## 2. ASTROPHYSICAL CONSTANTS

**Table 2.1**. Revised 1997 by D.E. Groom (LBNL) with the help of G.F. Smoot, M.S. Turner, and R.C. Willson. The figures in parentheses after some values give the one-standard deviation uncertainties in the last digit(s). While every effort has been made to obtain the most accurate current values of the listed quantities, the table does not represent a critical review or adjustment of the constants, and is not intended as a primary reference.

speed of light

Value:  $299792458 \text{ m s}^{-1}$ defined Ref. [1]

Newtonian gravitational constant

Value:  $6.67259(85) \times 10^{-11} \,\mathrm{m}^3 \,\mathrm{kg}^{-1} \,\mathrm{s}^{-2}$  Ref. [2]

astronomical unit AU

Value:  $1.495\,978\,706\,6(2) \times 10^{11}$  m Ref. [3,4]

tropical year (equinox to equinox) (1994)

Value: 31 556 925.2 s Ref. [3]

sidereal year (fixed star to fixed star) (1994)

Value: 31 558 149.8 s Ref. [3]

mean sidereal day

Value:  $23^{\rm h} 56^{\rm m} 04.09053$  Ref. [3]

Jansky

Value:  $10^{-26} \text{ W m}^{-2} \text{ Hz}^{-1}$ 

 $\sqrt{\hbar c/G_N}$ Planck mass

Value:  $1.221\,047(79) \times 10^{19} \,\mathrm{GeV}/c^2$  uses Ref. [2]

 $= 2.17671(14) \times 10^{-8} \text{ kg}$ Value:

parsec (1 AU/1 arc sec) рс

Value:  $3.0856775807(4) \times 10^{16} \text{ m} = 3.262...\text{ly} \text{ Ref. [5]}$ 

light year (deprecated unit) ly

Value: 0.3066... pc =  $0.9461... \times 10^{16}$  m

 $2G_N M_{\odot}/c^2$ Schwarzschild radius of the Sun

Value: 2.953 250 08 km Ref. [6]

<sup>†</sup> Subscript 0 indicates present-day values.

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 $M_{\odot}$  solar mass

Value:  $1.98892(25) \times 10^{30}$  kg Ref. [7]

 $L_{\odot}$  solar luminosity

Value:  $(3.846 \pm 0.008) \times 10^{26}$  W Ref. [8]

 $R_{\odot}$  solar equatorial radius

Value:  $6.96 \times 10^8 \text{ m}^{-1} \text{ Ref. [3]}$ 

 $R_{\oplus}$  Earth equatorial radius

Value:  $6.378140 \times 10^6$  m Ref. [3]

 $M_{\oplus}$  Earth mass

Value:  $5.97370(76) \times 10^{24}$  kg Ref. [9]

L luminosity conversion

Value:  $3.02 \times 10^{28} \times 10^{-0.4} M_b$  W Ref. [10]

Value:  $(M_b = absolute bolometric magnitude$ 

Value: = bolometric magnitude at 10 pc)

 $\mathscr{F}$  flux conversion

Value:  $2.52 \times 10^{-8} \times 10^{-0.4} \, \text{m}_b \, \text{W m}^{-2}$  from above

Value:  $(m_b = \text{apparent bolometric magnitude})$ 

 $\Theta_{\circ}$   $oldsymbol{v}_{\odot}$  around center of Galaxy

Value:  $220(20) \text{ km s}^{-1} \text{ Ref. [11]}$ 

 $R_{\circ}$  solar distance from galactic center

Value: 8.0(5) kpc Ref. [12]

 $H_0$  Hubble expansion rate<sup>†</sup>

Value:  $100 h_0 \text{ km s}^{-1} \text{ Mpc}^{-1}$ 

Value:  $= h_0 \times (9.778 \, 13 \, \text{Gyr})^{-1} \, \text{Ref.} [13]$ 

 $h_0$  normalized Hubble expansion rate<sup>†</sup>

Value:  $0.6 < h_0 < 0.8$  Ref. [14]

 $<sup>^\</sup>dagger$  Subscript 0 indicates present-day values.

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ho_c=3H_0^2/8\pi G_N critical density of the universe<sup>†</sup> Value: 2.775\,366\,27\times10^{11}\,h_0^2\,M_\odot\mathrm{Mpc}^{-3}
   Value: = 1.87882(24) \times 10^{-29} h_0^2 \text{ g cm}^{-3}
   Value: = 1.05394(13) \times 10^{-5} h_0^2 \text{ GeV cm}^{-3}
   Value: 3-12 \times 10^{-24} \text{ g cm}^{-3} \approx 2-7 \text{ GeV}/c^2 \text{ cm}^{-3} Ref. [15]
                          local halo density
   Value: 2-13 \times 10^{-25} \text{ g cm}^{-3} \approx 0.1-0.7 \text{ GeV}/c^2 \text{cm}^{-3} \text{ Ref. [16]}
                                        pressureless matter density of the universe^{\dagger}
\Omega_M \equiv \rho_M/\rho_c
   Value: 0.2 < \Omega_M < 1 Ref. [17]
\begin{array}{ll} \Omega_{\Lambda} = \Lambda c^2/3H_0^2 & {\bf scaled\ cosmological\ constant}^{\dagger} \\ {\rm Value:} & -1 < \Omega_{\Lambda} < 2 & {\rm Ref.\ [18]} \end{array}
                               scale factor for cosmological constant ^{\dagger}
c^2/3H_0^2
   Value: 2.853 \times 10^{51} h_0^{-2} \text{ m}^2
                    age of the universe<sup>†</sup>
   Value: 11.5 + 1 \pm 1.5 Gyr Ref. [19]
\Omega_0 h_0^2 for \Lambda = 0
   Value: \leq 2.4 for t_0 \geq 10 Gyr Ref. [10]
   Value: \leq 1 \text{ for } t_0 \geq 10 \text{ Gyr}, h_0 > 0.4 \text{ Ref. } [10]
   Value: \leq 0.53 for t_0 \geq 10 Gyr, h_0 > 0.6 Ref. [20]
                      cosmic background radiation (CBR) temperature<sup>†</sup>
   Value: 2.728 \pm 0.002 \text{ K} Ref. [21,22]
                  solar velocity with respect to CBR
   Value: 369.3 \pm 2.5 \text{ km s}^{-1} Ref. [22,23]
\begin{array}{ccc} \rho_{\gamma} & {\bf energy\ density\ of\ CBR} \\ {\rm Value:} & 4.662\ 3\times 10^{-34}\ (T/2.728)^4\ {\rm g\ cm^{-3}} & {\rm Ref.\ [10,22]} \end{array}
   Value: = 0.26153 (T/2.728)^4 \text{ eV cm}^{-3}

ho_R energy density of relativistic particles (CBR + \nu) Value: 7.8388 \times 10^{-34} \, (T/2.728)^4 \, \mathrm{g \ cm^{-3}} Ref. [10,22]
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Value:  $= 0.43972 (T/2.728)^4 \text{ eV cm}^{-3}$ 

 $n_{\gamma}$  number density of CBR photons

Value:  $411.87 (T/2.728)^3 \text{ cm}^{-3} \text{ Ref. } [10,22]$ 

s/k entropy density/Boltzmann constant

Value:  $2899.3 (T/2.728)^3 \text{ cm}^{-3} \text{ Ref.} [10]$ 

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- 1. B.W. Petley, Nature **303**, 373 (1983).
- 2. E.R. Cohen and B.N. Taylor, Rev. Mod. Phys. **59**, 1121 (1987). The set of constants resulting from this adjustment has been recommended for international use by CODATA (Committee on Data for Science and Technology).

In the context of the scale dependence of field theoretic quantities, it should be remarked that absolute lab measurements of  $G_N$  have been performed only on scales of  $10^{-1\pm 1}$  m.

- 3. The Astronomical Almanac for the year 1994, U.S. Government Printing Office, Washington, and Her Majesty's Stationary Office, London (1993). Where possible, the values as adjusted for the fitting of the ephemerides to all the observational data are used.
- 4. JPL Planetary Ephemerides, E. Myles Standish, Jr., private communication (1989).
- 5. 1 AU divided by  $\pi/648\,000$ ; quoted error is from the JPL Planetary Ephemerides value of the AU [4].
- 6. Heliocentric gravitational constant from Ref. 3 times  $2/c^2$ . The given 9-place accuracy appears to be consistent with uncertainties in actually defining the earth's orbital parameters.
- 7. Obtained from the heliocentric gravitational constant [3] and  $G_N$  [2]. The error is the 128 ppm standard deviation of  $G_N$ .
- 8. 1996 mean total solar irradiance (TSI) =  $1367.5 \pm 2.7$  [24]; the solar luminosity is  $4\pi \times (1 \text{ AU})^2$  times this quantity. This value increased by 0.036% between the minima of solar cycles 21 and 22. It was modulated with an amplitude of 0.039% during solar cycle 21 [25].

Sackmann et al. [26] use TSI =  $1370 \pm 2$  W m<sup>-2</sup>, but conclude that the solar luminosity ( $L_{\odot} = 3.853 \times 10^{26}$  J s<sup>-1</sup>) has an uncertainty of 1.5%. Their value is based on three 1977–83 papers, and they comment that the error is based on scatter among the reported values, which is substantially in excess of that expected from the individual quoted errors.

The conclusion of the 1971 review by Thekaekara and

<sup>†</sup> Subscript 0 indicates present-day values.

Drummond [27]  $(1353 \pm 1\% \text{ W m}^{-2})$  is often quoted [28]. The conversion to luminosity is not given in the Thekaekara and Drummond paper, and we cannot exactly reproduce the solar luminosity given in Ref. 28.

Finally, a value based on the 1954 spectral curve due to Johnson [29]  $(1395 \pm 1\% \text{ W m}^{-2}, \text{ or } L_{\odot} = 3.92 \times 10^{26} \text{ J s}^{-1})$ has been used widely, and may be the basis for higher value of the solar luminosity and corresponding lower value of the solar absolute bolometric magnitude (4.72) still common in the literature [10].

- Obtained from the geocentric gravitational constant [3] and  $G_N$  [2]. The error is the 128 ppm standard deviation of  $G_N$ .
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- 13. Conversion using length of tropical year.
- See the section on the Hubble Constant (Sec. 17 of this *Review*).
- G. Gilmore, R.F.G. Wyse, and K. Kuijken, Annu. Rev. Astron. Astrophys. 27, 555 (1989).
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  - papers setting limits on WIMP mass limits, e.g. in M. Mori et al., Phys. Lett. **B289**, 463 (1992).
- 17. As of April 1998 the concensus of observations seems to be  $0.2 < \Omega_M < 0.5$ , but systematic effects which raise the upper limit cannot be ruled out.
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