### 4.6 SURVEY, ALIGNMENT, AND GEODESY (WBS 1.1.6)

### 4.6.1 Introduction

For a long baseline neutrino experiment, properly aligning the neutrino beam to hit the far detector 735 km away is clearly important. Actually, as shown in Figure 4.6-1, the NuMI beam, for low neutrino energies, is several kilometers wide and modern geodetic survey techniques, especially the Global Positioning System (GPS) satellites, make hitting the far detector relatively straightforward. For the NuMI beamline, the physics-driven alignment goals from the MINOS experiment require that the neutrino beam center must be within 100 meters of the far detector.


Figure 4.6-1 Transverse distribution of the NuMI low energy tune neutrino beam at the far detector as a function of energy. Note that at low neutrino energy the beam is several kilometers wide

### 4.6.2 System Description: Determining the Line from Fermilab to Soudan

The relative positions of Fermilab and Soudan on the surface are determined by making simultaneous measurements using the Global Positioning System (GPS) satellites. Simultaneous GPS data at both Fermilab and Soudan were recorded in April 1999 as shown in Table 4.6-1. The data was analyzed at Fermilab and, independently, by the National Geodetic Survey (NGS). The agreement between the NGS result and two methods of analysis at Fermilab was excellent. The Fermilab to Soudan vector, averaged over the period of the observations used, is known to better than 1 cm horizontally and 6 cm vertically, well within requirements. The differential earth tide effect between Fermilab and Soudan is approximately the same as this uncertainty.

Included in Table 4.6-1 are the results from two less precise measurements also using professional GPS receivers, which agree to better than 1 meter, and a later result using an amateur hand held receiver. All four results are within the 12-meter tolerance goal for this measurement. Accuracy of a differential GPS measurement is increased by including CORS (Continuously Observed Reference Station) data in the analysis (Figure 4.6-2), simultaneous observations from both positions, and using the precise satellite positions calculated by NGS from the CORS data.

| Year | Receiver | Measure | Include | Simulta- | Precision | Deviation |
| :--- | :--- | :---: | :---: | :---: | :---: | ---: |
|  |  | time | CORS | neous | Satellite | from 1999 |
|  |  | (hour) |  |  | Positions | (meter) |
| 1999 | Professional | 26 | Yes | Yes | Yes |  |
| 1998 | Professional | 6 | No | Yes | No | 0.231 |
| 1994 | Professional | 1 | No | No | No | 0.785 |
| 2000 | Hand held | $<1$ | No | No | No | 10.140 |


| Year |  |  | Azimuth |  | Vertical | Distance | north | east | up | $\\|(\delta \mathrm{n}, \delta \mathrm{de}, \delta \mathrm{u})$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |$|$

Table 4.6-1. Relative position of the SHAFT monument on the surface at Soudan as measured from Fermilab surface monument 66589 by GPS. Results are given in the Local Geodetic Coordinate System (reference SHAFT). The values for the most accurate measurement are given on the first line, followed by the differences (other - best) of the three additional measurements relative to the best one. The professional receivers used were Trimble 4000 SSi's; the hand held receiver was a Garmin GPS III+ (Best Buy ~\$350).

CORS COVERAGE ( $100,200,300$, and 400 km ranges) MAY, 1998


Figure 4.6-2 CORS (Continuously Observed Reference Station) network. GPS data are recorded for over 100 accurately known locations in the United States, including 4 in Wisconsin. (Source: National Geodetic Survey www page: http://www.ngs.noaa.gov/CORS/Maps.html

The position of the $27^{\text {th }}$ level at the bottom of the Soudan Mine, relative to the surface, is determined using inertial survey. An inertial survey unit and operator were rented from the University of Calgary during the April 1999 GPS trip to Soudan. The inertial survey unit used (Honeywell Laseref III IMU) contains a triad of accelerometers and optical gyroscopes to measure force and angular velocity. The accelerometers are double integrated to yield position change along each of the 3 axes. Internal consistency of the several inertial survey runs indicated a 0.7 m per coordinate precision for the surface to bottom of the mine measurement, many times better than the 12 m goal. As shown in Table 4.6-2, these measurements agreed to better than 4 m per coordinate with the old mine values for the $27^{\text {th }}$ level relative to the surface.

|  | east | north | up |
| :--- | ---: | ---: | ---: |
|  | meter | meter | meter |
|  |  |  |  |
| 1999 INS values | -15.2 | 148.2 | -710.1 |
| INS-old mine \#'s | -0.2 | 3.7 | -3.4 |

Table 4.6-2. Inertial Survey (INS) measurement from the surface to level 27 at Soudan. The average of the 4 INS runs made on April 20, 1999 is given, together with the change of these measurements from the old mine values.

Conventional survey techniques are used to determine the position of the MINOS far detector relative to the bottom of the shaft at Soudan. Table 4.6-3 gives the position of monuments in the MINOS cavern and the nominal detector axis and edges in the Cartesian Local Geodetic Coordinate System (LGCS) relative to the surface monument called "SHAFT" (which was used in the surface GPS measurement above). Table 4.6-4 gives the same points in the Cartesian beam coordinate system, with origin at the nominal detector center, Y axis along the neutrino beam direction, and X axis horizontal.

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| POINT | X (+EAST) | Y (+NORTH) | Z (+UP) |
| :---: | :---: | :---: | :---: |
| NAME | (Meter) | (Meter) | (Meter) |
| BRASS 1 | 37.3668 | 10.8767 | -709.1782 |
| BRASS ${ }^{-} 2$ | 32.5269 | 20.5614 | -709.1638 |
| BRASS_3 | 24.9370 | 35.7484 | -709.1476 |
| BRASS ${ }^{-1} 4$ | 17.9893 | 49.6496 | -709.1606 |
| BRASS_5 | 3.3012 | 79.0429 | -709.1639 |
| CP_E11 | 27.1329 | 39.8453 | -705.0098 |
| CP_E14 | 24.6850 | 44.7639 | -705.0327 |
| CP E17 | 22.2376 | 49.6672 | -705.0330 |
| CP_E2 | 34.2510 | 25.6183 | -705.0434 |
| CP_E5 | 31.7950 | 30.5282 | -705.0347 |
| CP_E8 | 29.3449 | 35.4377 | -705.0233 |
| CP-W11 | 19.5038 | 36.0554 | -705.0210 |
| CP - W14 | 17.0549 | 40.9669 | -705.0257 |
| CP-W17 | 14.6069 | 45.8628 | -705.0210 |
| CP_W2 | 26.6014 | 21.8538 | -705.0311 |
| CP_W5 | 24.1563 | 26.7486 | -705.0431 |
| CP_W8 | 21.7098 | 31.6510 | -705.0386 |
| EI-01 | 34.1657 | 23.6082 | -709.2540 |
| EI_035 | 31.8929 | 28.1608 | -709.2580 |
| EI_065 | 29.5962 | 32.7045 | -709.2534 |
| EI_10 | 27.2189 | 37.4801 | -709.2451 |
| EI_125 | 24.9455 | 42.0243 | -709.2487 |
| EI_155 | 22.6748 | 46.5704 | -709.2416 |
| EI-18 | 20.5332 | 50.8897 | -709.2587 |
| EO_01 | 37.0840 | 23.7565 | -709.2491 |
| EO-09 | 29.9725 | 38.0342 | -709.2452 |
| EO_19 | 21.3997 | 54.7230 | -709.2630 |
| PP' $\overline{1}$ | 8.2536 | 51.7757 | -707.5768 |
| PP2 | 4.2885 | 59.6857 | -707.5483 |
| PP3 | 1.1212 | 66.0377 | -707.5610 |
| VULCAN_E | 31.7687 | 30.2899 | -707.0321 |
| VULCAN_W | 24.2997 | 26.7597 | -706.8035 |
| WBE_1 | 17.6527 | 55.4088 | -709.2568 |
| WBE_1_5 | 16.7981 | 60.6413 | -709.2508 |
| WBE-2 | 13.3126 | 64.1350 | -709.2516 |
| WBE_2_5 | 11.7837 | 70.7375 | -709.2529 |
| WBE ${ }^{-} 3$ | 8.2340 | 74.4346 | -709.2519 |
| WBW_1 | 10.6467 | 51.9149 | -709.2533 |
| WBW-1_5 | 7.8540 | 55.7006 | -709.2597 |
| WBW ${ }^{-1}{ }^{-} 7$ | 7.2439 | 59.4027 | -709.2612 |
| WBW ${ }^{-2}$ | 6.2549 | 60.6034 | -709.2562 |
| WBW_2_2 | 5.2874 | 63.5825 | -709.2643 |
| WBW-2_5 | 2.4974 | 66.3988 | -709.2517 |
| WBW-3 | 1.1941 | 70.8040 | -709.2534 |
| WI_01 | 28.3010 | 20.6410 | -709.2532 |
| WI-035 | 26.0234 | 25.2087 | -709.2504 |
| WI_065 | 23.7625 | 29.7489 | -709.2521 |
| WI-10 | 21.3667 | 34.5228 | -709.2503 |
| WI_125 | 19.1039 | 39.0775 | -709.2530 |
| WI-155 | 16.8175 | 43.6237 | -709.2527 |
| WI_18 | 14.6497 | 47.9674 | -709.2615 |
| WO-01 | 26.9941 | 18.7946 | -709.2483 |
| WO_09 | 19.8536 | 32.9234 | -709.2434 |
| WO_185 | 12.3356 | 47.9075 | -709.2598 |
| Dētctr_dsgn | 24.4433 | 35.7132 | -704.5203 |
| DetCtr_meas | 24.3847 | 35.8303 | -704.5203 |
| dcs_orígin | 31.3726 | 21.8483 | -704.5203 |
| FD_ds_axis | 17.3968 | 49.8124 | -704.5203 |
| FD_us_right | 34.9506 | 23.6365 | -704.5203 |
| FD_us_left | 27.7946 | 20.0601 | -704.5203 |
| FD_us_top | 31.3726 | 21.8483 | -700.5203 |
| FD_us_bot | 31.3726 | 21.8483 | -708.5203 |
| FD us t, r | 34.9506 | 23.6365 | -700.5203 |

Table 4.6-3. Far Cavern Monuments and Detector Points in the Local Geodetic coordinate system, reference point Shaft Monument, with the X axis East, Y axis North, Z axis up, to make a right handed orthogonal system.

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| POINT NAME | $\begin{aligned} & \mathrm{X}(+ \text { "West") } \\ & \text { (Meter) } \end{aligned}$ | $\begin{gathered} Y(+ \text { UP" }) \\ \text { (Meter) } \end{gathered}$ | $\begin{aligned} & \mathrm{Z}(+ \text { "North") } \\ & \text { (Meter) } \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| BRASS_1 | -0.3794 | -3.0428 | -28.3462 |
| BRASS_2 | -0.4095 | -3.6472 | -17.5364 |
| BRASS_3 | -0.4565 | -4.6014 | -0.5853 |
| BRASS_4 | -0.4992 | -5.5025 | 14.9291 |
| BRASS_5 | -0.5917 | -7.3838 | 47.7340 |
| CP_E11 | -4.2597 | -0.6231 | 2.3193 |
| CP_E14 | -4.2841 | -0.9599 | 7.8030 |
| CP_E17 | -4.3020 | -1.2735 | 13.2742 |
| CP_E2 | -4.2228 | 0.2526 | -13.5649 |
| CP_E5 | -4.2360 | -0.0525 | -8.0835 |
| CP_E8 | -4.2543 | -0.3547 | -2.6049 |
| CP_W11 | 4.2588 | -0.6368 | 2.3626 |
| CP_W14 | 4.2385 | -0.9551 | 7.8415 |
| CP_W17 | 4.2244 | -1.2633 | 13.3066 |
| CP_W2 | 4.3026 | 0.2605 | -13.4884 |
| CP_W5 | 4.2864 | -0.0642 | -8.0265 |
| CP_W8 | 4.2681 | -0.3728 | -2.5563 |
| EI_01 | -3.2430 | -3.8507 | -15.5599 |
| EI_035 | -3.2593 | -4.1455 | -10.4801 |
| EI_065 | -3.2502 | -4.4319 | -5.3970 |
| EI_10 | -3.2733 | -4.7285 | -0.0707 |
| EI_125 | -3.2853 | -5.0225 | 5.0019 |
| EI_155 | -3.3005 | -5.3058 | 10.0756 |
| EI_18 | -3.3291 | -5.5984 | 14.8878 |
| EO_01 | -5.9165 | -3.7784 | -16.7371 |
| EO_09 | -5.9821 | -4.6861 | -0.8124 |
| EO_19 | -5.8262 | -5.7762 | 17.9173 |
| PP1 | 7.2417 | -4.2800 | 21.2850 |
| PP2 | 7.2279 | -4.7573 | 30.1203 |
| PP3 | 7.2018 | -5.1756 | 37.2058 |
| VULCAN_E | -4.1054 | -2.0351 | -8.3983 |
| VULCAN_W | 4.1533 | -1.8186 | -8.1816 |
| WBE_1 | -2.7874 | -5.9013 | 20.2109 |
| WBE_1_5 | -4.3762 | -6.1844 | 25.2611 |
| WBE_2 | -2.8332 | -6.4531 | 29.9410 |
| WBE_2_5 | -4.4354 | -6.8308 | 36.5153 |
| WBE_3 | -2.9265 | -7.1097 | 41.4054 |
| WBW_1 | 5.0414 | -5.8994 | 20.2393 |
| WBW_1_5 | 5.8343 | -6.1708 | 24.8684 |
| WBW_1_7 | 4.7151 | -6.3770 | 28.4437 |
| WBW_2 | 5.0588 | -6.4587 | 29.9586 |
| WBW_2_2 | 4.5839 | -6.6437 | 33.0491 |
| WBW_2_5 | 5.8101 | -6.8466 | 36.8136 |
| WBW_3 | 4.9941 | -7.1067 | 41.3270 |
| WI_01 | 3.3296 | -3.8491 | -15.5740 |
| WI_035 | 3.3108 | -4.1380 | -10.4782 |
| WI_065 | 3.2895 | -4.4296 | -5.4146 |
| WI_10 | 3.2836 | -4.7331 | -0.0819 |
| WI_125 | 3.2575 | -5.0264 | 4.9954 |
| WI_155 | 3.2563 | -5.3170 | 10.0758 |
| WI_18 | 3.2401 | -5.6032 | 14.9219 |
| WO_01 | 5.3270 | -3.7835 | -16.6339 |
| WO_09 | 5.3542 | -4.6834 | -0.8288 |
| WO_185 | 5.3342 | -5.6579 | 15.9071 |
| DetCtr_dsgn | 0.0003 | 0.0075 | -0.1307 |
| DetCtr_meas | 0.0000 | 0.0000 | 0.0000 |
| dcs_origin | 0.0431 | 0.8934 | -15.6053 |
| FD_ds_axis | -0.0432 | -0.8934 | 15.6054 |
| FD_us_right | -3.9568 | 0.8940 | -15.6163 |
| FD_us_left | 4.0431 | 0.8927 | -15.5944 |
| FD_us_top | 0.0431 | 4.8868 | -15.3767 |
| FD_us_bot | 0.0431 | -3.1001 | -15.8340 |
| FD_us_t,r | -3.9568 | 4.8875 | -15.3877 |

Table 4.6-4. Far Cavern Monuments and Detector Points. In the "Beam" coordinate system with the Z -axis along the beam direction, X -axis horizontal, beam left, and Y -axis to make a right handed orthogonal system.

The line from Fermilab to Soudan is transferred from the surface at Fermilab to underground using conventional survey techniques. The most difficult parameter is the azimuth (horizontal angle). Table $4.6-5$ shows the two methods we are using to determine underground azimuth and the offset (horizontal deviation from the ideal beam line) resulting from the expected angular error at several distances. A gyro-theodolite is a precision theodolite combined with an accurate gyrocompass. One accurate to 15 microradians has been loaned to Fermilab by SLAC and has been in use on NuMI since mid 2001. Both mechanical and optical plumbing is being used down the sight risers and shafts constructed at Fermilab.

| Transferring Azimuth | Fermilab Surface to Tunnels |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Method: | Accuracy at: |  |  |  |  |
|  | distance > | 84 m | 460 m | 1040 m | 735 km |
|  | Accuracy | Downstream | Mid Decay | MINOS | Soudan |
|  | (milliradian) | Target Hall | Tunnel Vent | near det | far det |
| Best Gyro | 0.015 | 1.3 mm | 7 mm | 16 mm | 11 m |
| Widely Separated Plumb Bobs | 0.012 | 1.0 mm | 6 mm | 12 mm | 9 m |

Table 4.6-5 The two methods being used to determine underground azimuth and the offset (horizontal deviation from the ideal beam line) resulting from the expected angular error at several distances

### 4.6.3 System Description: Beamline Element Accuracy Requirements

The PBEAM_WMC Monte Carlo was used to calculate the effect of misalignments of each beamline element on the determination of the far detector spectrum (without oscillations) from the measured near detector spectrum. PBEAM is first run with all beam elements at their nominal values and positions ("on axis"). A parameter is selected to investigate and its position is varied from its nominal value. For example, in the Monte Carlo the first focussing horn is moved 4 mm transverse to the beam axis ("Horn 1 X shift of 4 mm "), and the resulting spectra at both near and far detectors are calculated.

The ratio $\mathrm{R}_{\text {far }}$, obtained by dividing the far detector flux with the beamline element displaced by the far detector flux with the beamline element on axis, is shown in Figure 4.6-3a. A dashed
line has been drawn for a flux ratio of 1.0 , which would be the result if there were no change in the flux. Figure 4.6-3b is a similar graph for the near detector. The ratio of these ratios (far ratio to near ratio, RR) is shown in Figure 4.6-3c. It is easy to pick out the largest fractional difference (in the interval 1 to 10 GeV ), which occurs near 5 GeV . Beam element misalignments breaking the azimuthal symmetry of the neutrino beam, such as this horn 1 X shift, are measurable in the near detector.


Fig 4.6-3 Effect of a 4 mm offset of horn 1 on (top) the far detector flux, (middle) near detector at 316.6 m beyond the end of the decay pipe, (bottom) far over near ratio(RR). These results are for the low energy beam configuration.

Figure 4.6-4 displays RR-1 for several horn 1 X shifts. These all start at RR-1=0 at low energy, but have been offset by multiples of $10 \%$ to clearly display the several curves on a single graph. To obtain sufficient statistical precision from the Monte Carlo in a reasonable time, X shifts much larger than the expected alignment tolerance of 0.35 mm have been calculated. At each peak and valley shown in Figure 4.6-4, the data are fit to the formula $R R-1=A x^{p}$. This formula forces the required result of $R R=1$ at $x=0$, i.e. no effect on the spectrum if there is no misalignment. The value of RR at the expected alignment tolerance is calculated using the parameters A and p determined by the fit.

## Low Energy Beam, Horn 1 X, Rdet=1.0 (1 Gev avg)



Fig 4.6-4 Curves of RR-1 for several horn 1 X shifts. These all start at RR-1=0 at low energy, but have been offset by multiples of $10 \%$ to clearly display the several curves on a single graph. These results are for the low energy beam configuration.

This analysis is repeated for all beam element misalignments shown in Table 4.6-6. A similar table is prepared for each 1 GeV neutrino energy interval and, to be conservative, lists the largest deviation of RR found for any neutrino energy up to the table value. The overall effect on RR is found by adding the individual element terms in quadrature. The table takes into account that most misalignments can occur in two transverse planes.

In the table, angle parameters are expressed by a single linear distance; the downstream end of the device is displaced by this amount and the upstream end is displaced by an equal amount in the opposite direction. These two displacements are what are actually measured by the surveyors. The length of the device, in meters, is given in square brackets after the description.


Table 4.6-6 The expected percentage error in $R R$ from each misalignment at 8 GeV neutrino energy. These results are for the low energy beam configuration

This result is plotted in Figure 4.6-5 as a function of neutrino energy. Also shown is the statistical error from a two-year run. The MINOS physics requirement is that the error due to neutrino beam misalignments be comfortably below the 2 year run statistical error, and Figure 4.6-5 shows this to be the case for the low energy beam.


Figure 4.6-5 The expected percentage error in RR from all misalignments listed in Table 4.6-6. Also shown is the statistical error for a two-year run. These results are for the low energy beam configuration

### 4.6.4 System Description: Construction QA

Fermilab surveyors are providing NuMI tunnels and halls quality assurance. Most of the decay tunnel was excavated using a 21.5 -foot diameter Tunnel Boring Machine (TBM). Figure 4.6-6 shows the vertical and horizontal deviations of the center of the TBM decay tunnel from the specified line from Fermilab to Soudan. Measurement of the completed tunnel by both the SA Healy (civil subcontractor) and Fermilab surveyors are shown. Agreement with the design is excellent; most vertical and horizontal centers are within 2 inches. No attempt was made by the two groups of surveyors to measure at the same station (horizontal distance along the tunnel), so
local tunnel variations could explain part of the differences between the measurements. The agreement for horizontal is worse than vertical; this is likely conformation that azimuth is the most difficult parameter to transfer underground. The Fermilab surveyors used the 15 microradian gyro-theodolite ( 0.36 inch in 2000 feet), while the SA Healy surveyors used a less precise 100 microradian instrument ( 2.4 inch in 2000 feet).


FIgure 4.6-6 The vertical and horizontal deviations of the "as built" center of the TBM decay tunnel from the specification. Measurements of the completed tunnel by both the SA Healy (civil subcontractor) and Fermilab surveyors are shown.

