# GENERAL DESIGN FEASIBILITY CURVES FOR BOOSTER FERRITE CAVITIES 

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For any particular ferrite, the method of establishing the feasibility of constructing a ferrite cavity is very straightforward. The curves presented in this note are intended to facilitate the selection, or rejection, of a ferrite material based upon an initial sample measurement. It is still essential to measure (small and large samples) ferrite thoroughly, and do more detailed computations, for any potentially acceptable ferrite.

The curves are in two groups for two different approaches. The first is very specific for Booster cavities I and II at 17 Kv . The second is more general for Booster cavities I, II, III for varying gap voltages.

# GENERAL DESIGN FEASIBILITY CURVES FOR BOOSTER FERRITE CAVITIES 

Martin Plotkin

## Design Criteria:

1. 17000 volts/cavity
2. Frequency Range
a. Cavity I - $178.5-675 \mathrm{KHz}$
b. Cavity II - $675-2500 \mathrm{KHz}$
3. Total axial length available/cavity - 250 cm .
4. These designs predicated on small samples of TDK Ferrite SY-7 (Mike Goldman data - Fig. I)
$V=\omega B A \times 10^{8}$ (B-gauss $A-\mathrm{cm}^{2}, V-$ volts $A=N\left(r_{2}-r_{1}\right) \times 2.5$, $N=$ number of 2.5 cm thick rings).
Using the data in appendix $I$, Fig, II represents a set of design curves for $S Y 7$ and $V=17 \mathrm{KV}$. For any $\mathrm{r}_{2}-\mathrm{r}_{1}$, ( $10 \mathrm{~cm}, 12.5 \mathrm{~cm}$ and 15 cm ) as shown and a power loss level selected, the number of rings is determined. The power loss level is a function of the method of cooling, the duty factor and the requirement for temperature control of the ferrite. For example, with water cooling and a $250 \mathrm{mw} / \mathrm{cc}$ power loss and a $50 \%$ duty factor, we look at the 500 $\mathrm{mw} / \mathrm{cc}$ line and see that we can use 48 rings at $\mathrm{r}_{2}-\mathrm{r}_{1}=15 \mathrm{~cm}$ or 56 rings at $r_{2}-r_{1}=12.5 \mathrm{~cm}$.

Available length of ferrite for a double cavity/station:

$$
\begin{array}{lr}
\text { gaps }(2)+\text { clearance }: 2 \times 15 \mathrm{~cm} & 30 \mathrm{~cm} \\
\text { center plates: } & 6 \mathrm{~cm} \\
\text { end plates: } 2 @ 1.5 \mathrm{~cm} & 3 \mathrm{~cm} \\
\text { end spaces: } 4 @ 2.5 \mathrm{~cm} & \frac{10 \mathrm{~cm}}{49 \mathrm{~cm}}
\end{array}
$$

For 250 cm total - 200 cm available for ferrite and cooling plates (or cooling spaces for air cooling). Cooling plates may range from 0.3 cm (for edge cooling) to 0.6 cm for overall cooling plates. Air cooling requires about 0.6 cm between ferrite rings.

Maximum number of rings of 2.5 cm thickness for various cooling $\mathrm{N}=\frac{200}{2.5+\mathrm{C}}$ $c=$ cooling thickness requirement.

N max
edge cooling (.3cm) 71.4 (72)
overall cooling (. 6 cm ) 64.5 (64)
air cooling (.6cm) 64.5 (64)

All the previous numbers are for the starting frequency. As the ferrites are dc biased to tune to the top frequency of 675 KHz the losses (at the same voltage level) may increase or decrease. This must be measured specifically for each ferrite. In general, when a ferrite is used within its normal frequency range, the impedance over the tuning range remains fairly uniform.

Since $P=V_{p k}^{2} / 2 Z$ the power loss does not vary too much. The top frequency for cavity I is well within the operating frequency range of TDK SY-7.

It is fortuitous that as the frequency rises by a factor of, let us say 3 , the inductance decreases by a factor of 9 and the $Q$ increases by about a factor of 3. Thus $Z=\omega L Q$ remains relatively constant.

Similarly for the heavy ion cavity II, the data in appendix II provides the curves in Figure III.

In Fig. III, for the same number of $r$ ings as in Cavity $I$, the power losses are considerably smaller. However, the top frequency of 2.5 MHz is above the normal, unbiased, operating frequency of SY7. With bias the ferrite behavior above its normal operating frequency is significantly improved. There may be larger losses at 2.5 MHz than at 675 KHz . for this reason, and also for the simplicity of making Cavity I and Cavity II identical, as many rings should be used in Cavity II as in Cavity I.

The sequence of steps in the cavity design necessitate a selection of the cooling method, which limits the maximum number of rings allowed. The diameter of the rings, commensurate with the manufacturer's capability of fabrication, should be kept as small as possible. The important criterion for the ferrite is the cross section area of the ferrite, not the ferrite volume. A ring $40 \mathrm{~cm} 0 D-20 \mathrm{~cm}$ ID will perform exactly the same as one 50 cm $O D-30 \mathrm{~cm}$ ID. The smaller ring has $25 \%$ less weight and, for the same mw/cc, $25 \%$ less total power loss. Since the cost is influenced by total weight the smaller rings may be cheaper. Also cavity structures will be smaller and the rings will be easier to handle.

Having selected the cooling method, which dictates the maximum number of rings, the ferrite ring size and the duty factor, the number of rings required can be read off the curves.
$40 \mathrm{~cm} \times 20 \mathrm{~cm}$ rings are closer to the size rings used in the old AGS cavities. these rings were $35 \mathrm{~cm} \times 20 \mathrm{~cm}$ and ran successfully with edge cooled copper plates. The voltage on the old AGS cavity was $8 \mathrm{KV} / \mathrm{gap}$ compared to the $8.5 \mathrm{KV} / \mathrm{gap}$ in the Booster cavities. If they can be manufactured, and if the duty cycle allows, $40 \mathrm{~cm} \times 20 \mathrm{~cm}$ rings seem to be a viable solution.

The ferrite rings experience a thermal shock if the temperature rise during the pulse, irrespective of the duty factor, is excessive. For the case of $1 \mathrm{w} / \mathrm{cc}$ the temperature rise is

$$
\begin{aligned}
& \Delta T=\frac{\mathrm{w} / \mathrm{cc} \times \text { duty factor }}{4.186 \times \mathrm{sp} \cdot \mathrm{gr} \cdot \mathrm{x} \mathrm{sp.heat}} \quad \begin{array}{l}
\text { ferrite specific grav }=5 \\
\text { ferrite specific heat } \approx .17
\end{array} \\
& \begin{aligned}
\Delta T=\frac{\mathrm{W} / \mathrm{cc} \times \text { duty factor }}{3.56}
\end{aligned} \\
& \begin{aligned}
& \text { If duty factor }=50 \% \text { at } 1 \mathrm{~W} / \mathrm{cc} \Delta \mathrm{~T}=.14^{\circ} \mathrm{C} / \mathrm{pulse} \\
&=25 \% \text { at } 1 \mathrm{~W} / \mathrm{cc} \Delta \mathrm{~T}=.07^{\circ} \mathrm{C} / \mathrm{pulse}
\end{aligned}
\end{aligned}
$$

These values are not large but a mechanical analysis should be made.
If we consider using the old AGS cavities and rebuilding them for the vacuum requirements we can estimate the cavity behavior. The cavity will require a high vacuum flange in the center and an additional section can be added allowing for about $10 \%$ more ferrite (Peter Cameron information). We can use rings which are 42 cm OD and 20 cm ID and use the $1 / 8^{\prime \prime}$ copper, edge cooled, cooling plates.

If $N$ is the number of rings in each of 4 stacks in the double cavity, and the thickness of the ferrites is 2.5 cm , then $4 \mathrm{~N}(2.5)+(4 \mathrm{~N}+4)(0.3)=\mathrm{L}$, the available length for the stacks. $\left(0.3 \mathrm{~cm} \approx 1 / 8^{\prime \prime}\right.$ the cooling plate thickness.) Cameron indicates enough space for 88 rings at 2.1 cm which yields an available length of 214 cm . Solving for N for 2.5 cm rings we get $\mathrm{N}=18$, or 72 rings in four stacks.

$$
\begin{array}{ll}
B_{\text {gauss }}=\frac{V \times 10^{8}}{\omega \mathrm{~A}} & V=17000 \text { volts } \\
B=765 \text { gauss } & \omega=2 \pi \times .1785 \times 10^{6}=1.122 \times 10^{6} \\
A=72\left(\frac{42.20}{2}\right) 2.5=1980 \mathrm{~cm}^{2}
\end{array}
$$

For SY7, at $0.1785 \mathrm{MHz}, \mathrm{P}=390 \mathrm{mw} / \mathrm{cc}$.
With a $50 \%$ duty cycle the average power loss is $195 \mathrm{mw} / \mathrm{cc}$. This is an acceptable value for water cooling with edge cooled plates.

Another approach to generate a more useful set of curves is to have plots of flux density vs number of rings at a given frequency (the starting frequency) with peak voltage as a parameter. Three curves are presented for each starting frequency for the difference in inner and outer radii of 10 cm , 12.5 cm and 15 cm , for 178.5 KHz and also for 675 Hz .

The curves are used by selecting a power level which considers the cooling system and the duty cycle. The flux density for this condition is found from measured data and, for the voltage desired, the number of rings are determined. Similar curves can be readily made for any set of conditions.

Figure IV $\mathrm{A}, \mathrm{B}, \mathrm{C}$ is for a starting frequency of 0.1785 MHz .
Figure $V A, B, C$ is for a starting frequency of 0.675 MHz .
Figure VI A,B,C is for a starting frequency of 2.5 MHz .
The data are presented in appendix III.

TDK SY7-smailsample data. (DATA- MIKE GOLDMAN)

|  |
| :--- | :--- | :--- |








$f=0.675 \mathrm{MH}_{3} r_{2}-r_{1}=15 \mathrm{~cm}$
 $\begin{array}{r}7 \\ 7 \\ +\quad+1 \\ +1 \\ \hline\end{array}$
 *
$\qquad$
 1 1 , Z


## Cox mis

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## 20




$f=2.5 \mathrm{mit} \quad r_{2}-r_{i}=15 \mathrm{~cm}$

 llan














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$\square$--

## APPENDIX I

Cavity I: $\omega=2 \pi \mathrm{f}=1.1 \mathrm{x} 10^{6}$ (Data was taken at 175 KHz but 178.5 KHz was used in the evaluations.)
$B A=\frac{1.7 \times 10^{4} \times 10^{8}}{1.1 \times 10^{6}}=1.515 \times 10^{6}$

| $r_{2} \quad r_{1}$ | N | A | B | $\mathrm{mw} / \mathrm{cc}$ |
| :---: | :---: | :---: | :---: | :---: |
| $50 \quad 30$ | 44 | 1100 | 1409 | excessive |
| $r_{2}-r_{1}=10$ | 48 | 1200 | 1292 | excessive |
|  | 52 | 1300 | 1192 | 970 |
|  | 56 | 1400 | 1107 | 840 |
|  | 60 | 1500 | 1033 | 720 |
|  | 64 | 1600 | 969 | 625 |
|  | 68 | 1700 | 911 | 550 |
|  | 72 | 1800 | 861 | 500 |
|  | 76 | 1900 | 816 | 435 |
|  | 80 | 2000 | 775 | 390 |
| $50 \quad 25$ | 44 | 1375 | 1127 | 870 |
|  | 48 | 1500 | 1033 | 720 |
| $\mathrm{r}_{2}-\mathrm{r}_{1}=12.5$ |  |  |  |  |
|  | 52 | 1625 | 953 | 610 |
|  | 56 | 1750 | 886 | 520 |
|  | 60 | 1875 | 826 | 440 |
|  | 64 | 2000 | 775 | 390 |
|  | 68 | 2125 | 729 | 345 |
|  | 72 | 2250 | 689 | 310 |
|  | 76 | 2375 | 652 | 270 |
| $50 \quad 20$ | 44 | 1650 | 939 | 590 |
|  | 48 | 1800 | 861 | 500 |
| $r_{2}-r_{1}=15$ | 52 | 1950 | 795 | 415 |
|  | 56 | 2100 | 738 | 365 |
|  | 60 | 2250 | 689 | 310 |
|  | 64 | 2400 | 646 | 275 |
|  | 68 | 2550 | 608 | 235 |
|  | 72 | 2700 | 574 | 205 |
|  | 76 | 2850 | 544 | 185 |

APPENDIX II
Cavity II: $\omega=4.24 \times 10^{6}, B A=4.01 \times 10^{5}$

| $r_{2}-r_{1}$ | $N$ | $A$ | $B$ | $m w / c c$ |
| :---: | :---: | :---: | :---: | :---: |
| 10 | 44 | 1100 | 364 | 890 |
|  | 48 | 1200 | 334 | 750 |
|  | 52 | 1300 | 308 | 630 |
|  | 56 | 1400 | 286 | 550 |
|  | 60 | 1500 | 267 | 470 |
|  | 64 | 1600 | 251 | 425 |
|  | 68 | 1700 | 236 | 375 |
|  | 72 | 1800 | 223 | 325 |
|  | 76 | 1900 | 211 | 295 |
|  | 80 | 2000 | 200 | 255 |
| 12.5 | 44 | 1375 | 292 | 570 |
|  | 48 | 1500 | 267 | 470 |
|  | 52 | 1625 | 247 | 410 |
|  | 56 | 1750 | 220 | 350 |
|  | 60 | 1815 | 214 | 305 |
|  | 64 | 2000 | 200 | 255 |
|  | 68 | 2125 | 189 | 235 |
|  | 72 | 2250 | 178 | 208 |
|  | 76 | 2375 | 169 | 190 |
| 15 | 44 | 1650 | 243 | 400 |
|  | 48 | 1800 | 223 | 335 |
|  | 52 | 1950 | 206 | 285 |
|  | 56 | 2100 | 191 | 245 |
|  | 60 | 2250 | 178 | 208 |
|  | 64 | 2400 | 167 | 180 |
|  | 68 | 2550 | 157 | 160 |
|  | 72 | 2700 | 143 | 143 |
|  | 76 | 2850 | 141 | 130 |

## APPENDIX III

| $V=\omega B A \times 10^{-8}$ |  |  |  | $\mathrm{N}=$ Number of 2.5 cm rings |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $B=\frac{V \times 10^{8}}{V}=\frac{V \times 10^{8}}{}$ |  |  |  |  |  |  |
| $\omega \mathrm{A}=\frac{}{2 \pi f N \times 2.5\left(r_{2}-r_{1}\right)}$ |  |  |  |  |  |  |
|  |  | $\frac{366 v_{k v}}{4 H z\left(r_{2}-r_{1}\right.}$ | $\frac{1}{\mathrm{~N}}$ |  |  |  |
| $r_{2}-r_{1}=10 \quad f=.1785$ |  |  |  |  |  |  |
| $B=\frac{3566}{N} V_{K V}$ |  |  |  |  |  |  |
| N | $\mathrm{B}(9 \mathrm{KV})$ | $\mathrm{B}(11 \mathrm{KV})$ | B(13KV) | B(15 KV) | B(17KV) | B(19 KV) |
| 44 | 729 | 892 | 1054 |  |  |  |
| 48 | 669 | 817 | 965 | 1114 |  |  |
| 52 | 617 | 754 | 892 | 1029 |  |  |
| 56 | 573 | 701 | 828 | 955 | 1082 |  |
| 60 | 535 | 654 | 773 | 892 | 1020 | 1129 |
| 64 | 502 | 613 | 724 | 836 | 947 | 1059 |
| 68 | 472 | 577 | 682 | 787 | 892 | 996 |
| 72 | 446 | 545 | 64.4 | 743 | 842 | 941 |
| $\mathrm{r}_{2}-\mathrm{r}_{1}=12.5 \quad \mathrm{f}=.1785 \quad \mathrm{~B}=\frac{2853 \mathrm{~V}_{K V}}{\mathrm{~N}}$ |  |  |  |  |  |  |
| N | B (9 KV) | $B(11 \mathrm{KV})$ | B(13 KV) | B(15 KV) | $B(17 \mathrm{KV})$ | $\mathrm{B}(19 \mathrm{KV})$ |
| 44 | 584 | 713 | 843 | 972 | 1102 | 1232 |
| 48 | 535 | 654 | 773 | 892 | 1010 | 1129 |
| 52 | 494 | 604 | 713 | 823 | 933 | 1042 |
| 56 | 459 | 560 | 662 | 764 | 866 | 968 |
| 60 | 428 | 523 | 618 | 713 | 808 | 903 |
| 64 | 401 | 490 | 580 | 669 | 758 | 847 |
| 68 | 378 | 462 | 545 | 629 | 713 | 797 |
| 72 | 357 | 436 | 515 | 594 | 674 | 753 |




$$
\begin{aligned}
& r_{2}-r_{1}=12.5 \quad f=2.5 \mathrm{MHz} \quad B=\frac{203.7 \mathrm{~V}}{\mathrm{~N}}
\end{aligned}
$$

$$
\begin{aligned}
& r_{2}-r_{1}=15 \quad B=\frac{169.7 \mathrm{~V}}{\mathrm{~N}} \quad \mathrm{f}=2.5 \mathrm{MHz}
\end{aligned}
$$

