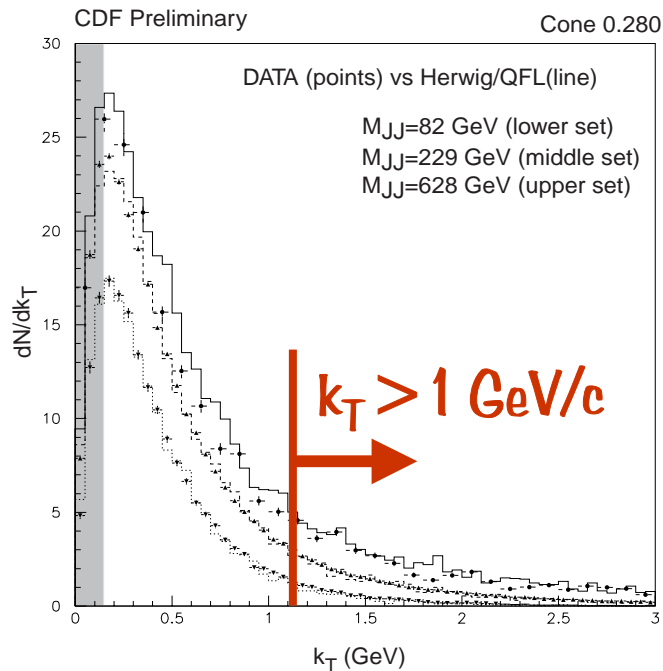
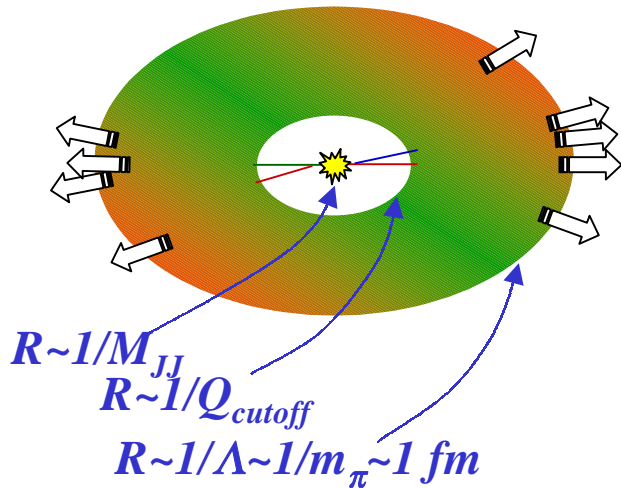


Jet Fragmentation at CDF

Andrey Korytov
University of Florida

Jet Fragmentation: pQCD + hadronization

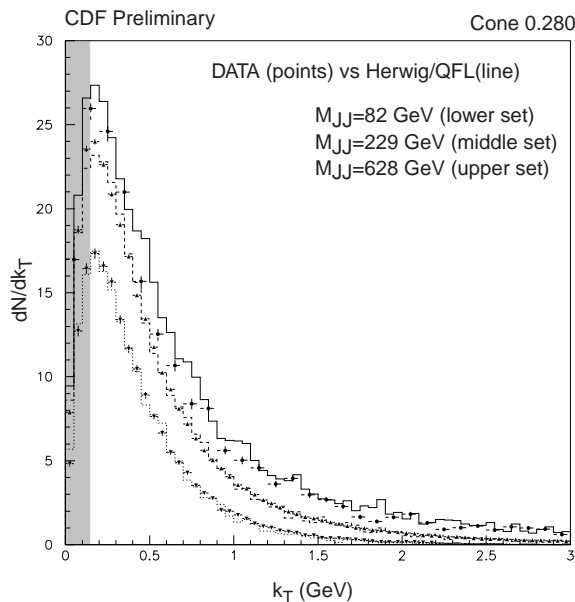
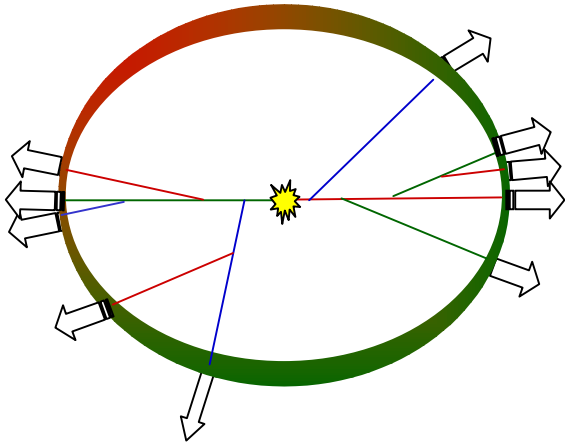


Fragmentation can be thought of as the two-stage process:

- pQCD stage that governs development of a parton shower
- phenomenological hadronization that converts partons into hadrons
- the fuzzy border between the two stages is usually associated with a k_T cut-off scale Q_{cutoff}

pQCD with comfortably high $k_T > 1 \text{ GeV}$ ($R < 0.2 \text{ fm}$) inevitably implies the dominance of the phenomenological hadronization stage

Jet Fragmentation: pQCD dominance scenario



MLLA, Modified Leading Log Approximation, after re-summing pQCD terms in all orders, gives analytical infrared stable expressions where one can set $Q_{\text{cutoff}} = \Lambda_{\text{QCD}} = Q_{\text{eff}}$ (~ 200 MeV?); it explicitly accounts for soft partons $x_p = p/E_{\text{jet}} \ll 1$.

Mueller (1983); Dokshitzer, Troyan (1984); Malaza, Webber (1984)

LPHD, Local Parton Hadron Duality, hypothesis assumes that hadronization occurs locally at the very last moment and, therefore, hadrons “remember” parton distributions: e.g., $N_{\text{hadrons}} = K_{\text{LPHD}} \cdot N_{\text{partons}}$

- if all hadrons are accounted for, $K_{\text{LPHD}(\text{all hadrons})} \sim 1$
- if only charged hadrons are observed, $K_{\text{LPHD}(\pm)} \sim 2/3$ (adding $l=1/2$ particles, e.g., K^+K^0 , and particles with predominantly neutral decay modes, e.g., η , may somewhat reduce this number)

Azimov, Dokshitzer, Khoze, Troyan (1985)

MLLA: Modified Leading Log Approximation

Gluon Jets:

- Multiplicity: $N_g(Y)$, $Y = \ln(E_{\text{jet}} \sin\theta / Q_{\text{eff}})$
- Momentum distribution: $dN_g(\xi, Y)/d\xi$, $\xi = \log(1/x_p)$, $x_p = p/E_{\text{jet}}$

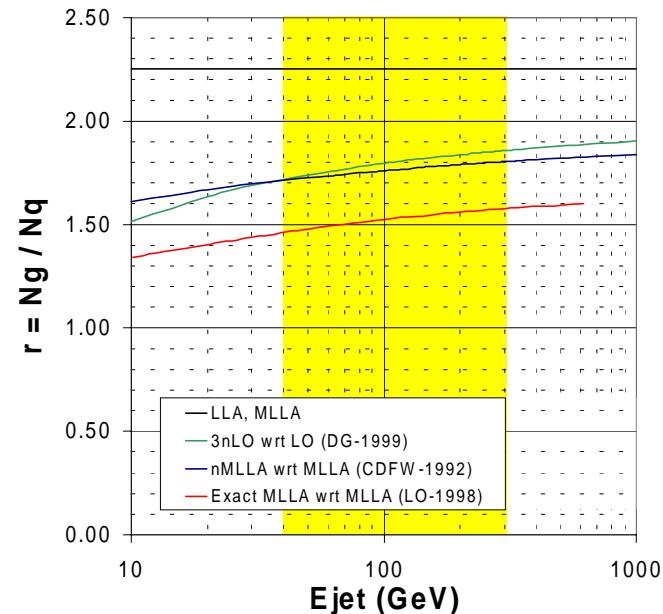
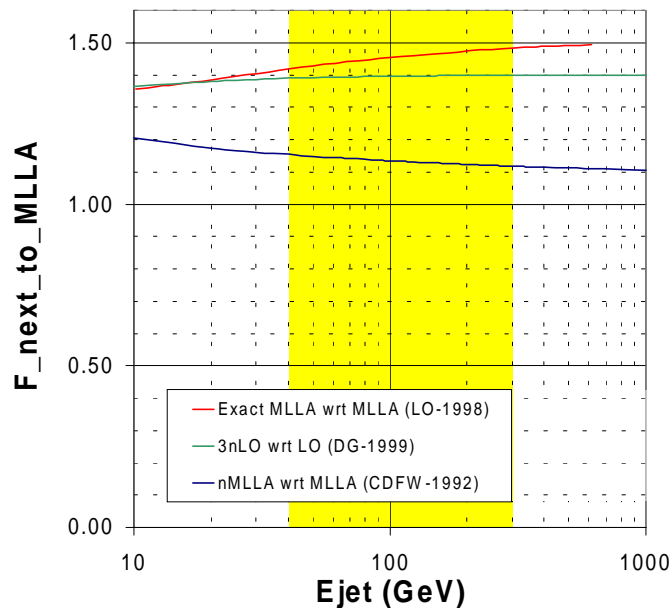
Quark Jets:

- quark jet is different by a normalization factor $1/r$, $r = C_A/C_F = 9/4$
- Multiplicity: $N_q(Y) = (1/r) \cdot N_g(Y)$
- Momentum distribution: $dN_q/d\xi = (1/r) \cdot dN_g/d\xi$

Next-to-MLLA corrections

Next-to-MLLA corrections to multiplicity of parton in gluon and quark jets:

- $N_{\text{next-to-MLLA}} = F_{\text{next-to-MLLA}} \times N_{\text{MLLA}}$ (gluon jet)
- $r \neq 9/4$



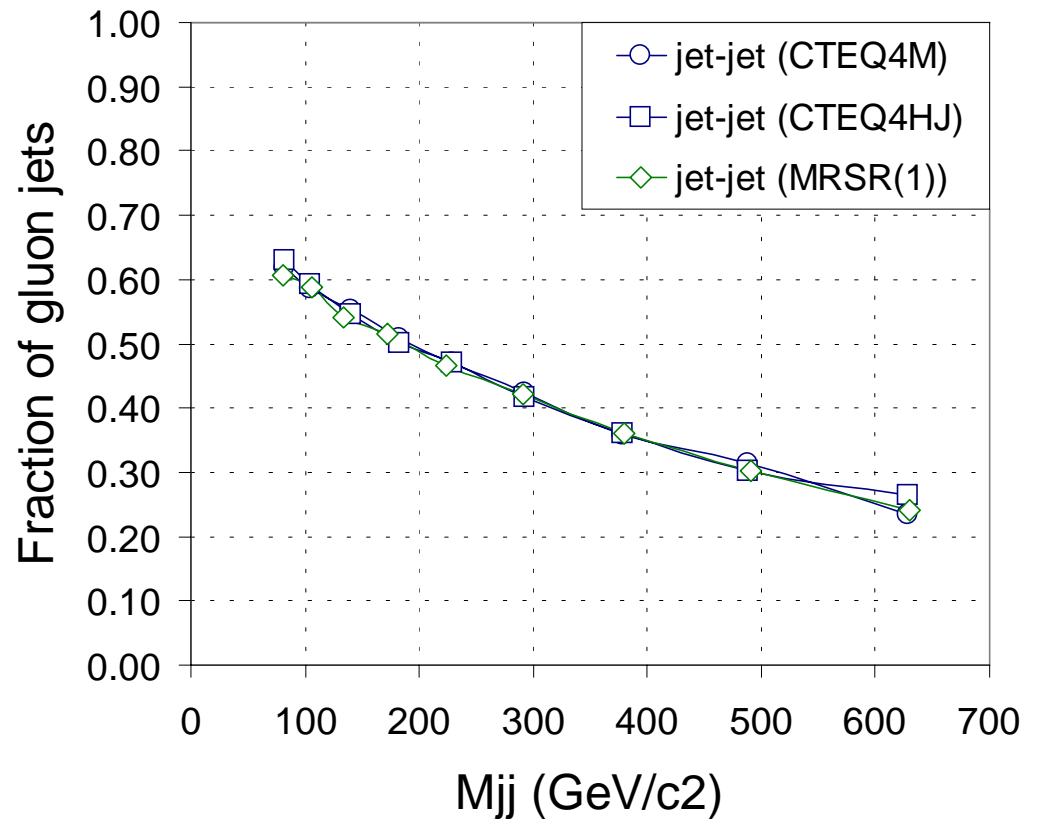
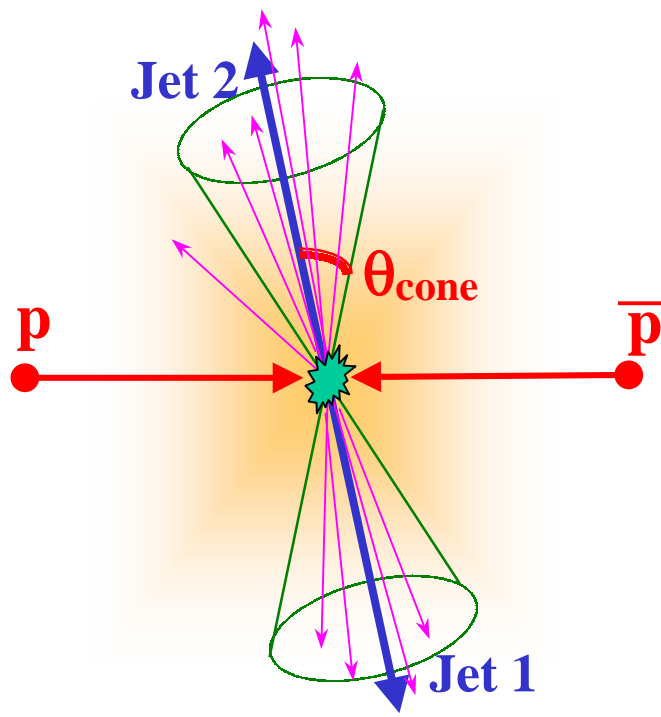
CDFW-1992 Catani, Dokshitzer, Fiorani, Webber, Nucl.Phys. B377(1992)445

LO-1998 Lupia, Ochs, Phys.Lett. B418(1998)214 and Nucl.Phys.B (Proc. Suppl.) 64(1998)74

DG-1999 Dremin, Gary, hep-ph/9905477v2, 3 Sep 1999

Analysis at CDF

- dijet events with $80 < M_{JJ} < 630 \text{ GeV}/c^2$
- both jets are in central region, well balanced
- opening angle $0.17 < \theta_{\text{cone}} < 0.47$

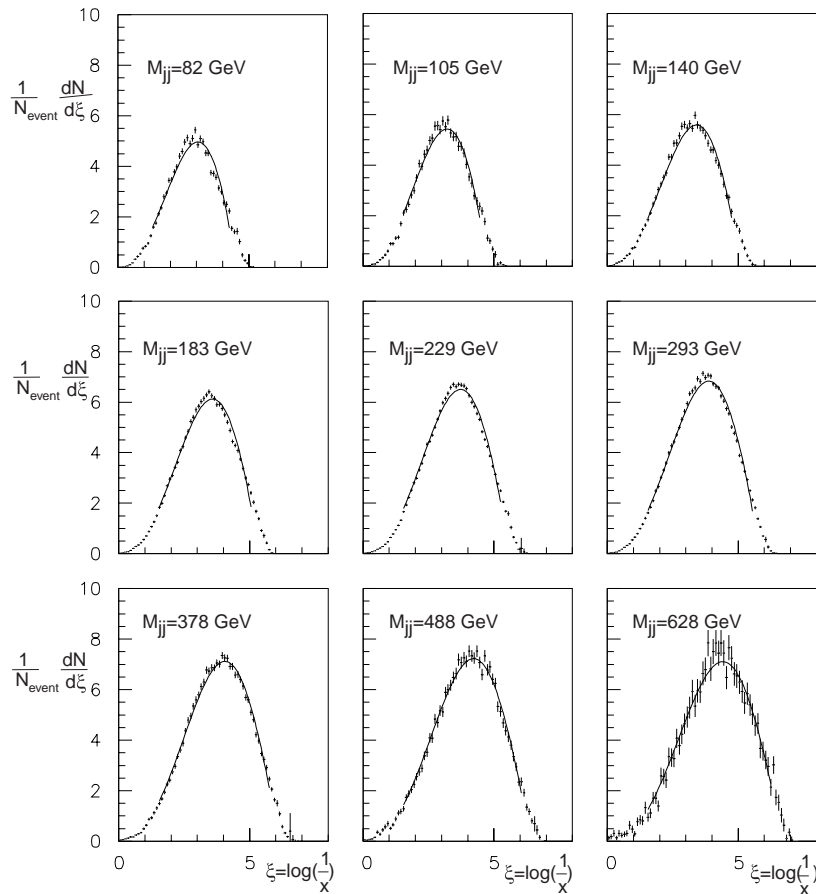


Momentum distribution of tracks

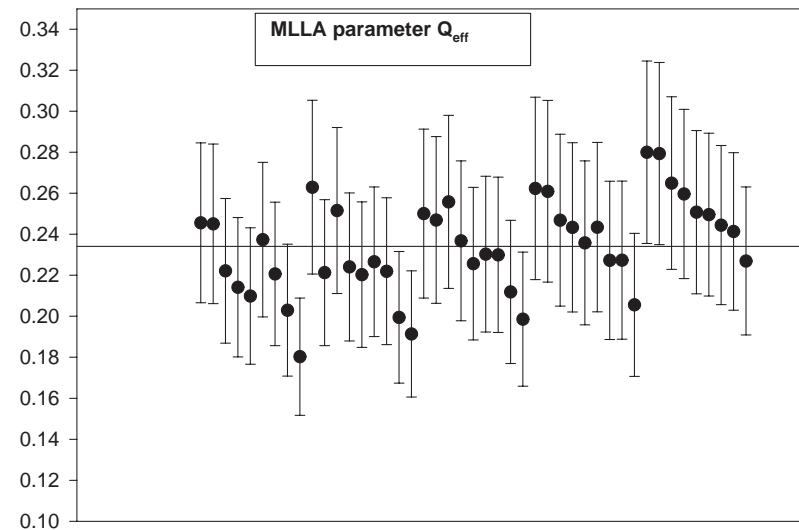
M_{jj} -scan ($\theta_{\text{cone}}=0.47$), MLLA fit

Q_{eff} for all 9 M_{jj} 's and 5 opening angles θ_{cone} 's

CDF preliminary



CDF Preliminary

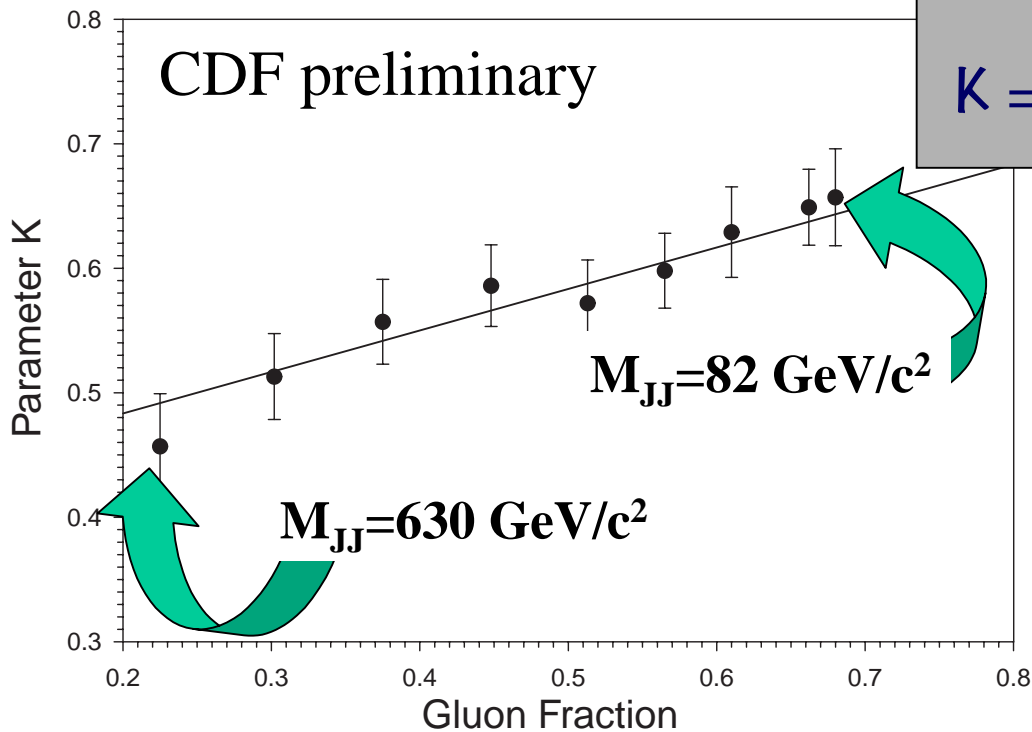


MLLA fit $dN(\xi, Y)/d\xi$

$Q_{\text{eff}} \approx \text{constant} = 240 \pm 40 \text{ MeV}$

Momentum distribution of tracks

$$\begin{aligned}
 N_{\text{hadrons}} &= K_{\text{LPHD}} \times N_{\text{partons}} = K_{\text{LPHD}} \times (\epsilon_g N^{\text{g-jet}} + \epsilon_q N^{\text{q-jet}}) = \\
 &= K_{\text{LPHD}} \times (\epsilon_g + (1-\epsilon_g)/r) \times N^{\text{g-jet}} = \\
 &= K_{\text{LPHD}} \times (\epsilon_g + (1-\epsilon_g)/r) \times F_{\text{next-to-MLLA}} \times N^{\text{g-jet}} = K \times N^{\text{g-jet}}
 \end{aligned}$$



$$\begin{aligned}
 N_{\text{hadrons}} &= K \times N^{\text{g-jet}} \\
 K &= K_{\text{LPHD}} \times (1/r + (1-1/r)\epsilon_g) \times F_{\text{next-to-MLLA}}
 \end{aligned}$$

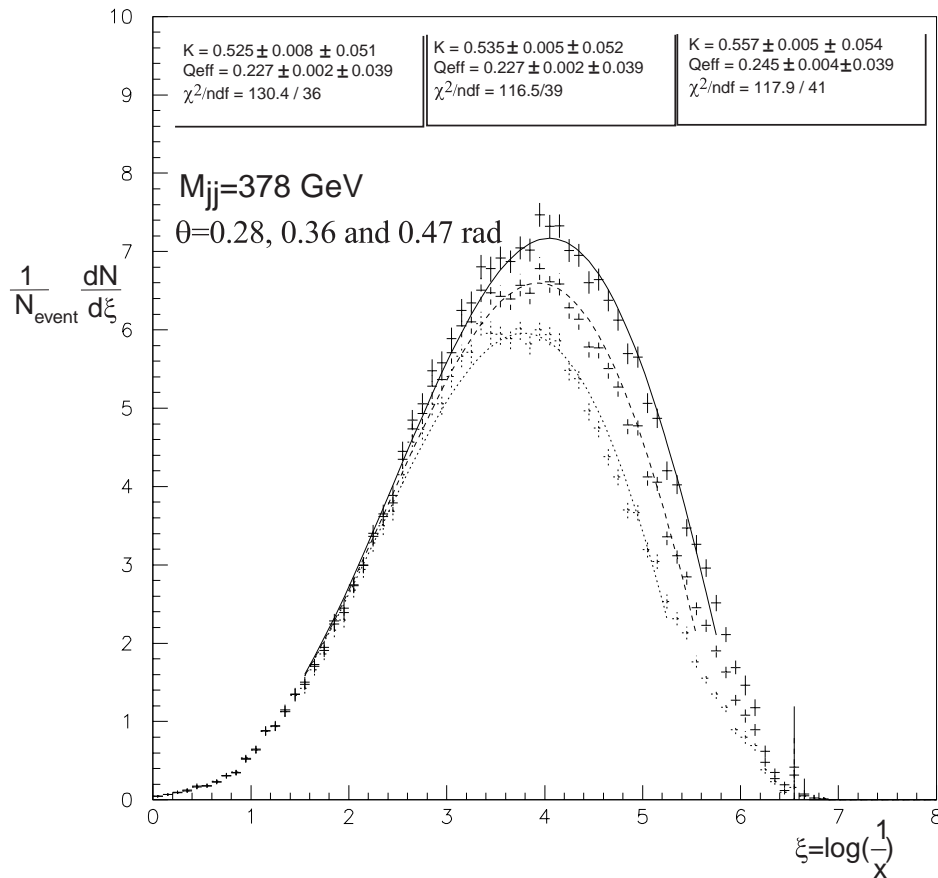
K vs. gluon jet fraction fit:

- $r=1.8 \pm 0.4$ (indirect)
- $K_{\text{LPHD}}=0.58 \pm 0.05 \pm 0.08$

the measurement is "indirect":
the result relies on MLLA-
predicted $dN_g(\xi, E_{\text{Jet}})/d\xi$

Momentum distribution of tracks

CDF preliminary



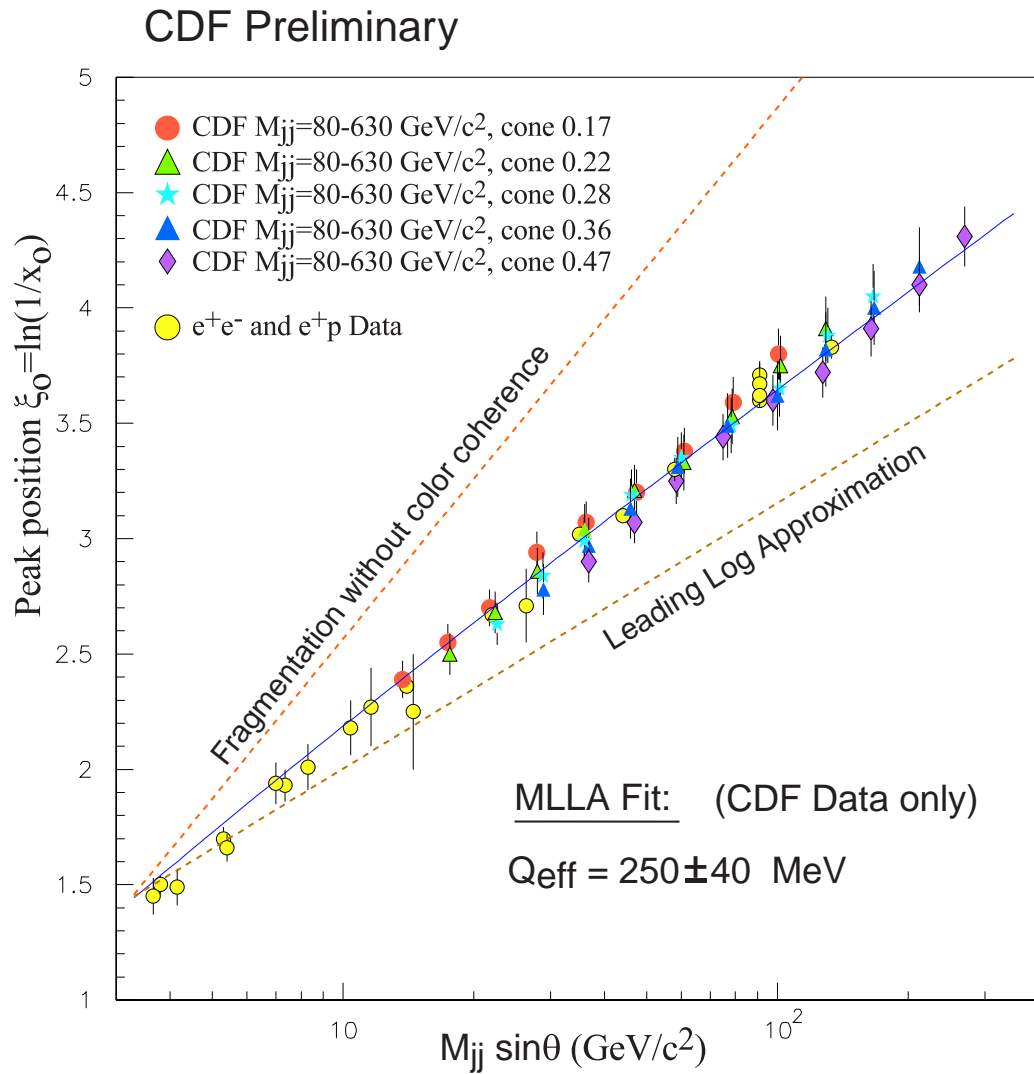
For fixed M_{jj}

K should be angle independent

MLLA-fitted values of K :

- $\theta_{\text{cone}}=0.47$ $K=0.56 \pm 0.05$
- $\theta_{\text{cone}}=0.36$ $K=0.54 \pm 0.05$
- $\theta_{\text{cone}}=0.28$ $K=0.53 \pm 0.05$

Peak of momentum distribution of tracks



In MLLA peak ξ_0 vs. M_{JJ} :

$$\xi_0 = 1/2 Y + (cY)^{1/2} - c,$$

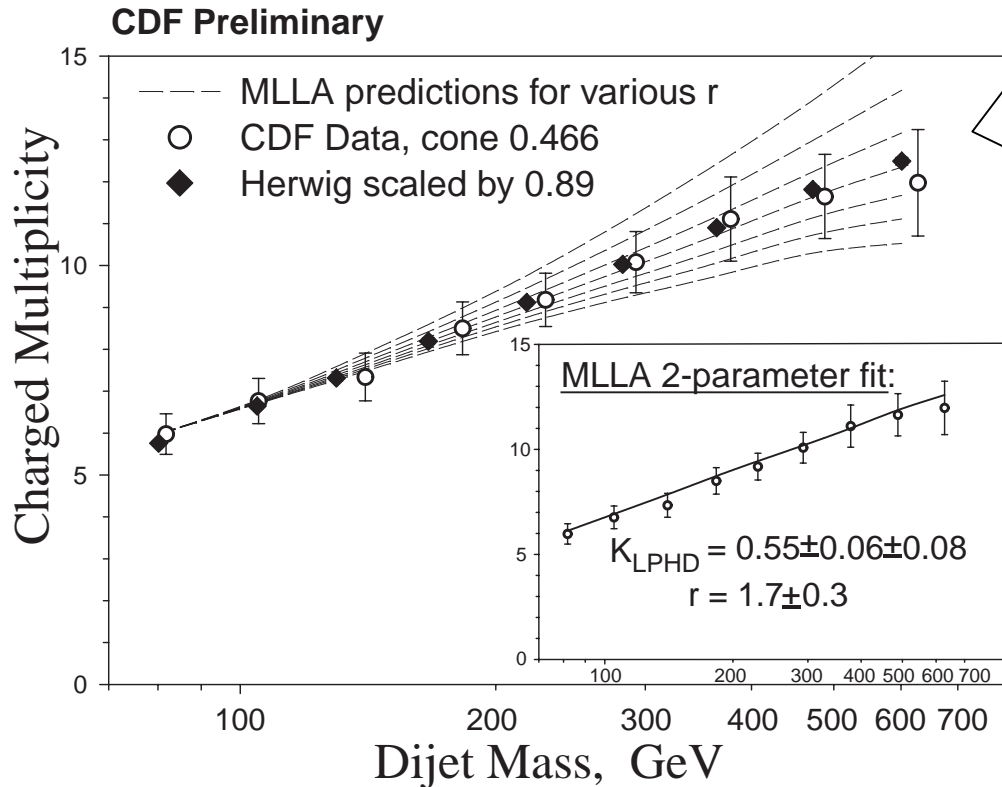
$$Y = \ln(E_{\text{jet}} \sin\theta / Q_{\text{eff}})$$

$$c = 0.29 \text{ for } n_f = 3$$

Peak ξ_0 vs. M_{JJ} fit:

$$Q_{\text{eff}} = 250 \pm 40 \text{ MeV}$$

Multiplicity in dijet events



*dashed curves from top to bottom
 $r=1.0, 1.2, 1.4, 1.6, 1.8, 2.0, 2.25$*

MLLA fit of N_{jet} vs. M_{JJ}

- indirect $r=1.7 \pm 0.3$
- $K_{LPHD}=0.55 \pm 0.06 \pm 0.08$

the measurement is "indirect", i.e. the result relies on MLLA-governed dependence $N_g(E_{Jet})$

Intermediate Summary

Analysis in the framework of MLLA

- $Q_{\text{eff}} = 240 \pm 40 \text{ MeV}$
- $K_{\text{LPHD}} = 0.56 \pm 0.10$ (assuming next-to-MLLA correction 1.30 ± 0.20)
- $r = 1.7 \pm 0.3$
 - r , though being treated as a free parameter, is measured in MLLA-context, i.e. strictly speaking it is an indirect measurement
 - r is self-consistent with the next-to-MLLA predictions

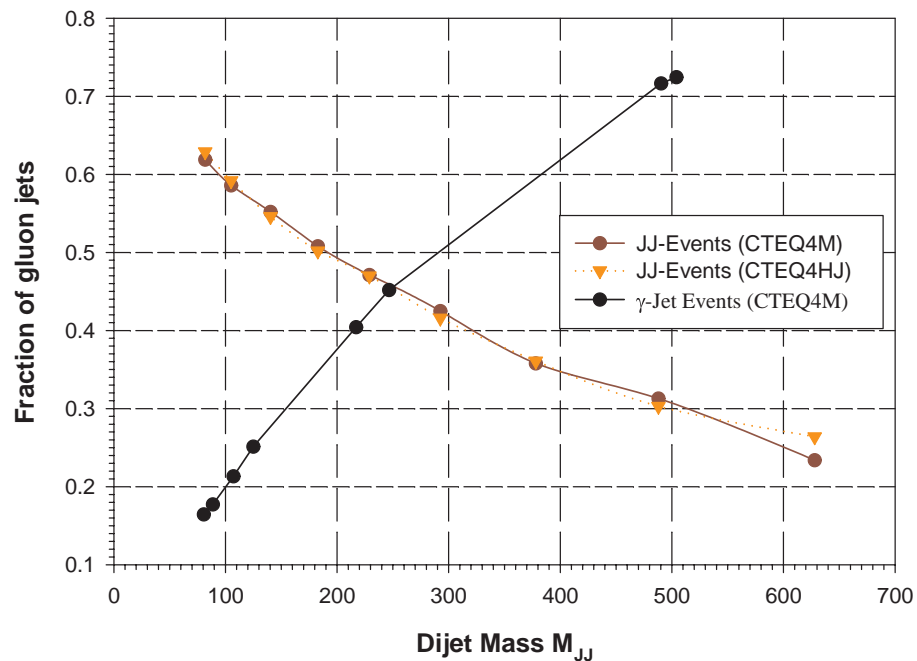
Does it all make sense?

$r, K_{\text{LPHD}}, Q_{\text{eff}}?$

Model-independent measurement of r

Jet-jet sample: $N_{\text{hadrons}} = K_{\text{LPHD}} \times (\epsilon_g + (1-\epsilon_g)/r) \times F_{\text{next-to-MLLA}} \times N^{\text{g-jet}}$

γ -jet sample: $N'_{\text{hadrons}} = K_{\text{LPHD}} \times (\epsilon'_g + (1-\epsilon'_g)/r) \times F_{\text{next-to-MLLA}} \times N^{\text{g-jet}}$

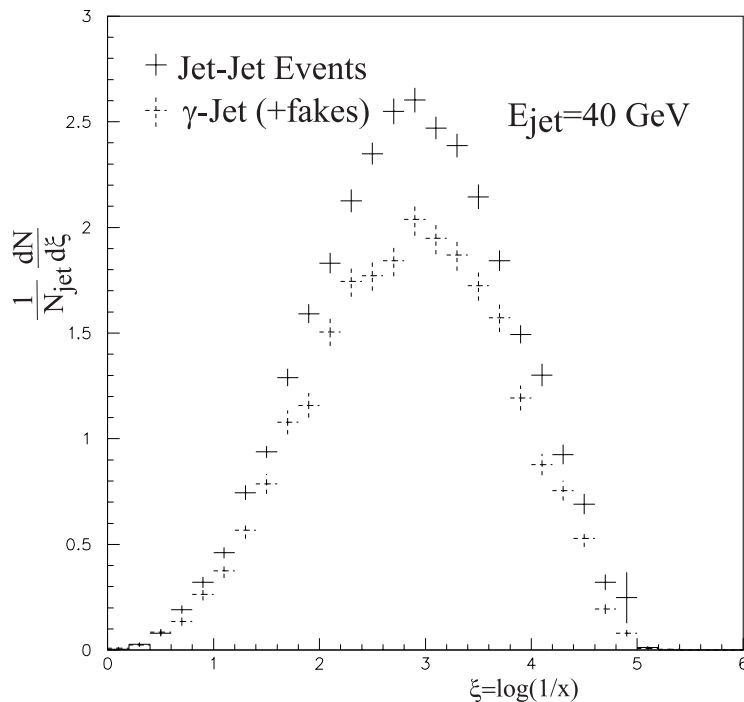


Model-independent measurement of r

Jet-jet sample: $N_{\text{hadrons}} = K_{\text{LPHD}} \times (\varepsilon_g + (1-\varepsilon_g)/r) \times F_{\text{next-to-MLLA}} \times N^{\text{g-jet}}$

γ -jet sample: $N'_{\text{hadrons}} = K_{\text{LPHD}} \times (\varepsilon'_g + (1-\varepsilon'_g)/r) \times F_{\text{next-to-MLLA}} \times N^{\text{g-jet}}$

CDF preliminary



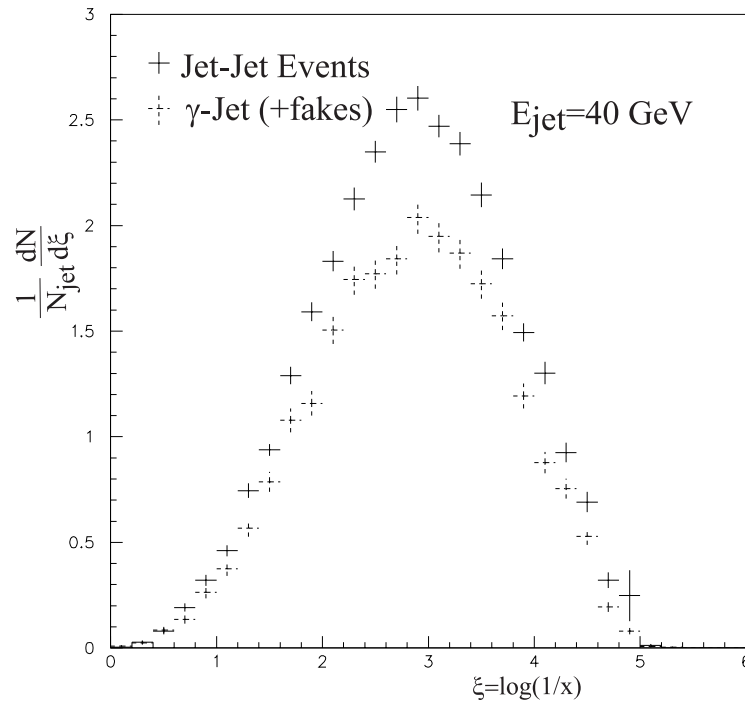
- Dijets with $M_{jj} = 80 \text{ GeV}/c^2$:
 $N = 5.77 \pm 0.03 \text{ tracks/jet}$
- Gamma-jets with $M_{\gamma j} = 80 \text{ GeV}/c^2$:
 $N'_{\text{jet}} = 4.83 \pm 0.05 \text{ tracks/jet}$
(gamma-jet sample has $\sim 70\%$ of true γ -jets and $\sim 30\%$ of fakes--dijets)

direct measurement of r

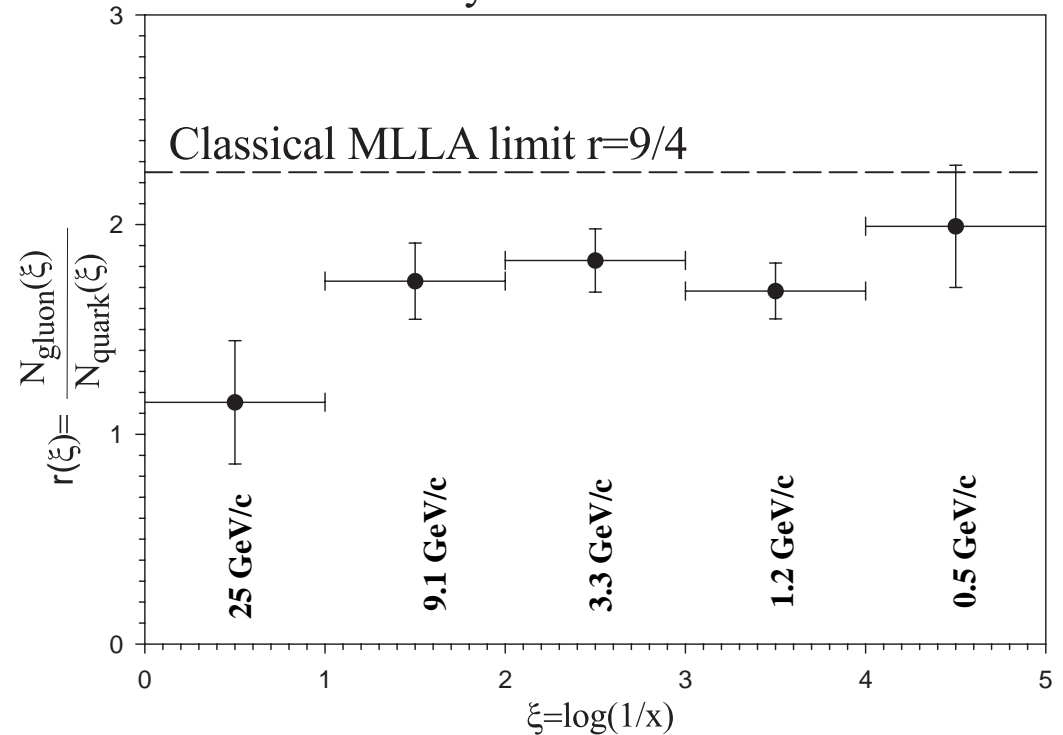
$$r = 1.74 \pm 0.11 \pm 0.07$$

Does r depend on particle momenta?

CDF preliminary



CDF Preliminary



r may depend on particle momentum, being larger for soft particles, but errors are too large for conclusive judgements

Does $K_{\text{LPHD}(+/-)}$ make sense?

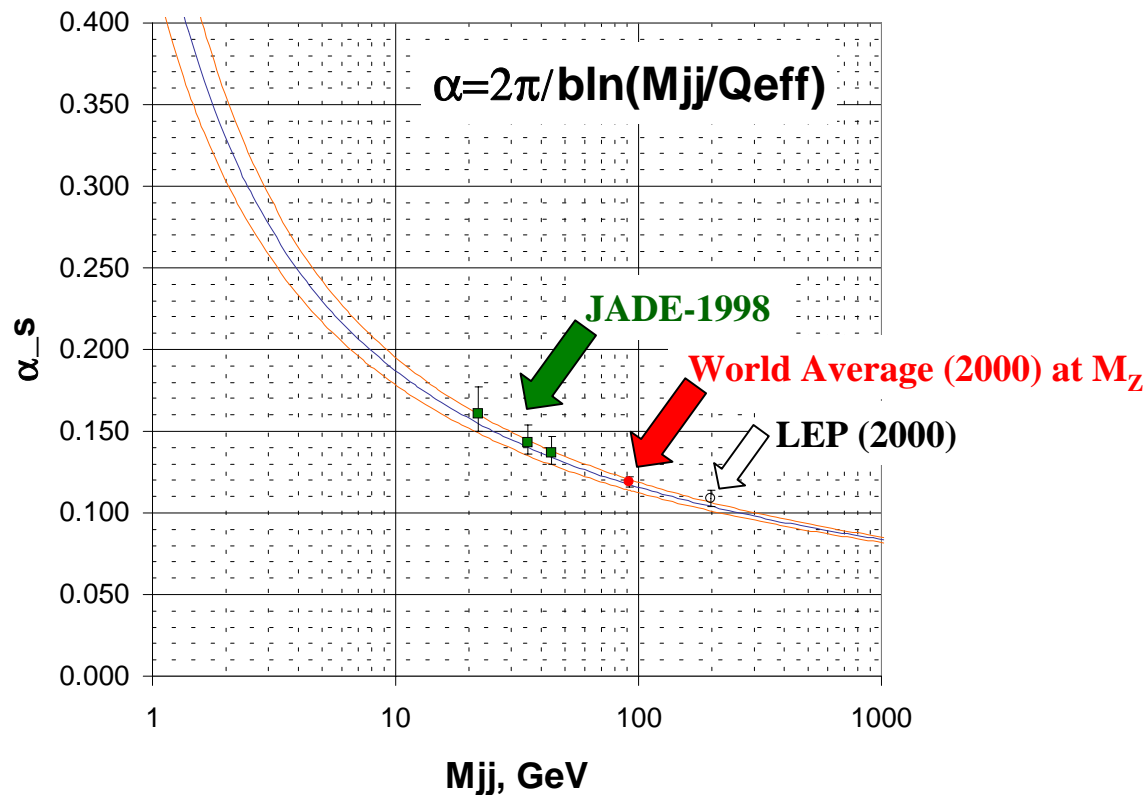
LPHD:

- We measured $K_{\text{LPHD}(+/-)} = N_{\text{hadrons}(+/-)} / N_{\text{partons}} = 0.56 \pm 0.10$
- Energy fraction carried by charged particles:
TASSO: 0.59 ± 0.01 for $Q=12-42$ GeV -- Z.Phys.C22(1984)307

Does Q_{eff} make sense?

MLLA Q_{eff} :

- MLLA $\alpha_s = 2\pi / (b \cdot \ln(k_T / \Lambda_{\text{QCD}}))$
- $Q_{\text{cutoff}} = \Lambda_{\text{QCD}} = Q_{\text{eff}}$
- Measured $Q_{\text{eff}} = 240 \pm 40 \text{ MeV}$



Jet Fragmentation at CDF: conclusions

Momentum distribution of tracks at $80 < M_{jj} < 630 \text{ GeV}/c^2$:

$$Q_{\text{eff}} = 240 \pm 40 \text{ MeV}$$

$$r = 1.8 \pm 0.4 \text{ (in the framework of MLLA)}$$

$$K_{\text{LPHD}} = 0.58 \pm 0.10 \text{ (assuming next-to-MLLA corrections)}$$

Peak position vs M_{jj} :

$$Q_{\text{eff}} = 250 \pm 40 \text{ MeV}$$

Multiplicity in dijet events vs. M_{jj} ($80 < M_{jj} < 630 \text{ GeV}/c^2$):

$$r = 1.7 \pm 0.3 \text{ (in the framework of MLLA)}$$

$$K_{\text{LPHD}} = 0.55 \pm 0.10 \text{ (assuming next-to-MLLA corrections)}$$

Multiplicity in dijet events vs. gamma-jet events at $M_{jj} = 82 \text{ GeV}/c^2$:

$$r = 1.74 \pm 0.11 \pm 0.07 \text{ (model independent)}$$