

NS 102 Lecture 9 April 27, 2005

Open: For me this is heaven- Jimmy Eat World



Close: Cold in the Sun-Red Eyed Legends

Pieter Bruegel the Elder, ca. 1563

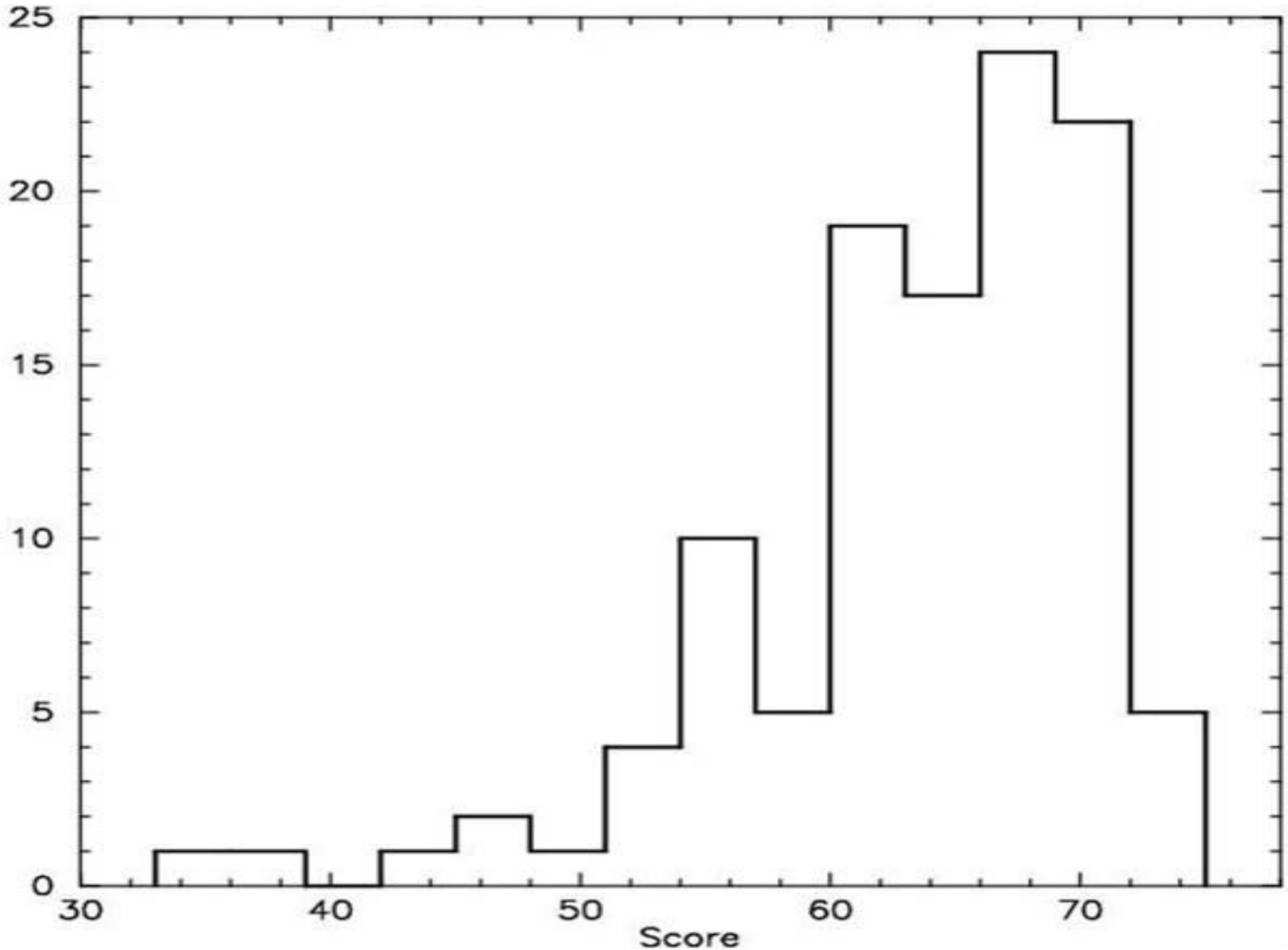
GnatSigh News

(all the news that fits)

- Website <http://home.fnal.gov/~rocky/NS102/>
- Need violinist volunteer
- Review logarithms
- Review basic trigonometry (definition of sine, tangent, etc.)
- Exam #1 returned today
- Galileo's Depositions, Defense, and Papal Condemnation on the website

Lab this week: Temperature of the Universe

Lab next week: Geometry of the Universe



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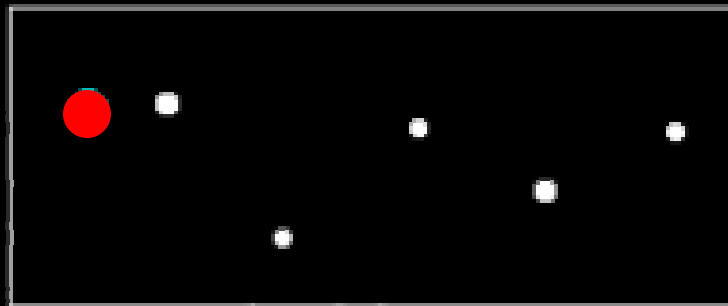
Pieter Bruegel the Elder, ca. 1563

The Cosmological Distance Scale

Gustav Doré, ca. 1866



DISTANT



VIEW FROM A

A



NEARBY



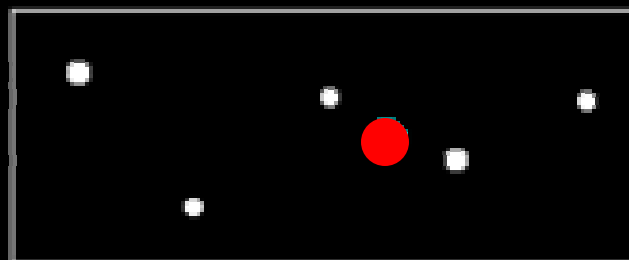
STAR

SUN

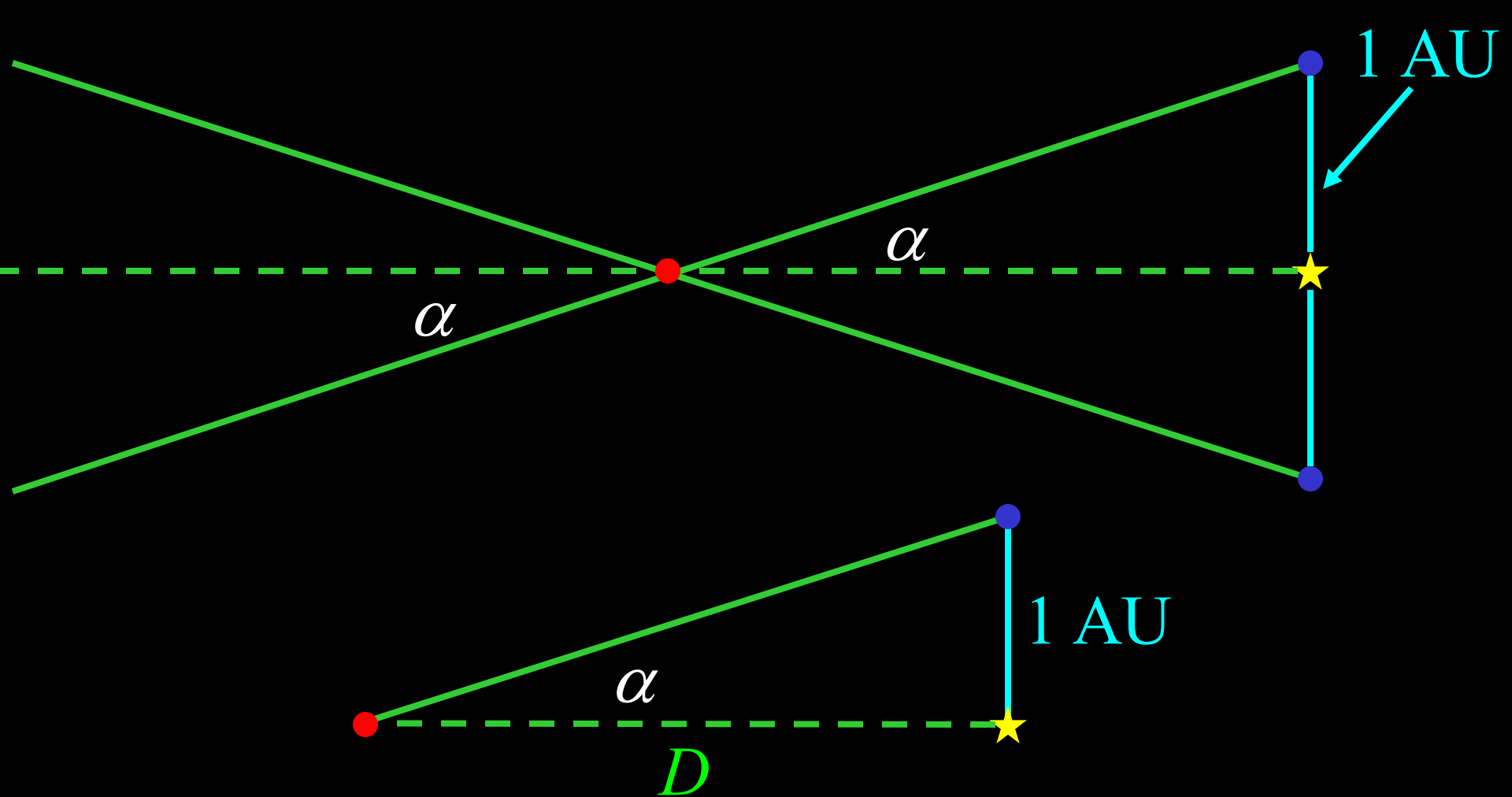


B

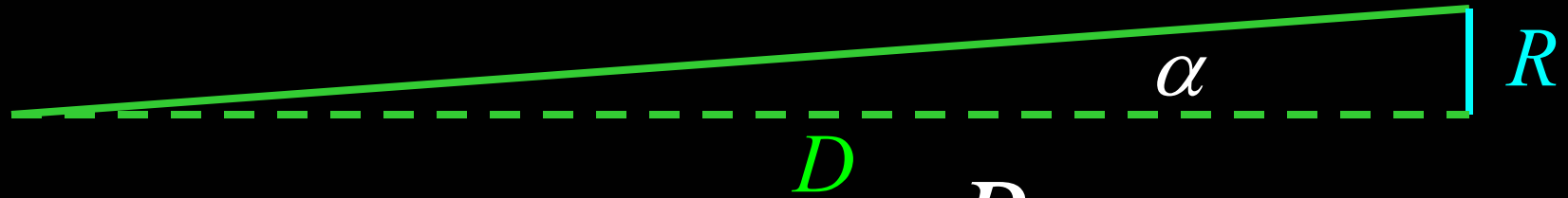
VIEW FROM B



STARS



$$\tan \alpha = \frac{1 \text{ AU}}{D}$$



$$\tan \alpha = \frac{R}{D}$$

law of skinny triangles:

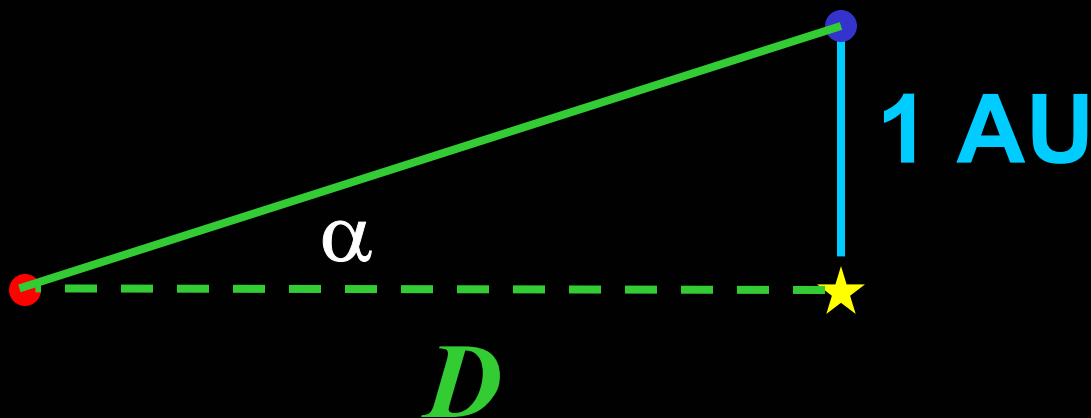
$$\tan \alpha = \sin \alpha = \alpha \quad (\text{in radians})$$

$$\alpha \text{ (in radians)} = \frac{R}{D}$$

$$\alpha \text{ (in seconds of arc)} = \frac{R}{D} \times 206,264.8$$

$$\frac{D}{200,000 \text{ AU}} = \frac{\text{seconds}}{\alpha}$$

$$\frac{D}{\text{pc}} = \frac{\text{seconds}}{\alpha}$$



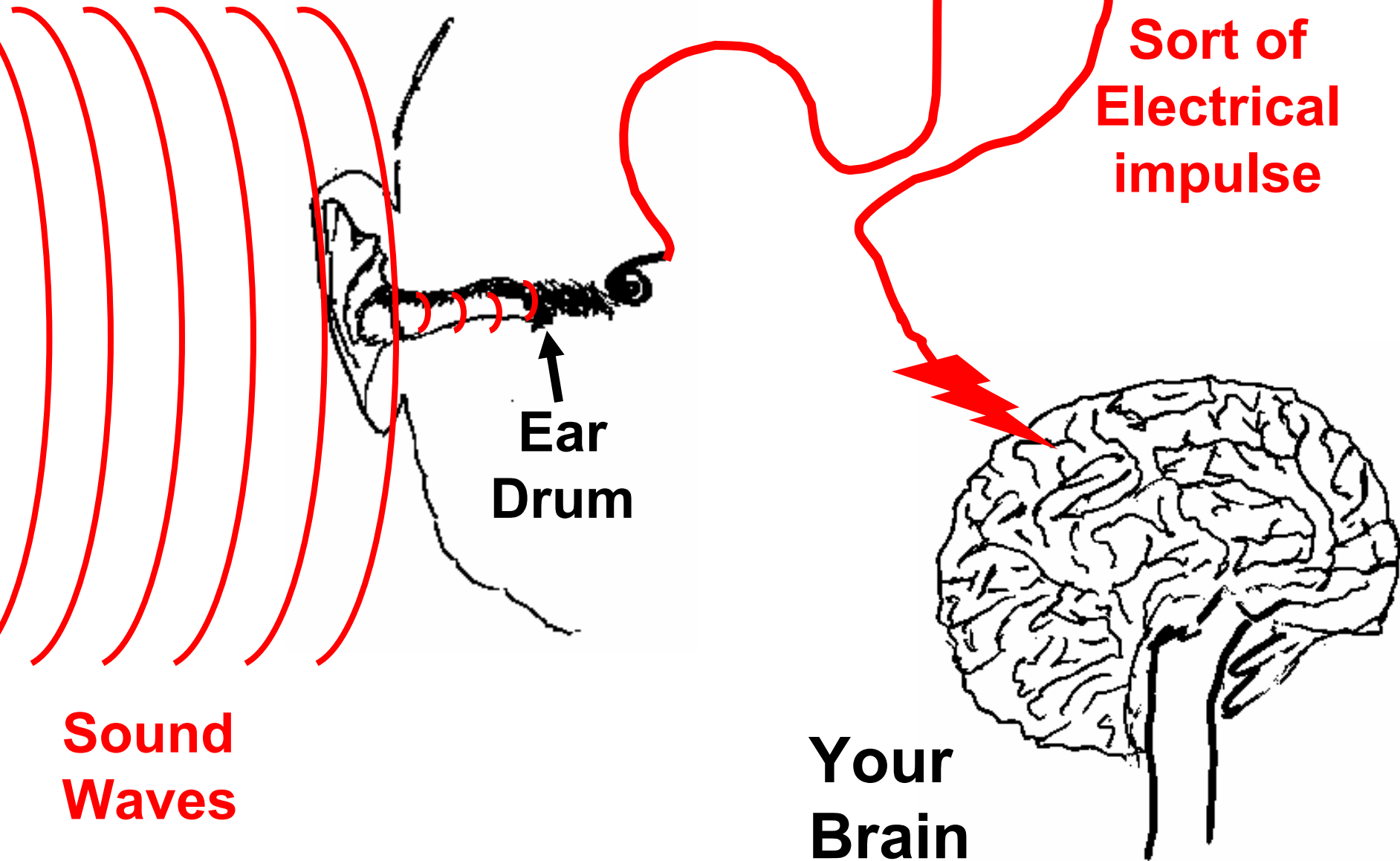
They have different apparent brightness

They have different colors

They move

They change in brightness

Logarithmic Ear



Intensity: energy per time per area

$$I = \frac{\text{Energy}}{\text{Time Area}} = \frac{\text{Power}}{\text{Area}}$$

$\frac{\text{Energy}}{\text{Time}}$ (Power)

measured in
watts

Area

measured in
 cm^2

Intensity in watts per cm^2

Intensity: energy per time per area

$$I = \frac{\text{Energy}}{\text{Time Area}}$$

$$\text{dB} = 10 \log (I / I_0)$$

I_0 = threshold of hearing

Hearing threshold

$$\text{dB} = 10 \log (I / I_0)$$

$$\text{dB} = 0$$

$$I_0 = 10^{-16} \text{ watts per cm}^2$$



Pain threshold



$$\begin{aligned} \text{dB} &= 10 \log (I / I_0) \\ &= 10 \log(10^{12}) \end{aligned}$$

$$\text{dB} = 120$$

$$I = 10^{12} I_0 = 10^{-4} \text{ watts per cm}^2$$

I_0 is intensity at threshold of hearing

| I/I_0 | $\log (I/ I_0)$ | $\text{dB} = 10 \log (I/ I_0)$ |
|-----------|-----------------|--------------------------------|
| 10^{-2} | -2 | -20 |
| 1 | 0 | 0 |
| 10^2 | 2 | 20 |
| 10^6 | 6 | 60 |
| 10^{12} | 12 | 120 |
| 10^{20} | 20 | 200 |

Difference of about 1 dB is about the smallest change that can be noticed by the human ear

$$\text{dB}_1 = 10 \log(I_1/I_0) \qquad \text{dB}_2 = 10 \log(I_2/I_0)$$

$$\text{dB}_1 - \text{dB}_2 = 10 \log(I_1/I_0) - 10 \log(I_2/I_0)$$

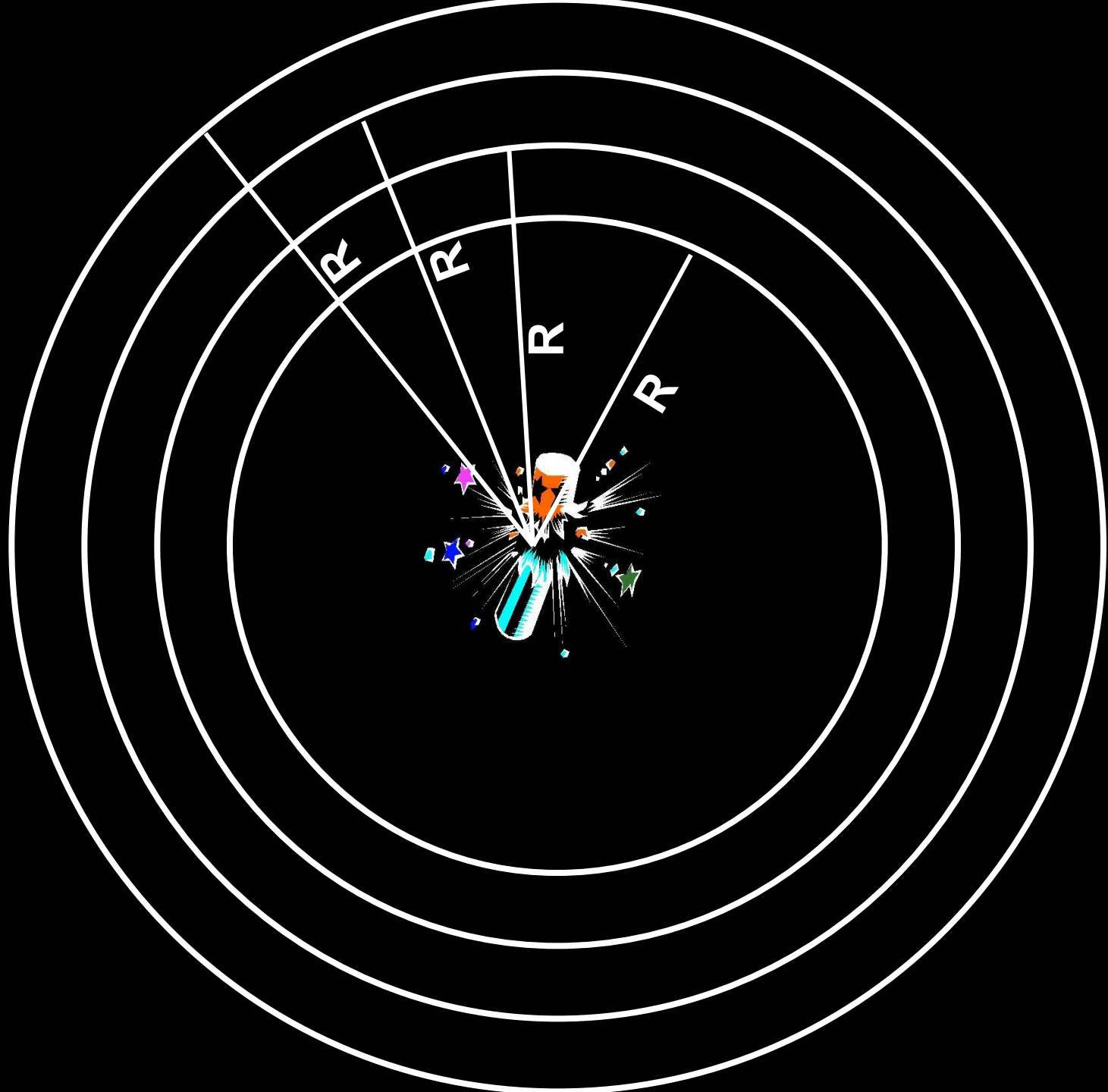
$$= 10 \left[\log(I_1/I_0) - \log(I_2/I_0) \right]$$

$$= 10 \left[\log(I_1) - \cancel{\log(I_0)} - \log(I_2) + \cancel{\log(I_0)} \right]$$

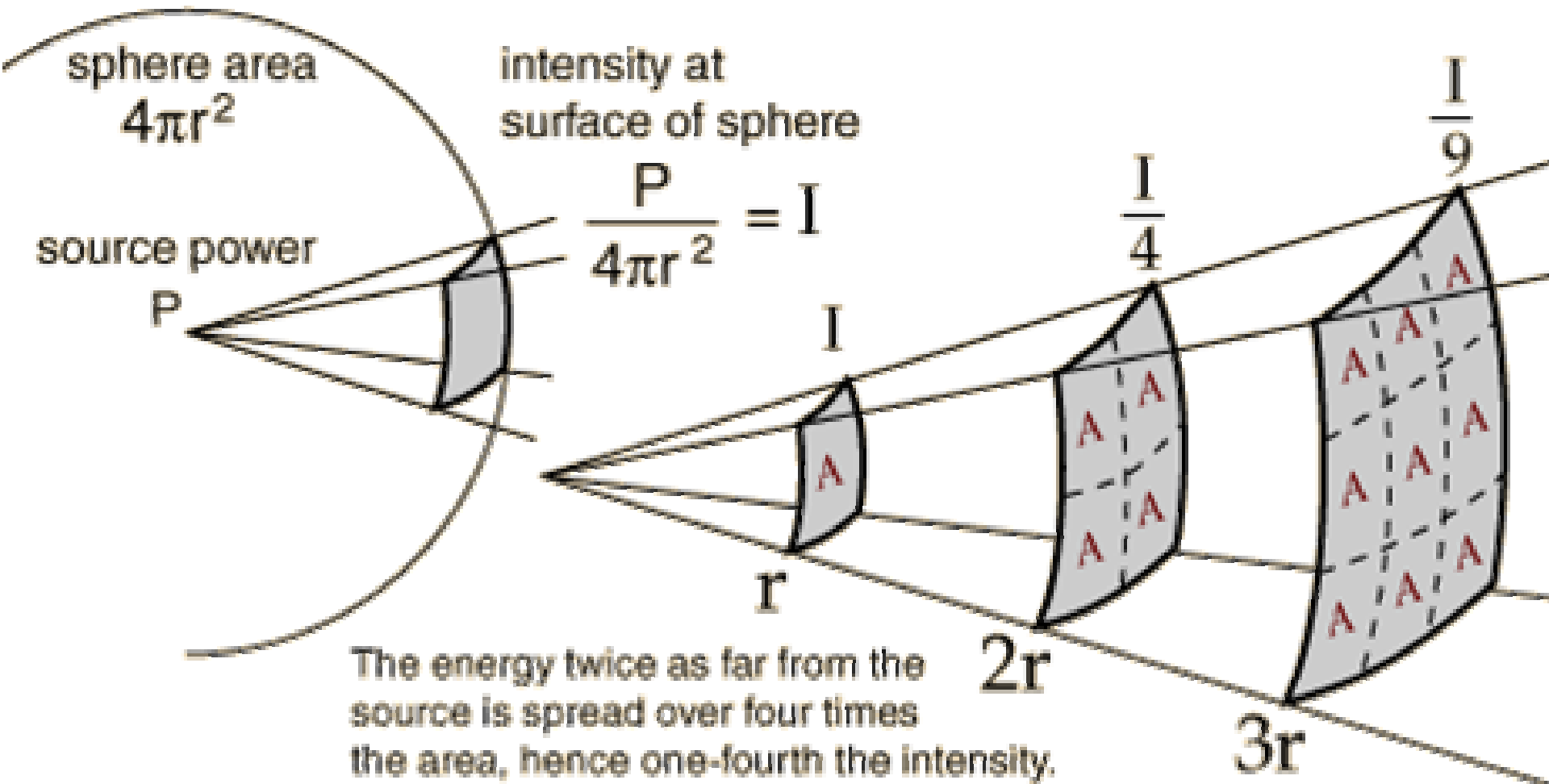
$$= 10 \left[\log(I_1) - \log(I_2) \right] = 10 \log(I_1/I_2)$$

$$1 = 10 \log(I_1/I_2)$$

$$0.1 = \log(I_1/I_2) \rightarrow 10^{0.1} = I_1/I_2 \rightarrow 1.25 = I_1/I_2$$



Inverse-square law



Intensity: energy per time per area

$$I = \frac{\text{Energy}}{\text{Time Area}} = \frac{\text{Power}}{\text{Area}}$$

Power **property of source**

Intensity **depends on power
and distance between
source and detector**

$$\text{Intensity} = \frac{\text{power}}{4\pi R^2}$$

Let there be light



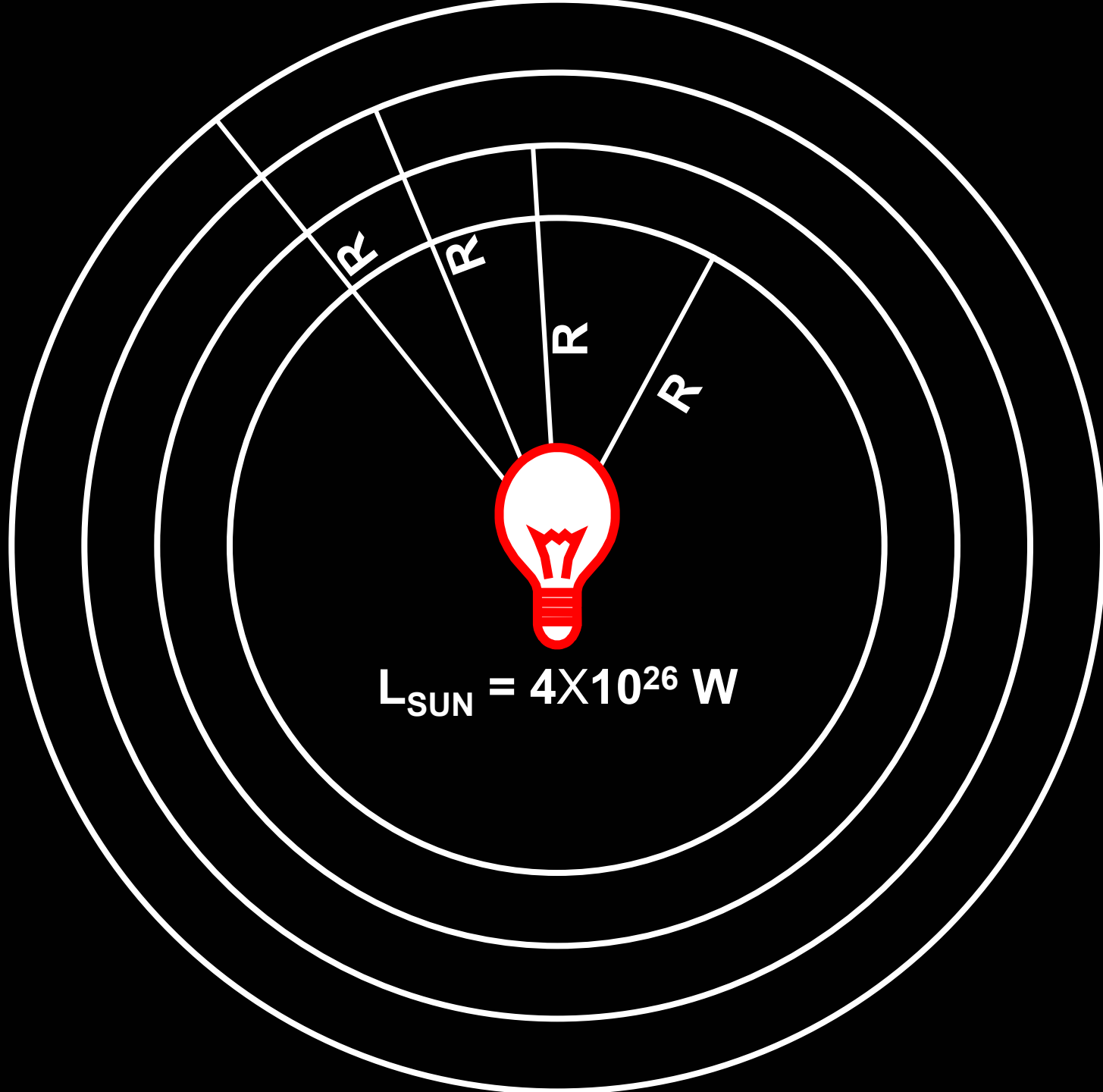
For light!!!

$$I = \frac{\text{Energy}}{\text{Time Area}}$$

$\frac{\text{Energy}}{\text{Time}}$ (Luminosity) measured in watts

Area measured in cm^2

Intensity in watts per cm^2



$$L_{\text{SUN}} = 4 \times 10^{26} \text{ W}$$

For light!!!

$$I = \frac{\text{luminosity}}{\text{cm}^2}$$

Luminosity property of source

Intensity depends on power
and distance between
source and detector

$$\text{Intensity} = \frac{\text{luminosity}}{4\pi R^2}$$

Logarithmic Eye



**Eyes, like ears, are
logarithmic detectors.**

LET THERE BE LIGHT!

**Greeks classified stars into 6 classes,
or magnitudes**

Brightest stars were 1st magnitude

Dimmest stars were 6th magnitude

Intensity of brightest stars = 100 X dimmest.

For sound: $\text{dB}_1 - \text{dB}_2 = \alpha \log(I_1/I_2)$

To define scale:

1. Define α for convenience,

- $\Delta\text{dB} \equiv 120$ between threshold and pain
- Measure ratio of intensities

$$120 = \alpha \log(I_{\text{pain}}/I_0)$$

$$= \alpha \log(10^{12}) = \alpha \times 12 \rightarrow \alpha = 10$$

$$\text{dB}_1 - \text{dB}_2 = 10 \log(I_1/I_2)$$

2. One measurement & one definition

$$I_0 = 10^{-16} \text{ watts cm}^{-2} \quad \text{dB}_0 \equiv 0$$

$$\text{dB} = 10 \log\left(I/10^{-16} \text{ watts cm}^{-2}\right)$$

For light: $m_1 - m_2 = \alpha \log(I_1/I_2)$

To define scale:

1. Define α for convenience,

- $\Delta m \equiv 1-6 = -5$ between brightest & dimmest
- Measure ratio of intensities

$$-5 = \alpha \log(I_{\text{brightest}} / I_{\text{dimmest}})$$

$$= \alpha \log(10^2) = \alpha \times 2 \rightarrow \alpha = -5/2 = -2.5$$

$$m_1 - m_2 = -2.5 \log(I_1/I_2)$$

2. One measurement & one definition

$$I_{\odot} = 0.137 \text{ watts cm}^{-2} \quad m_{\odot} = -26.8$$

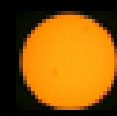
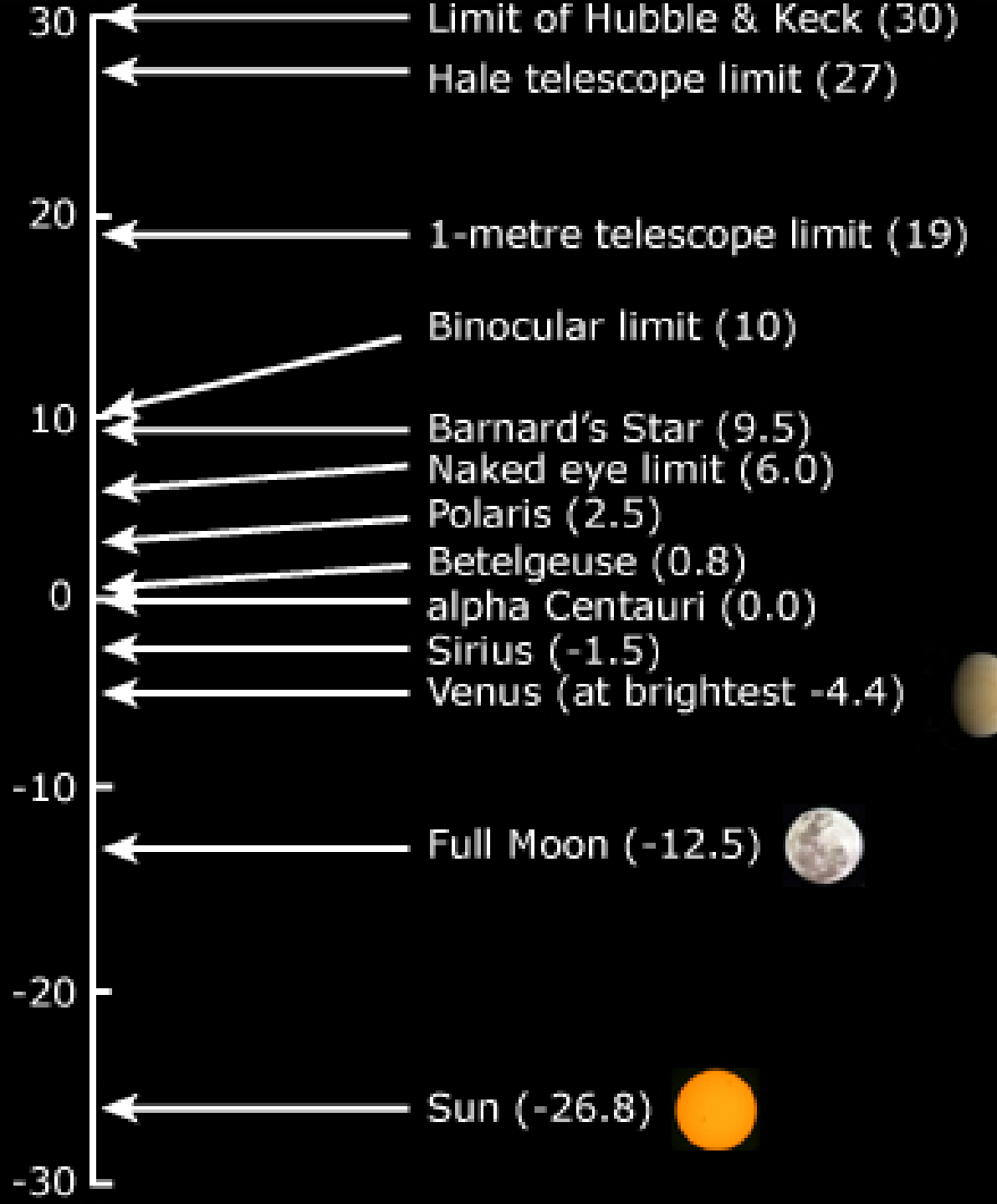
$$m_1 - (-26.8) = -2.5 \log(I_1 / 0.137 \text{ watts cm}^{-2})$$

For sound: $\text{dB}_1 - \text{dB}_2 = 10 \log(I_1/I_2)$

For light: $m_1 - m_2 = -2.5 \log(I_1/I_2)$

“—” means smaller m is brighter!

Apparent Magnitude



Intensity of sun vs. naked eye limit

Sun $m_S = -26.8$

Naked eye limit $m_N = 6$

$$m_S - m_N = -2.5 \log(I_S/I_N)$$

$$-27 - 6 = -2.5 \log(I_S/I_N)$$

$$\cancel{33} = \cancel{5} \frac{2}{5} \log(I_S/I_N)$$

$$33 \times \frac{2}{5} = 13 = \log(I_S/I_N)$$

$$10^{13} = I_S/I_N$$

Intensity of Venus vs. Pluto

Venus

$$m_{\text{♀}} = -4$$

Pluto

$$m_{\text{♁}} = 15$$

$$m_{\text{♀}} - m_{\text{♁}} = -2.5 \log(I_{\text{♀}}/I_{\text{♁}})$$

$$-4 - 15 = -2.5 \log(I_{\text{♀}}/I_{\text{♁}})$$

$$\cancel{-} 19 = \cancel{-} \frac{5}{2} \log(I_{\text{♀}}/I_{\text{♁}})$$

$$19 \times \frac{2}{5} = 8 = \log(I_{\text{♀}}/I_{\text{♁}})$$

$$10^8 = I_{\text{♀}}/I_{\text{♁}}$$

Intensity of Venus vs. Sirius

Venus

$$m_{\text{♀}} = -4$$

Sirius

$$m_{\text{♁}} = -1.5$$

$$m_{\text{♀}} - m_{\text{♁}} = -2.5 \log(I_{\text{♀}}/I_{\text{♁}})$$

$$-4 - (-1.5) = -2.5 \log(I_{\text{♀}}/I_{\text{♁}})$$

$$\cancel{-2.5} = \cancel{-2.5} \log(I_{\text{♀}}/I_{\text{♁}})$$

$$1 = \log(I_{\text{♀}}/I_{\text{♁}})$$

$$10^1 = 10 = I_{\text{♀}}/I_{\text{♁}}$$

The luminosity of nearby stars?

Measure: intensity of light, I

parallax \rightarrow distance

$$I = \frac{L}{4\pi R^2}$$

$$\frac{D}{\text{pc}} = \frac{\text{seconds}}{\text{parallax}}$$

$$I = \frac{L}{4\pi R^2}$$

$$-26.8 - m = -2.5 \log(0.137 \text{ watts cm}^{-2} / I)$$

| star | parallax (") | distance (pc) | apparent magnitude | luminosity (solar) |
|-------------------|-----------------|------------------|-----------------------|-----------------------|
| α Centauri | 0.75 | 1.3 | 0 | 1.5 |
| Barnard's star | 0.5 | 2.0 | 9.5 | 0.0005 |
| Sirius | 0.4 | 2.5 | -1.5 | 25 |
| Altair | 0.2 | 5.0 | 0.8 | 10 |
| Canopus | 0.003 | 330 | -0.7 | 200,000 |
| Arcturus | 0.1 | 10 | 0 | 90 |
| Betelgeuse | 0.01 | 100 | 0.5 | 14,000 |