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# Land Mobile Satellite Channel Modeling

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# Outline

- Introduction
- L Band Channel Model
- Ka Band Channel Model
- Summary



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# Introduction

- Measurement program
- Measurement procedure
- Channel modeling procedure



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## L Band Channel Models

- Shadowed Rician Model
- Total Shadowed Model
- Shadowing on both LOS and Multipath Model
- Lognormal Shadowing Model
- Empirical Roadside Shadowing Model and Extension
- High Elevation Angle Model



## Shadowed Rician Model

$$r \exp(j\theta) = z \exp(j\phi_0) + w \exp(j\phi)$$

$\phi_0$  and  $\phi$  are uniformly  
distributed

$z$  is lognormal

$w$  is Rayleigh



When  $z$  is constant and  $z = A$ , this is Rician.

$$p_R(r) = r/b_0 \exp[-(r^2 + A^2)/2b_0] I_0(rA/b_0)$$

When there is shadowing,  $z$ , but, no  
multipath fading,  $w = 0$ ,

$$p(r) = 1/(r\sqrt{2\pi d_0}) \exp[-(\ln r - \mu)^2/2d_0]$$

When there is no shadowing and no LOS  
component,  $z = 0$ ,

$$p(r) = r/b_0 \exp(-r^2/2b_0)$$



## Shadowed Rician Model

$$p(r) = r / (b_0 \sqrt{2\pi d_0} \int_0^\infty 1/z$$
$$\exp[-(\ln z - \mu)^2 / 2d_0$$
$$-(r^2 + z^2) / 2b_0] I_0(rz/b_0) dz$$

where  $\mu$  and  $d_0$  are the mean and variance  
 $b_0$  represents the average scattered power  
 $I_0(\cdot)$  is the modified Bessel function of zeroth  
order.



## Total Shadowing Model

Let  $S = r^2$  and  $S_0 = b_0$

$$p_{Rice}(S) = K \exp[-K(S+1)] I_0(2K\sqrt{S})$$

where  $K$  is the ratio of LOS power to multi-path power

$$p_{Ray}(S/S_0) = \frac{1}{S_0} \exp(-S/S_0)$$

$$p_{LN}(S_0) = \frac{10}{\sqrt{2\pi d_0 \ln 10}} \frac{1}{S_0} \exp\left[-\frac{(10 \log S_0 - \mu)^2}{2d_0}\right]$$

where  $\mu$  is the mean and  $d_0$  is the variance due to shadowing.





$$p(S) = (1 - F)p_{Rice}(S) + F \cdot \int_0^{\infty} p_{Ray}(S/S_0) p_{LN}(S_0) dS_0.$$

The values of  $F$  and model parameters are given in their paper.



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## Lognormal Shadowing Model

$$P(r) = (1 - F) P_{Rice}(r) + F P_{Loo}(r)$$

where  $P_{Rice}(r)$  denotes the Rician model and  $P_{Loo}(r)$  denotes the shadowed Rician model.  $F$  is the percentage of shadowed conditions.



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## Shadowing of LOS and Multipath Model

$$p(r) = \int_0^{\infty} \frac{1}{z} p_R(r/z) p(z) dz$$

## Shadowing Rician Model

$$p(r) = \int_0^{\infty} p_R(r/z) p(z) dz$$



$K$ ,  $\mu$  and  $\sqrt{d}$  as a function of  $\alpha$   
valid in the range  $20^\circ < \alpha < 80^\circ$ :

$$K(\alpha) = K_0 + K_1\alpha + K_2\alpha^2$$

$$\mu(\alpha) = \mu_0 + \mu_1\alpha + \mu_2\alpha^2 + \mu_3\alpha^3$$

$$\sqrt{d}(\alpha) = \alpha_0 + \sqrt{d_1}\alpha.$$



## Conditions of comparison

Model	Frequency(MHz)	Elevation (deg)
Shadowed Rician	870	15
Total shadowing	1540	24

For city  $F = 0.79$   
For highway  $F = .19$

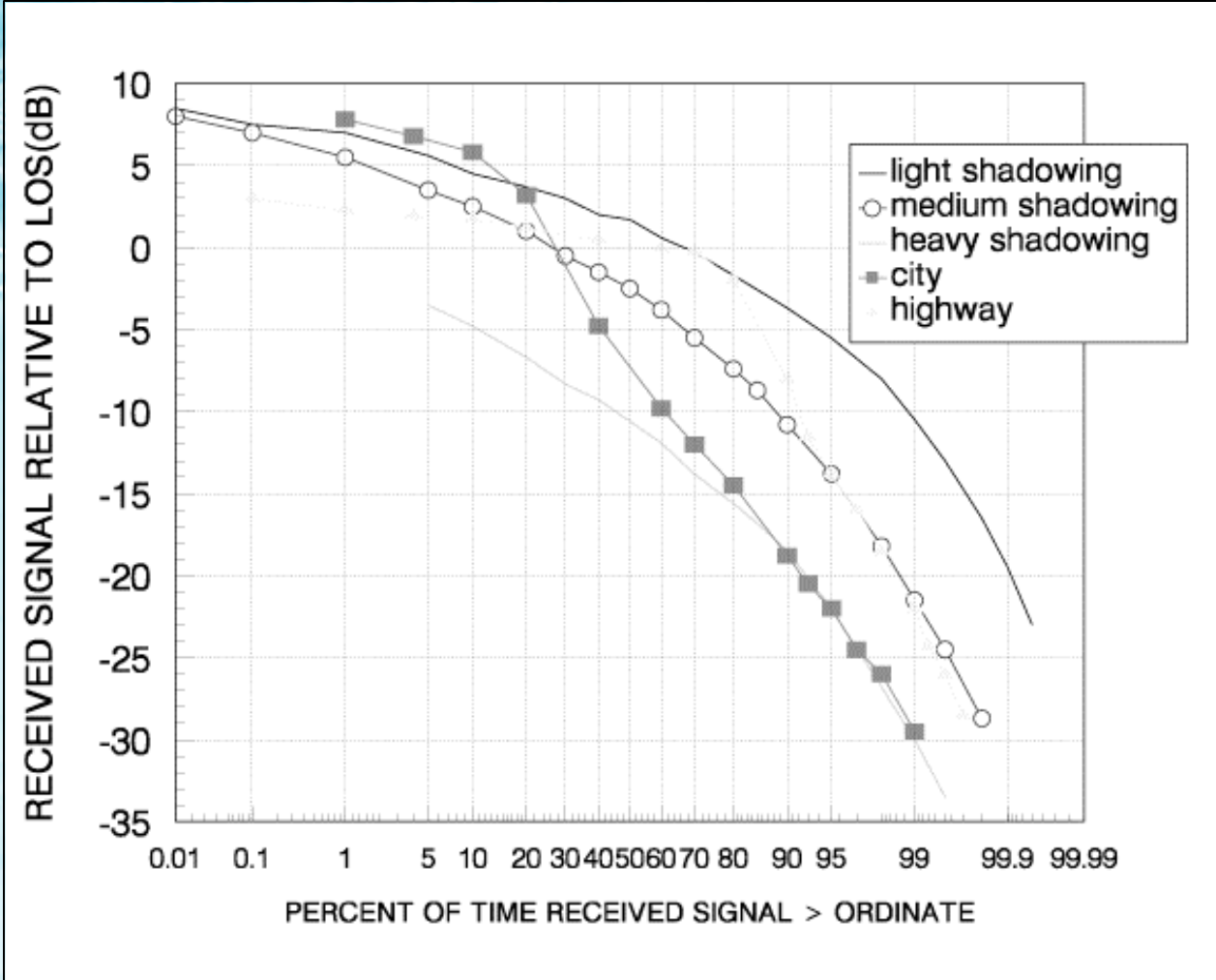


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## Ka Band Measurement

- Elevation angle to Olympus:  $14.2^\circ$
- Transmit frequency(GHz): 28.07225
- Receive frequency(GHz): 18.925
- Weather conditions: cloudy with sunny break



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## Ka Band Channel Models

- Gaussian Model for Fixed Channel  
(weather conditions)
- Shadowed Rician Model for Mobile Channel





## Ka Band Fixed and Mobile Channel Model

$$p(r) = p_w(r) \cdot p_{Loo}(r)$$

$$p_w(r) = \frac{1}{\sqrt{2\pi} \sigma_w} \exp\left(-\frac{(r - m_w)^2}{2\sigma_w^2}\right)$$

where  $m_w$  and  $\sigma_w^2$  are the mean and variance respectively

$p_{Loo}(r)$  is the shadowed Rician model



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## Signal Phase Model for both Fixed and Mobile is Gaussian

$$p(\phi) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(\phi - m)^2}{2\sigma^2}\right)$$

where  $m$  and  $\sigma^2$  are the mean and variance of  
the signal phase model

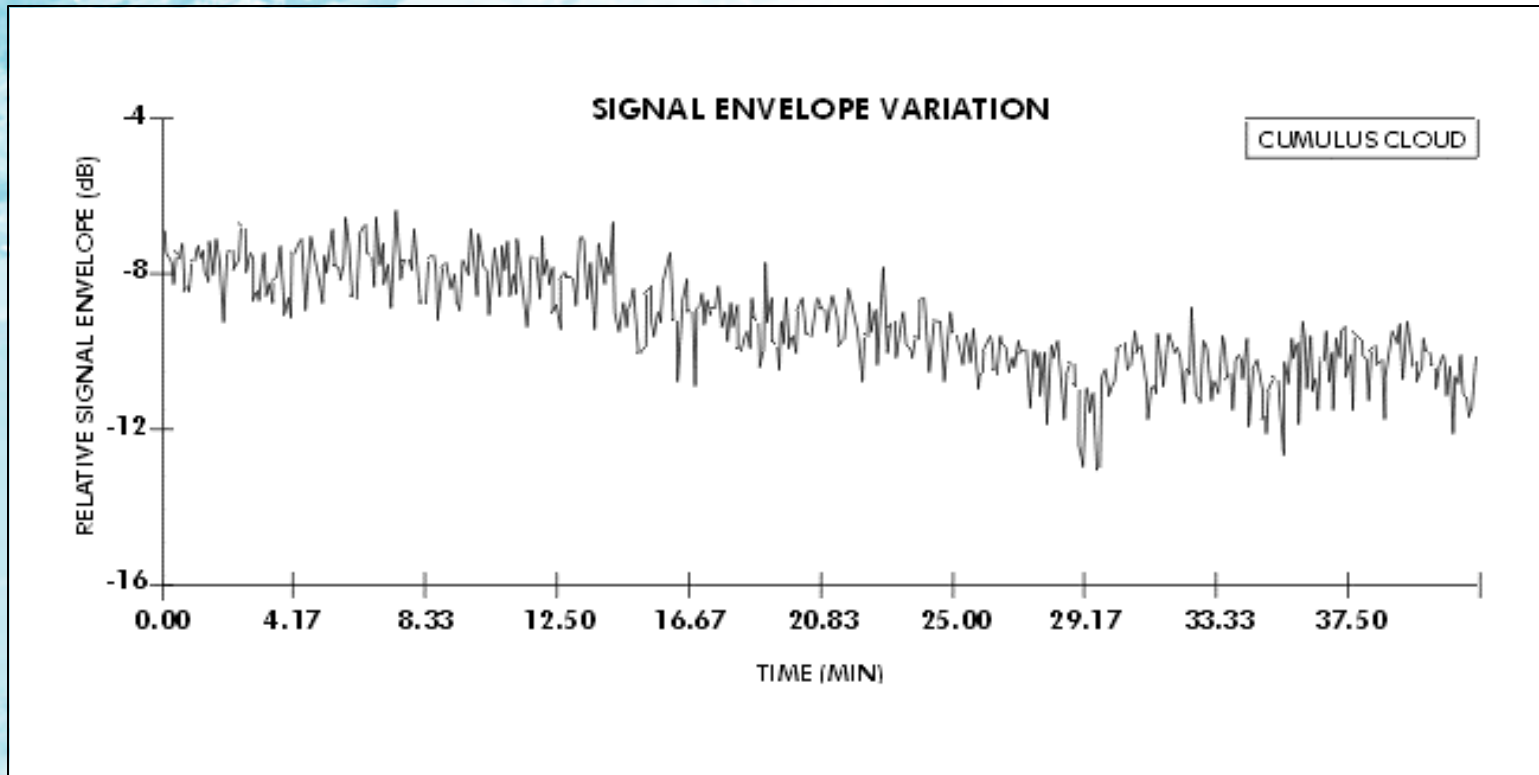


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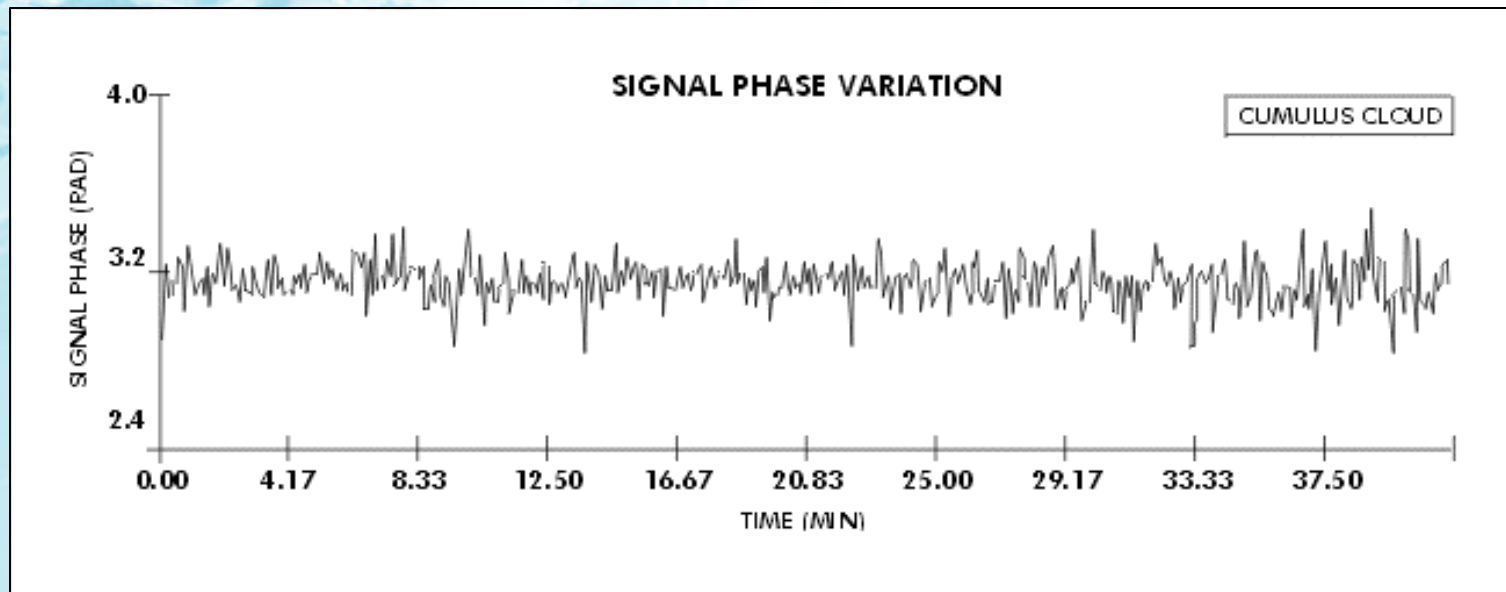


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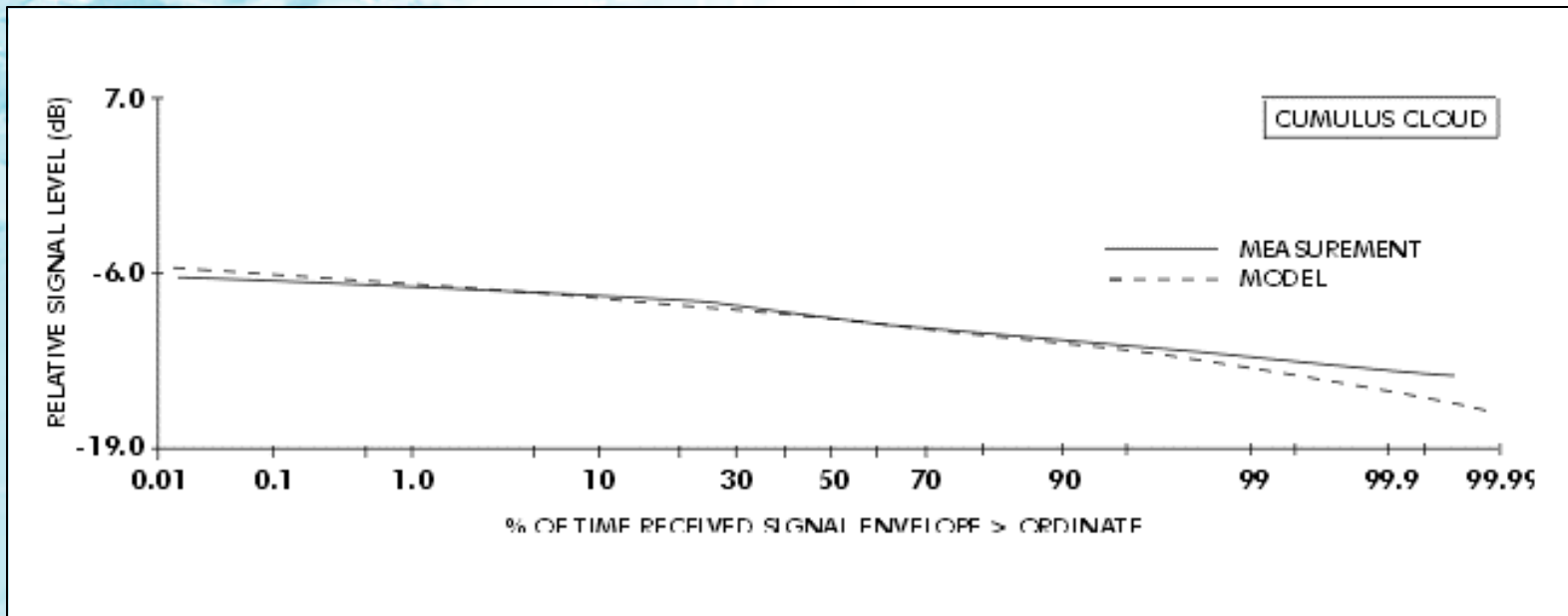


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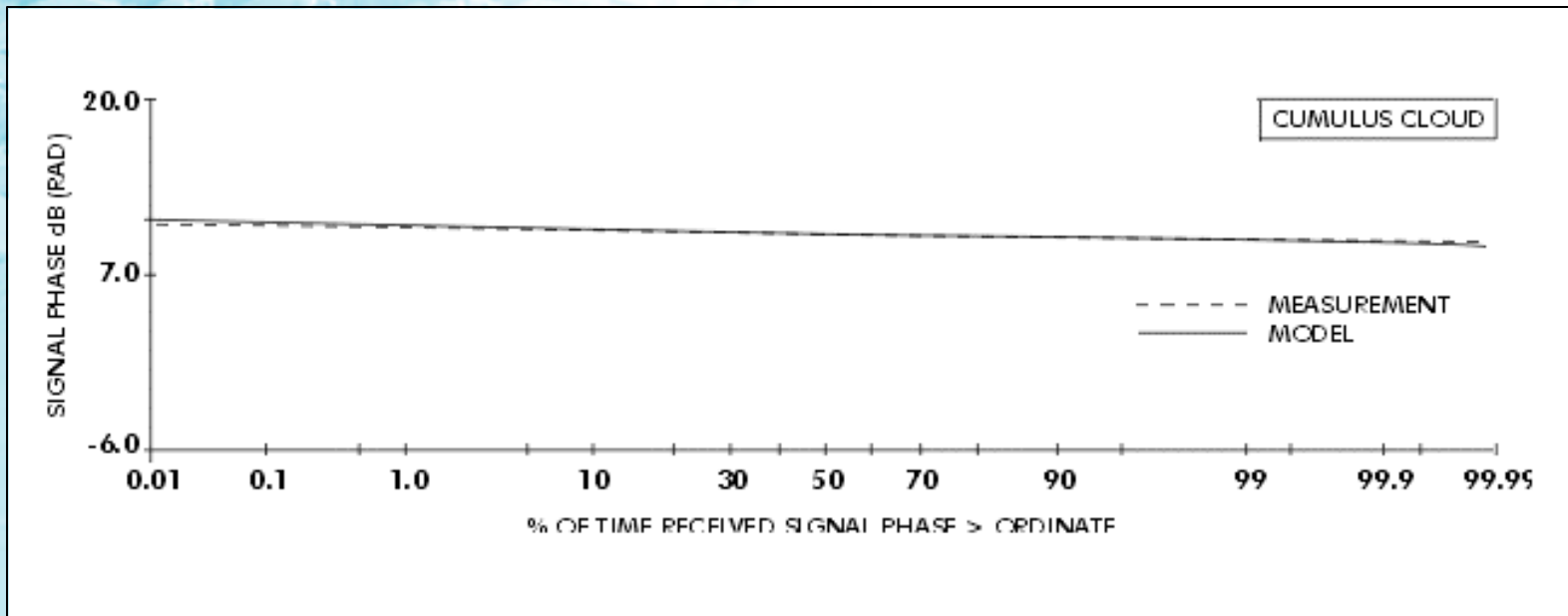


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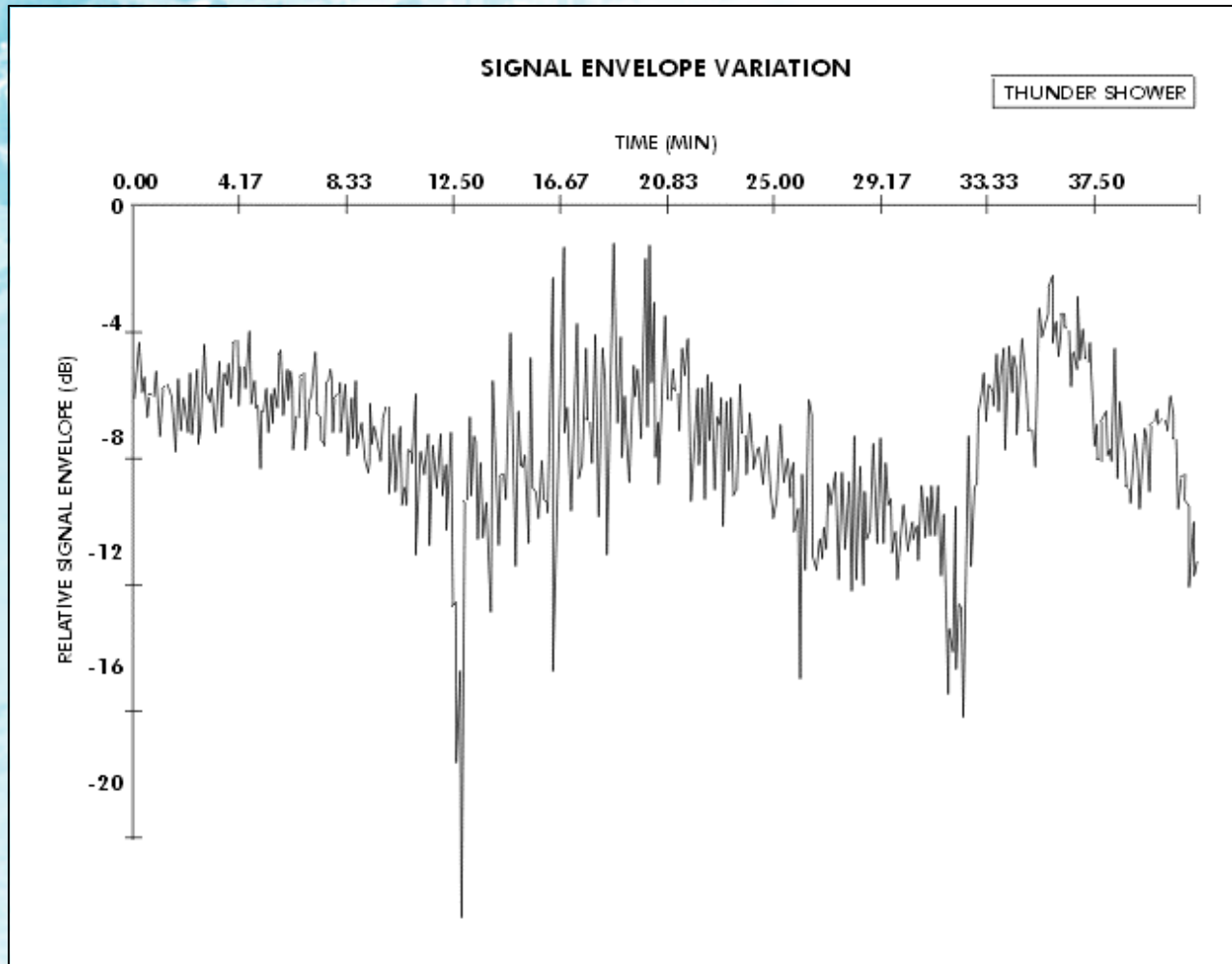


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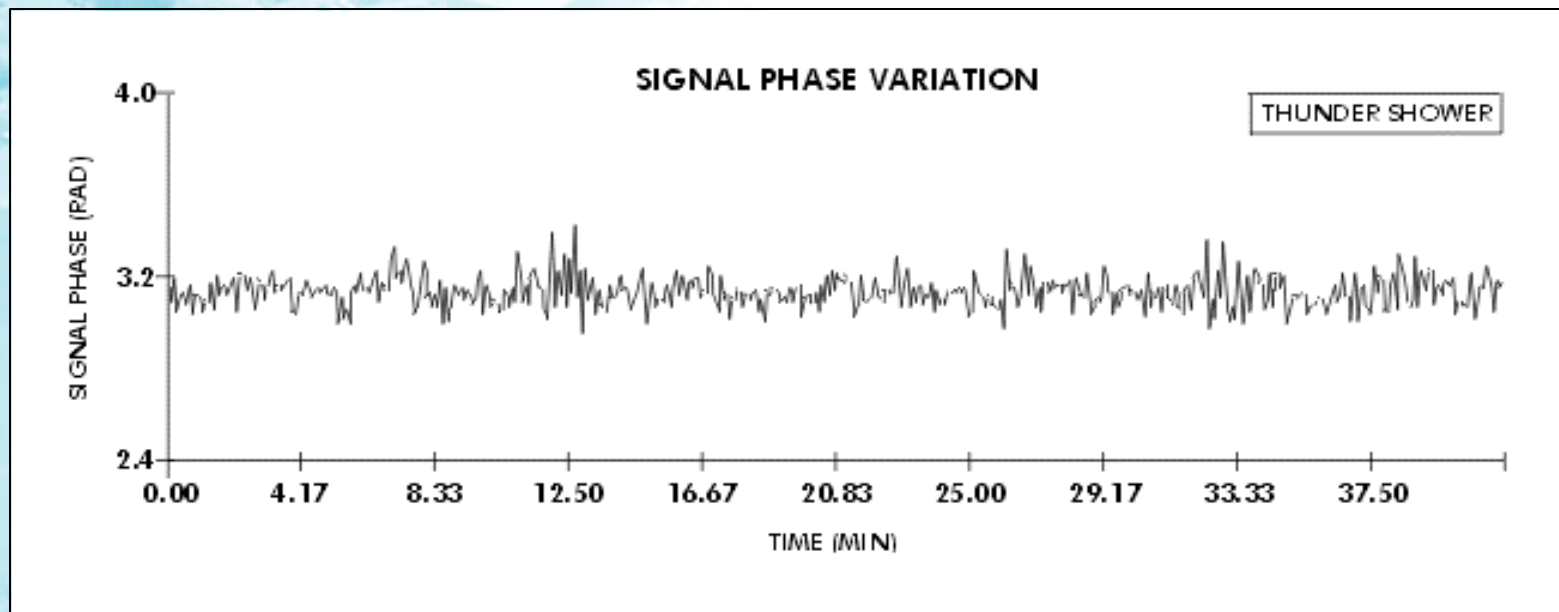


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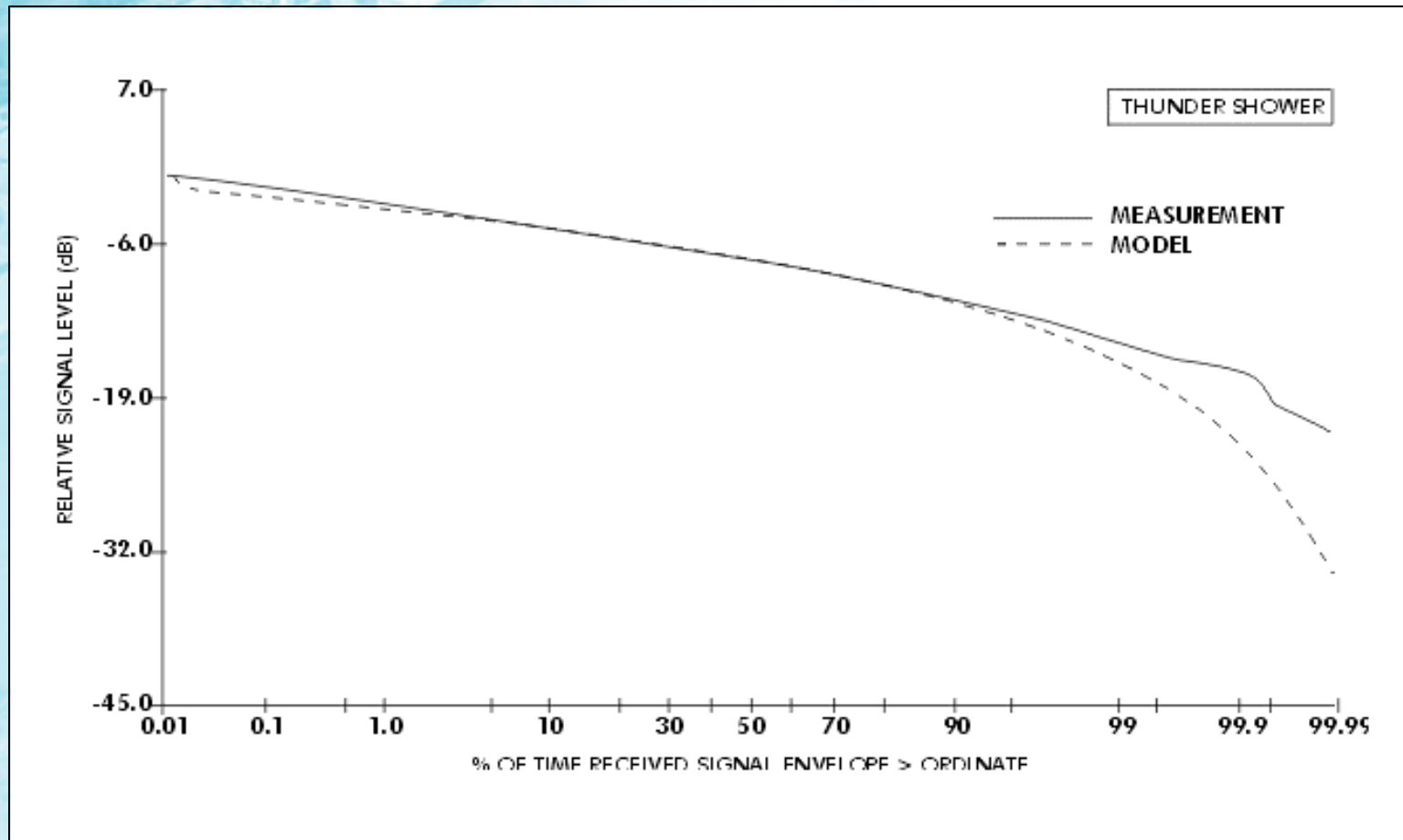


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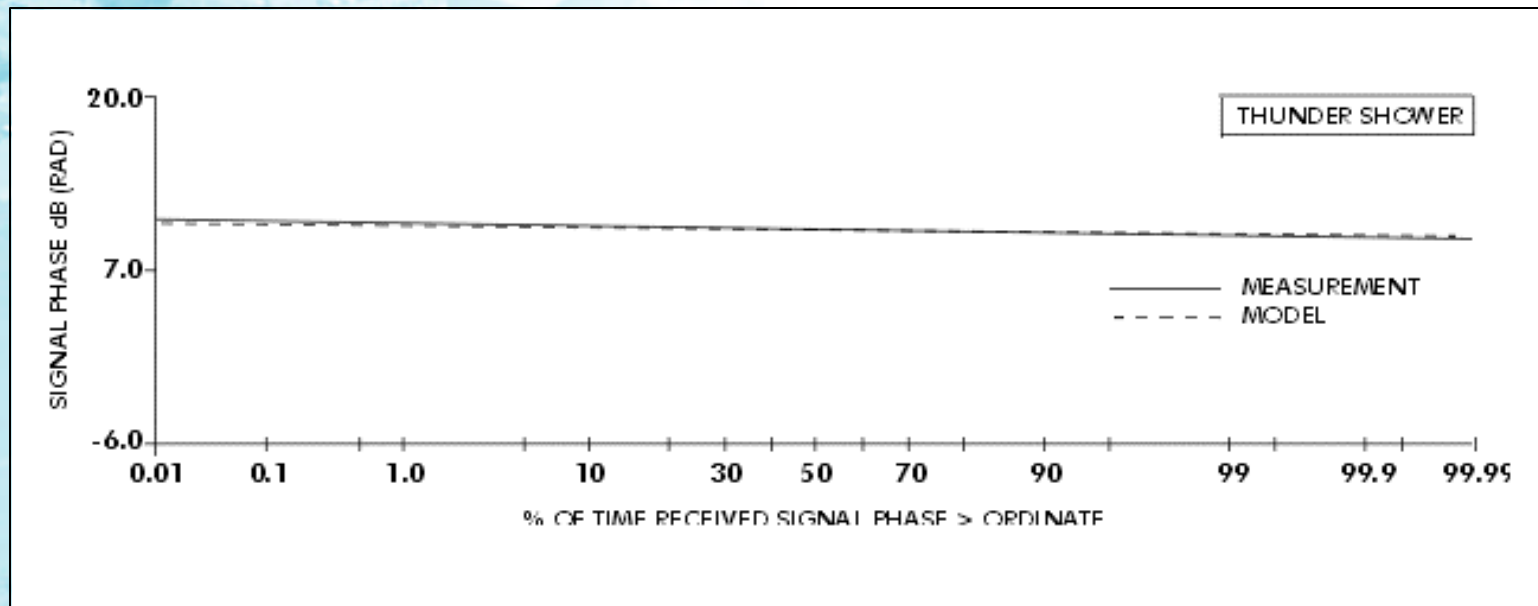


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## Signal Envelope Model Parameters

Weather conditions	mean*	variance
Cumulus cloud	0.346	0.00272
Thunder shower	0.436	0.01386
Ice pellets	0.482	0.00062

\*nominal signal envelope level is 1. volt

## Signal Phase Model Parameters

Weather conditions	mean(rad)	variance(rad <sup>2</sup> )
Cumulus cloud	0.0154	0.00864
Thunder shower	0.0068	0.00414
Ice pellets	0.0094	0.00544

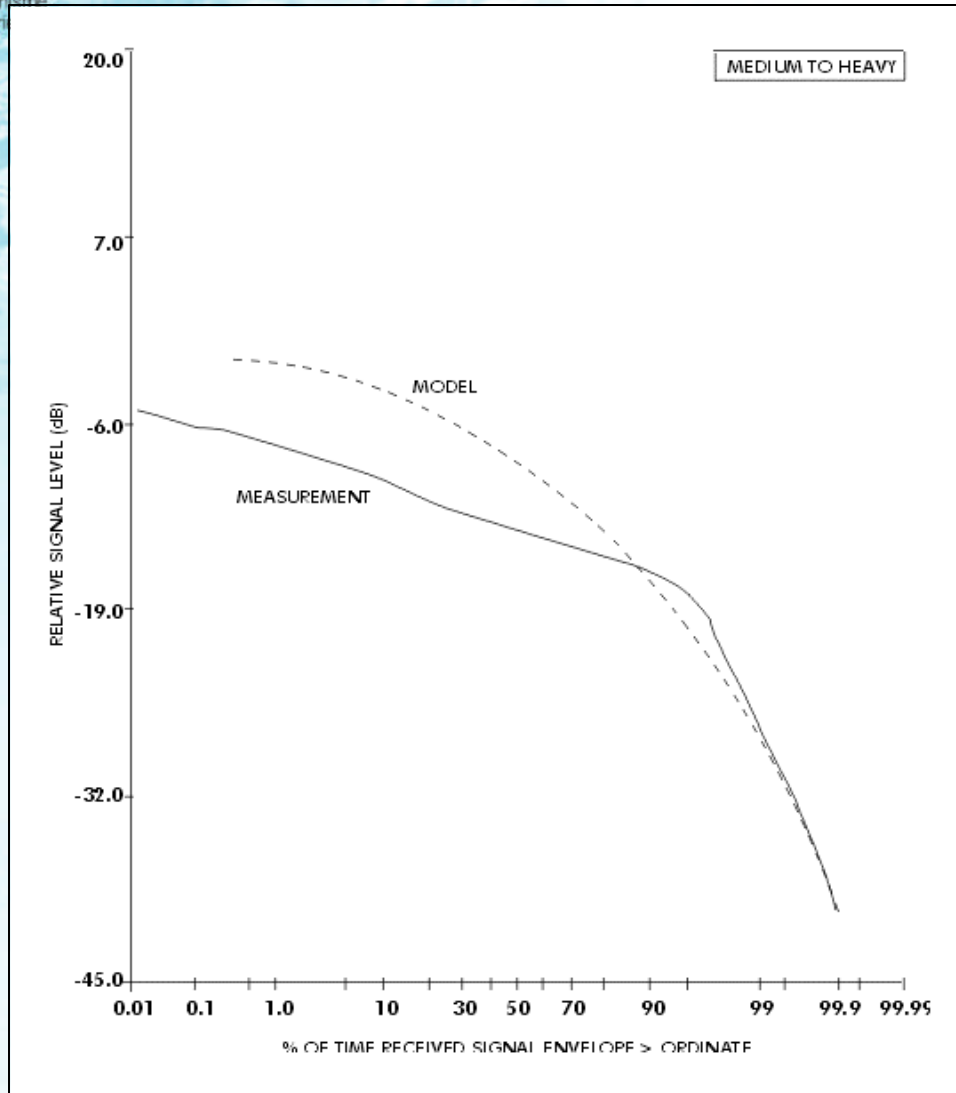


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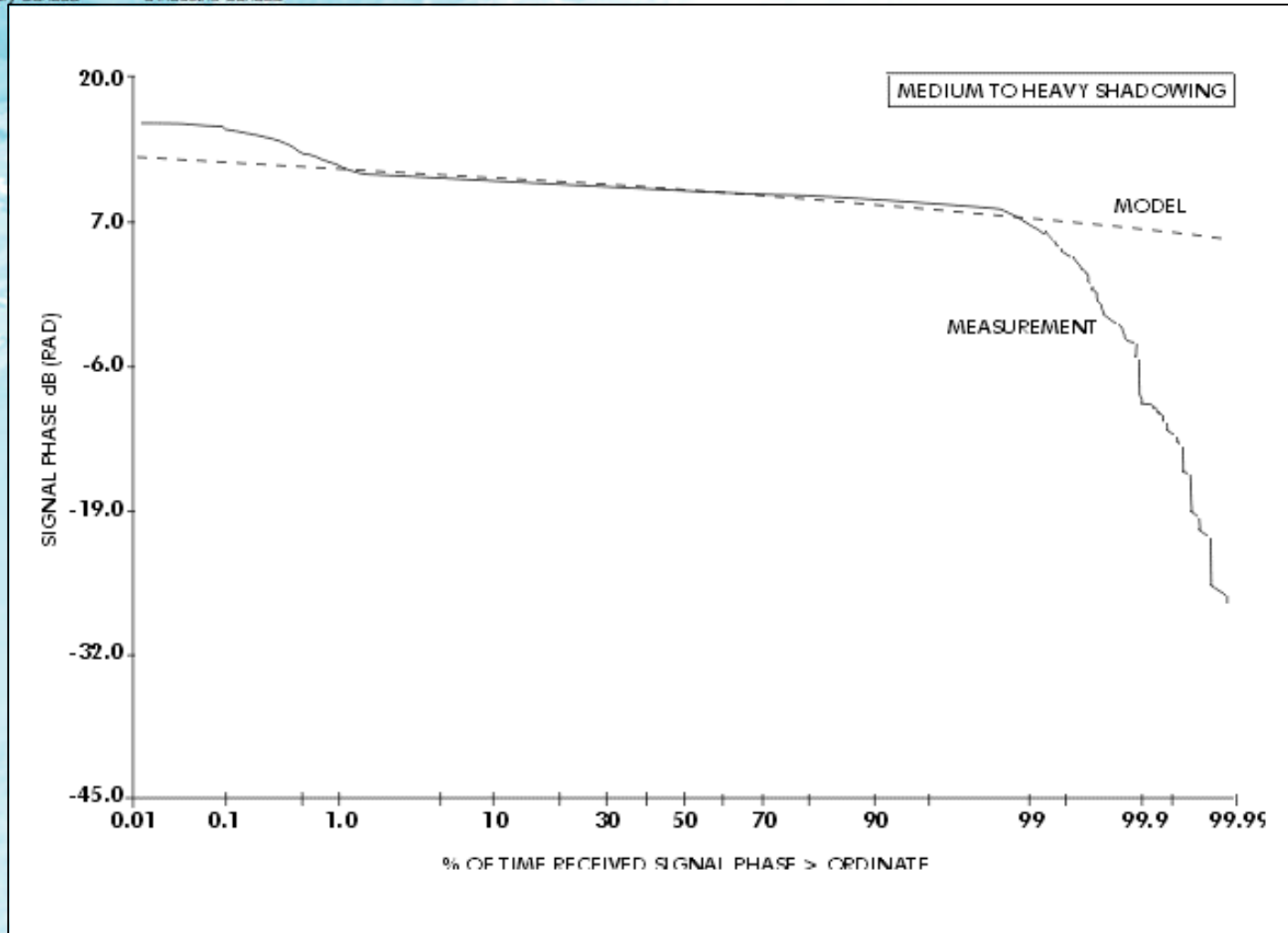


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## Ka Band Mobile Channel Medium-to-Heavy Shadowing Conditions

### Signal Envelope Model Parameters

$$\mu = -2.30 \quad \sqrt{d_0} = 0.046 \quad b_0 = 0.10$$

### Signal Phase Model Parameters

$$m = -0.0144 \quad \sigma^2 = 0.1124$$



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## Summary

- Described various channel models
- Compared measured and modeling results
- Provided modeling parameters for the shadowed Rician model and some weather conditions



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