

# Maximal Information Systems

Hugh Durrant-Whyte  
ARC Federation Fellow, Research Director  
ARC Centre of Excellence for Autonomous Systems  
The University of Sydney, Australia  
[hugh@cas.edu.au](mailto:hugh@cas.edu.au)

ARC=Australian version of NSF

# The Thesis

- Large Scale “Systems of Autonomous Systems”
- We would like to:
  - Provide a quantitative model of system components
  - Reason *a priori* about combinations of components
  - Predict performance of complete systems

**Information** provides a measure for a large class of system designs



# Information: A Reminder

- Entropic Information
  - Measures surprise
  - Is additive by construction

$$H_p(\mathbf{x}) = -E[\log P(\mathbf{x})]$$

- Mutual Information
  - Belief compression
  - Incorporates “context”

$$I(\mathbf{x}, \mathbf{y}) = E\left[\log \frac{P(\mathbf{x} | \mathbf{y})}{P(\mathbf{x})}\right]$$

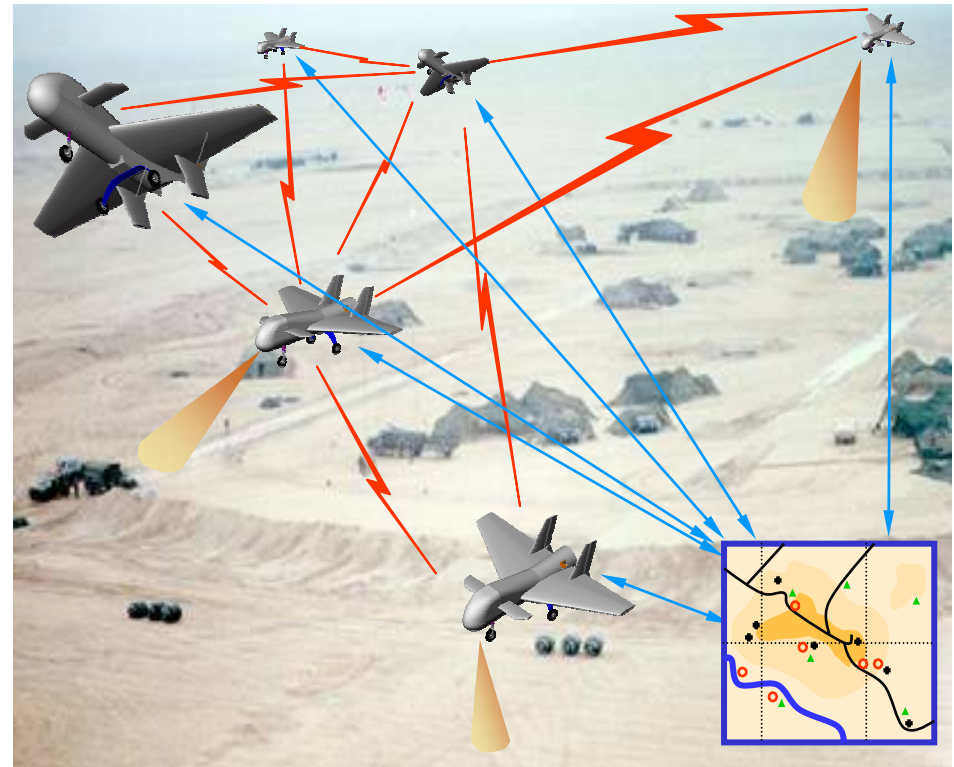
- Combinations are additions:
  - Sensing, control
  - Abstraction

$$H(\mathbf{x}, \mathbf{y}) = H(\mathbf{x}) + H(\mathbf{y}) - I(\mathbf{x}, \mathbf{y})$$

And now a story about information in systems of systems

# Decentralised Data Fusion (DDF)

- Way back in 1988 ...
- A set of network Data Fusion methods:
  - Ad Hoc Network
  - Fusion at Sensor/Platform
  - No Central Fusion Site
  - Fully Scalable
- Decentralised Algorithms:
  - Information-methods
  - For target tracking
  - For cooperative navigation
  - For cooperative control



# The Information Filter

**Bayes:** 
$$P(\mathbf{x}(k) | \mathbf{Z}^k) = C \cdot P(\mathbf{x}(k) | \mathbf{Z}^{k-1}) \prod_j P(z_j(k) | \mathbf{x}(k))$$

**Log-Likelihood:**

$$\ln P(\mathbf{x}(k) | \mathbf{Z}^k) = \ln P(\mathbf{x}(k) | \mathbf{Z}^{k-1}) + \sum_j \ln P(z_j(k) | \mathbf{x}(k)) + K$$

**(Fisher or Canonical) Information form for Gaussians:**

$$\hat{\mathbf{y}}(k | k) = \mathbf{P}^{-1}(k | k) \hat{\mathbf{x}}(k | k) \quad \mathbf{i}_j(k) = \mathbf{H}_j^T \mathbf{R}_j^{-1} \mathbf{z}_j(k)$$

$$\mathbf{Y}(k | k) = \mathbf{P}^{-1}(k | k) \quad \mathbf{I}_j(k) = \mathbf{H}_j^T \mathbf{R}_j^{-1} \mathbf{H}_j$$

# The Information Filter

**Observation updates are simple sums (unlike KF):**

$$\hat{\mathbf{y}}(k | k) = \hat{\mathbf{y}}(k | k - 1) + \sum_j \mathbf{i}_j(k)$$
$$\mathbf{Y}(k | k) = \mathbf{Y}(k | k - 1) + \sum_j \mathbf{I}_j(k)$$

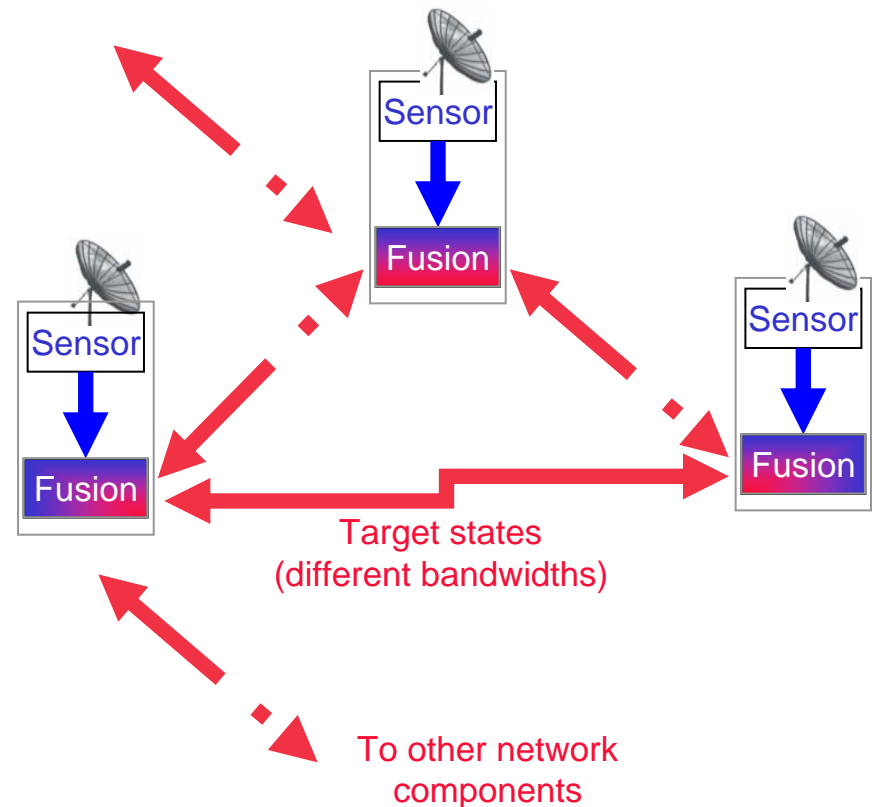
**Time/Structure updates are Dual to state (KF) Observation Updates :**

$$\hat{\mathbf{y}}(k + 1 | k) = \hat{\mathbf{y}}(k | k) + \mathbf{\Omega}[\hat{\mathbf{y}}(k | k) + \mathbf{Y}(k | k)\mathbf{B}\mathbf{u}(k)]$$

$$\mathbf{Y}(k + 1 | k) = \mathbf{Y}(k | k) - \mathbf{\Omega}(k)\mathbf{\Sigma}(k)\mathbf{\Omega}^T(k)$$

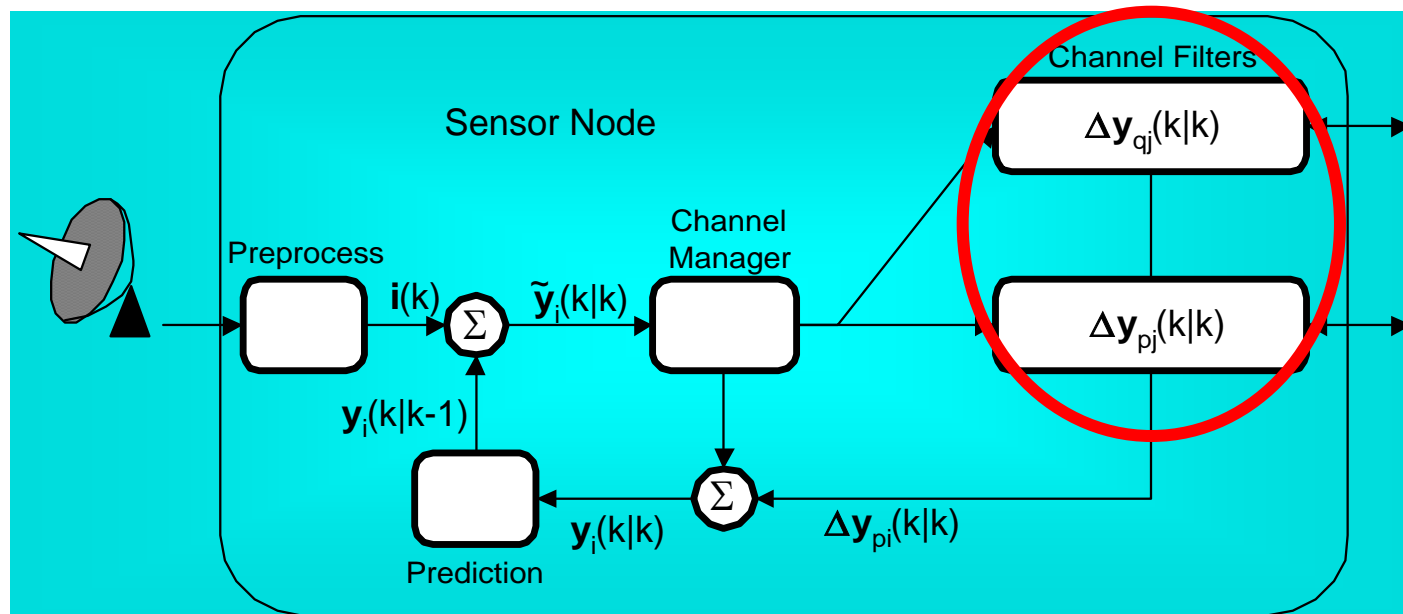
# DDF: The Basic Idea

- Operation:
  - Fusion of local sensor data and communicated states
  - Common, re-configurable, ad-hoc network interface
  - No global fusion location
  - Fully scalable structure



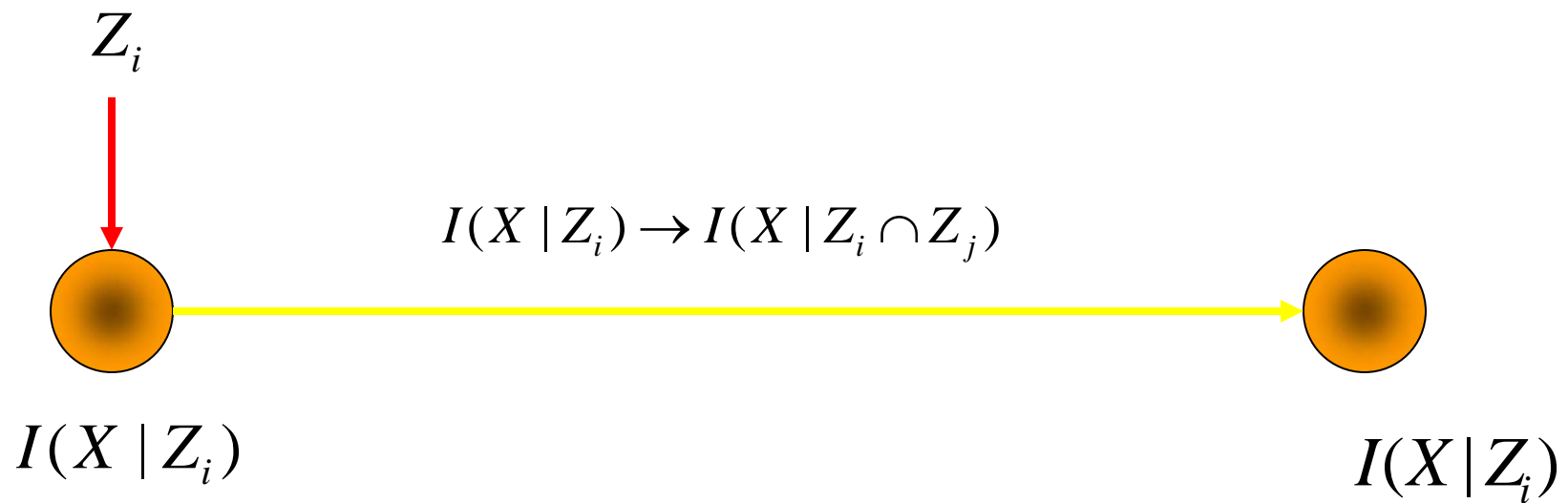
# Operation of Sensor Nodes

- Nodes fuse information from:
  - Local observations, Local predictions, and
  - Communicated information
- Focus on Channels:
  - Communicate local information gain (MI)
  - Assimilate information gains from neighbourhood

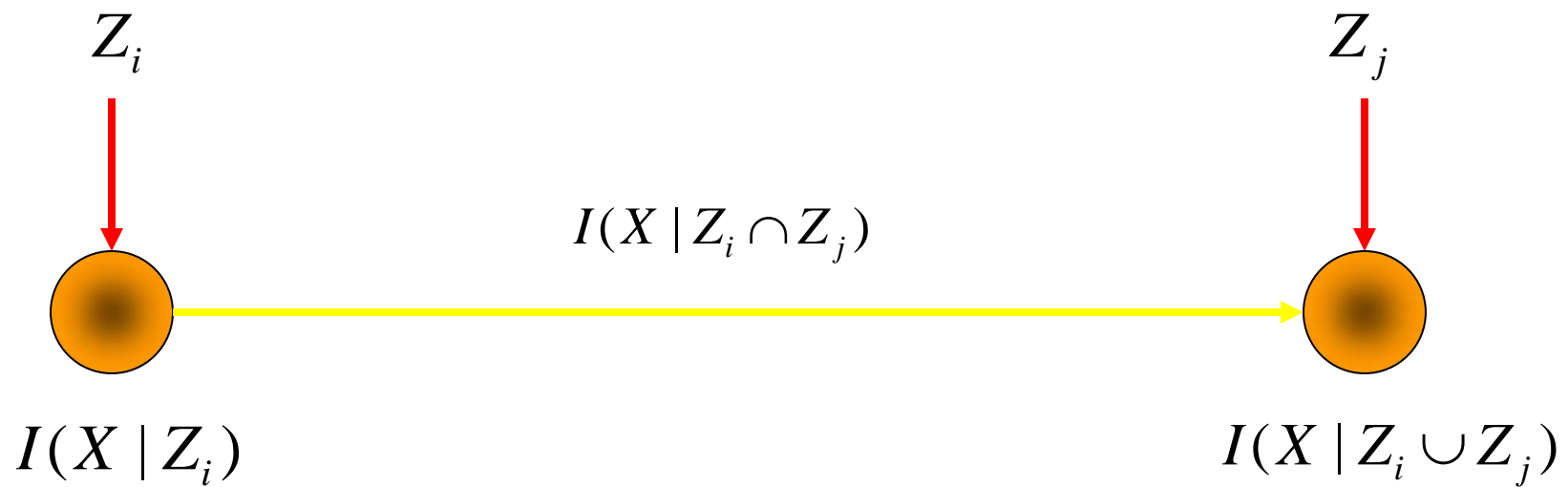




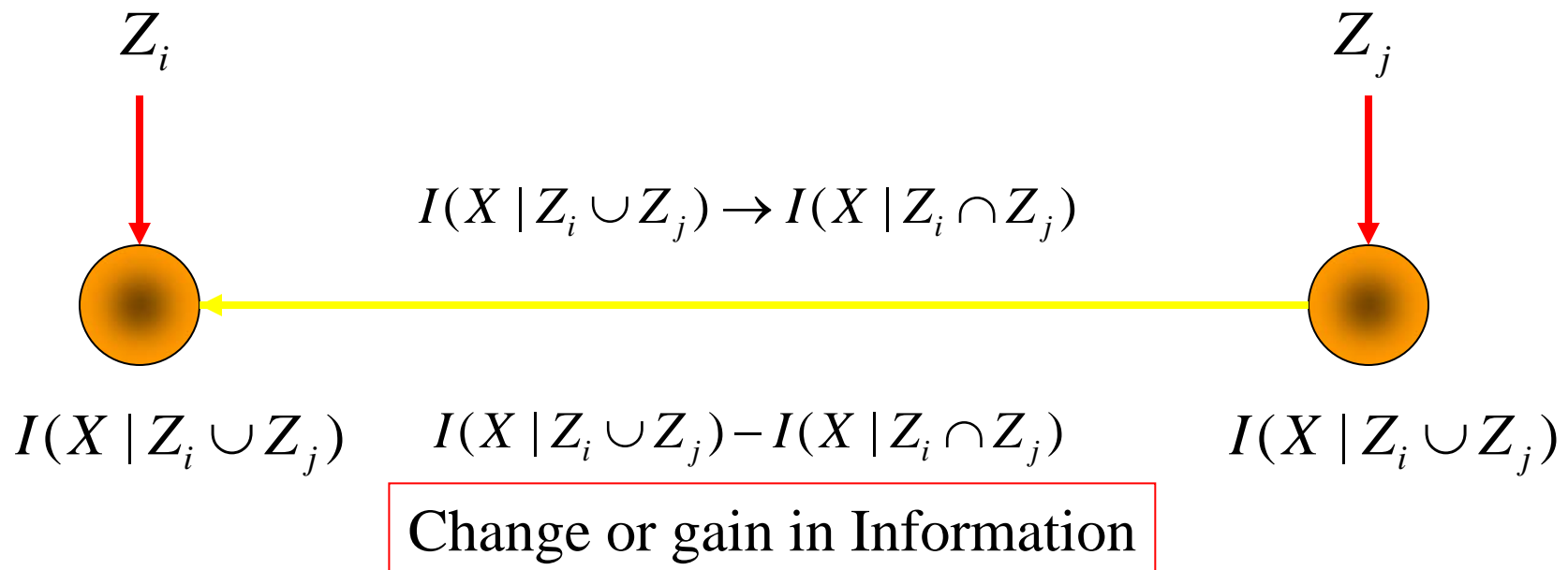
# Operation of Channels



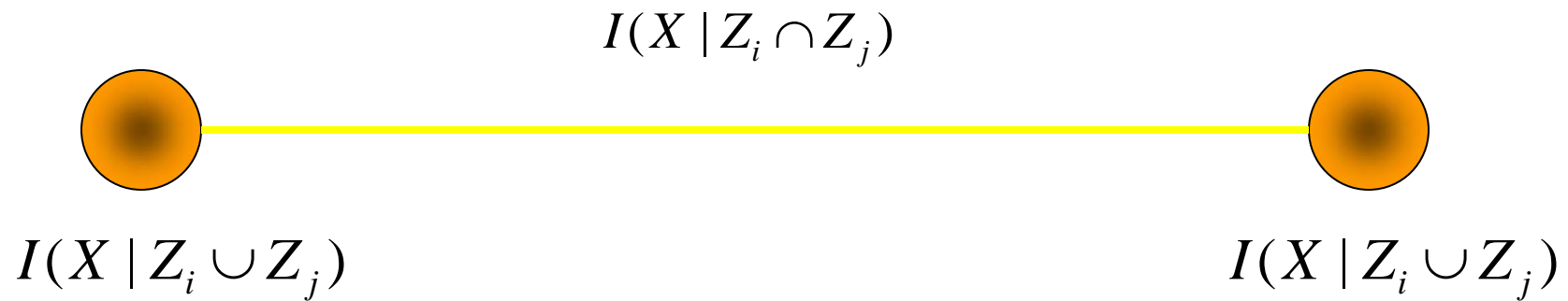
# Operation of Channels



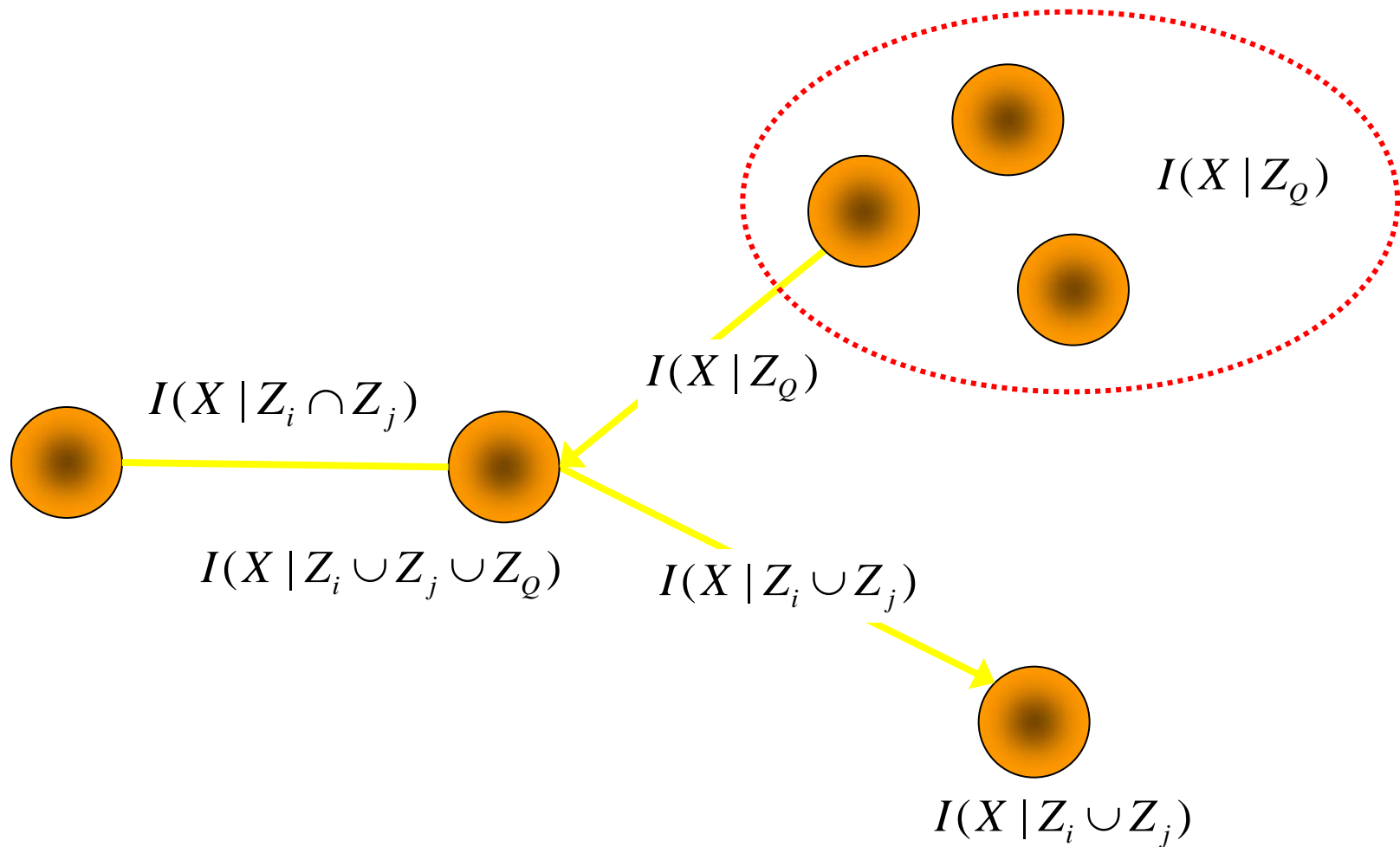
# Operation of Channels



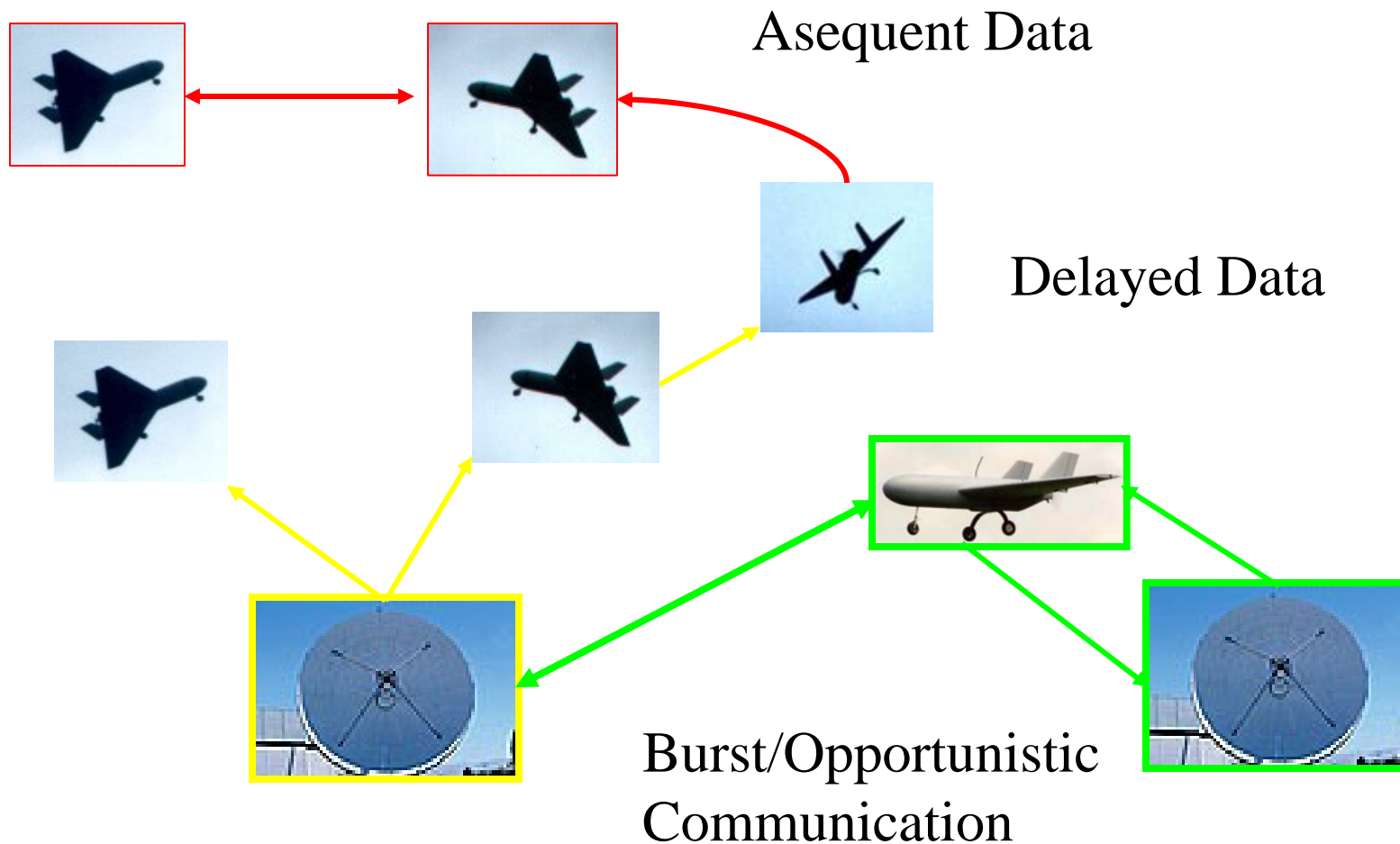
# Operation of Channels



# Scaling The Network

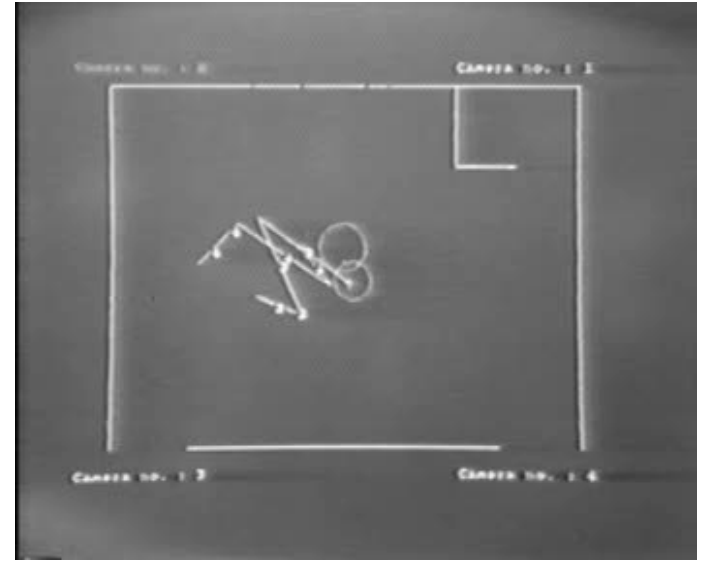


# Issues of Timing

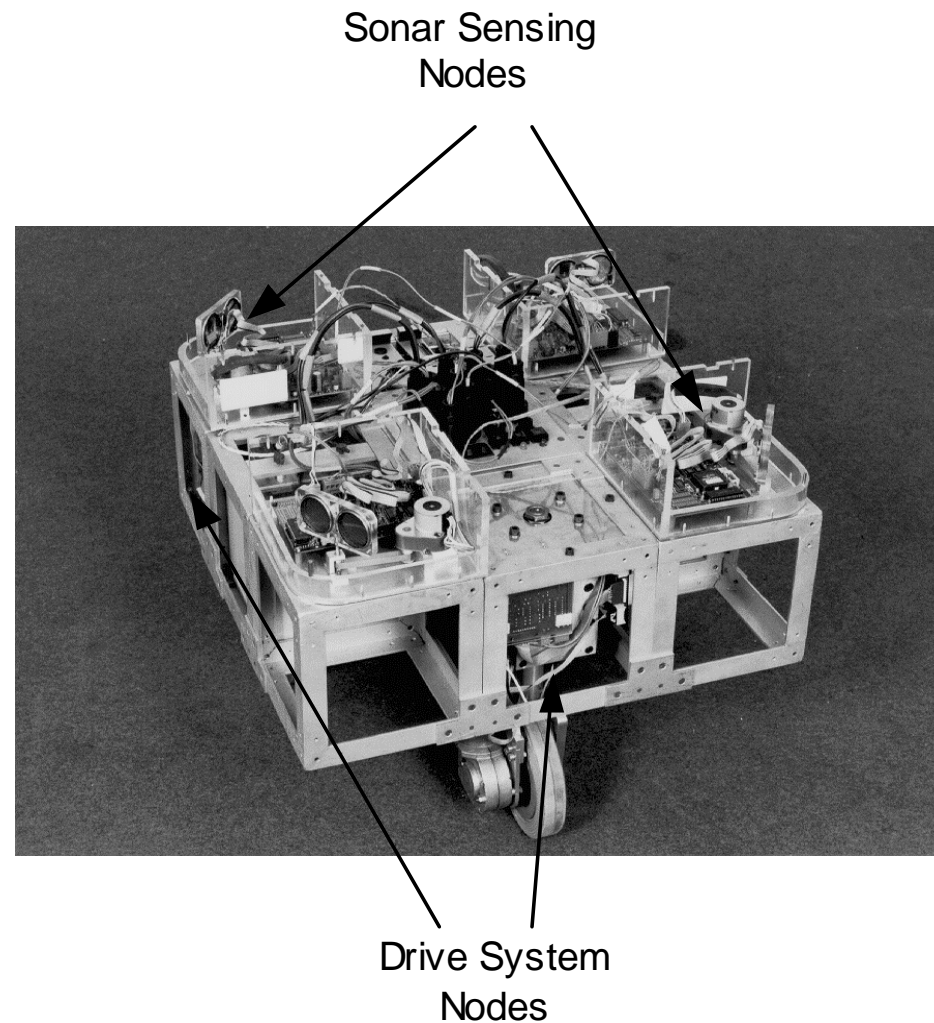


# Early DDF Projects

- SKIDS (1986-1991): Prove essential idea
  - Distributed Tracking of people
  - Cameras, optical barriers, etc
- ISSS (1990-1994): Scalability
  - Large Scale Process plant
  - 250 distributed sensors
- OxNav (1991-1995): Modularity, management
  - Decentralised Navigation
  - Decentralised Sensor Management



# OxNav(1994): A system of modular information components





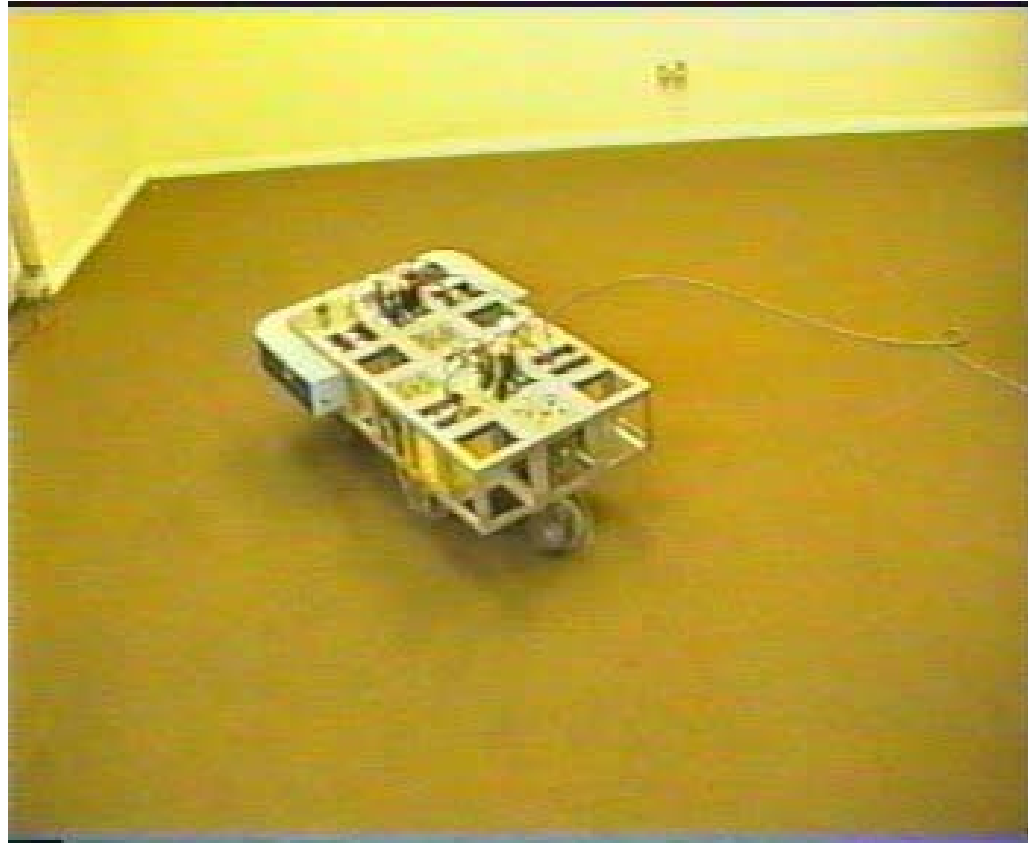
# Navigation and Sensor Management



“Data Fusion and Sensor Management: An Information-Theoretic Approach”

J. Manyika and H. Durrant-Whyte, Prentice Hall 1994. Now only \$900 on Amazon !

# Modular Control

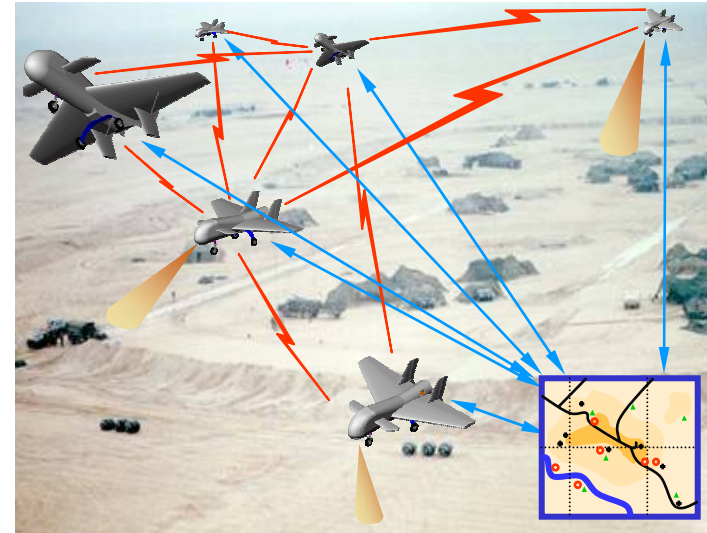


“Decentralised Control”, Arthur Mutambara, CRC Press 1995

In 1995 nobody was interested in sensor networks  
So I went to Australia to do Field Robotics  
Then ...

# ANSER I: Autonomous Navigation and Sensing Experimental Research

**BAE SYSTEMS**



- **Objectives:**
  - To deploy a fully decentralised data fusion system on a group of four or more UAVs
  - To demonstrate functions of target tracking and simultaneous localisation and mapping, decentralised on many sensors in a network of platforms
  - To demonstrate, algorithmically and practically, key network-centric features: Modularity, Scalability, Flexibility and Survivability

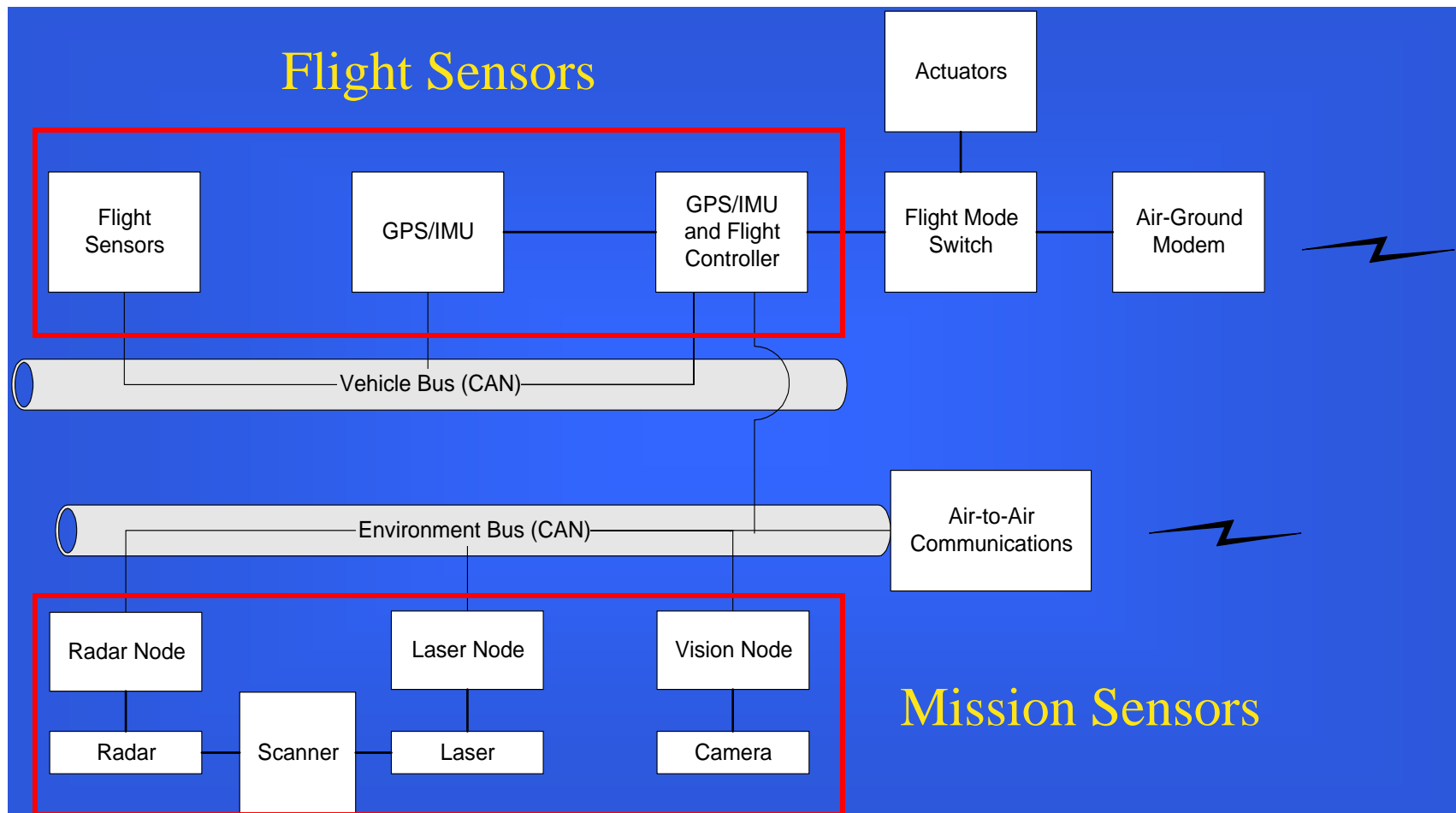
# Flight Platforms



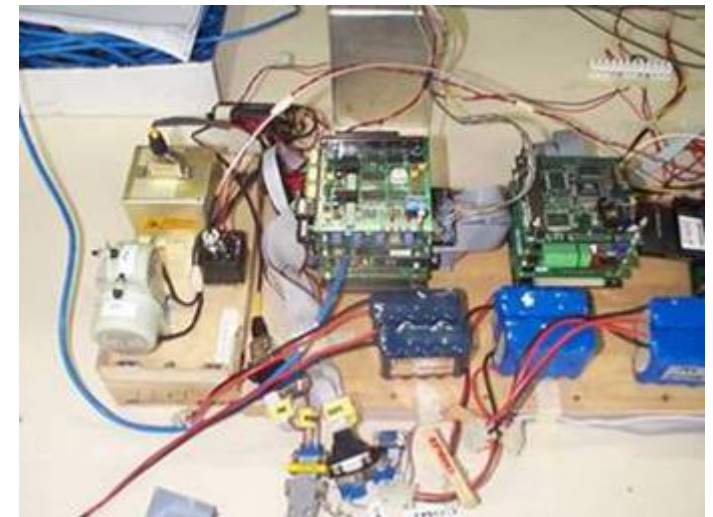
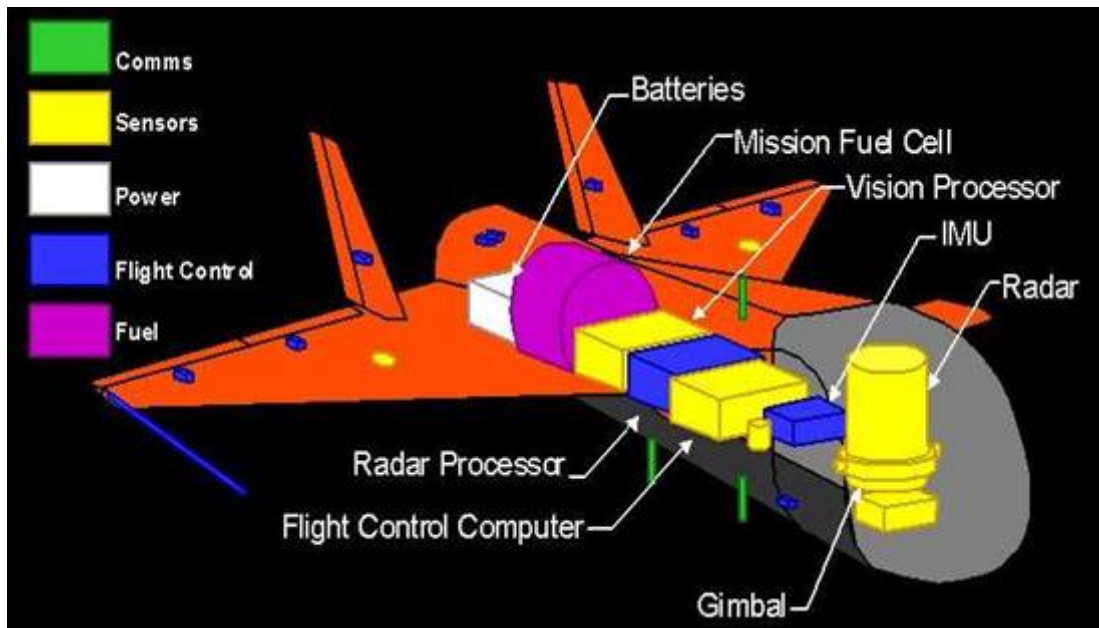
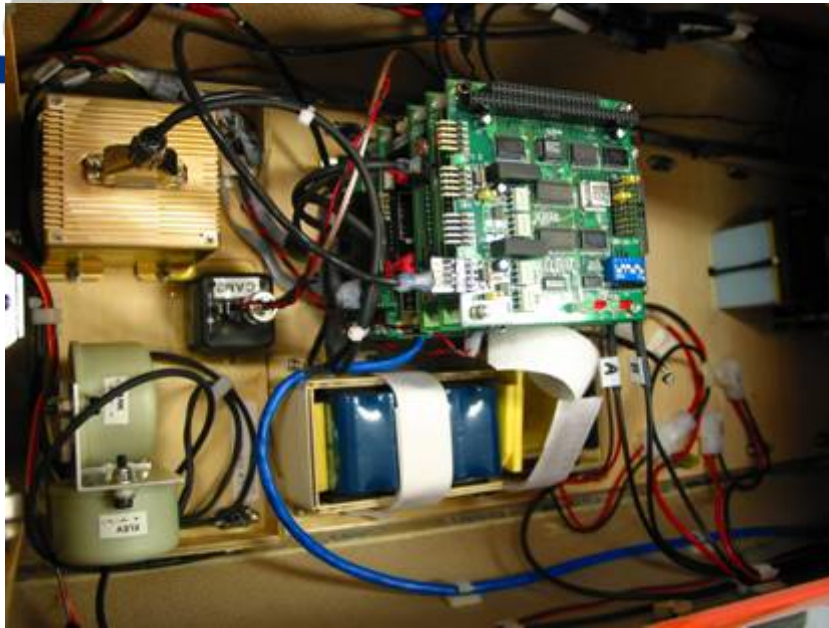
- Four Platforms – Delta Wing Configuration
- Max Speed – 80kts
- Payload Capacity – 20kg
- Wing Span – 3m
- Multiple Sensors per platform
- All modular pay-loads
- All parts interchangeable



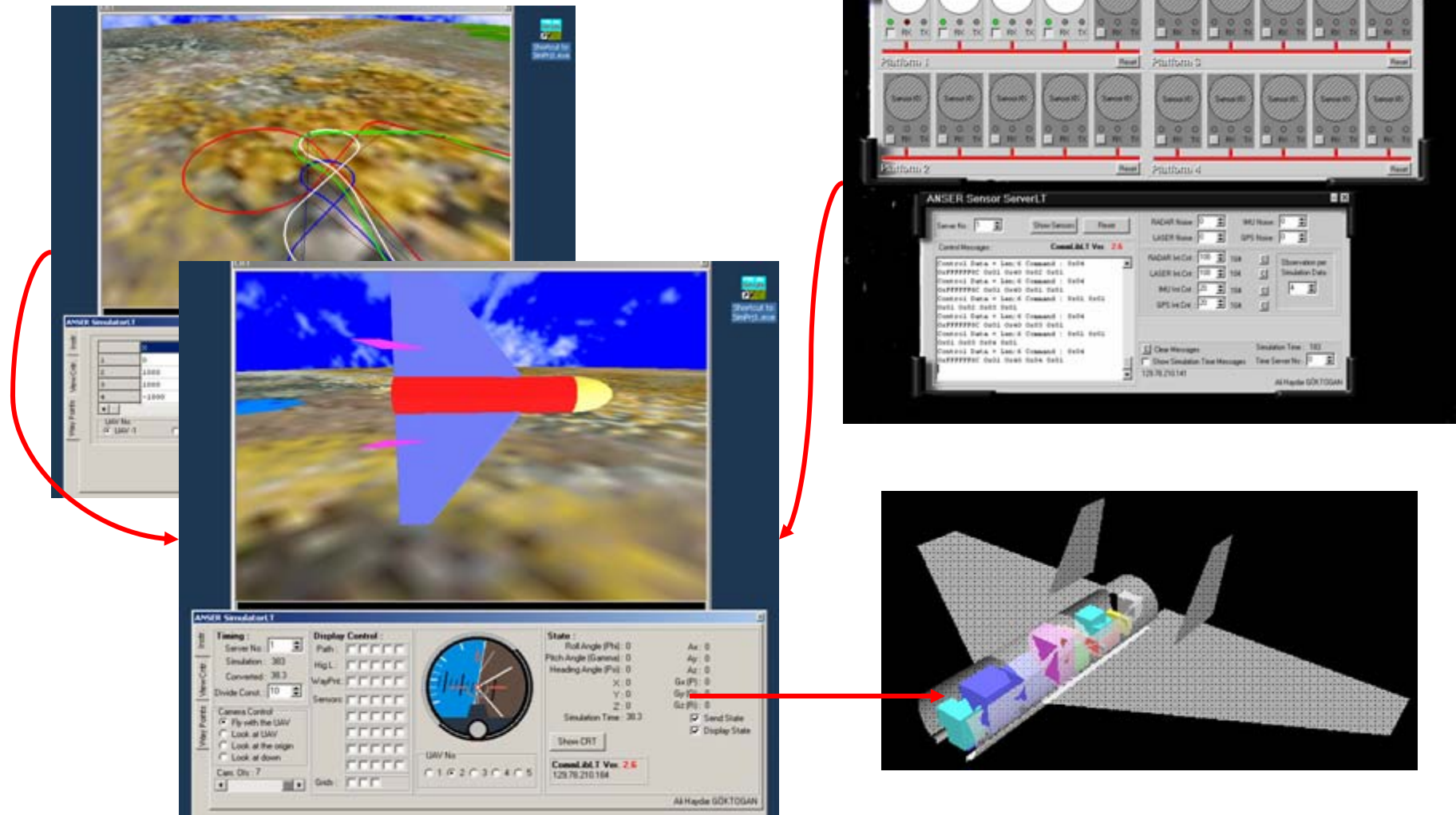
# On-Board Components







# Mission Planning System





# Multi-Vehicle Flights (2000-2001)



# ANSER I: Conclusions

- **Information Communications is key:**
  - Timing, delay, asequent and burst communication
  - Maintaining integrity, extensible network operation
  - Channel and information management
- **Data Fusion issues:**
  - Registration and platform bias estimation
  - Cross-platform data association
  - Weak target information not captured well by information filter alone
- **Non-technical issues**
  - BAE Systems Chairman's Gold Award
  - Output integrated in a number of BAE Systems UK, US and Australian defence programmes

# Decentralised Control

- Mutual Information as a metric for sensor management and control ?
- Maximise the gain in information:
  - Tracking
  - Exploration
  - Search
  - ...

# Mutual Information Gain as a Control Metric

- Mutual Information is an *a priori* measure of average Information gain following observation

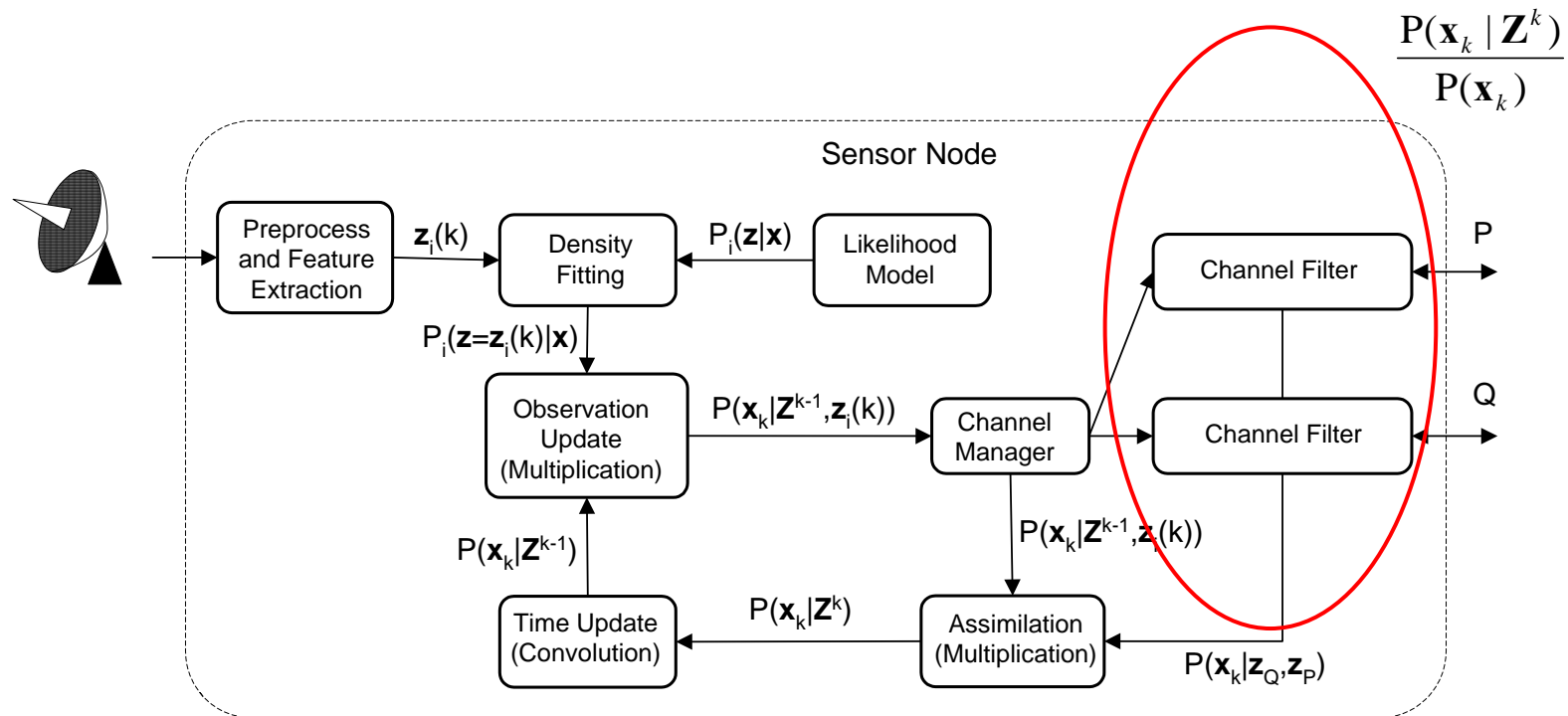
$$I(\mathbf{x}(t) : \mathbf{z}(t)) = \mathbb{E} \left[ \log \left( \frac{P(\mathbf{x}(t) | \mathbf{z}(t))}{P(\mathbf{x}(t))} \right) \right]$$

Measures “compression”  
of posterior density

- Choose the sequence of observations  $\mathbf{z}(t)$  which maximise mutual information gain over a horizon
- Observations depend on platform state  $\mathbf{x}(t)$
- State is governed by some control input  $\mathbf{u}(t)$
- Choose  $\mathbf{u}(t)$  to maximise information gain

# Mutual Information in DDF

- Mutual Information or information gain, is exactly what is communicated in the DDF !
- Can be easily exploited in sensor management, communications and platform control

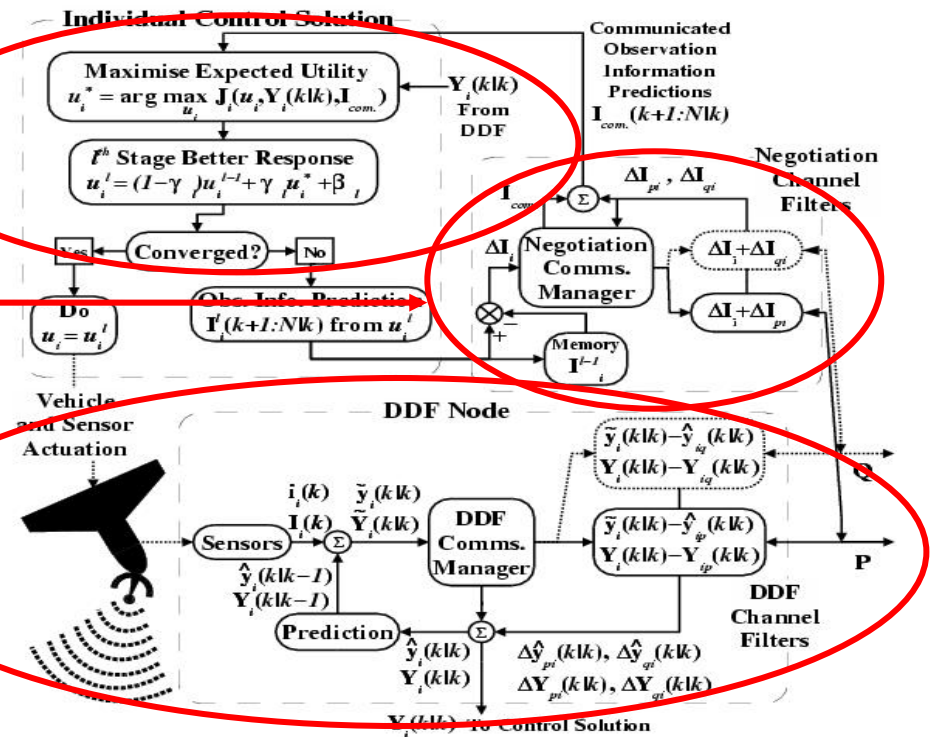


# Information and Systems Design

Local  
Controller

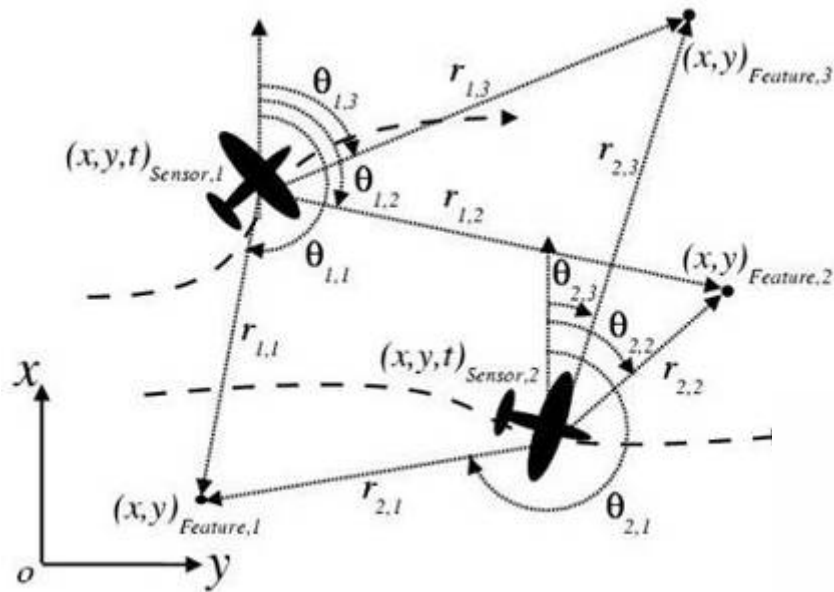
Internode  
Negotiation

Conventional  
DDF Node



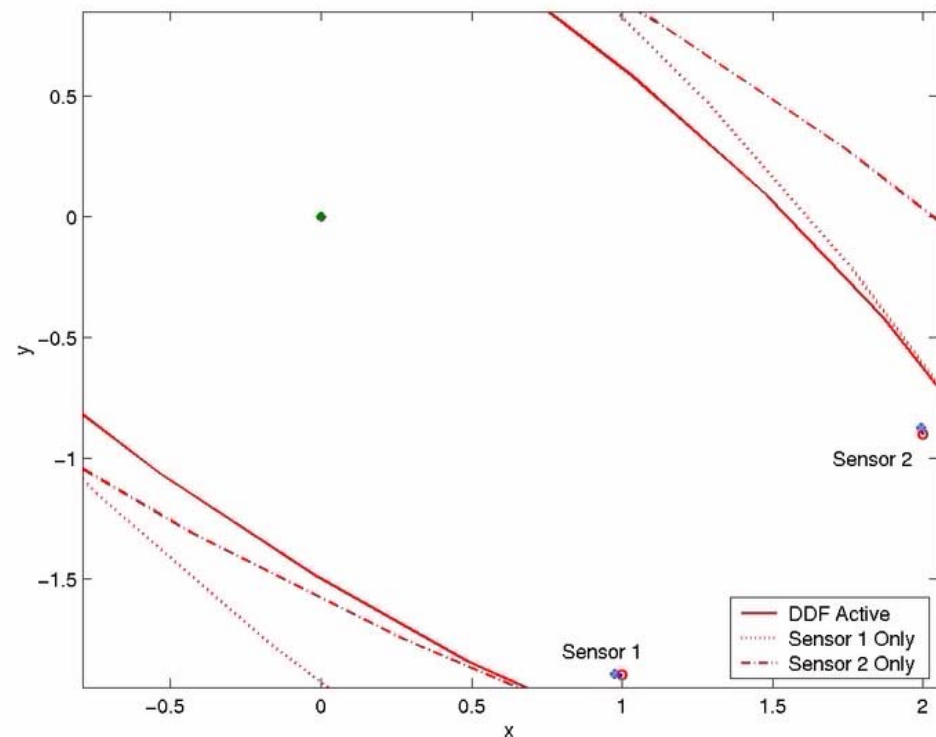
Ben Grocholsky, PhD U. Sydney 2002

# Example Cooperative Control



- The trajectory that maximises information
- Information shared (DDF)

- Inherits DDF properties:
  - Scalability
  - Survivability

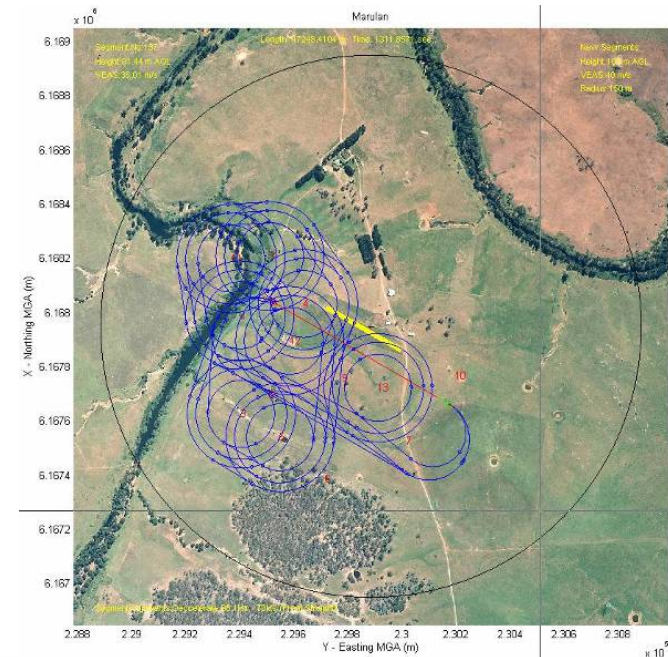




# Future Cooperative UAVs



- How best to use tactical UAV fleets ?
- A list of candidate targets of interest
- Coordinate a UAV fleet with mixed sensors to:
  - Locate,
  - identify and
  - prosecute targets
- Demonstrate this





## Set-up

- DDF Enabled on all platforms
- Mutual information on target location and IDs
- A set of UAV manoeuvres:
  - Point-to-Point
  - Orbits
- K-step look-ahead

$$\mathbf{I}_{Orbit} = \frac{R\omega}{V} \int_{\varphi_s}^{\varphi_e} \mathbf{I} d\varphi$$



# Targets





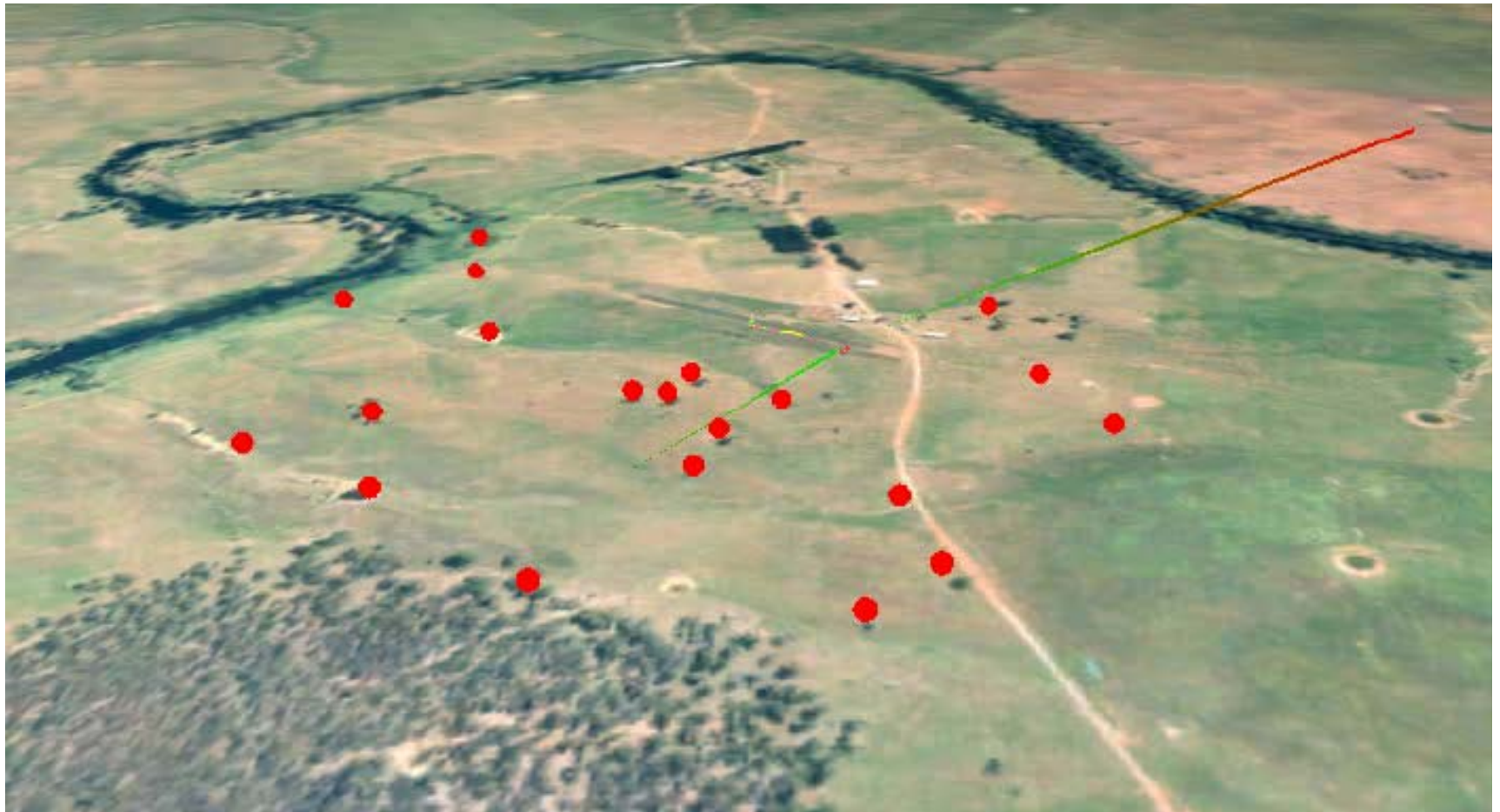
# Cooperative Demonstration



# Two Vehicle Demonstration



# From the Ground Station



# ANSER II - Aims

BAE SYSTEMS

- Develop a general mathematical framework for probabilistic fusion in information networks.
- Address issues of efficient information communication and assimilation in information fusion networks.
- Develop explicit models of node performance and use these in designing and building networks of “systems of systems”.
- Demonstrate these in combined air/ground human/autonomous sensory networks



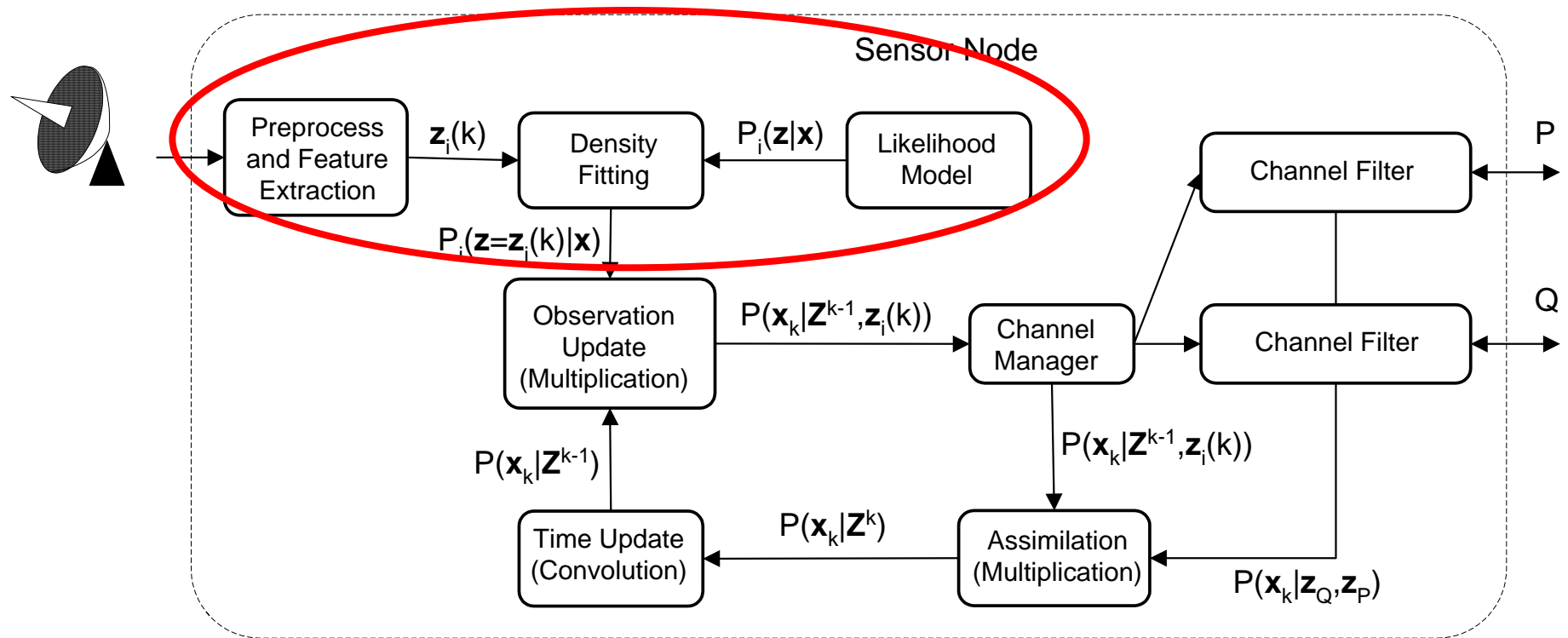


# ANSER II Demonstration Project (2004-06)



- Full Bayes DDF for fusion of heterogeneous data from UAVs, UGVs, human and data base sources
- Model general feature types; trees, buildings, dams, etc
- Identify and label features, integrate human inferences
- Real-time exploitation of network data by air, ground, human

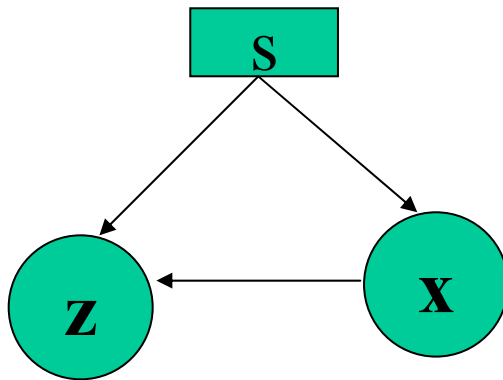
# Bayesian DDF Node Structure



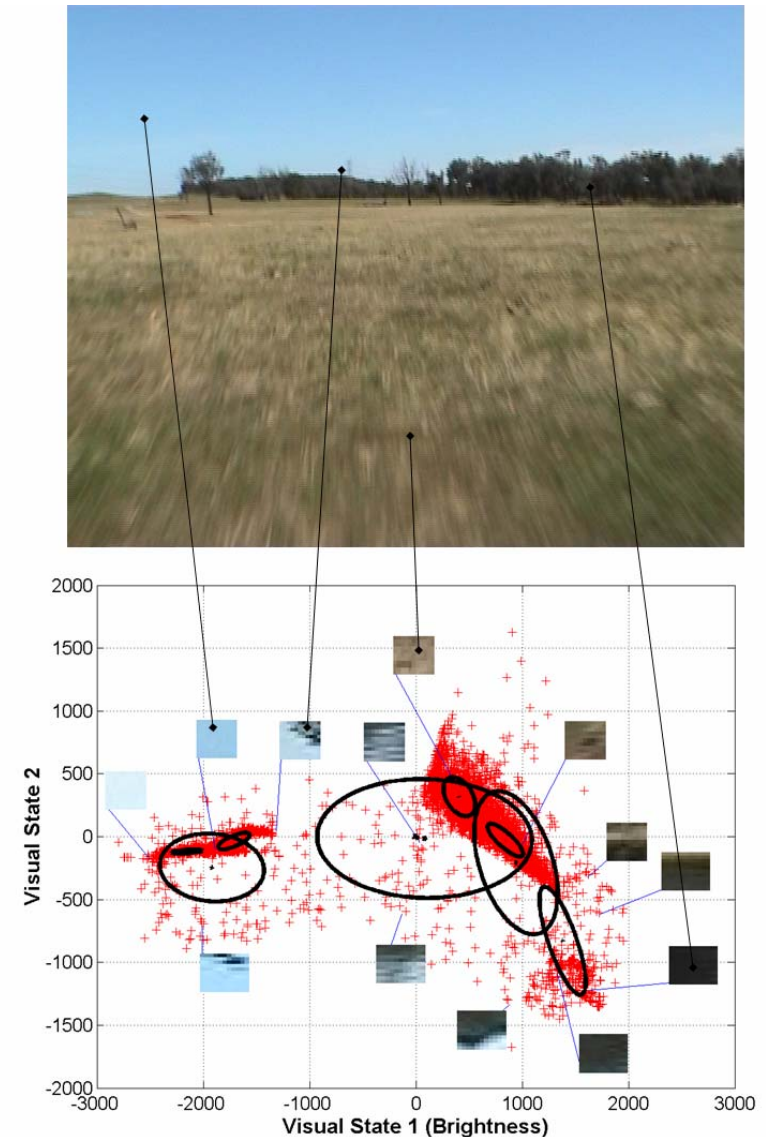


## Step I: Model Generation

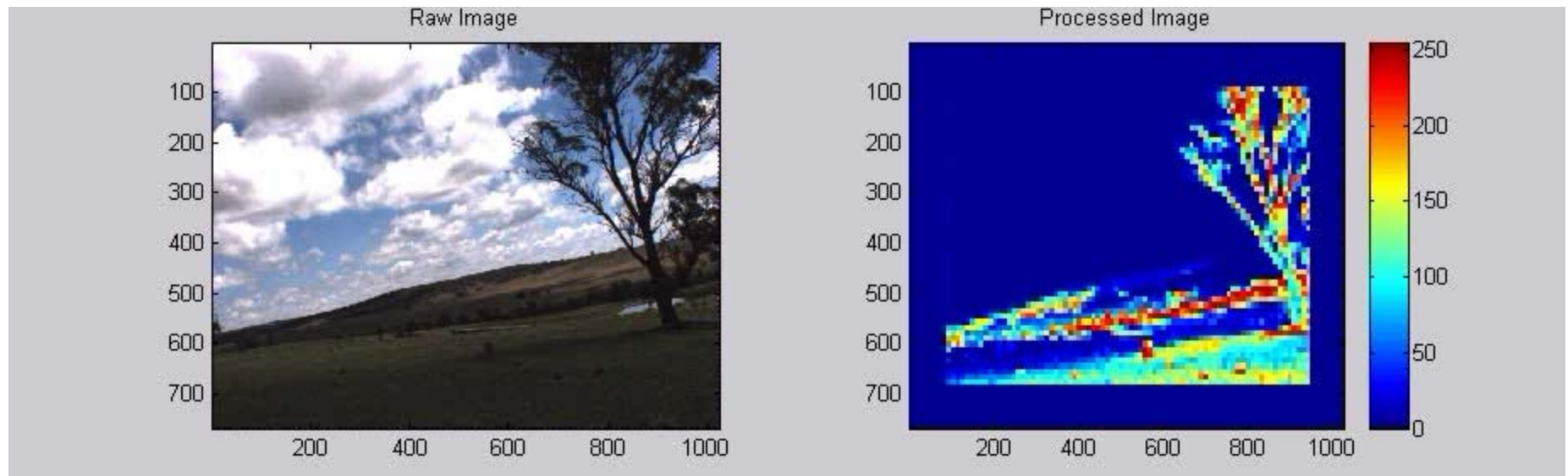
- NLDR (ISOMAP) on image patches
- Find low-D representation for significant patches of interest
- Use VBEM to find number and centre for mixture model



$$P(\mathbf{z}, \mathbf{x}, \mathbf{s}) = P(\mathbf{z} | \mathbf{x}, \mathbf{s})P(\mathbf{x} | \mathbf{s})P(\mathbf{s})$$

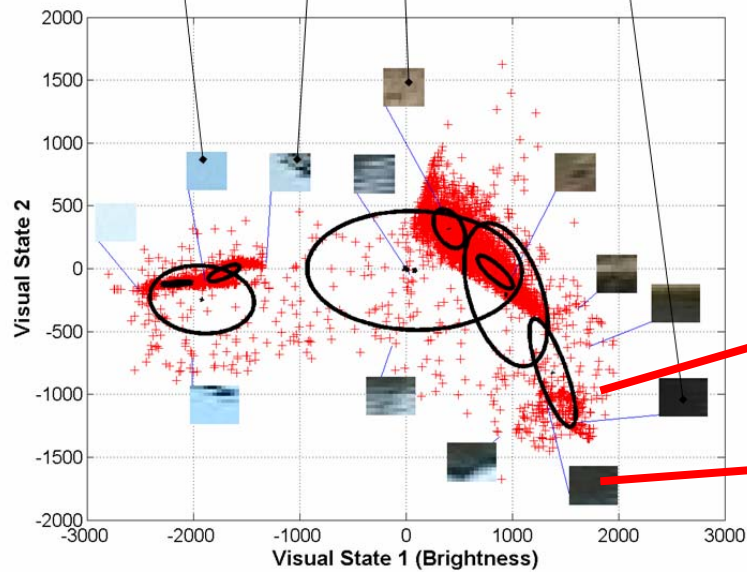


## Step II: Model Inference



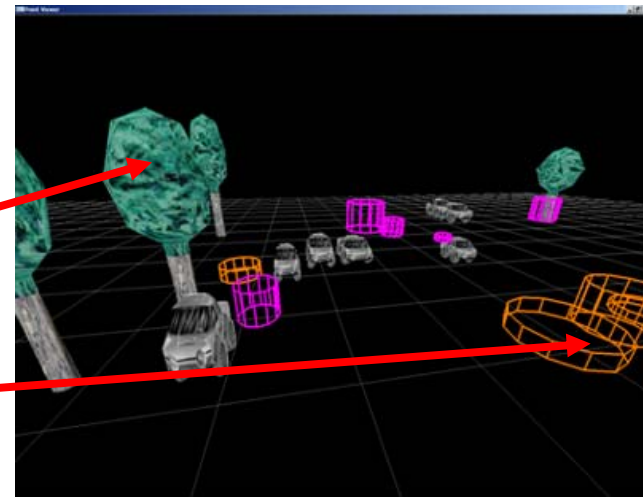
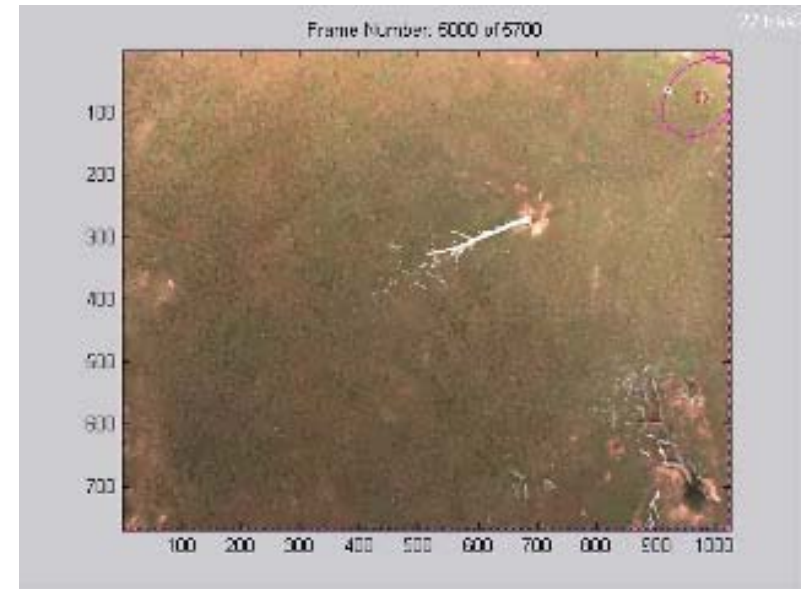
$P(\mathbf{z} \mid \mathbf{x}, \mathbf{s}) = P(\mathbf{z} \mid \mathbf{x} = [\mathbf{x}, \mathbf{s}])$  is the required likelihood for inference

## Step III: Assigning Labels



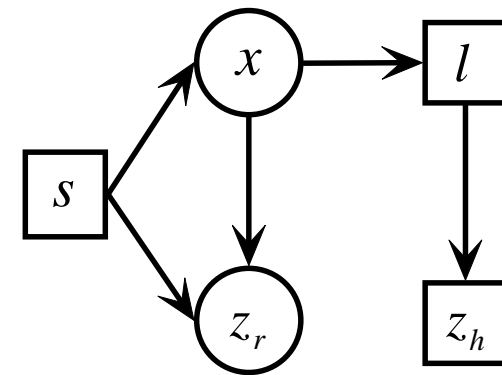
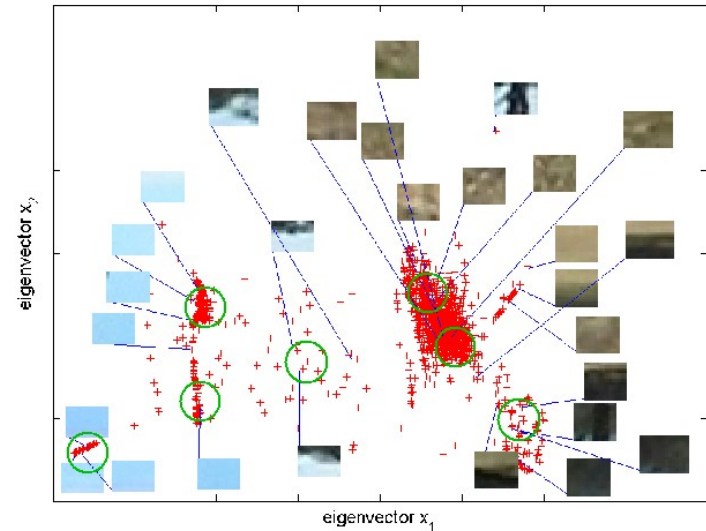
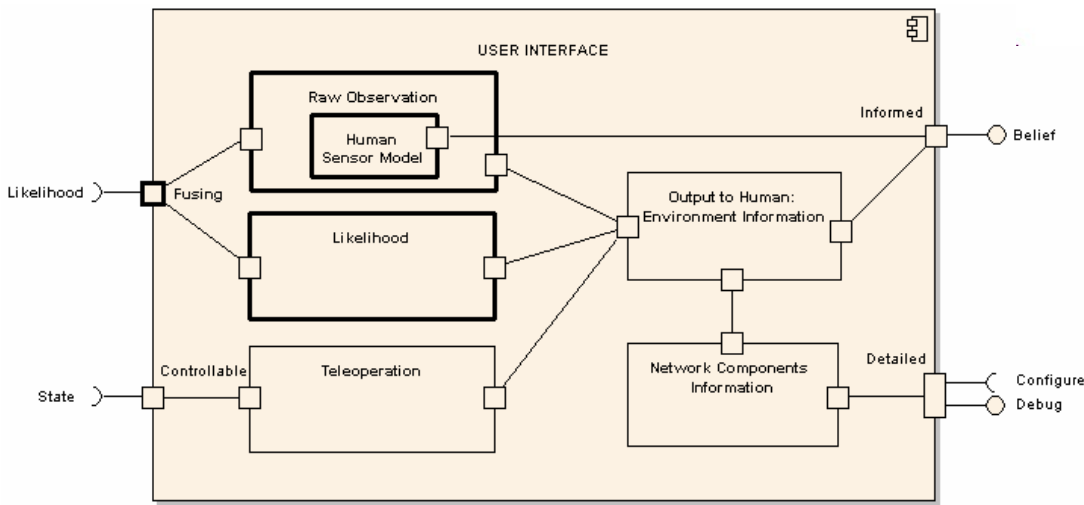
“Tree”

“Stuff”

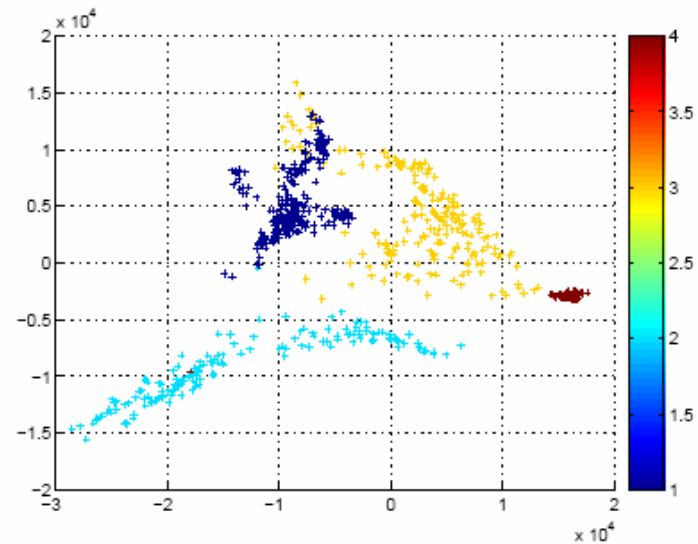
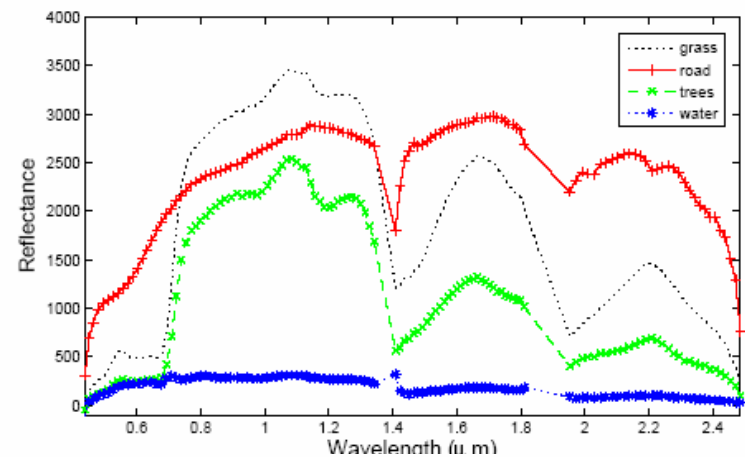


# Human DDF Node

- Human operator input:
  - Metric Information
  - Labels
  - Context
- On-line estimation of “operator likelihood”
- Anonymous network queries



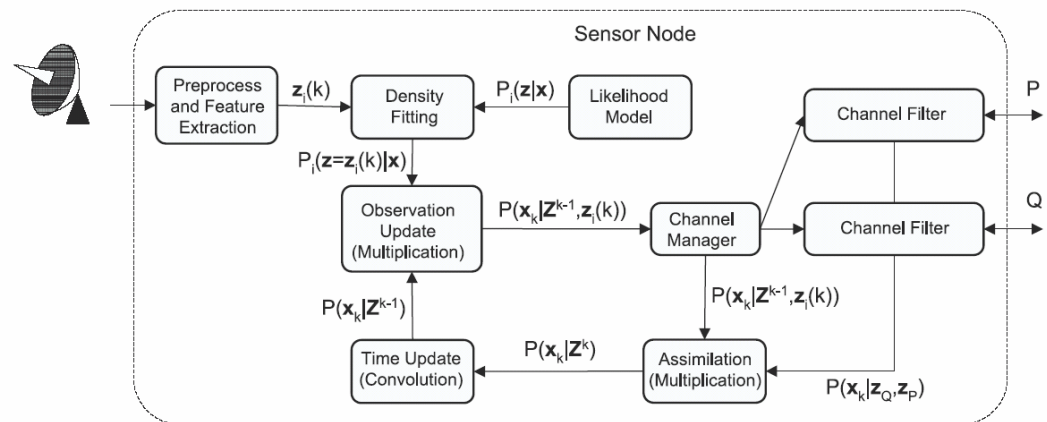
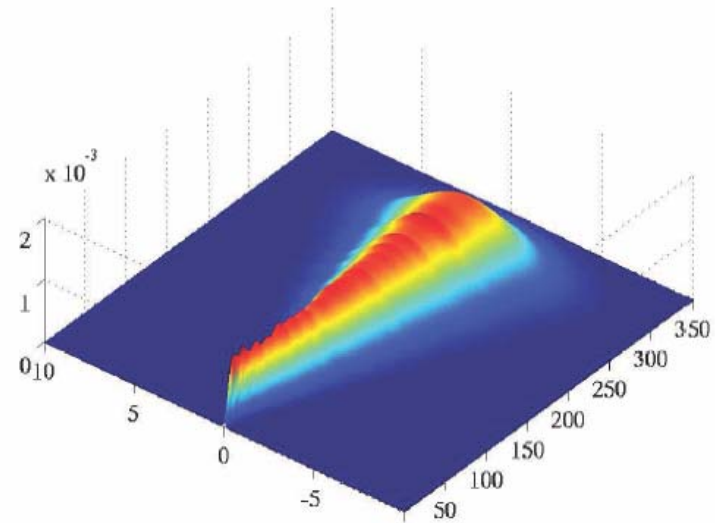
# Example External Data Source: Hyperspectral Imagery





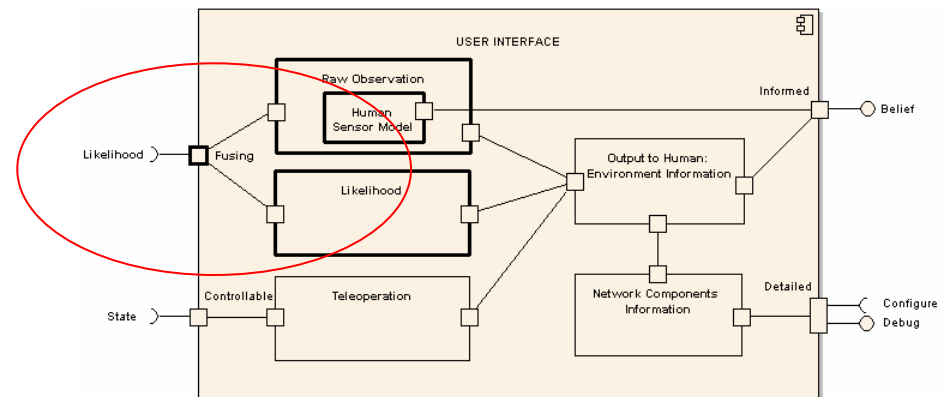
# Feature-Based Tracking

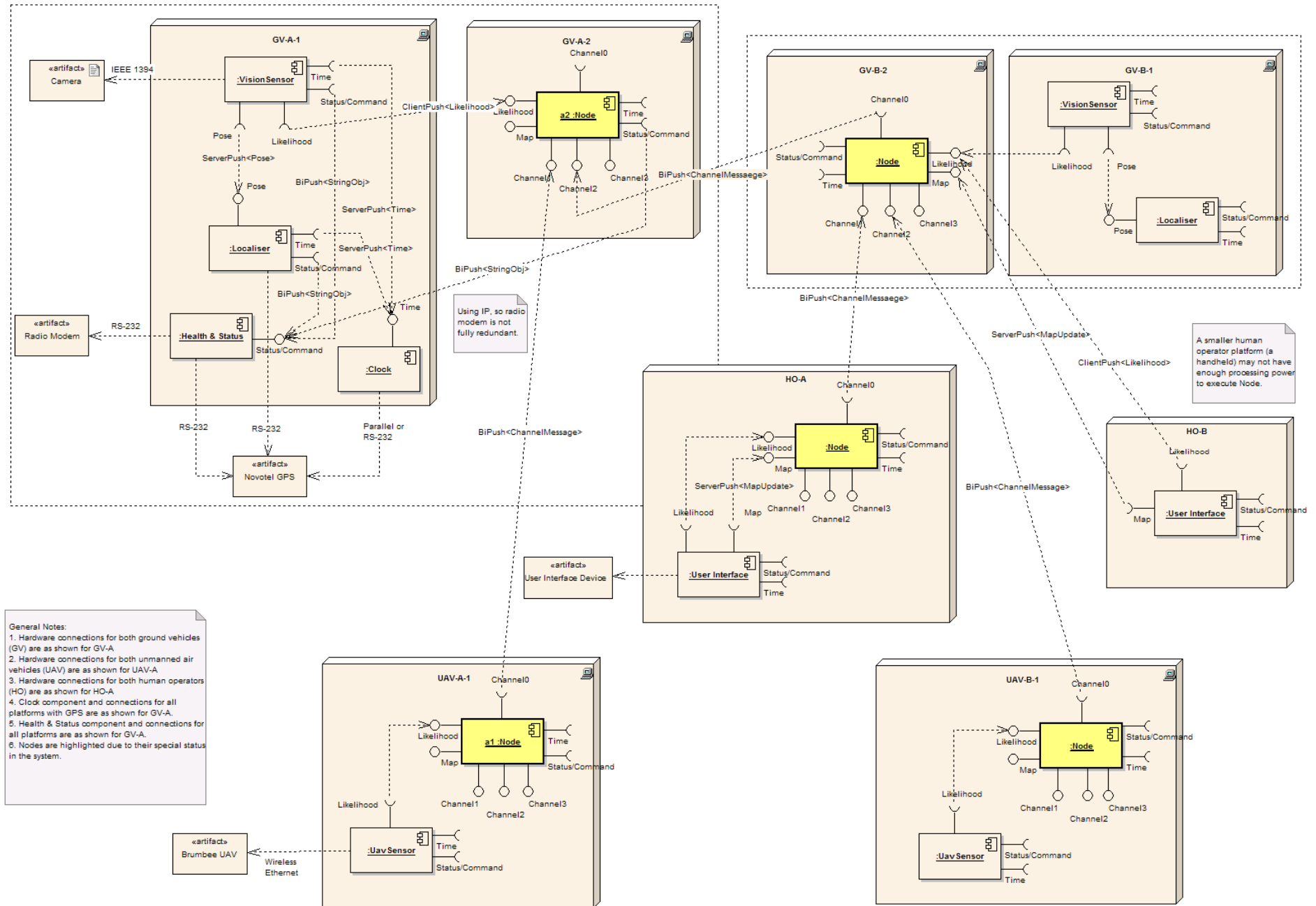
- General probability models:
  - Non-Gaussian location
  - Feature properties
  - Target IDs



# System Configuration and Design

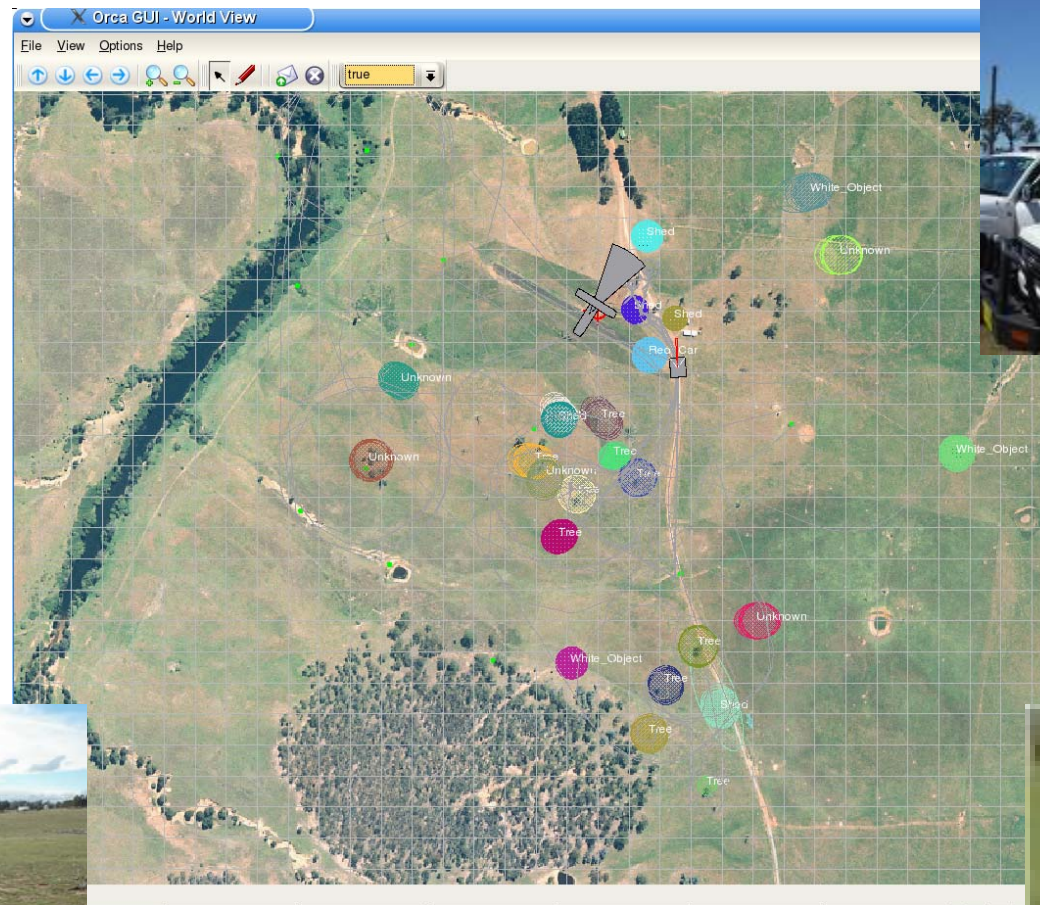
- Each module
  - Presents a likelihood
  - Generates a posterior
  - Computes a mutual information wrt a prior
- Mutual information in network determines
  - Who does what
  - Who talks to who
- Network properties
  - Survivable
  - Scalable





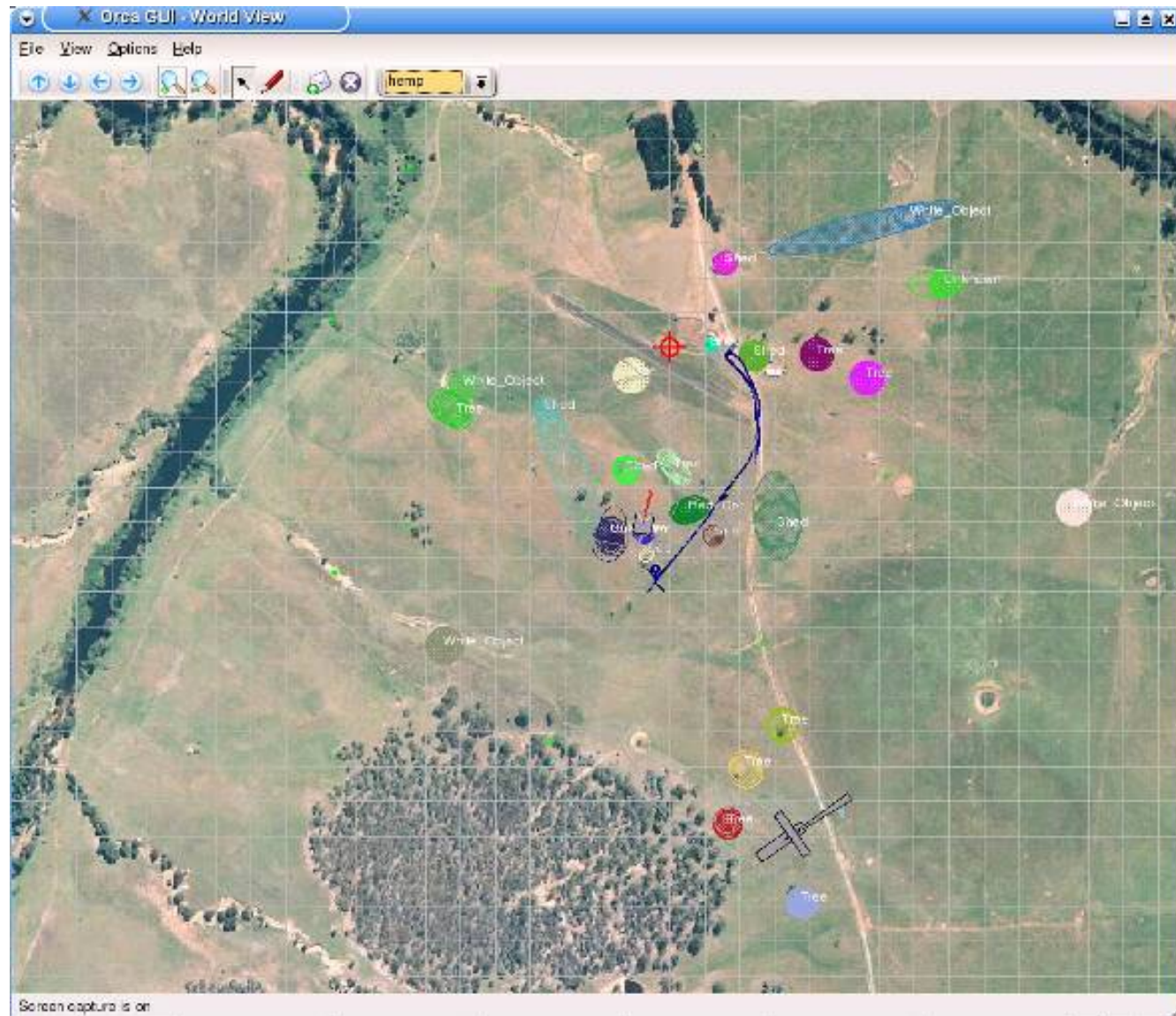


# Mission System Implementation



System Video

# ANSER II System Demonstration



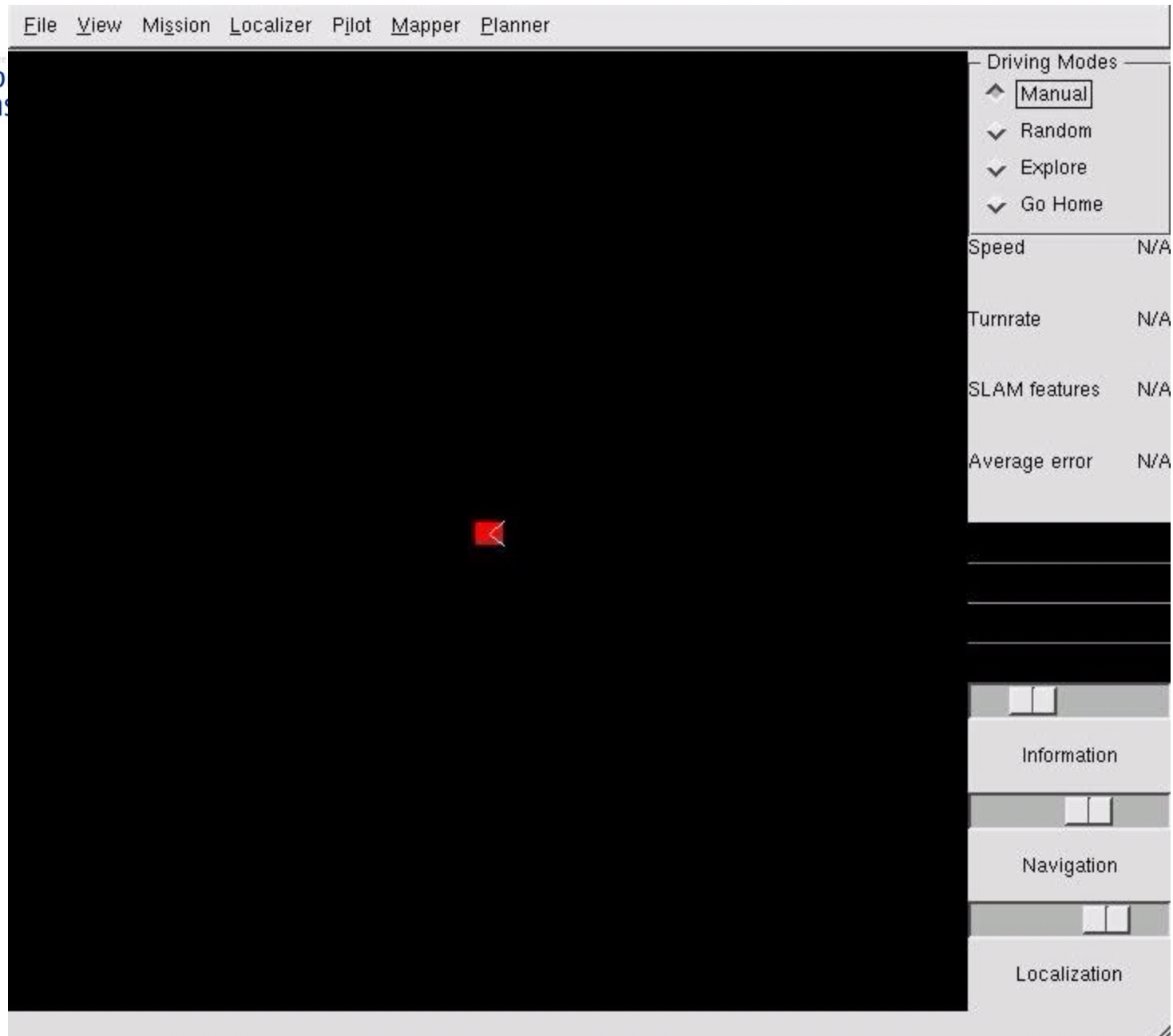


# ANSER II Conclusions

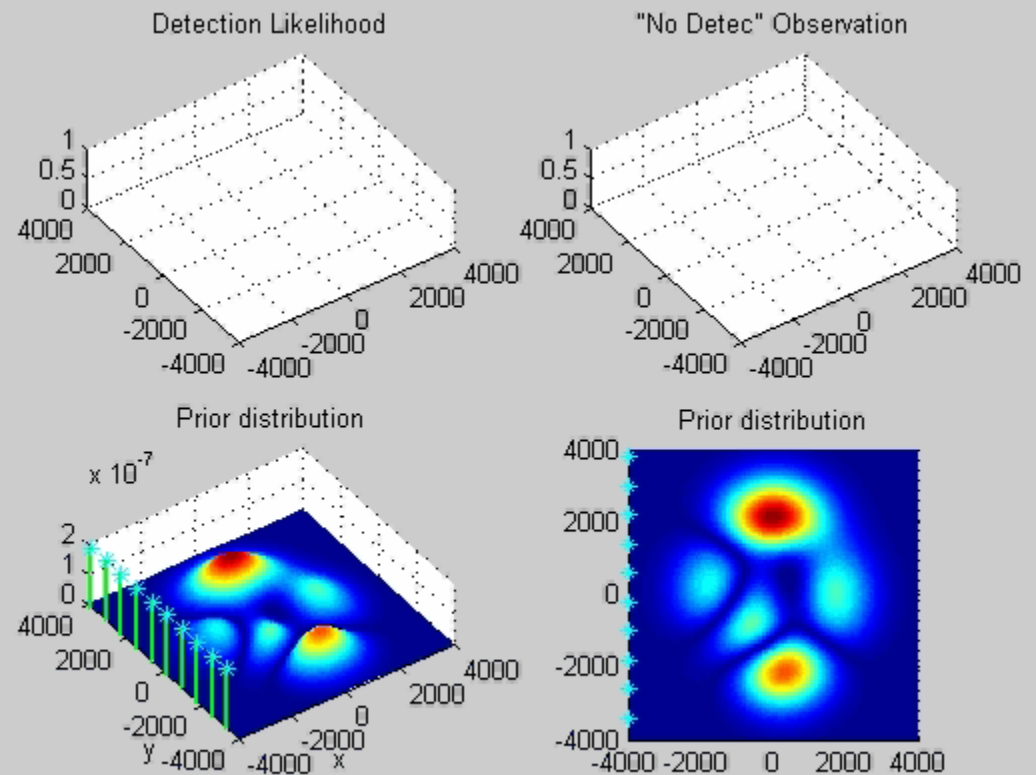
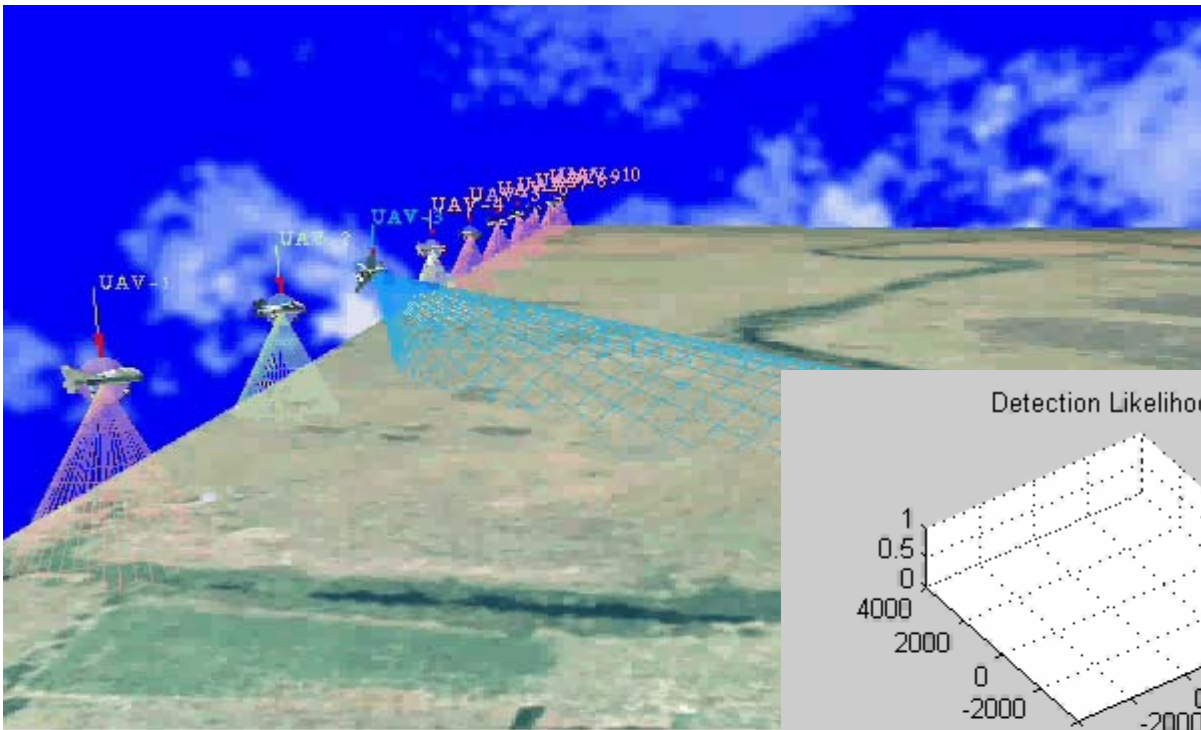
- Fusion
  - General probabilistic models can be effectively decentralised
  - Modular, scalable, heterogeneous systems
  - Network management
- Systems design
  - Quantitative metrics for information-gathering systems
  - A priori and context dependent performance prediction
- This is a limited class of systems

# Extending the Paradigm

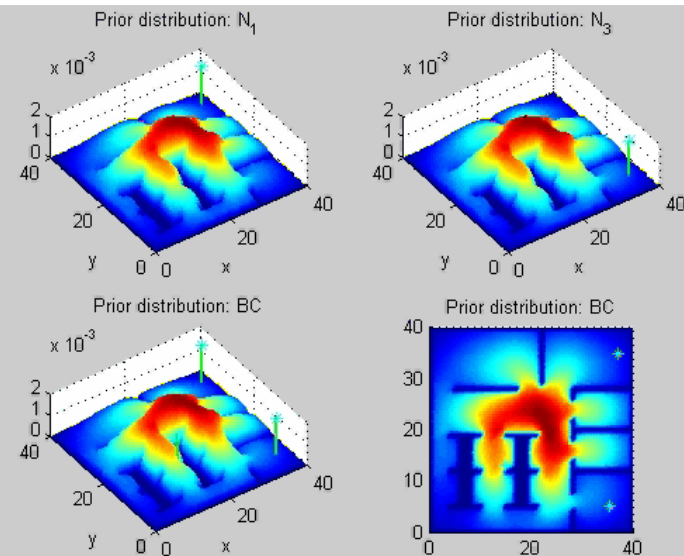
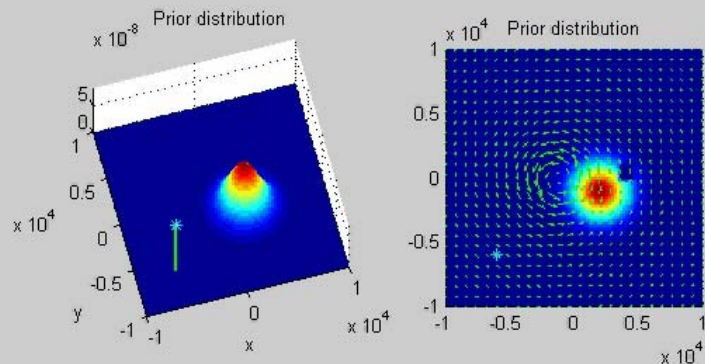
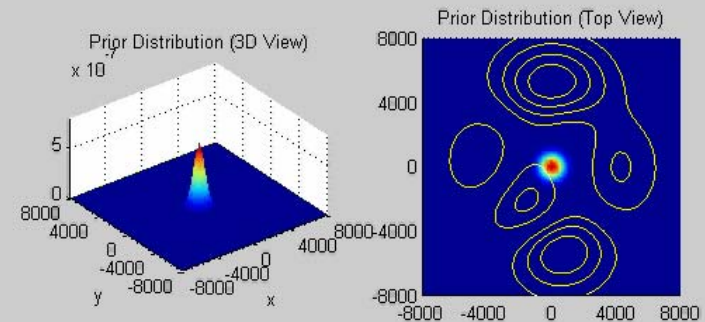
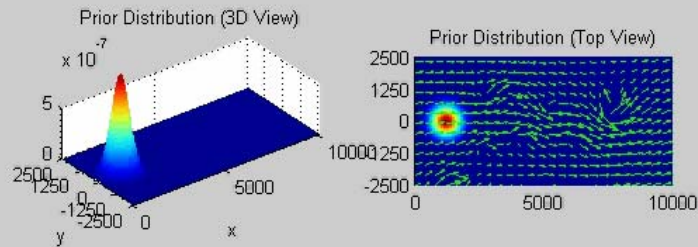
- Information maximisation control:
  - Decentralised structure
  - Scalable and system-robust
- Other information-maximising control
  - Resource use (platform, communications)
  - Target cuing, hand-off, etc
  - Search
  - Exploration



# Multi-UAV Simple Search



# Exploiting Domain Knowledge: Dynamic, soft and hard constraints





# Multi-UAV, Multi-Objective Control

- **Exploration**

$$J_i^{(expl)} = \int_0^T [\omega_i \delta_i(t) (i_i(t) - i_{\max}(t)) + (\omega_i - 1) \|\dot{\mathbf{u}}_i(t)\|] dt$$

- **Search**

$$J_i^{(search)} = \int_0^T f(t) dt$$

- **Tracking**

$$J_i^{(track)} = m \int_0^T \dot{v}(t) dt$$

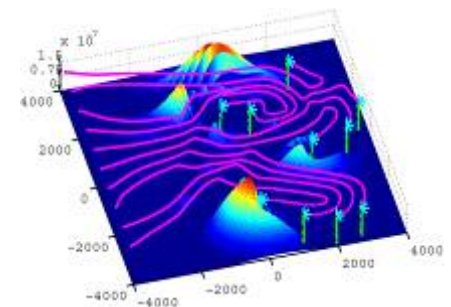
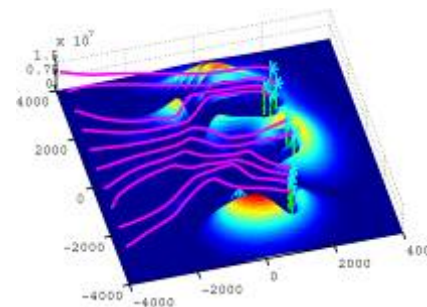
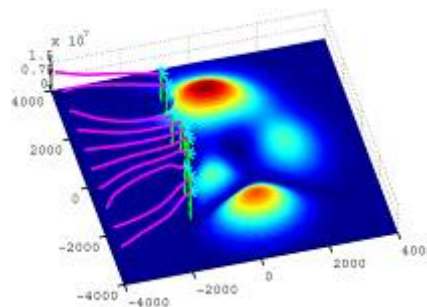
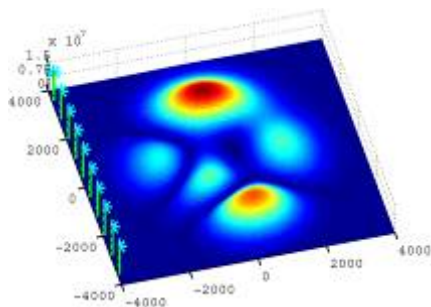
- **Engagement**

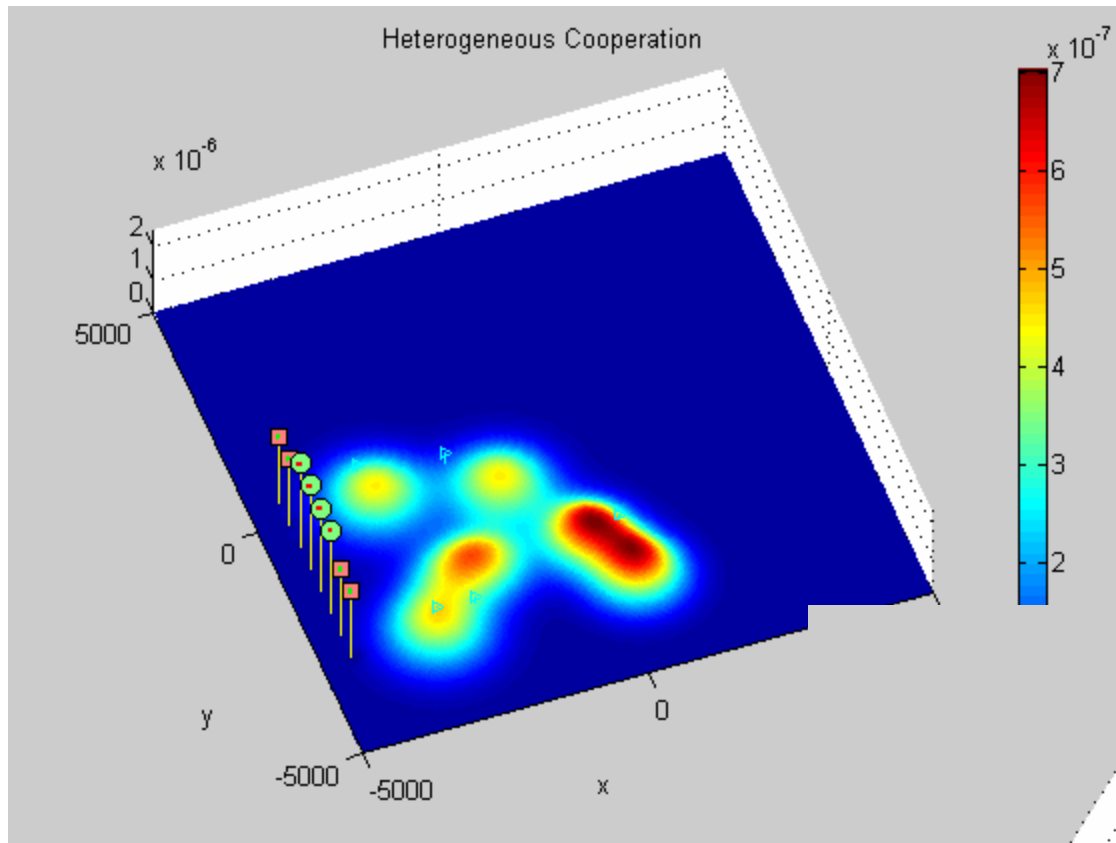
$$J_i^{(engage)} = T$$

- **AFRL WP AFB Vehicles**  
Directorate and AOARD

- **Objectives:**

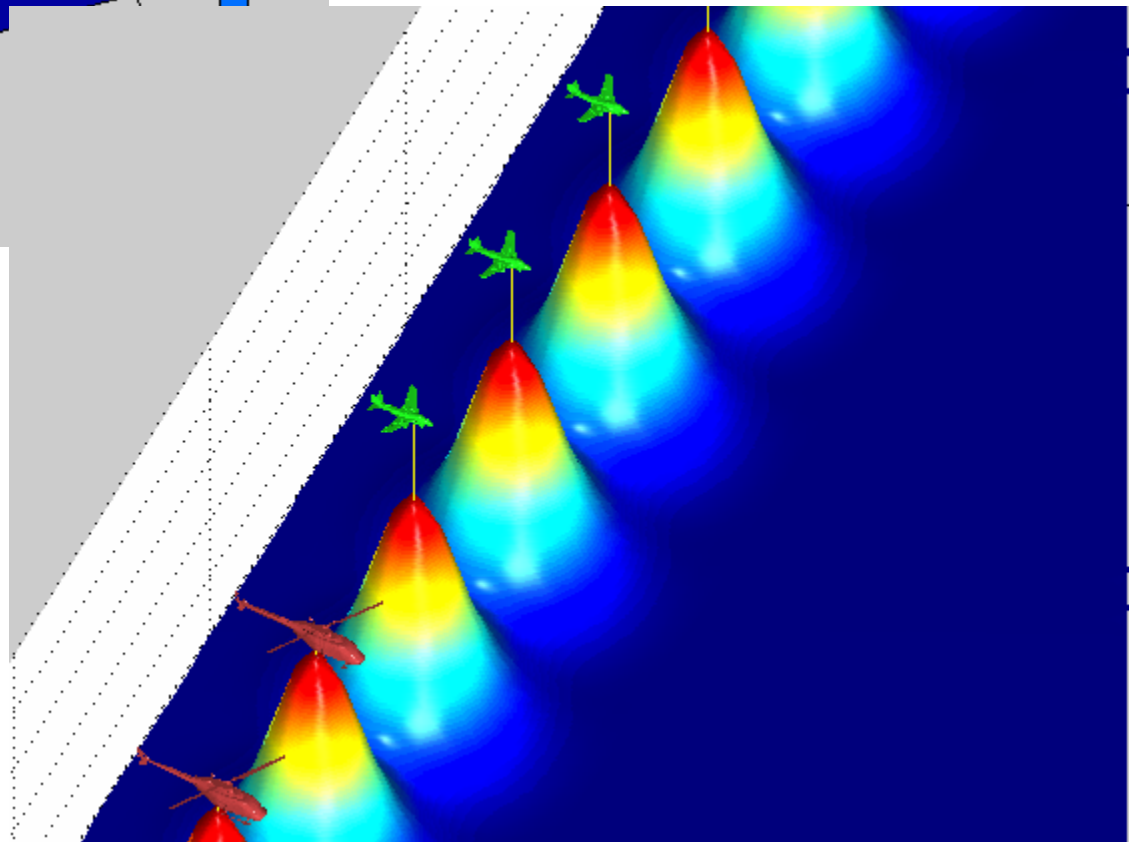
- A general information framework for cooperative control
- On-line decentralised controllers for networks



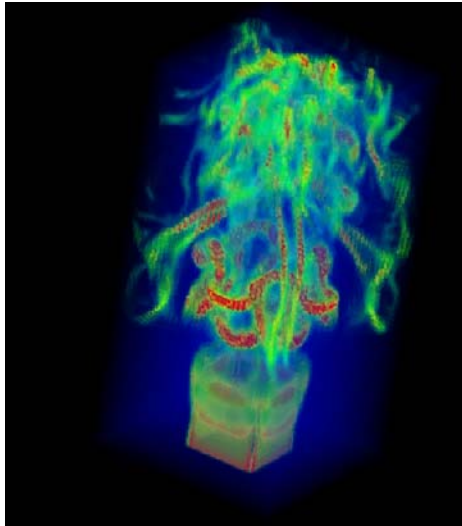


Search and Rescue

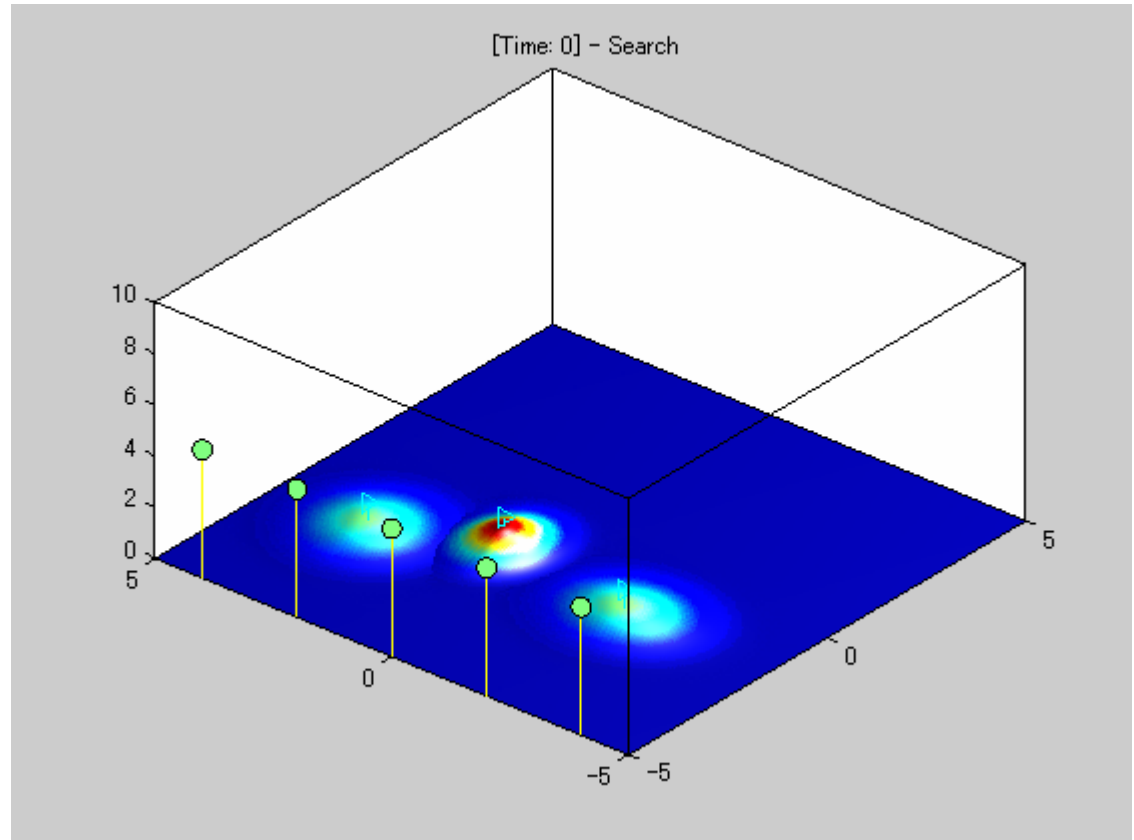
Multi-Objective  
Heterogeneous Platforms



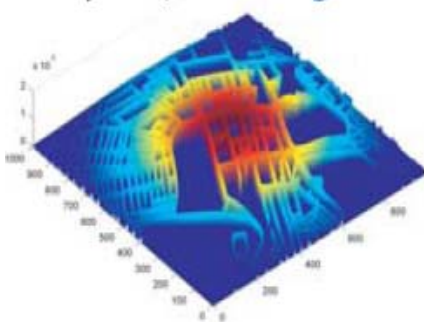
# Cooperative plume-source localisation



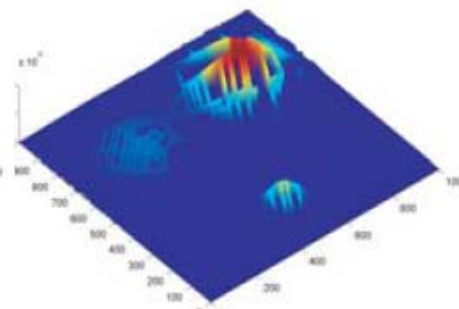
Putting the “physics”  
in the network



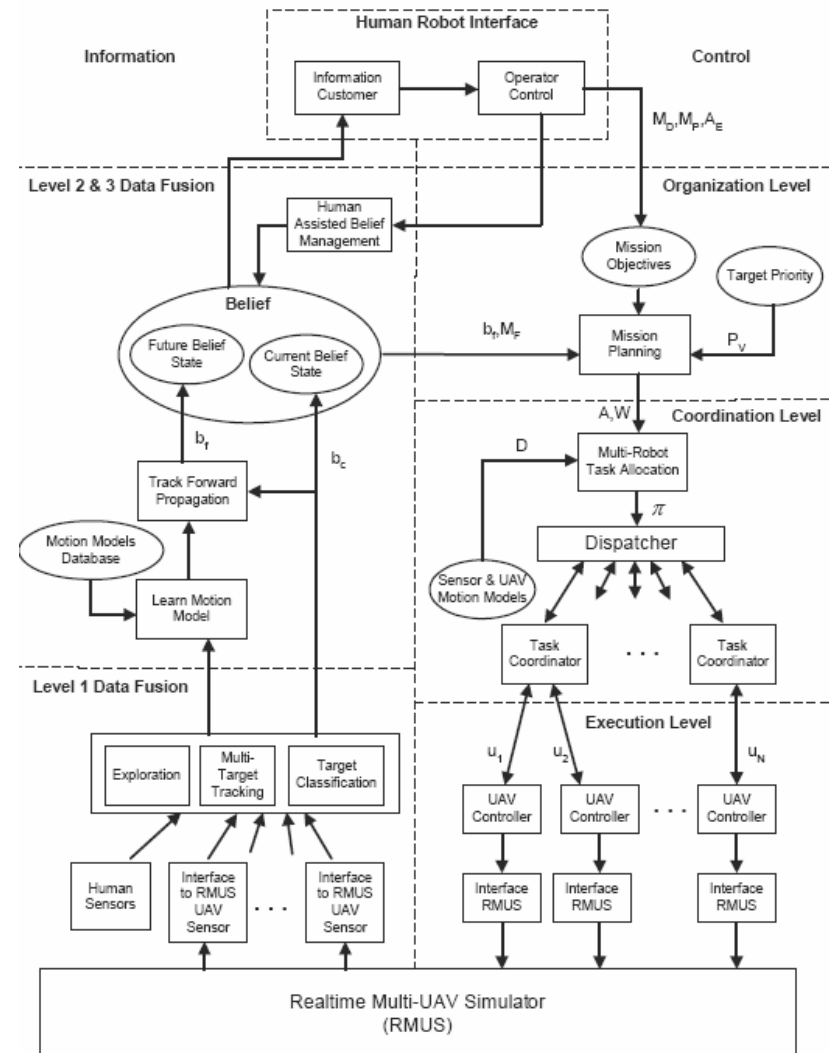
# Human UAV Cooperation



Probable locations of an object



Utility Map





Find

---

X 1988

Y 124

Reset

+

-



Mission

&gt;|

|

||

End

UAV1

UAV

UAV 1



Current

X: 227

Y: 212

Height: 250

Airspeed: 30.00

Waypoint

X: 0

Y: 0

Height: 0

Current Task: Observing Area 4

Height

Height

Airspeed

Airspeed

Targets

Target

ID

Class Group: ----

Target Type: ----

Probability: ----

----

## Display Options

☒ Show All UAVs☒ Show Path☒ Show Waypoints☒ Show Labels☐ Show Search State☒ UAV1☒ UAV2☒ Show All Targets☒ Show Vehicles☒ Show Labels☒ Show Areas

Memo1

Mission Time 0.5

☐ Log Data

Save Targets

# Conclusions

- Information
  - Mathematical basis for network fusion
  - An a priori measure of performance
  - An integrated idea of context
  - A system design measure
- Future directions
  - Automate system design process
  - Extend complexity of information-gathering
  - Non-information problems and pay-off seperability



# Questions ?

