} p_{ij}^{a} r_{j\theta}^{a} V_{t+1}[T(\pi \mid a, \theta)] \right]$$

where

 $\pi_{i} = \text{probability of being in state } i$ $q_{i}^{a} = \text{immediate reward for taking action } a \text{ in state } i$ $p_{ij}^{a} = \text{probability of moving from state } i \text{ to state } j$ after taking action a $r_{j\theta}^{a} = \text{probability of observing } \theta$ after taking action a and moving to state j

T = function updating beliefs based on prior and θ

POMDP Value Function



POMDP Value Function

