LATTICES FOR A HIGH-FIELD 30 TeV HADRON COLLIDER

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ABSTRACT

Long arc cells would lead to major cost savings in a high field high T_c hadron collider, operating in the regime of significant synchrotron radiation. Two such lattices, with half cell lengths of 110 and 260 m, are compared. Both allow flexible tuning, and have large dynamic apertures when dominated by chromatic sextupoles. Lattices with longer cells are much more sensitive to systematic magnet errors, which are expected to dominate.

I. INTRODUCTION

Contemporary hadron colliders operate in a regime of insignificant synchrotron radiation damping. Conceptual designs of a high field post-LHC "Really Large Hadron Collider" (RLHC), with parameters only slightly beyond those of the SSC, benefit greatly from damping times much less than the storage time. They deliberately incorporate 'short' damping times to desensitize machine operations with respect to sources of phase space dilution, and to increase the integrated luminosity[1, 2]. High field RLHC designs explicitly use "high T_c" superconducting magnets, to safely absorb the radiation heat load of up to 5 W/m. They implicitly assume that the high T_c commercial magnets which are beginning to appear will, in due course, be developed into accelerator quality magnets. Magnet R&D based on recent advances in high T_c materials suggest the possibility of practical tape wound magnets[3].

This paper addresses lattice optimization issues, taking for granted the primary parameters listed in Table I that are discussed elsewhere[1, 2]. The advantages of very long arc cells are examined by studying two detailed lattices, one near each end of the spectrum of plausible arc cell length. The short cell lattice has 6 dipoles per half cell of length $L = 110$ m, while the long cell lattice has 15 dipoles per half cell of length $L = 260$ m. The optical and dynamical aperture performance of each lattice is discussed.

II. HALF CELL LENGTH

The optimum half arc cell length, L, depends on a dynamic balance between two effects pushing for longer cells, and one pushing for shorter cells. Longer cells save money through fewer quadrupoles, fewer correctors, and fewer spool pieces. They also have reduced strength chromaticity sextupoles, and an increased dynamic aperture from this source. However, shorter cells and smaller beams make more modest demands on magnetic field quality.

The SSC half cell length stayed remarkably constant at $L \approx 100$ m during repeated optimization exercises[4]. This is largely due to the consistent use of an almost invariant set of magnet error statistics, which assumed that random errors would dominate systematics. Recent experience with RHIC magnets shows (scaled) errors that are much smaller than in the SSC model, and shows, to the contrary, that systematics dominate randoms[5]. Measured errors in several real SSC dipoles were significantly smaller than in the standard SSC model used for tracking[6]. This suggests that RLHC half cells might be much longer than 100 meters.

Table I: Primary design parameters. Values which vary significantly with time, such as ϵ, are quoted at injection.

Parameter	units	value
Storage energy	[TeV]	30.0
Injection energy	[TeV]	1.0
Dipole field (store)	[T]	12.5
Dipole length	[m]	17.0
Dipole coil ID	[mm]	50 - 60
Triplet quad gradient (store)	[T/m]	300
Number of Interaction Regions		2
Transverse rms emittance, ϵ	[μm]	1.0
Longitudinal rms bunch area, S	[eV-s]	0.1
Longitudinal rms emittance, ϵ_s	[m]	.0102
RF frequency, f_{RF}	[MHz]	360
Transverse damping time (store)	[hr]	$\approx$ 2.1

It is not yet possible to postulate a plausible magnet error model for high T_c dipoles. Instead, suppose that particle motion is stable within a "good field aperture" of $r_{GF} = 15$ mm, about half of the coil radius, in the arcs. If the phase advance per cell is 90 degrees, the maximum beta function is given by $\widehat{\beta} = 3.41\ L$, generating a maximum transverse rms injection beam size of

$$\widehat{\sigma}_\beta = \sqrt{\epsilon\widehat{\beta}/(\beta\gamma)} \tag{1}$$

The maximum allowable value of L occurs when the beam size fills the good field aperture. This is written as $r_{GF} = n\widehat{\sigma}_\beta$, where a conservative value for n is 15. This yields a maximum allowable half cell length of

$$\widehat{L} = \frac{\beta\gamma}{\epsilon}\frac{r_{GF}^2}{3.41\,n^2} = 313\ \ [\mathrm{m}] \tag{2}$$

Long arc cells have a significant impact on longitudinal parameters, as shown in the values in Table II. The maximum dispersion, $\widehat{\eta} = 2.71\,L^2/R$, increases quadratically with L, causing the horizontal beam width contribution from momentum spread to rise much faster than the betatron contribution. The small momentum spreads quoted in Table II are determined

Table II: Longitudinal parameters for SHORT and LONG cell lattices, at injection. There are two sextupoles per cell.

Parameter	units	SHORT	LONG
Half cell length, L	[m]	110	260
Max. cell beta, $\widehat{\beta}$	[m]	376	898
Max. cell dispersion, $\widehat{\eta}$	[m]	3.85	22.9
Max. betatron size, $\widehat{\sigma}_\beta$	[mm]	.594	.918
Circumference, C	[km]	55.44	54.08
Horizontal tune, Q_x		65.195	28.195
Vertical tune, Q_y		66.185	29.185
Number of dipoles		2888	2900
Number of sextupoles		456	168
Slip factor, α	$[10^{-3}]$	.299	1.813
Mmtm. width, σ_p/p	$[10^{-3}]$	.1545	.0401
RMS bunch length, σ_s	[m]	.0619	.238
Synchrotron tune, Q_s	$[10^{-3}]$	6.59	2.63
Voltage slope, dV/ds	[MV/m]	103.29	2.78
RF voltage, V	[MV]	13.69	.37

by setting

$$\sigma_p/p = \widehat{\sigma}_\beta/\widehat{\eta} \tag{3}$$

to equalize the two contributions to the total beam width. The large slip factor in the LONG lattice ($\approx 1/Q_{arc}^2$) compensates for the small momentum width to make the beam acceptably resistant to collective effects, such as the microwave instability. The small LONG RF voltage (at 360 MHz) yields acceleration times of order 10^4 seconds.

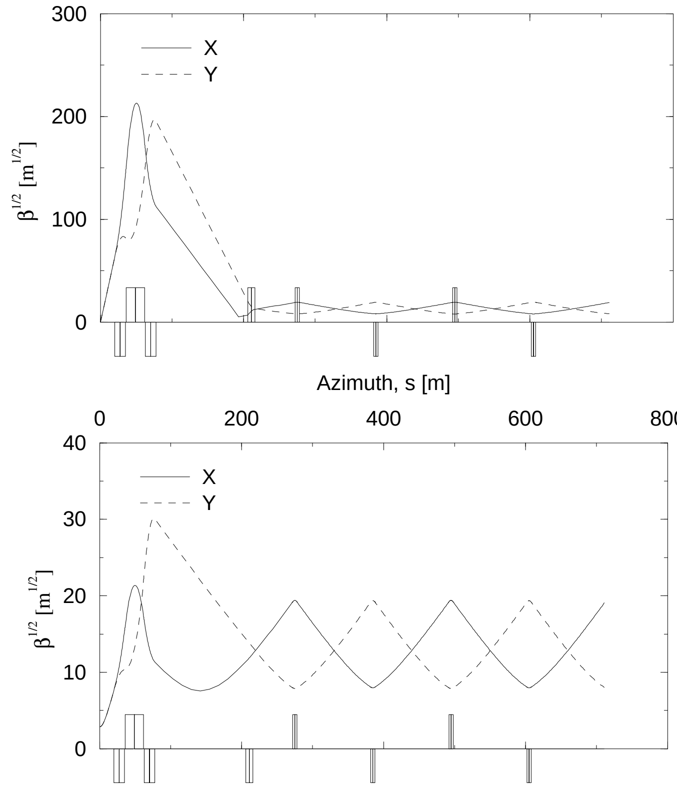

Figure 1: Telescope optics, with $\beta^* = 0.1$ m (storage) in the top figure, and $\beta^* = 8.0$ m (injection) in the bottom.

III. LATTICE OPTICS

Figure 1 shows a simple 4 quad telescope matching into empty arc cells. The telescope consists of a close packed triplet starting at $L^* = 20$ m from the collision point, followed by a 4th quadrupole placed $L/2$ from the first regular strength arc cell quadrupole [7]. The same optics also match into dispersion suppressor (DS) cells, as shown for the Interaction Regions (IR) cluster in Figure 2. Each DS has four 90 degree cells, with 3/4 the length of regular arc cells, and 2/3 of the number of dipoles. The 2 IRs are separated by back-to-back DSs, in addition to the DSs that match into the regular arcs. On the opposite side of the RLHC circumference are two utility straights of identical geometry, constructed from empty arc cells.

The maximum triplet gradient of 300 T/m causes peak and collision point betas to be related by an “effective length” L_e, defined by

$$\widehat{\beta} = L_e^2/\beta^* \tag{4}$$

and given by $L_e \approx 70$ m for both lattices [1, 8]. When $\beta^* = 0.1$ m at 30 TeV, the triplet beam size is $\sigma_{trip} \approx 1.2$ mm. Triplet quads can have modest bores.

IV. DYNAMIC APERTURE

When β^* is varied with the net chromaticities held constant ($\chi_x = \chi_y = 2.0$), the total sextupole strength has a contribution proportional to $1/\beta^*$, due to the natural chromaticity from the telescopes. Figure 3 illustrates this, with LONG strengths much weaker than the SHORT.

The ON momentum dynamic aperture is inversely proportional to the sextupole strength, as shown by the computed dynamic apertures recorded in Figure 4. Particles are launched with equal betatron motion amplitudes, parameterized by n where, if the motion is linear, $x_{max}/\sigma_x = y_{max}/\sigma_y = \sqrt{0.5}\,n$. The OFF momentum dynamic aperture is also plotted, for particles with a synchrotron oscillation amplitude of σ_p/p (injection value). In most cases the OFF and ON momentum dynamic apertures are indistinguishable, owing to the small momentum spread. The exception is the SHORT lattice with $\beta^* = 0.1$ m ($S_F = 24.4 \times 10^{-3}$ m^{-2}), where chromatic distortions due to the telescopes are at their strongest.

The huge dynamic apertures with only chromatic sextupoles present ($n_{DA} \geq 33$) are rather illusory, since neither a realistic physical aperture ($n \sim 40$) nor realistic dipole errors have been included. The apparent advantages of very long cells may disappear when realistic errors for tape wound high T_c magnets become known. Another paper in these Snowmass 96 proceedings makes a simple calculation of the tolerable systematic errors in arc dipoles, as a function of half cell length [9].

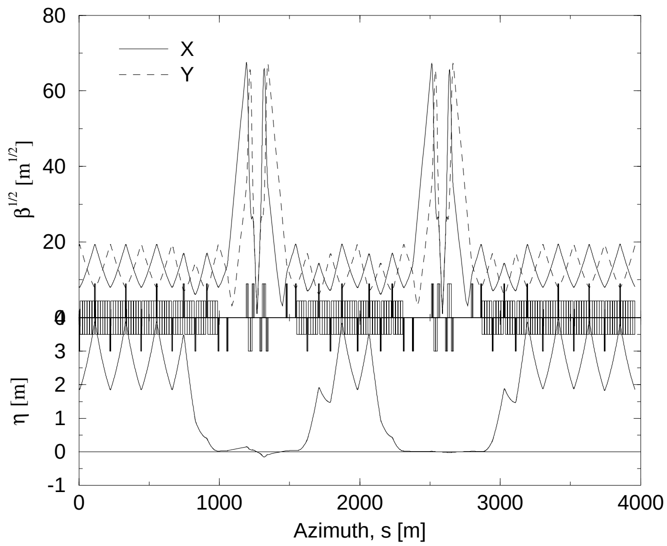

Figure 2: Layout of the IR cluster, with $\beta^* = 1.0$ [m].

V. CONCLUSIONS

Lattices with unusually long arc cells have potential advantages, including large cost savings, in a high field high T_c RLHC. Both LONG and SHORT lattices, with half cell lengths of 110 and 260 m, allow β^* to be squeezed down from 8.0 m at injection to 0.1 m at storage. However, to optimize the cell length it is necessary derive realistic magnet errors. This includes addressing the relative importance of random and systematic harmonics - do systematics dominate, as at RHIC, or do randoms dominate, as assumed for the SSC? [9] It is also necessary to explore the scaling of collective instabilities with respect to arc cell length.

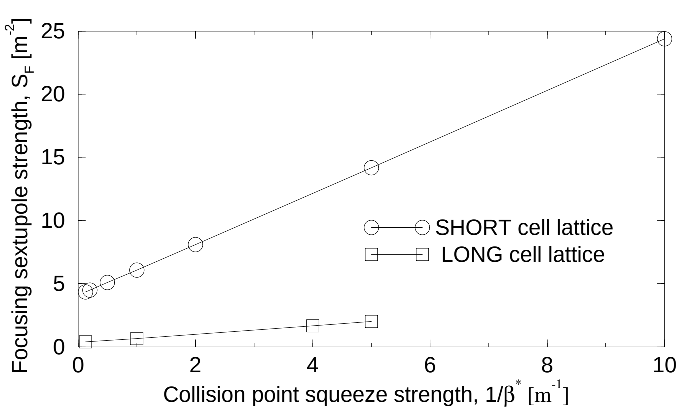

Figure 3: Chromaticity sextupole strength versus squeeze strength at constant net chromaticity.

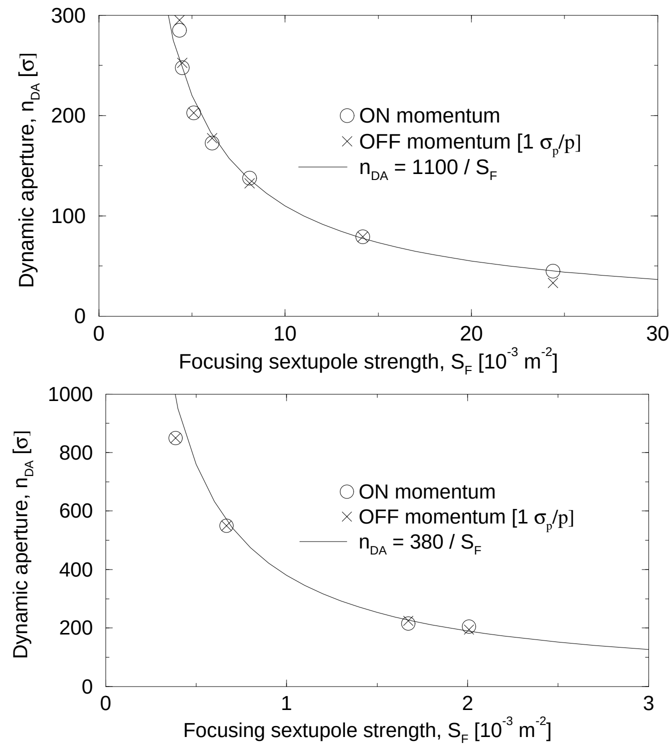

Figure 4: Dynamic aperture (10^4 turns) in the SHORT lattice (top) and the LONG lattice (bottom).

VI. REFERENCES

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