2. ASTROPHYSICAL CONSTANTS

Table 2.1. Revised 1997 by D.E. Groom (LBNL) with the help of G.F. Smoot, M.S. Turner, and R.C. Willson. The figures in parentheses after some values give the one-standard deviation uncertainties in the last digit(s). While every effort has been made to obtain the most accurate current values of the listed quantities, the table does not represent a critical review or adjustment of the constants, and is not intended as a primary reference.

Quantity	Symbol, equation	Value	Reference
speed of light	с	$299792458 \mathrm{\ m\ s}^{-1}$	defined Ref. [1]
Newtonian gravitational constant	G_N	$6.67259(85) \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$	Ref. [2]
astronomical unit	AU	$1.4959787066(2) \times 10^{11}$ m	Ref. [3,4]
tropical year (equinox to equinox) (1994)	yr	$31556925.2~{ m s}$	Ref. [3]
sidereal year (fixed star to fixed star) (1994)		$31558149.8~{ m s}$	Ref. [3]
mean sidereal day		$23^{h}56^{m}04.09053$	Ref. [3]
Jansky	Jy	$10^{-26} \mathrm{W} \mathrm{m}^{-2} \mathrm{Hz}^{-1}$	
Planck mass	$\sqrt{\hbar c/G_N}$	$\begin{array}{l} 1.221047(79)\times10^{19}~{\rm GeV}/c^2\\ = 2.17671(14)\times10^{-8}~{\rm kg} \end{array}$	uses Ref. $[2]$
parsec $(1 \text{ AU}/1 \text{ arc sec})$	\mathbf{pc}	$3.0856775807(4) \times 10^{16}$ m = 3.262 ly	Ref. [5]
light year (deprecated unit)	ly	0.3066 pc = 0.9461×10^{16} m	
Schwarzschild radius of the Sun	$2G_N M_{\odot}/c^2$	$2.95325008~{ m km}$	Ref. [6]
solar mass	M_{\odot}	$1.98892(25) \times 10^{30} \text{ kg}$	Ref. [7]
solar luminosity	L_{\odot}	$(3.846 \pm 0.008) \times 10^{26} \text{ W}$	Ref. [8]
solar equatorial radius	$\stackrel{\smile}{R_{\odot}}$	$6.96 \times 10^8 \text{ m}$	Ref. [3]
Earth equatorial radius	$\stackrel{\smile}{R_{\oplus}}$	$6.378140 \times 10^6 \text{ m}$	Ref. [3]
Earth mass	$\stackrel{\smile}{M_\oplus}$	$5.97370(76) imes 10^{24} \text{ kg}$	Ref. [9]
luminosity conversion	L	$3.02 \times 10^{28} \times 10^{-0.4} M_b$ W	Ref. [10]
		$(M_b = absolute bolometric magnitude$	
		= bolometric magnitude at 10 pc)	
flux conversion	Ŧ	$2.52 \times 10^{-8} \times 10^{-0.4} {}^m_b \mathrm{W} \mathrm{m}^{-2}$	from above
		$(m_b = apparent bolometric magnitude)$	
v_{\odot} around center of Galaxy	Θ	$220(20) \text{ km s}^{-1}$	Ref. [11]
solar distance from galactic center	$\stackrel{\circ}{R_{\circ}}$	8.0(5) kpc	Ref. [12]
Service and Service control	100	() .	10011 [12]
Hubble expansion rate ^{\dagger}	H_0	$100 h_0 \text{ km s}^{-1} \text{ Mpc}^{-1}$ - $h_0 \times (0.778 13 \text{ Cyr})^{-1}$	Rof [12]
normalized Hubble expansion rate	ho	$-n_0 \times (9.17813 \text{ Gyr})$ 0.6 < ho < 0.8	Ref. $[13]$
critical density of the universe	$a = 3H^2/8\pi G M$	$2.775.366.27 \times 10^{11} h^2 M_{\odot} Mpc^{-3}$	101. [14]
critical density of the universe.	$p_c = 5\Pi_0/8\pi G_N$	$-1.878.82(24) \times 10^{-29} h^2 \text{ g cm}^{-3}$	
		$= 1.07002(24) \times 10^{-5} h^2 \text{ GeV cm}^{-3}$	
local disk density	0.11.1	$n_0 = 1.05554(15) \times 10^{-24} \text{ m}_0^{-3} \approx 2-7 \text{ GeV}/c^2 \text{ cm}^{-3}$	Ref [15]
local halo density	P disk	$2-13 \times 10^{-25} \text{ g cm}^{-3} \approx 0.1-0.7 \text{ GeV}/c^2 \text{ cm}^{-3}$	Ref [16]
pressureless matter density of the universe [†]	$\Omega_{M} = \rho_{M} / \rho_{0}$	$0.2 \le \Omega_M \le 1$	Ref [17]
scaled cosmological constant [†]	$\Omega_M = \rho_M/\rho_c$ $\Omega_A = \Lambda c^2/3H^2$	$-1 < \Omega_{\Lambda} < 2$	Ref [18]
scale factor for cosmological constant [†]	$a_{\Lambda}^{2} = nc / 6n_{0}^{2}$	$2853 \times 10^{51} h^{-2} m^2$	Iton [10]
scale factor for cosmological constant	c / 511 ₀	$2.000 \times 10^{-10} m_0$	D.f. [10]
age of the universe	t_0	$11.3 + 1 \pm 1.3$ Gyr	Ref. [19]
	$\Omega_0 n_0^-$ for $\Lambda = 0$	$\leq 2.4 \text{ for } t_0 \geq 10 \text{ Gyr}$ $\leq 1 \text{ for } t \geq 10 \text{ Cyr}$ $h \geq 0.4$	Ref. [10]
		$\leq 1 \text{ for } t_0 \geq 10 \text{ Gyr}, \ h_0 > 0.4$	$\mathbf{Rel.} [10]$
CDD) to show on the disting (CDD) to see the	t T	$\leq 0.53 \text{ for } t_0 \geq 10 \text{ Gyr}, n_0 > 0.0$	Ref. $[20]$
cosmic background radiation (CBR) temperatur	e' 10	2.728 ± 0.002 K	Ref. [21,22]
solar velocity with respect to CBR		309.3 ± 2.5 km s $^{-1}$	Ref. [22,23]
energy density of CBR	$ ho_\gamma$	$4.662.3 \times 10^{-0.1} (T/2.728)^4$ g cm $^{-3}$ = 0.261 53 $(T/2.728)^4$ eV cm $^{-3}$	Ref. [10,22]
energy density of relativistic particles (CBR + ν)) ρ_R	$7.8388 \times 10^{-34} (T/2.728)^4 \text{ g cm}^{-3}$	Ref. [10,22]
much an also sites of CDD		$= 0.439 (2 (1 / 2.128)^{2} \text{ eV cm}^{-3}$	D.f. [10.00]
number density of UBR photons	n_{γ}	$411.87 (1/2.728)^{\circ} \text{ cm}^{\circ}$ 2.800.2 (77/2.728)3 =3	Kei. [10,22]
entropy density/Boltzmann constant	s/κ	$2899.3(1/2.(28)^\circ\mathrm{cm}^\circ)$	Kei. [10]

[†] Subscript 0 indicates present-day values.

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- 1. B.W. Petlev, Nature **303**, 373 (1983).
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In the context of the scale dependence of field theoretic quantities, it should be remarked that absolute lab measurements of G_N have been performed only on scales of $10^{-1\pm 1}$ m.

- 3. The Astronomical Almanac for the year 1994, U.S. Government Printing Office, Washington, and Her Majesty's Stationary Office, London (1993). Where possible, the values as adjusted for the fitting of the ephemerides to all the observational data are used.
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- 1 AU divided by $\pi/648000$; quoted error is from the JPL 5. Planetary Ephemerides value of the AU [4].
- 6. Heliocentric gravitational constant from Ref. 3 times $2/c^2$. The given 9-place accuracy appears to be consistent with uncertainties in actually defining the earth's orbital parameters.
- 7. Obtained from the heliocentric gravitational constant [3] and G_N [2]. The error is the 128 ppm standard deviation of G_N .
- 1996 mean total solar irradiance (TSI) = 1367.5 ± 2.7 [24]; the 8. solar luminosity is $4\pi \times (1 \text{ AU})^2$ times this quantity. This value increased by 0.036% between the minima of solar cycles 21 and 22. It was modulated with an amplitude of 0.039% during solar cycle 21 [25].

Sackmann et al. [26] use TSI = 1370 ± 2 W m⁻², but conclude that the solar luminosity $(L_{\odot} = 3.853 \times 10^{26} \text{ J s}^{-1})$ has an uncertainty of 1.5%. Their value is based on three 1977-83 papers, and they comment that the error is based on scatter among the reported values, which is substantially in excess of that expected from the individual quoted errors.

The conclusion of the 1971 review by Thekaekara and Drummond [27] $(1353 \pm 1\% \text{ W m}^{-2})$ is often quoted [28]. The conversion to luminosity is not given in the Thekaekara and Drummond paper, and we cannot exactly reproduce the solar luminosity given in Ref. 28.

Finally, a value based on the 1954 spectral curve due to Johnson [29] $(1395 \pm 1\% \text{ W m}^{-2}, \text{ or } L_{\odot} = 3.92 \times 10^{26} \text{ J s}^{-1})$ has been used widely, and may be the basis for higher value of the solar luminosity and corresponding lower value of the solar absolute bolometric magnitude (4.72) still common in the literature [10].

- 9. Obtained from the geocentric gravitational constant [3] and G_N [2]. The error is the 128 ppm standard deviation of G_N .
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papers setting limits on WIMP mass limits, e.g. in M. Mori et al., Phys. Lett. **B289**, 463 (1992).

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