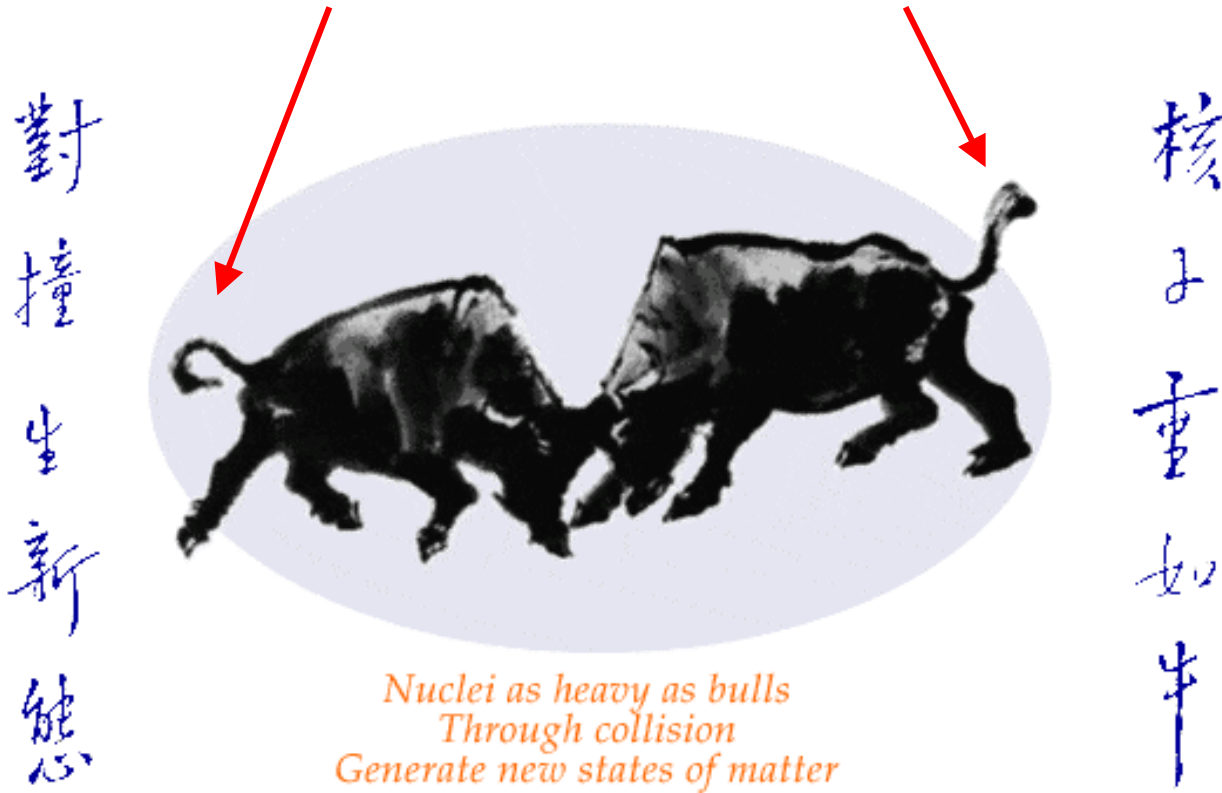
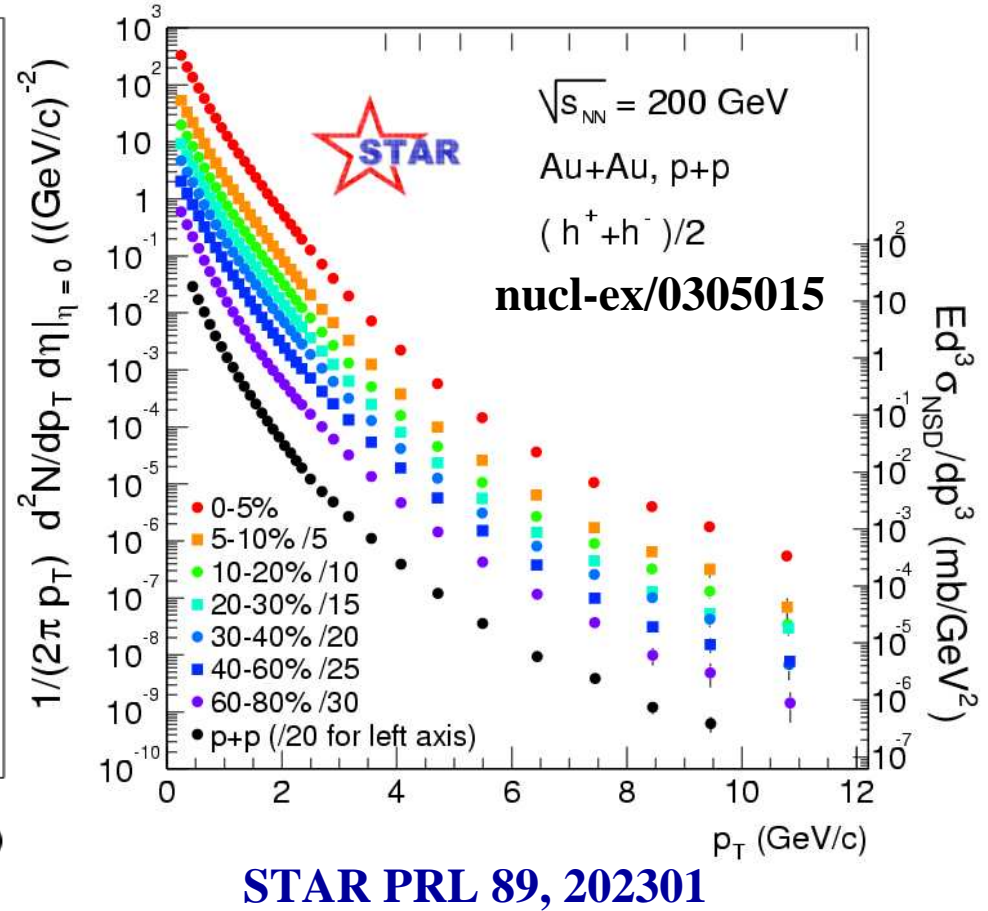
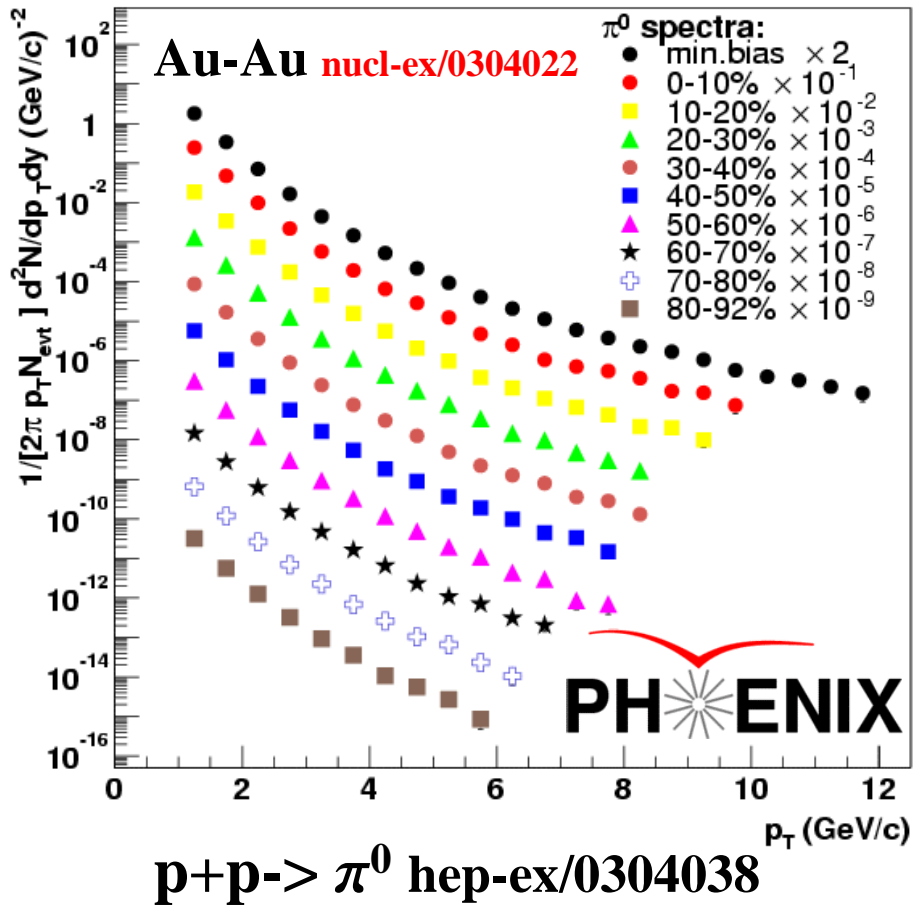


# The pQCD tails provide indicators of What the Bulk is doing



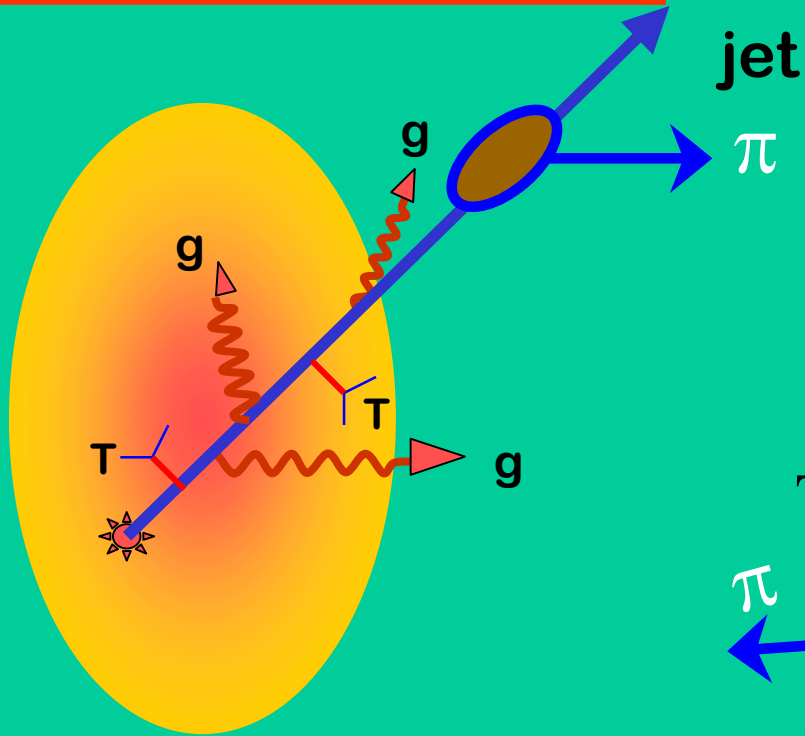
# The high $p_T$ window at RHIC is wide open



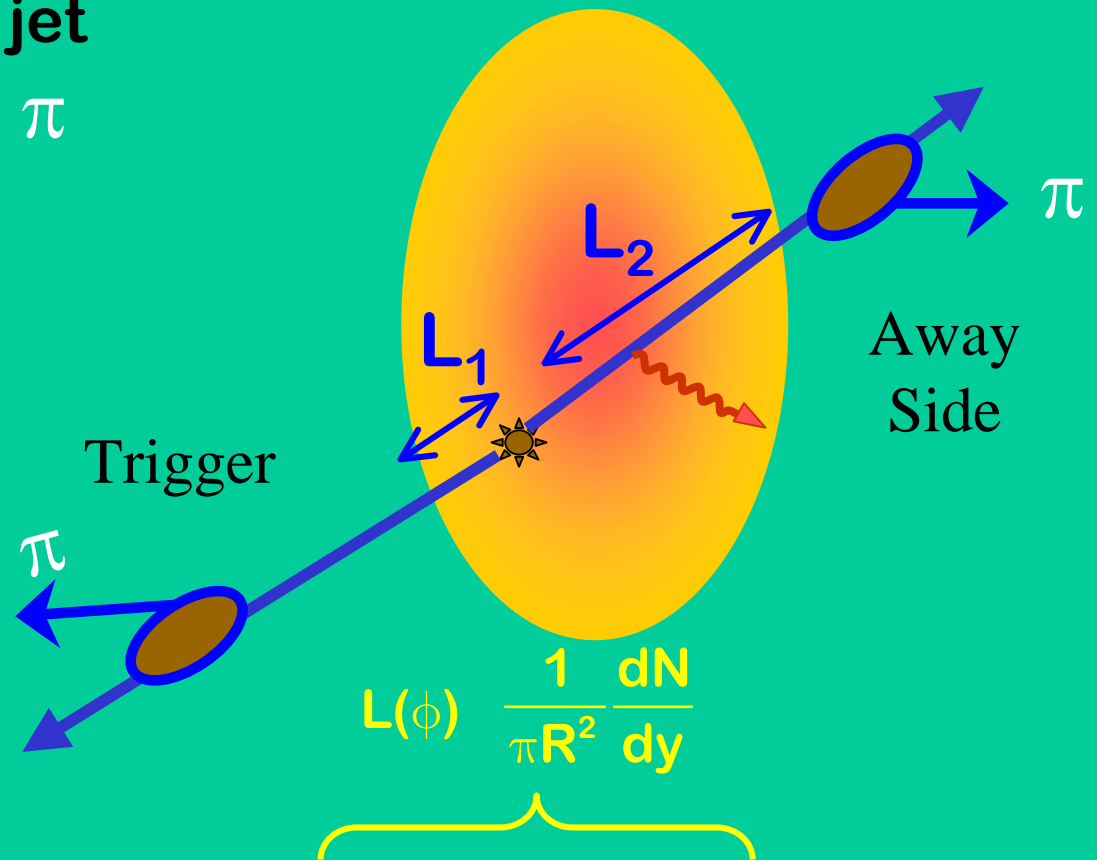
# High $p_T$ Tomography of the QGP

MG, I.Vitev, P. Levai; X.N. Wang, E.Wang, B.W.Zhang  
Review nucl-th/0302077

## Single Hadron Tomography



## Di-Hadron Tomography

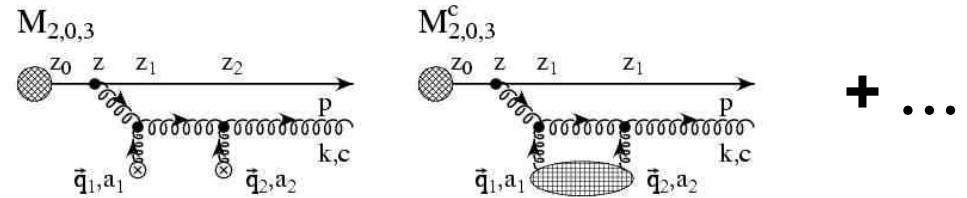


$$\Delta E_{GLV} \sim C_{Jet} C_T \alpha_S^3 \ln \frac{p_T}{\mu^2 L} \int d\tau \tau \rho(\tau, r(\tau))$$

# GLV Opacity Induced Radiation generalized to finite M

GLV: Nucl.Phys.B594(01)

M. Djordjevic, MG (03)



$$x \frac{dN^{(n)}}{dx d^2\mathbf{k}} = \frac{C_R \alpha_s}{\pi^2} \frac{1}{n!} \int \prod_{i=1}^n \left( d^2\mathbf{q}_i \frac{L}{\lambda_g(i)} [\bar{v}_i^2(\mathbf{q}_i) - \delta^2(\mathbf{q}_i)] \right) \times$$

$$\times \left( -2 \tilde{C}_{(1,\dots,n)} \cdot \sum_{m=1}^n \tilde{B}_{(m+1,\dots,n)(m,\dots,n)} \left[ \cos \left( \sum_{k=2}^m \Omega_{(k,\dots,n)} \Delta z_k \right) - \cos \left( \sum_{k=1}^m \Omega_{(k,\dots,n)} \Delta z_k \right) \right] \right)$$

# Hard, Gunion-Bertsch, and Cascade ampl. in GLV generalized to finite M

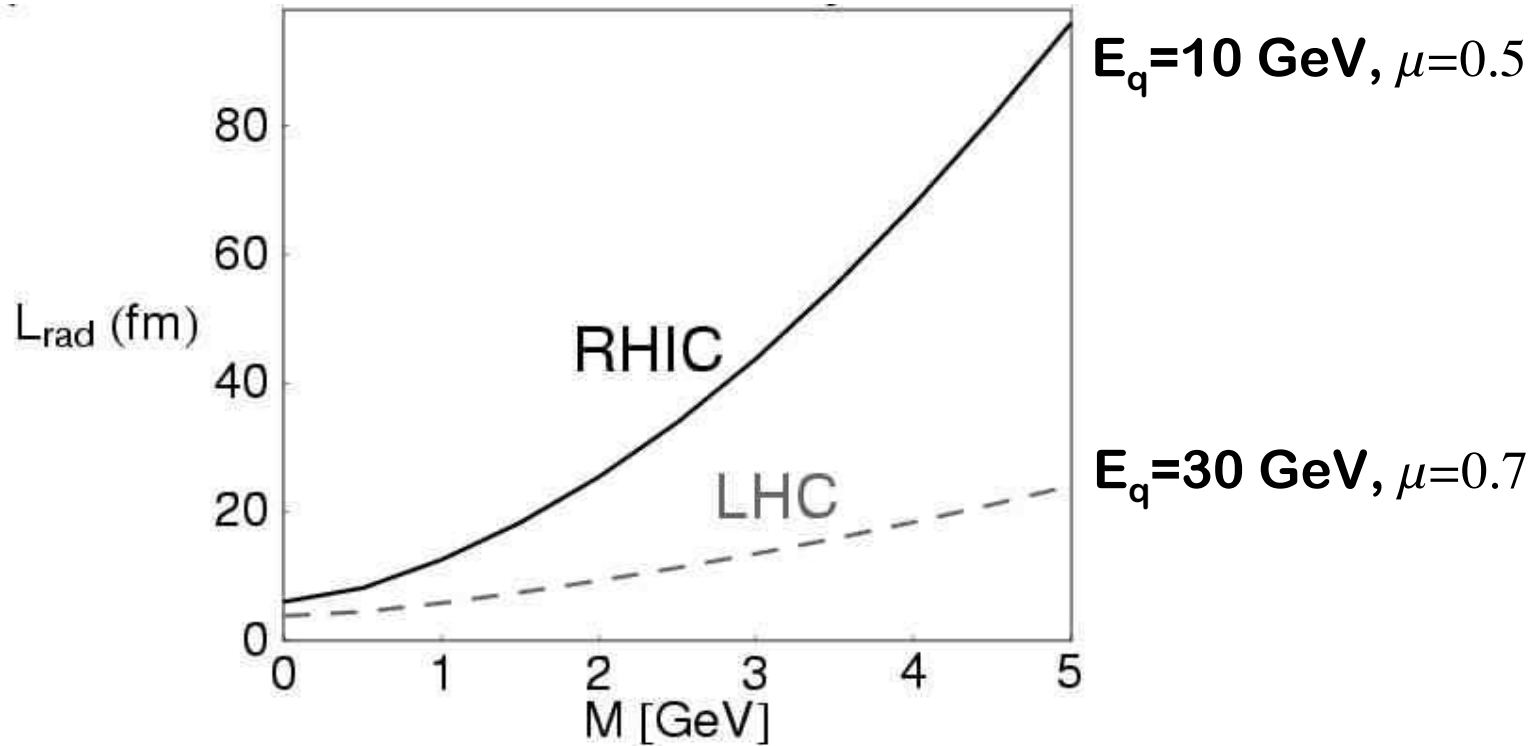
$$\tilde{H} = \frac{\mathbf{k}}{\mathbf{k}^2 + m_g^2 + M^2 x^2}, \quad \tilde{C}_{(i_1 i_2 \dots i_m)} = \frac{(\mathbf{k} - \mathbf{q}_{i_1} - \mathbf{q}_{i_2} - \dots - \mathbf{q}_{i_m})}{(\mathbf{k} - \mathbf{q}_{i_1} - \mathbf{q}_{i_2} - \dots - \mathbf{q}_{i_m})^2 + m_g^2 + M^2 x^2}$$

$$\tilde{B}_i = \tilde{H} - \tilde{C}_i, \quad \tilde{B}_{(i_1 i_2 \dots i_m)(j_1 j_2 \dots j_n)} = \tilde{C}_{(i_1 i_2 \dots j_m)} - \tilde{C}_{(j_1 j_2 \dots j_n)}$$

$$\omega_{(m,\dots,n)} = \frac{(\mathbf{k} - \mathbf{q}_m - \dots - \mathbf{q}_n)^2}{2xE} \rightarrow \Omega_{(m,\dots,n)} \equiv \omega_{(m,\dots,n)} + \frac{m_g^2 + M^2 x^2}{2xE}$$

# Radiation Length in QGP

$$\frac{d\Delta E}{dL} \equiv \frac{E}{L_{\text{rad}}(M, m_g, E, L)}$$



$$dN_{AB \rightarrow H} = T_{AB} \otimes (f_{a/A} \otimes f_{b/B})_{\Delta k_T}^{\text{shad}} \otimes d\sigma_{ab \rightarrow c} \otimes P(\Delta E) \otimes D_{H/c}$$

## 3 Milestones passed at RHIC

$$\begin{aligned} \text{QGP} &= P_{\text{QCD}} + \text{pQCD} + \text{dA} \\ &= v_2(p_T, m) + (R+I)_{AA} + (R+I)_{DA} \end{aligned}$$

1                      2                      3

- 1) Evidence for  $P_{\text{QCD}}$  via  $v_2$  bulk collective flow of  $10^4 \pi, K, p, \Lambda, \Xi$
- 2) Evidence for pQCD jet quenching in Au+Au at RHIC
- 3) Evidence jet *un*-quenching in D+Au = Null Control

**Conclusion: QGP Matter seen in AuAu at 200 AGeV**

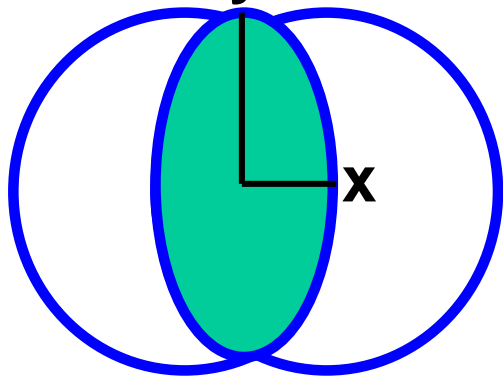
# Bulk Collective Flow of QCD matter

$$\partial_\mu T^{\mu\nu} = \partial_\mu \left\{ u^\mu u^\nu (\epsilon(T) + P(T)) - g^{\mu\nu} P(T) \right\} = 0$$

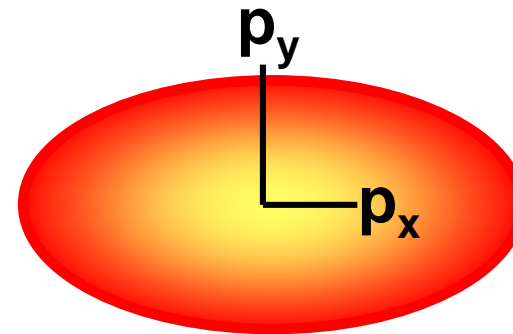
QCD EOS

H. Stocker, W. Greiner (1980)  
 J. Ollitrault (1992)  
 P. Kolb, U. Heinz et al (2000)  
 D. Teaney, E. Shuryak et al  
 T. Hirano, Y. Nara **3+1D**

Initial *spatial*  
 anisotropy



Final *momentum* anisotropy



$$\partial_\mu T^{\mu\nu}(x) = 0$$

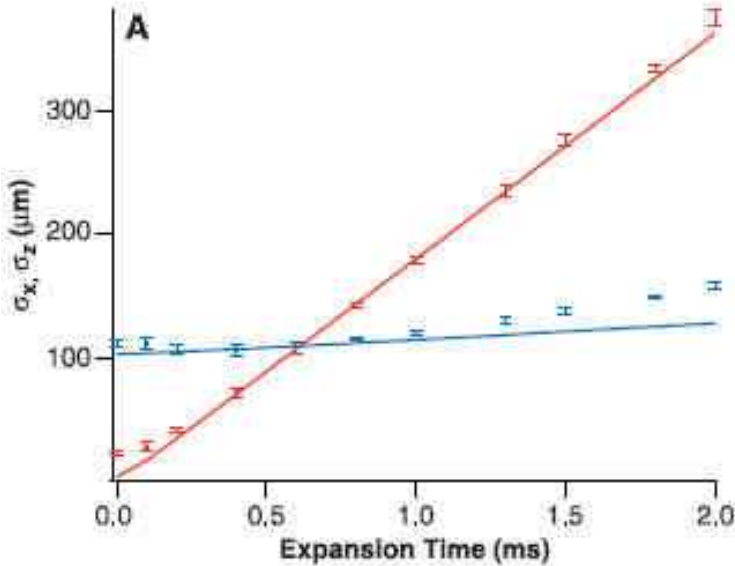
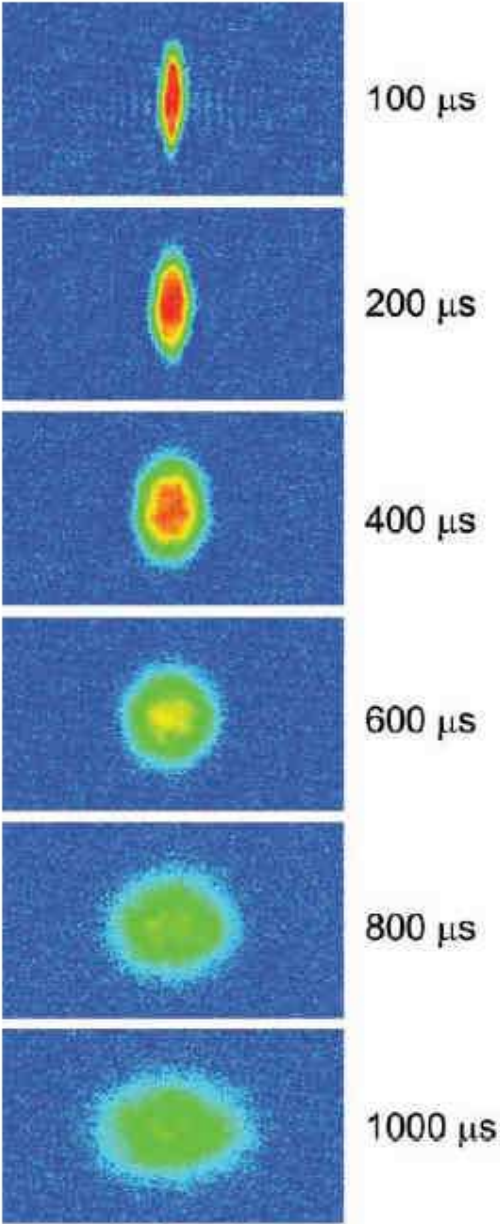
Elliptic Flow

$$\frac{dN}{dy dp_T^2 d\phi} = \rho(y, p_T) \left\{ 1 + 2v_2(p_T) \cos(2\phi) + \dots \right\}$$

# Elliptic Flow of Ultracold Li<sub>6</sub> Atoms

K.M.O'Hara et al, Science 2002

$T \sim 50 \cdot 10^{-9} \text{ K}$





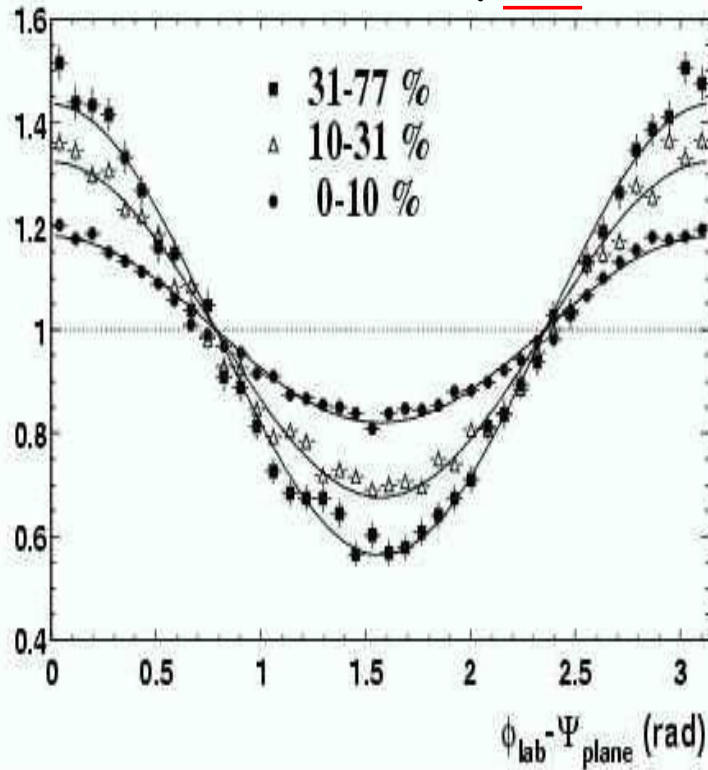
# Observed Elliptic Flow of $10^{12}K$ QGP at RHIC

Hydro: P.Kolb et al, D.Teany et al

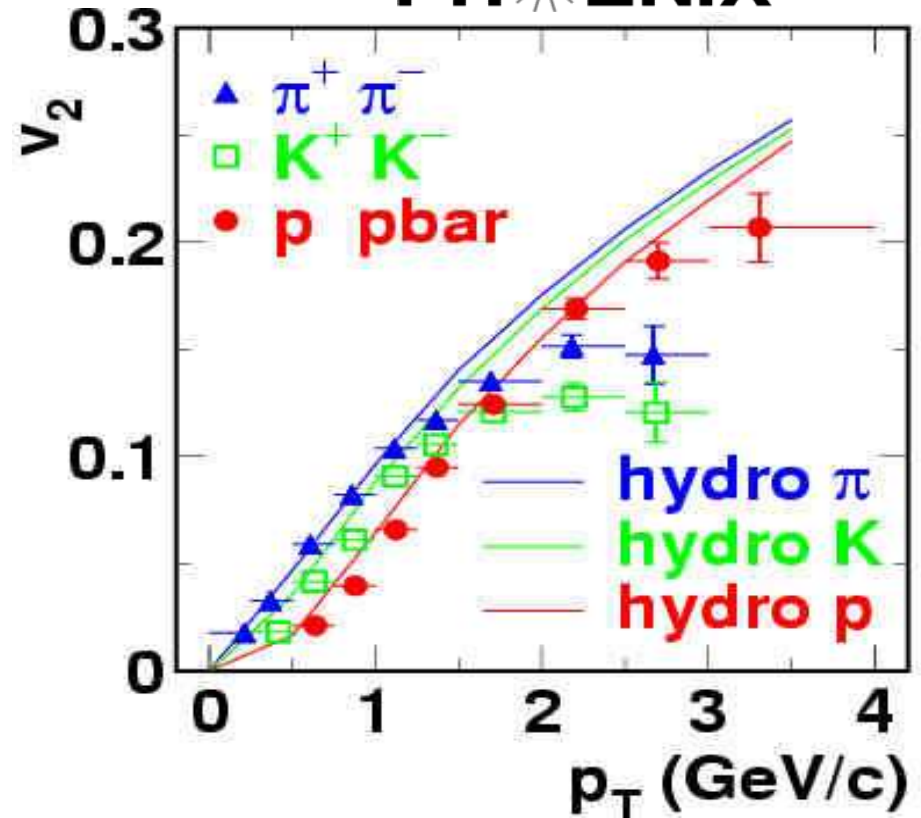
Exp: A. Poskanzer, S. Voloshin, ....



$d^3N/dydp_T d\phi$



PHENIX



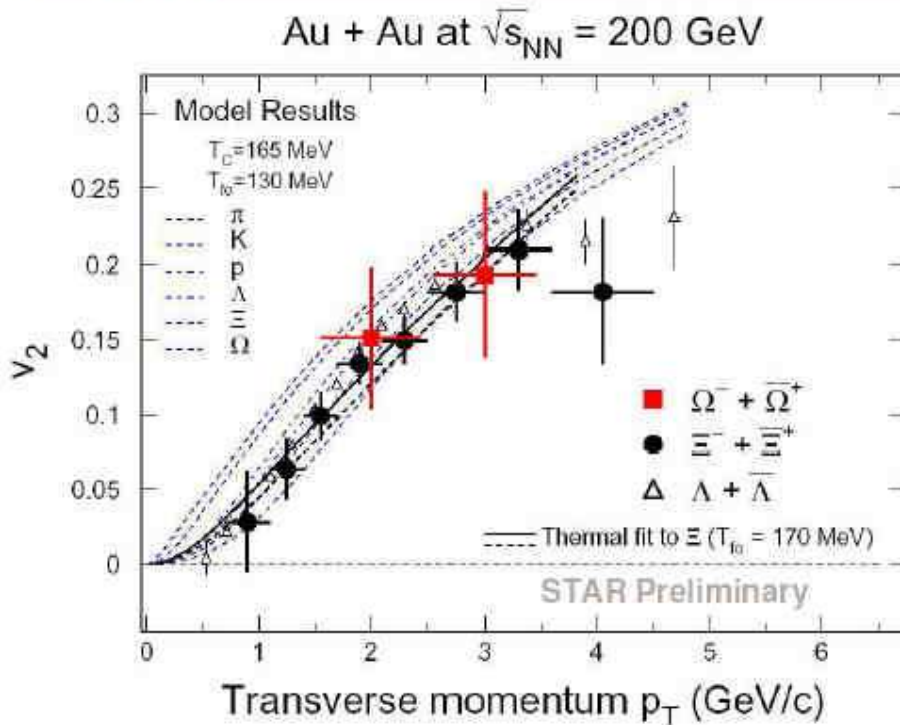
Azimuthal Fourier Expansion

$$\frac{dN}{dydp_T^2 d\phi} = \rho(y, p_T) \left\{ 1 + 2 v_1(p_T) \cos(\phi) + 2 v_2(p_T) \cos(2\phi) + \dots \right\}$$

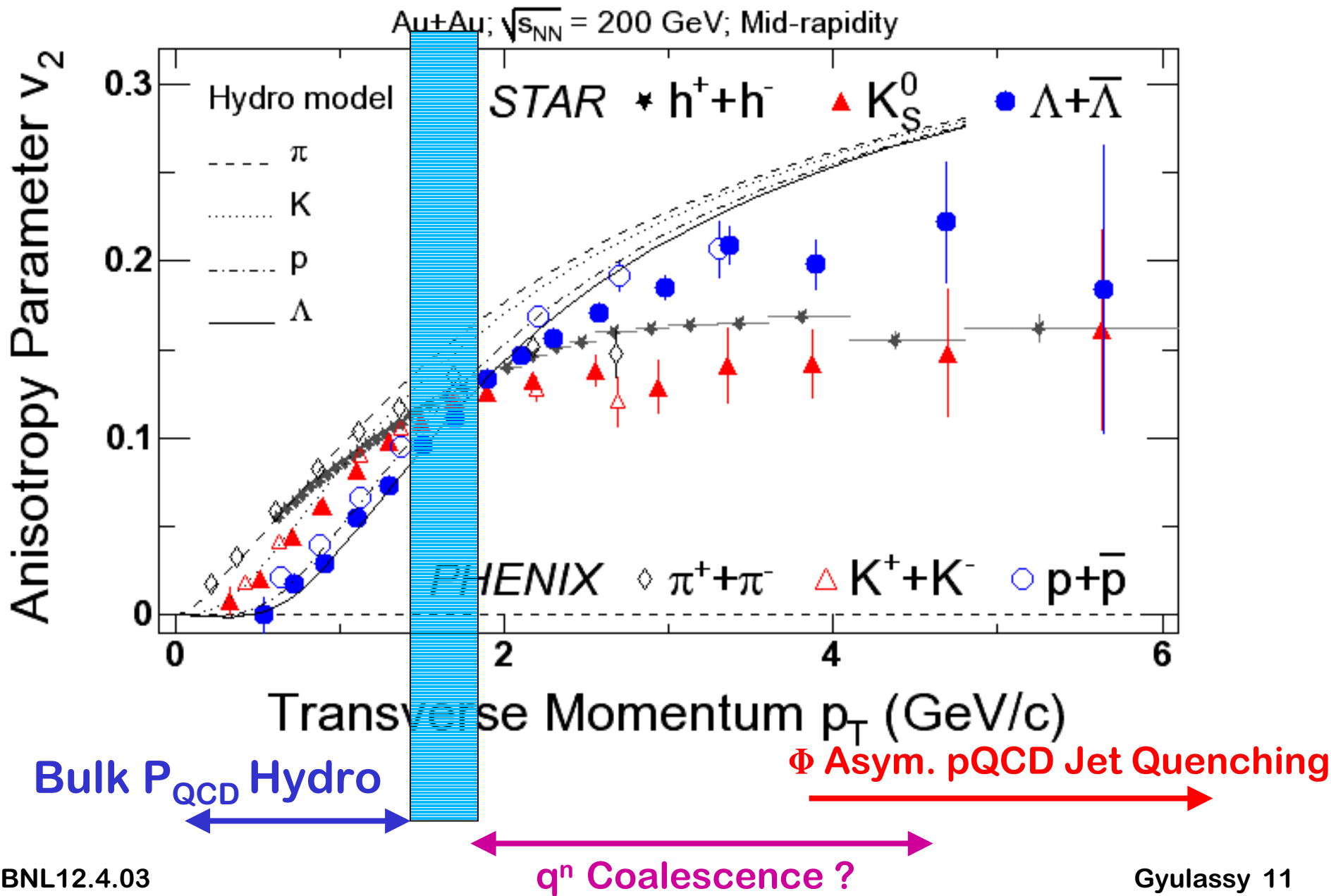
Even  $\Omega(sss)$  marches in lock step with  $\Xi, \Lambda, p, K, \pi$  !



## Multi-Strange Baryons $v_2$

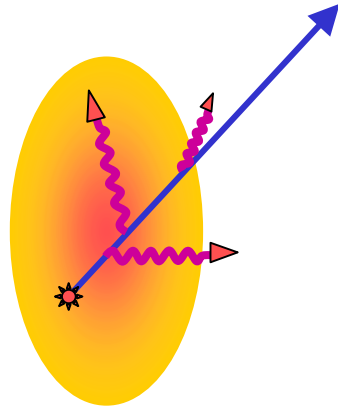


q Multi-strange baryons show collectivity !  
 q **Partonic collectivity at RHIC!**



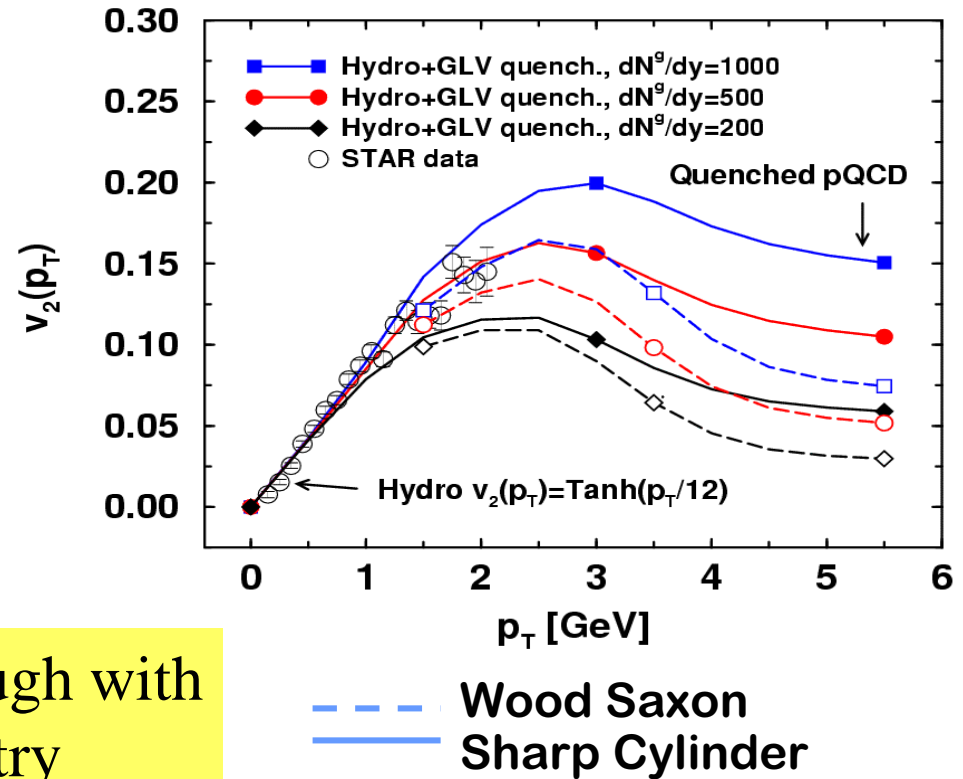
# Azimuthal $v_2(p_T)$ Tomography

$$\rho_{\text{QGP}}(\tau, \mathbf{x}_0 + \hat{\mathbf{n}}\tau)$$



Energy Loss Asymmetry not enough with  
Wood-Saxon diffuse geometry

I. Vitev, X.N. Wang, MG, PRL86(01)



Need an asymmetry amplifier

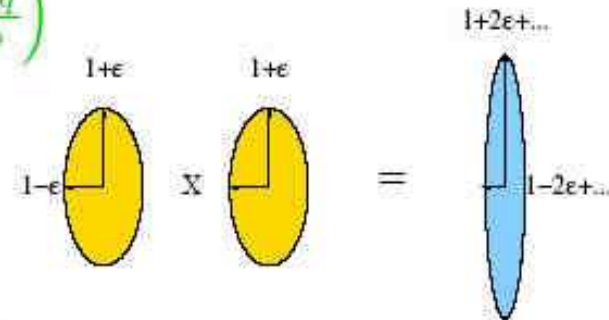
# Coalescence amplifies elliptic flow

D. Molnar and S. Voloshin, PRL 91 (03)

narrow wave fn. limit ( $\vec{q} = 0$ ):  $\frac{dN_M}{d\phi} \propto \left(\frac{dN_q}{d\phi}\right)^2$

$$v_2^M(p_\perp) \approx v_2^a\left(\frac{p_\perp}{2}\right) + v_2^a\left(\frac{p_\perp}{2}\right)$$

$$v_2^B(p_\perp) \approx v_2^a\left(\frac{p_\perp}{3}\right) + v_2^b\left(\frac{p_\perp}{3}\right) + v_2^c\left(\frac{p_\perp}{3}\right)$$

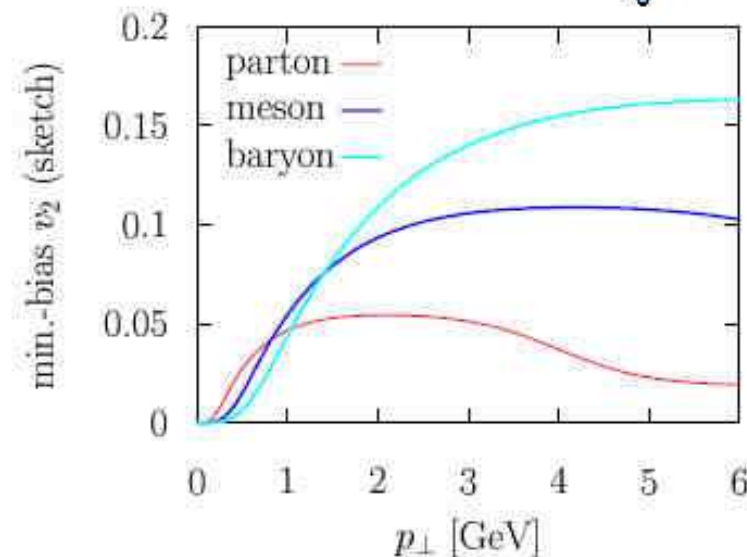


⇒ hadron flow amplified at high  $p_\perp$   
if all quarks have same  $v_2$ :

3× for baryons

2× for mesons

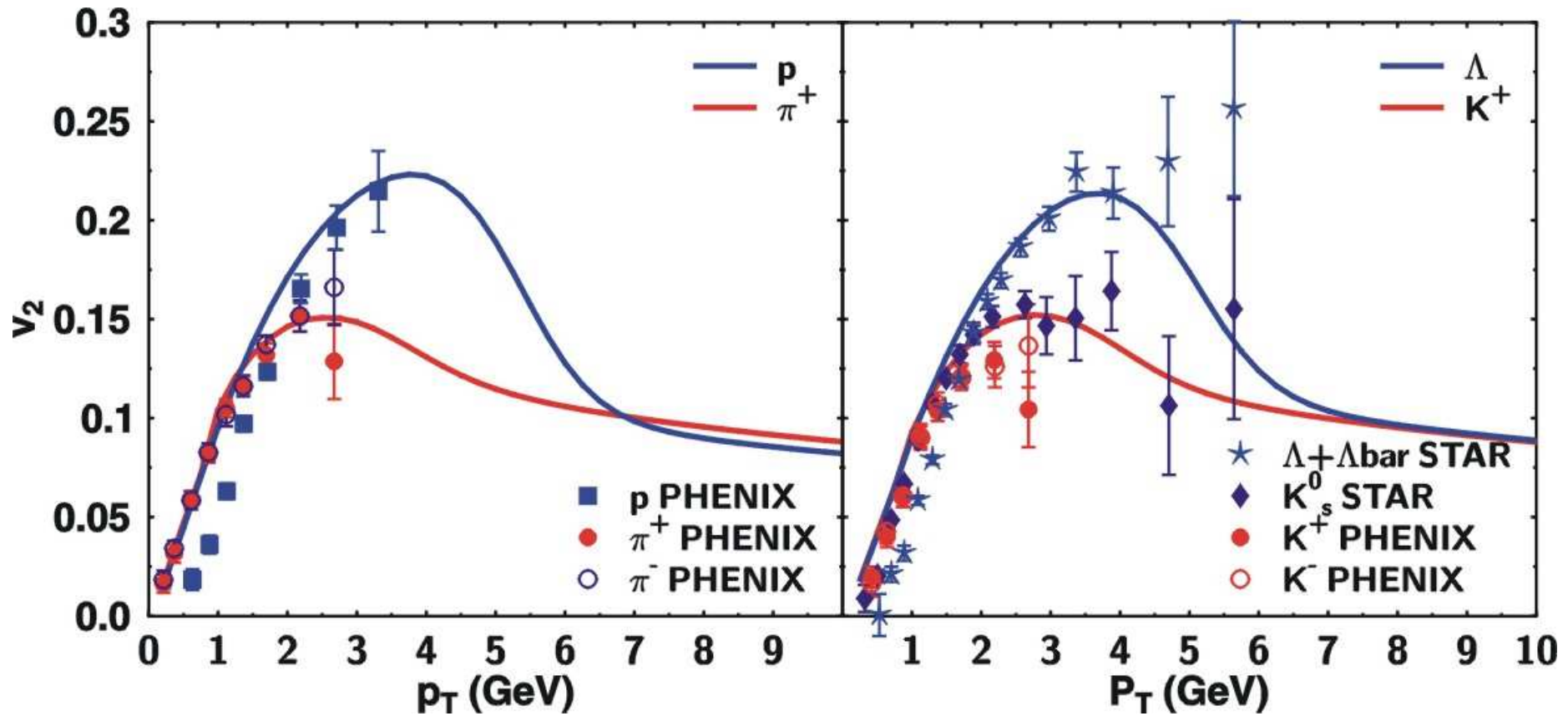
$$v_2^h(p_\perp) \approx n \times v_2^q(p_\perp/n)$$



• this **KEY EFFECT** solves opacity puzzle (much smaller parton  $v_2$  needed)

# Flavor Dependence of $v_2$ via Recombination

Rainer J. Fries: BNL Flow Workshop 11.19.03

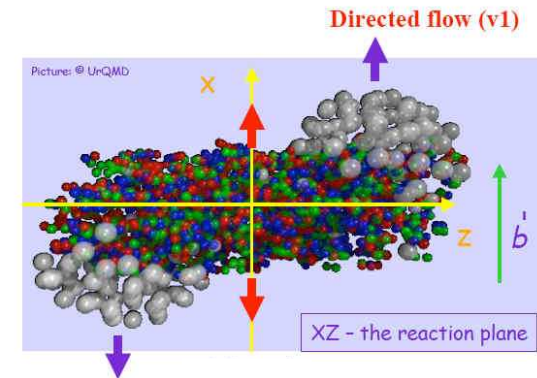
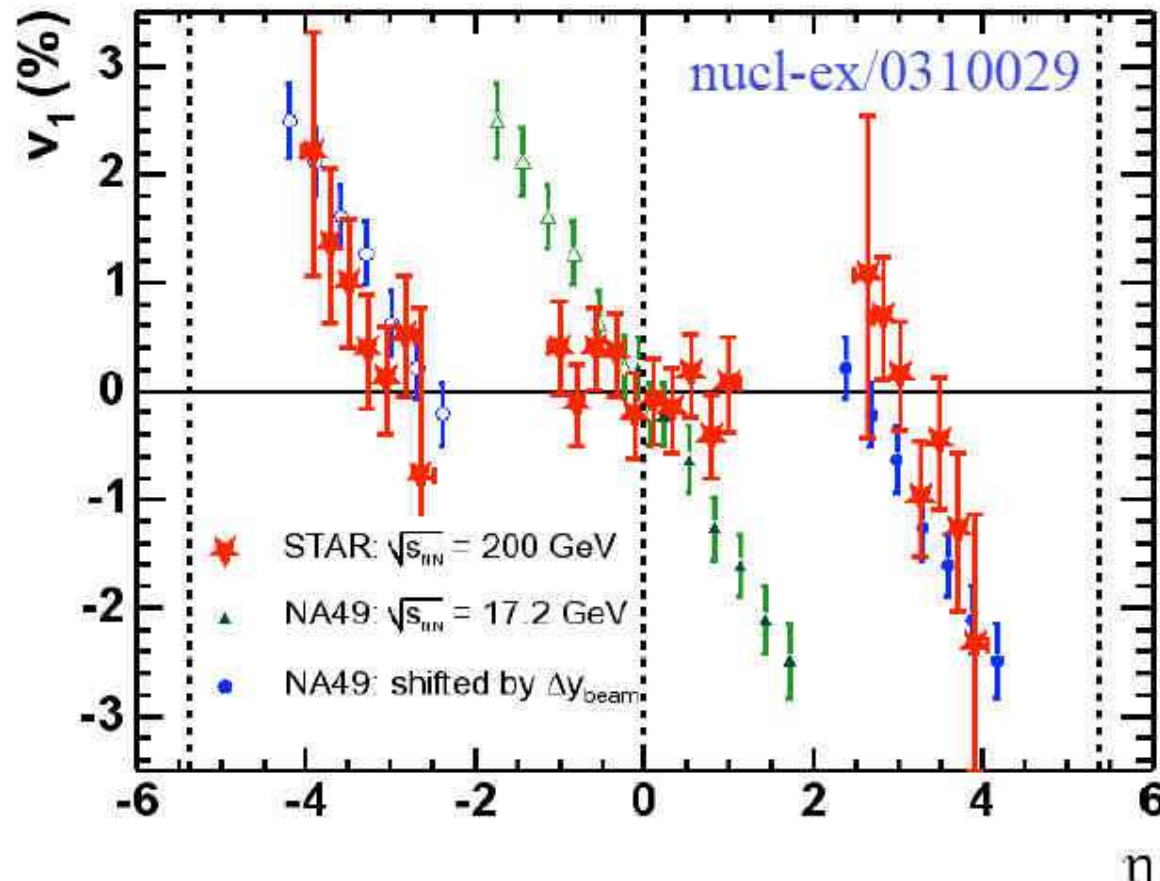


➤ Recombination describes measured flavor-dependence of  $v_2$ !

# Collectivity correlated over 8 units of rapidity !!

New!

## Directed flow at RHIC



Limiting Frag Pattern

$v_1(y=3)$  reaction plane  $\Phi_R$  same as from  $v_2(0)$  !



Aihong Tang, Flow workshop Nov. 2003

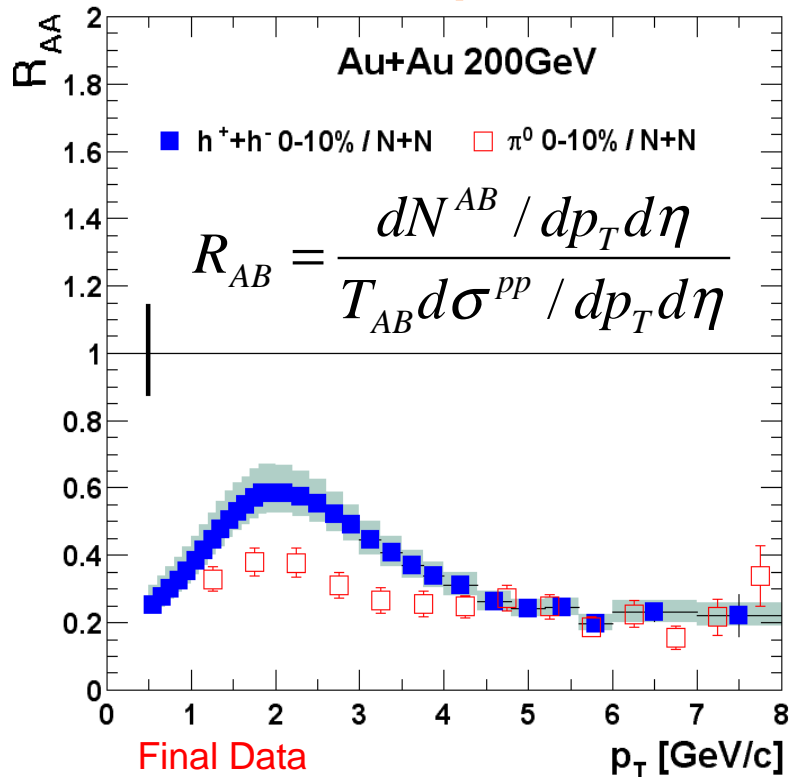
BNL

6

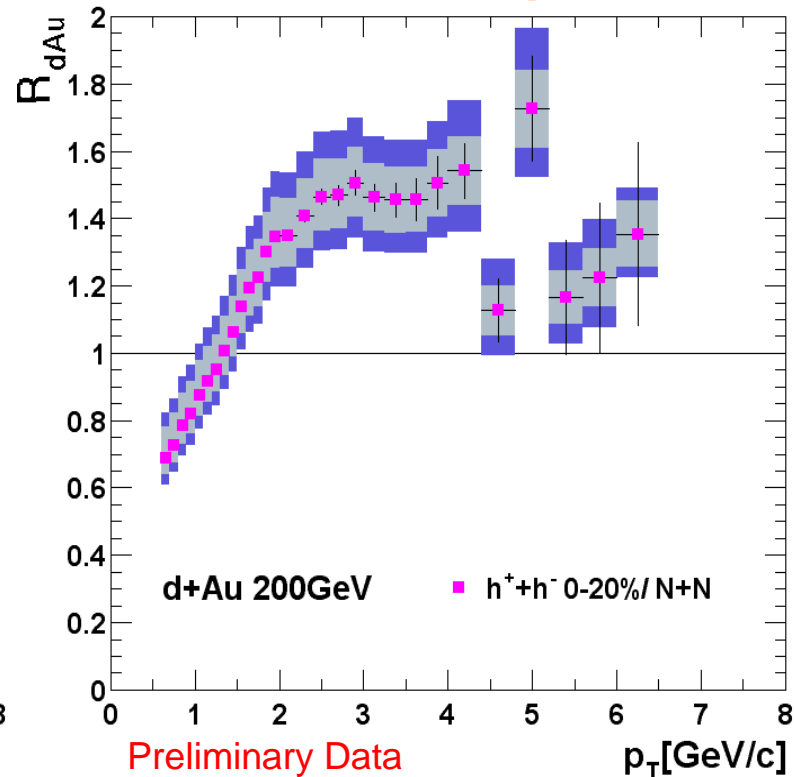
# Centrality Dependence of High $p_T$ A+B vs p+p



**Au + Au Experiment**



**d + Au Control Experiment**

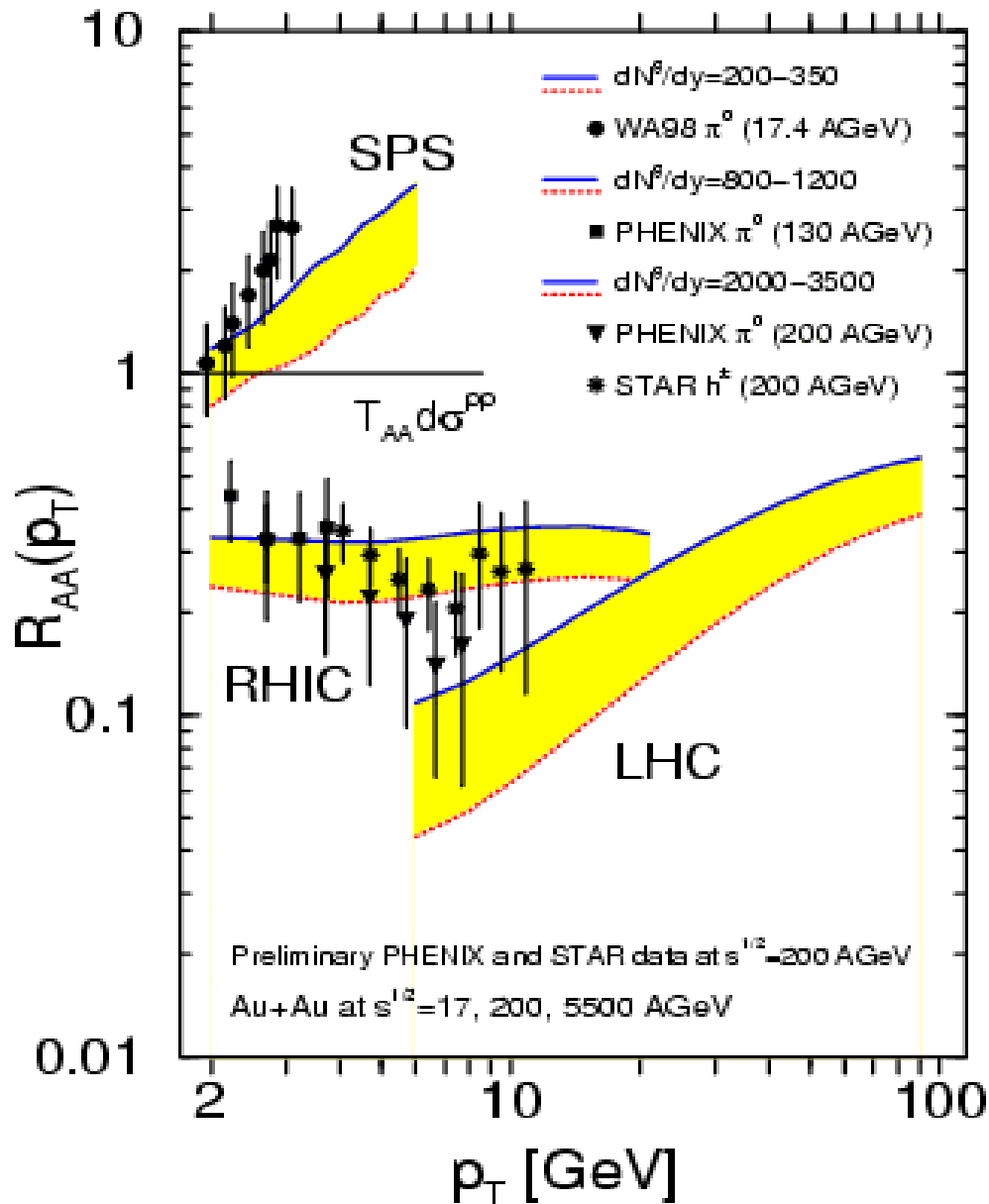


- Dramatically different and opposite centrality evolution of Au+Au experiment from d+Au control.



# Single Hadron Tomography from SPS, RHIC, LHC

Ivan Vitev and MG, Phys.Rev.Lett. 89 (2002)



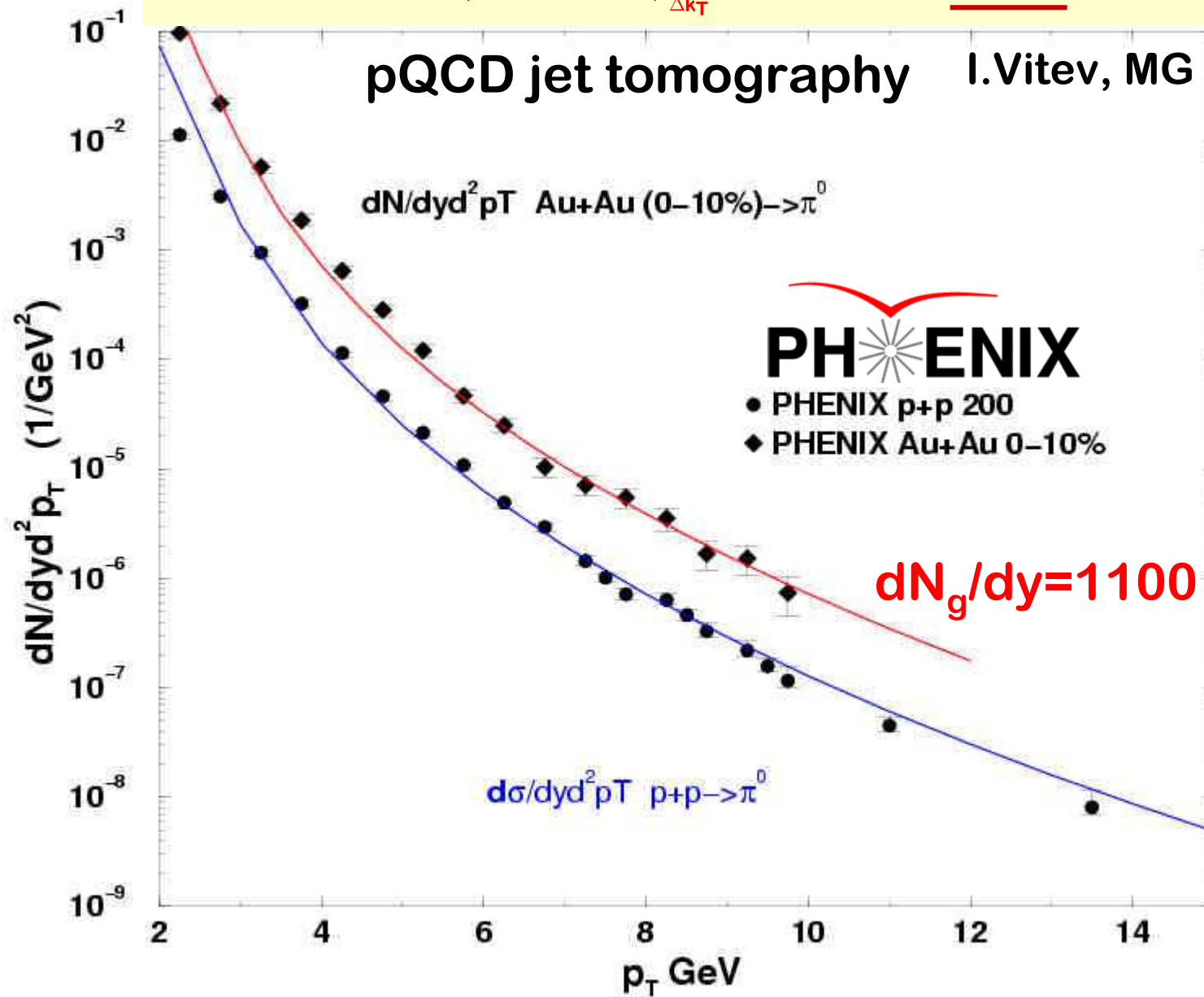
1) Cronin *enhancement*  
dominates at SPS

2) Cronin+Quench+Shadow  
conspire to give ~ flat  
 $R_{AA} \sim N_{part}/N_{bin}$  at RHIC

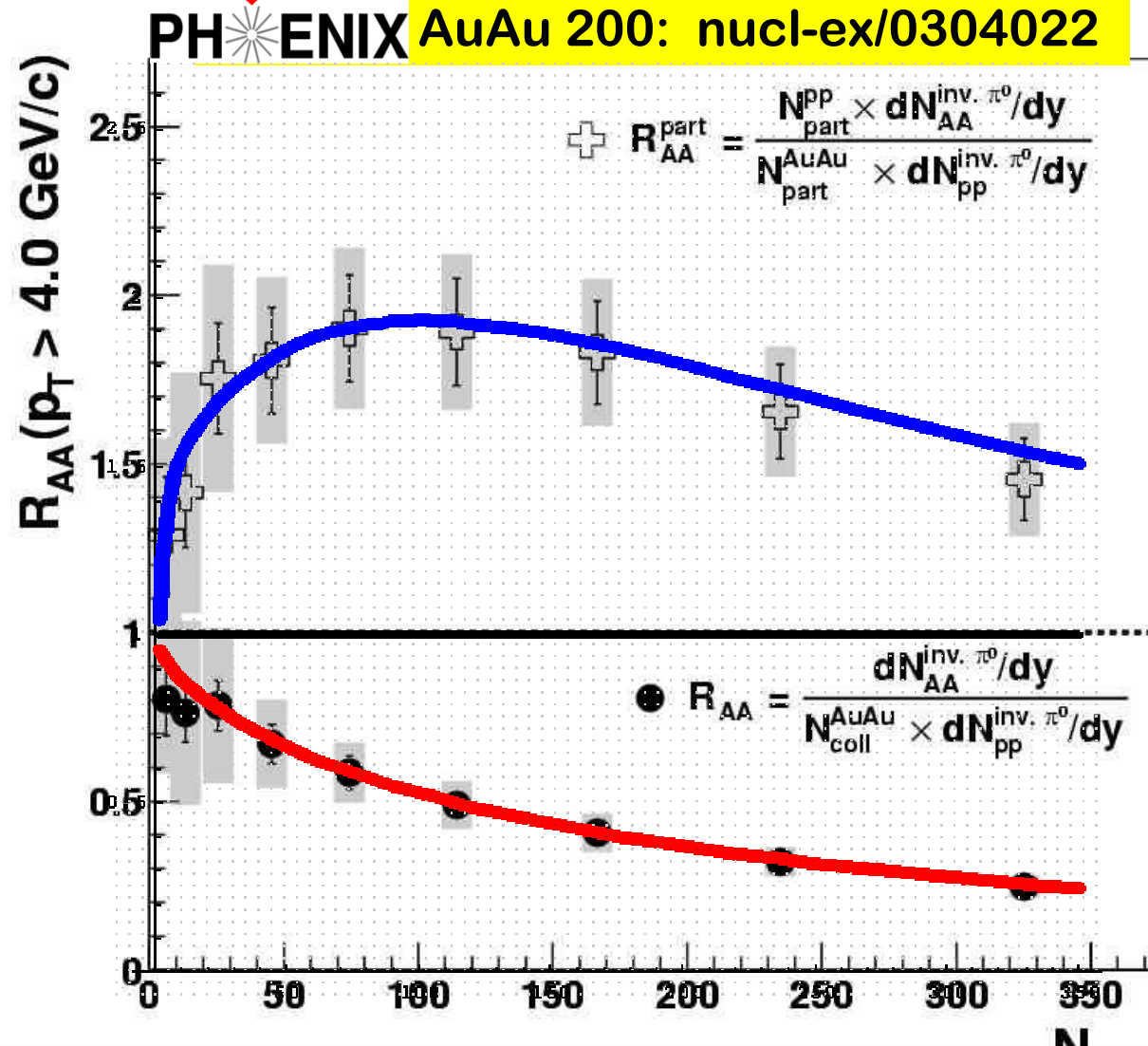
3)  $R_{AA} + I_{AA}$  data indicate  
 $dN_g/dy \sim 1000 \rightarrow \rho_g \sim 100 \rho_0$

$$dN_{AB \rightarrow \pi} = T_{AB} \otimes (f_{a/A} \otimes f_{b/B})_{\Delta k_T}^{\text{shad}} \otimes d\sigma_{ab \rightarrow c} \otimes \underline{P(\Delta E)} \otimes D_{\pi/c}$$

GRV  
EKS  
BKK  
GLV



# Centrality Dependence of $\pi^0$ Quenching

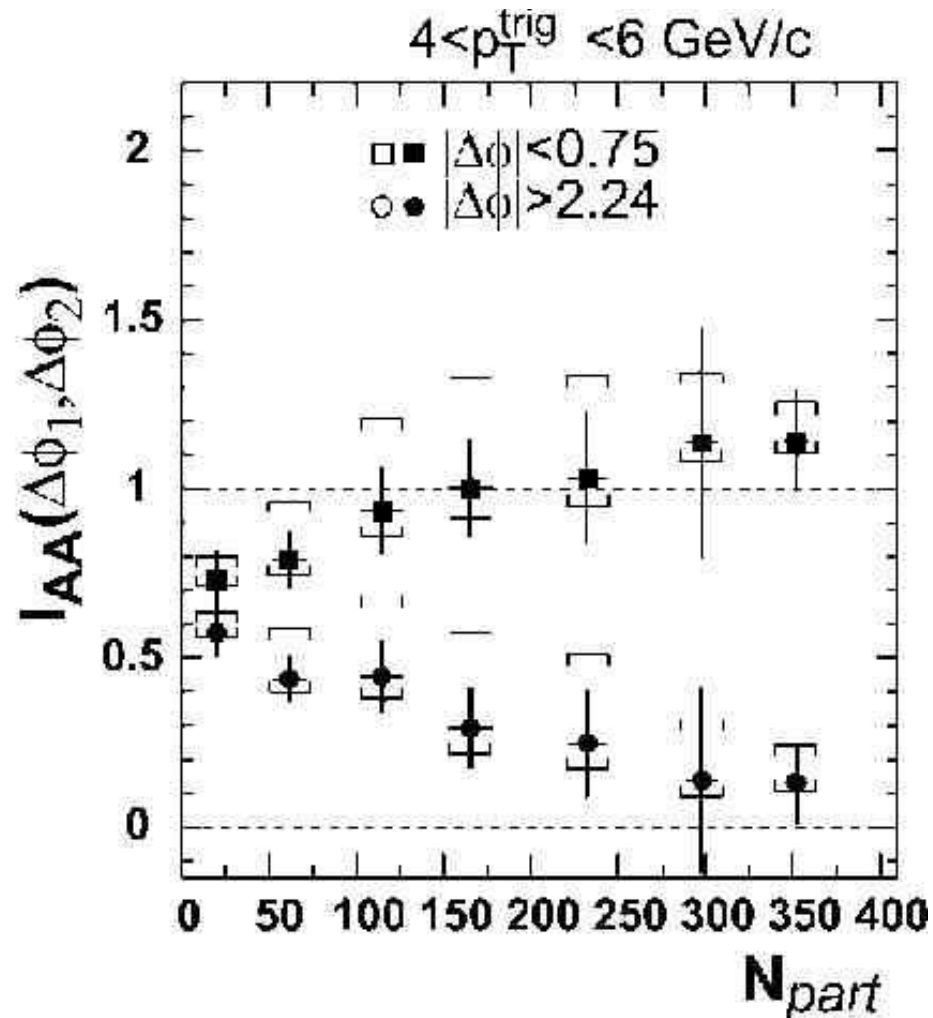
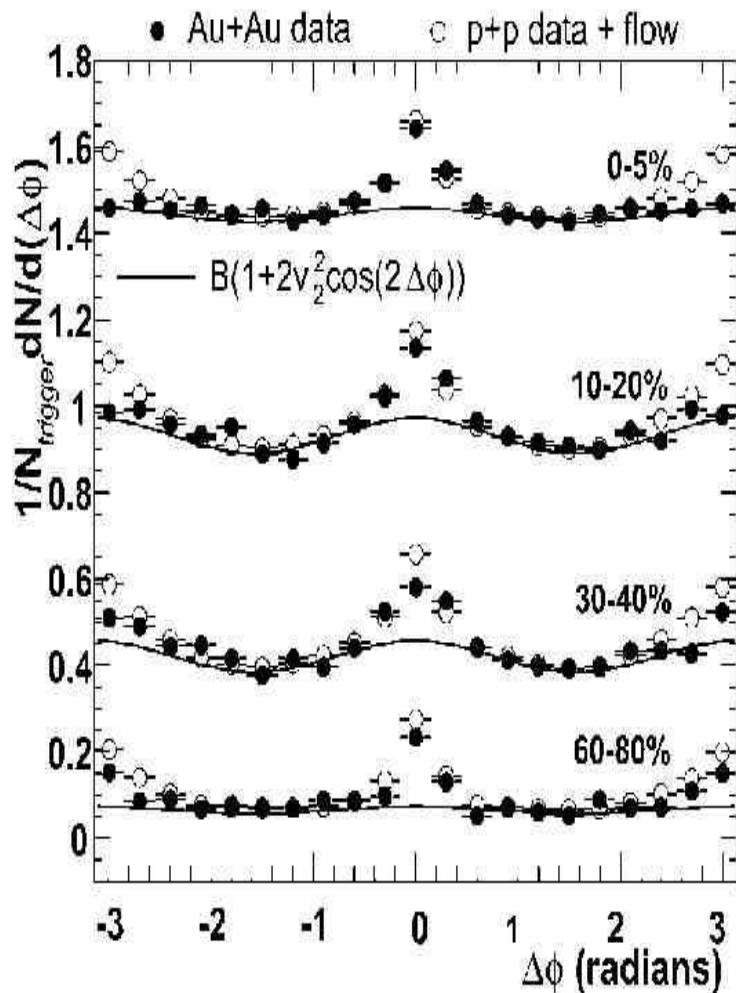


Consistent  
With GLV  
Formalism

$$\Delta E_{GLV} \propto \int d\tau \tau \rho(\tau, r(\tau)) \propto \frac{R}{\pi R^2} \frac{dN_g}{dy} \propto N_{part}^{2/3}$$

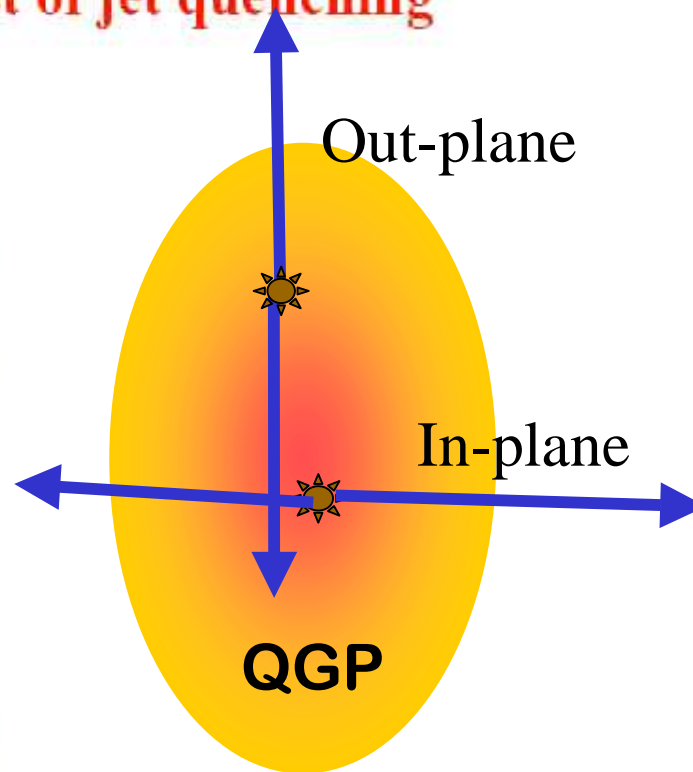
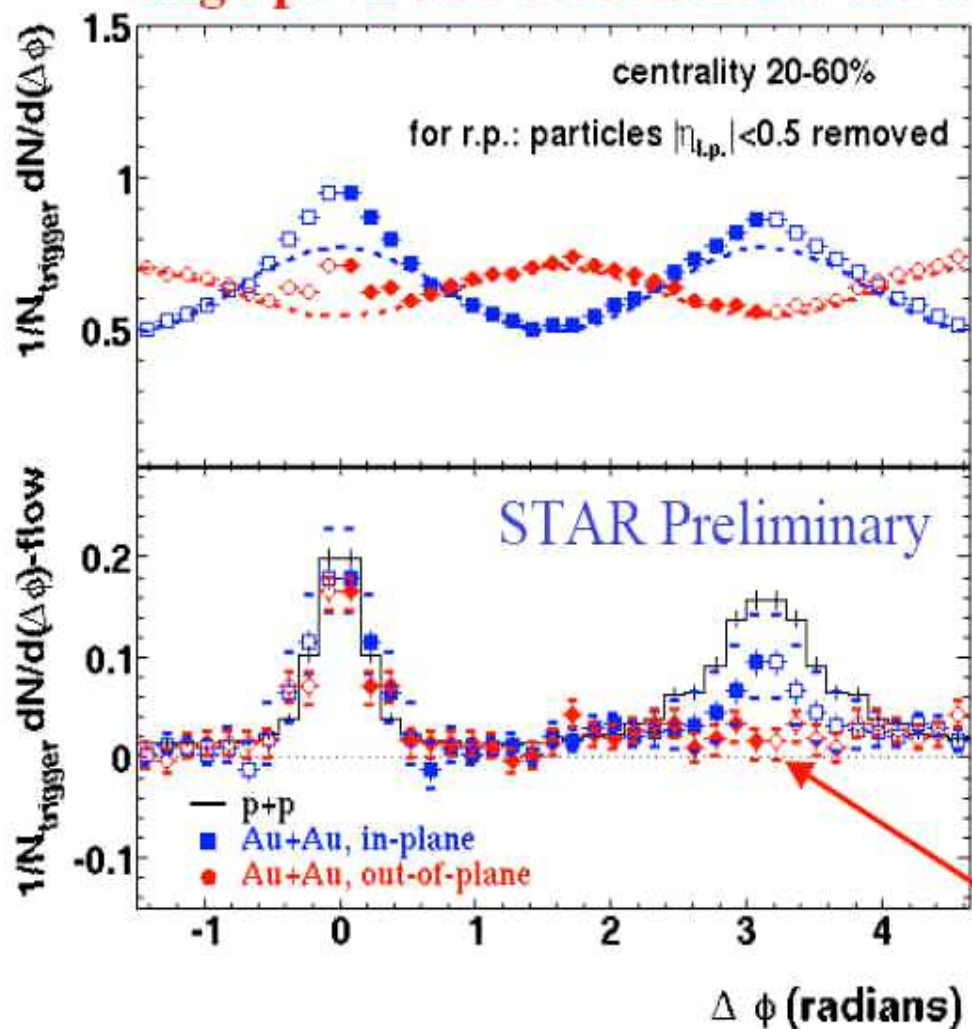
STAR: C. Adler et al. Phys. Rev. Lett. 90, 082302 (2003)

$$I_{AA}(\Delta\phi_1, \Delta\phi_2) = \frac{\int_{\Delta\phi_1}^{\Delta\phi_2} d(\Delta\phi) \{D^{AuAu} - B[1 + 2v_2^2 \cos(2\Delta\phi)]\}}{\int_{\Delta\phi_1}^{\Delta\phi_2} d(\Delta\phi) D^{pp}}$$



Correlation of Associated hadrons  $2 < p_T < 4 \text{ GeV}$  with triggered  $4 < p_T < 6$

High pt v2 and correlation : the test of jet quenching

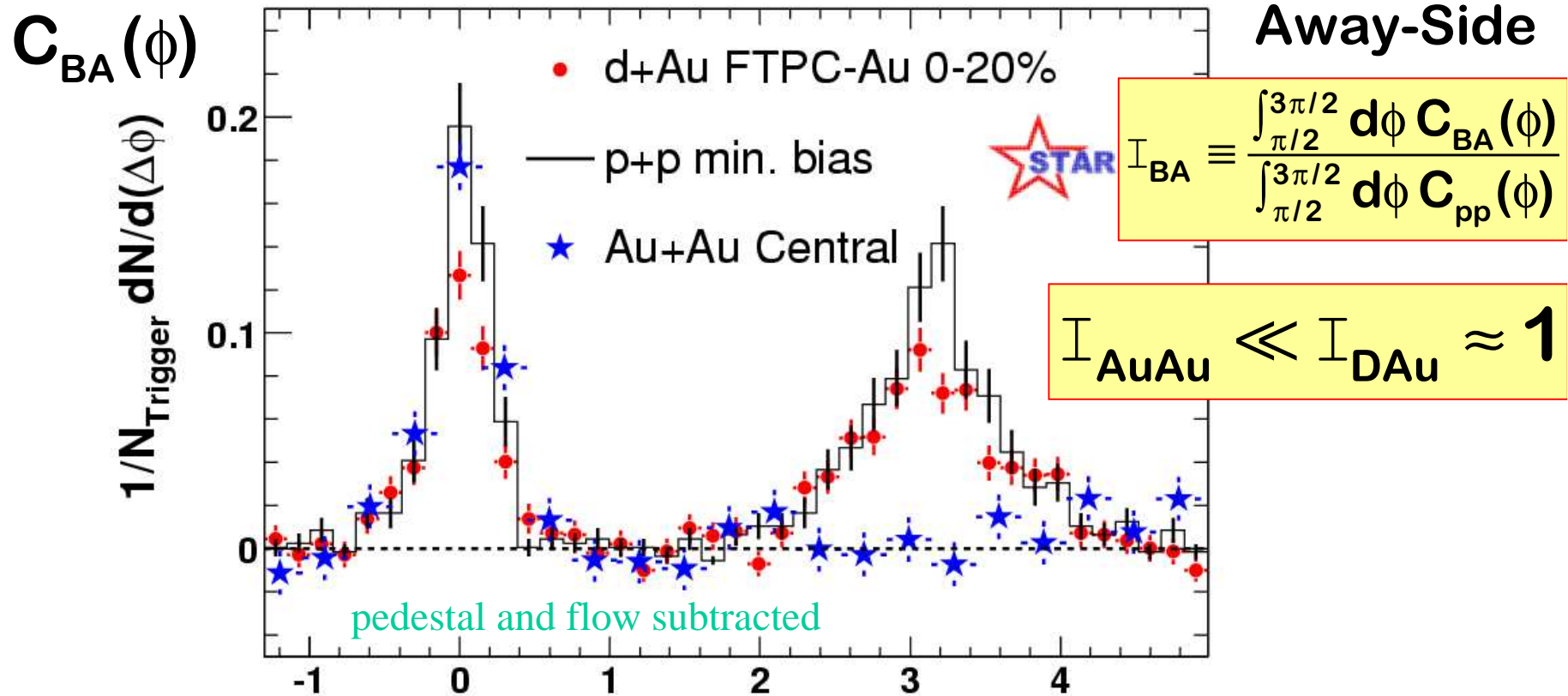


Back-to-back suppression is larger in the out-of-plane direction

A.Tang: BNL 11.18.03



# “The Return of the Jeti” in D+Au



Near-side: p+p, d+Au, Au+Au similar  $\Delta\phi$  (radians)

Away-side: Au+Au strongly suppressed relative to p+p and d+Au

Suppression of the back-to-back correlation  
in central Au+Au is a final-state effect

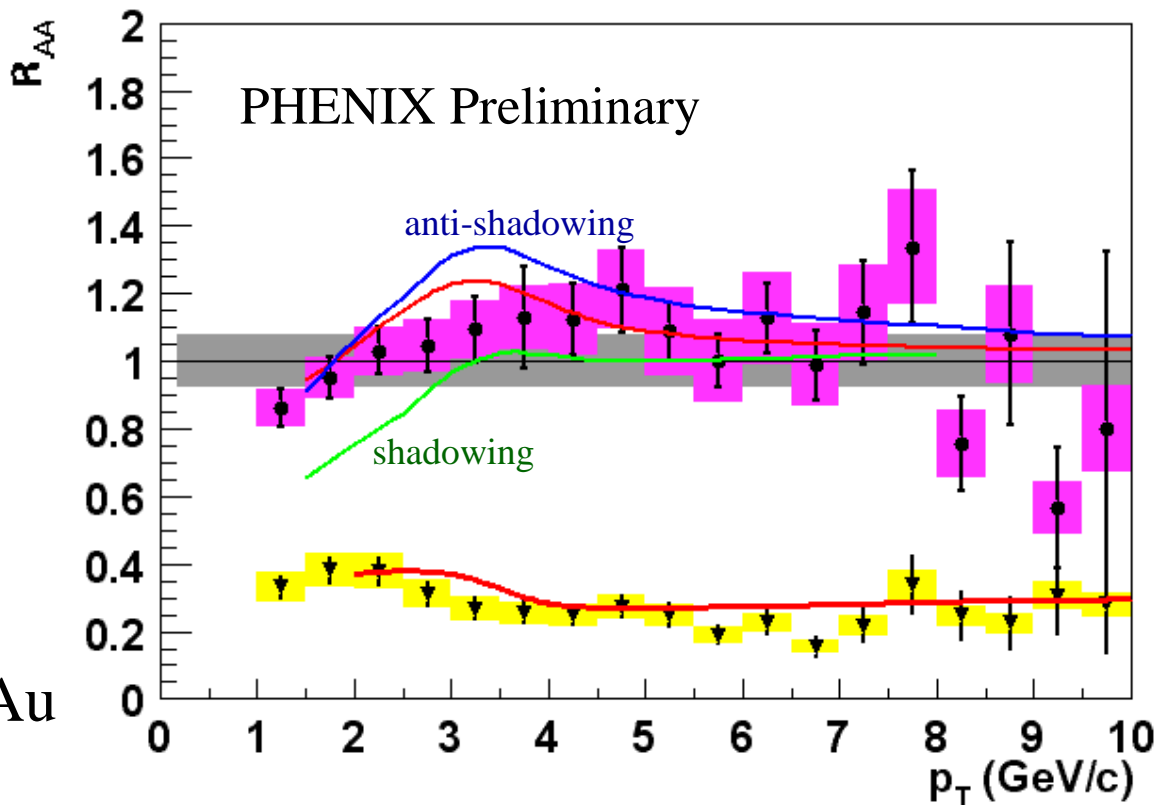
# $\pi^0$ $R_{BA}(p_T)$ Predictions vs Experiment for central Au+Au and d+Au collisions

I. Vitev, nucl-th/0302002

I. Vitev and M. Gyulassy, PRL89  
(2002) 252301

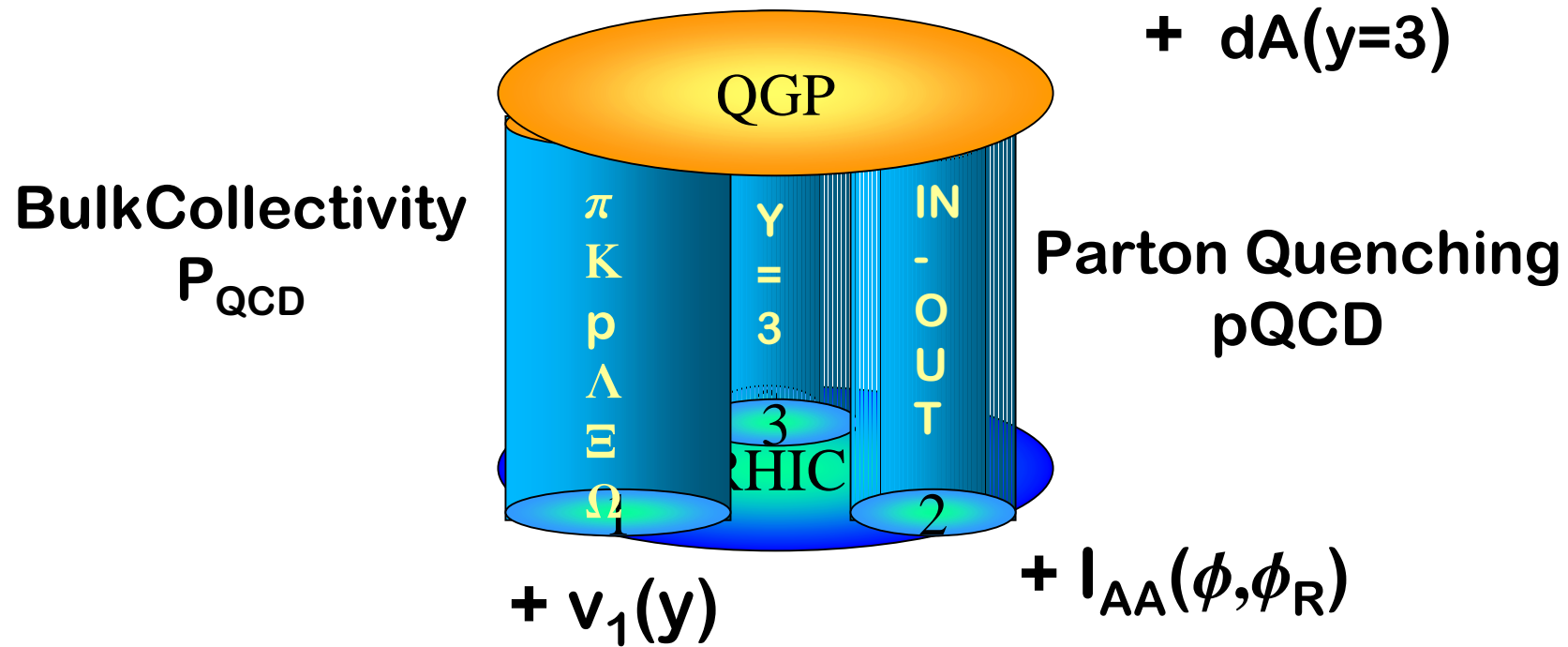
$$R_{AuAu} \ll R_{DAu} \sim 1$$

Consistent with QGP in AuAu



# Converging Evidence to QGP at RHIC

## Null Control D+Au



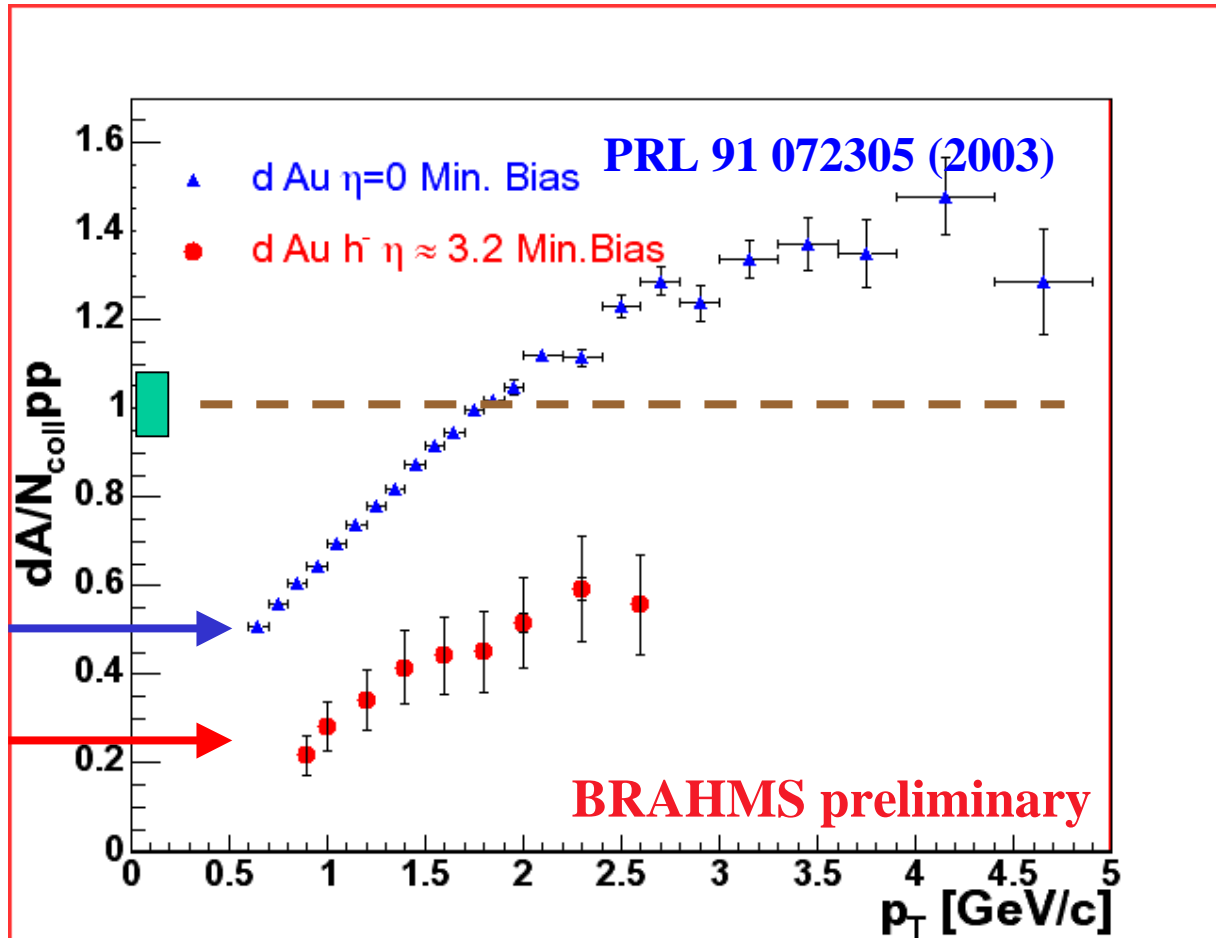
$$\text{QGP} = P_{\text{QCD}} + p\text{QCD} + dA = v_2 + (R+I)_{AA} + (R+I)_{dA} + v_1 + I_{AA}(\phi, \phi_R) + dA(y=3)$$



**The preliminary D+AU data at  $y=3$**

**Is this the CGC or Limiting Quark Fragmentation?**

# BRAHMS: d-Au Nuclear Modification factor at $\eta \sim 3.2$



RdAu compares the yield of **negative particles** produced in dAu to the scaled number of particles with same sign in p-p

The scale is the number of binary collisions:

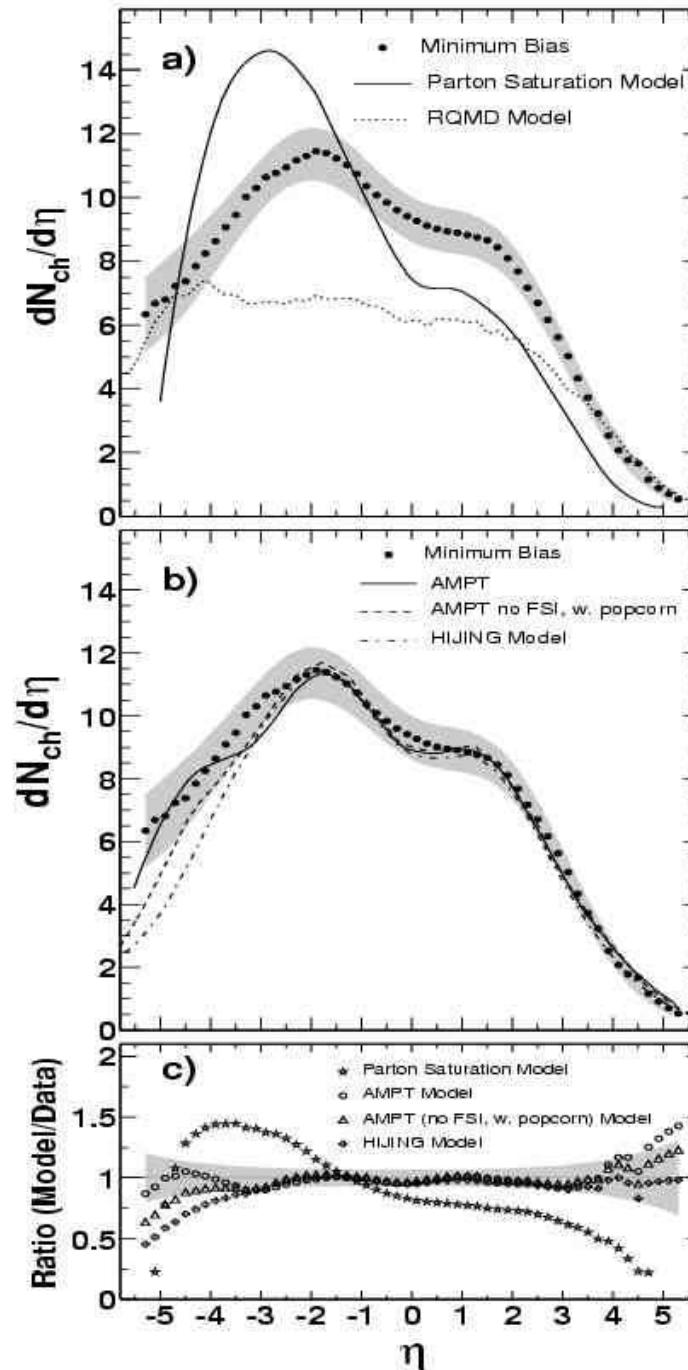
$$N_{coll}=7.2$$

(minimum biased)

# PHOBOS Global View $dN/d\eta$ in D+Au

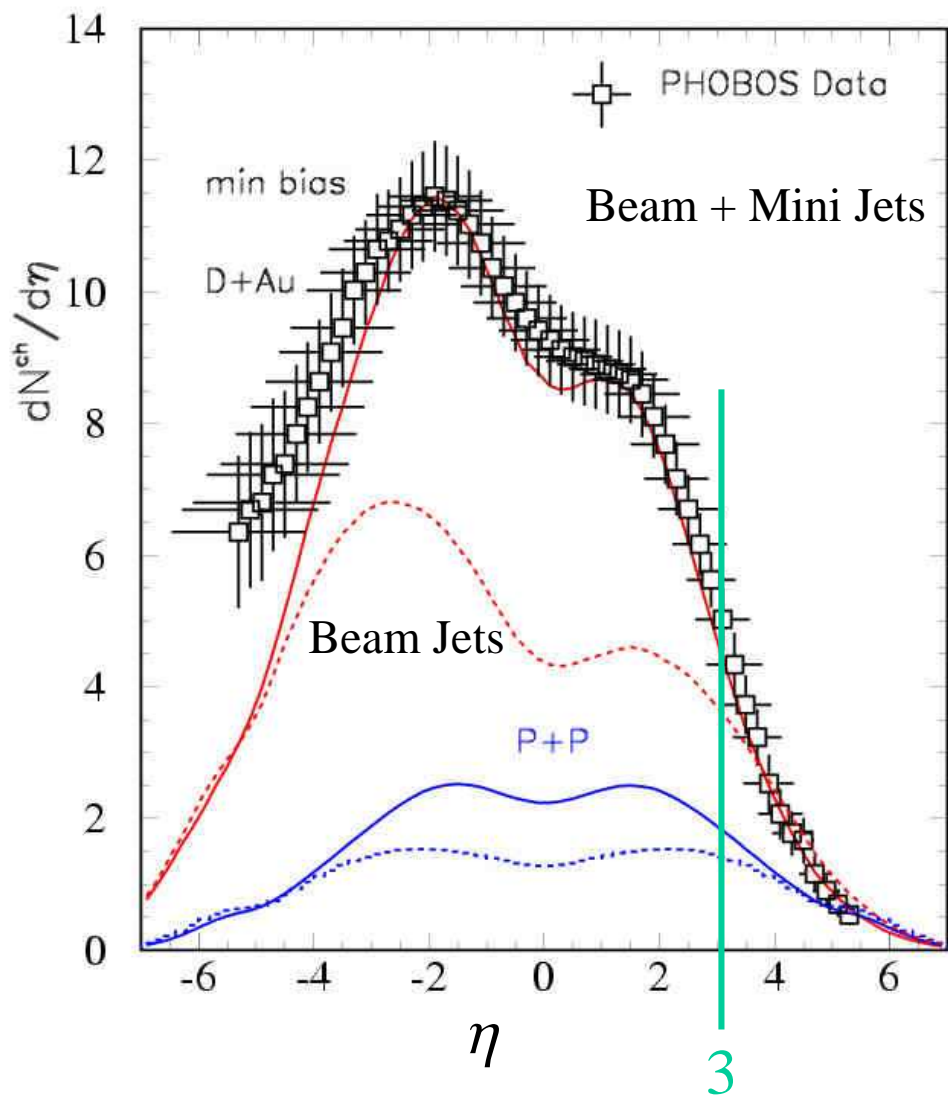
nucl-ex/0311009

HIJING, AMPT  
Predictions  
account for D+Au



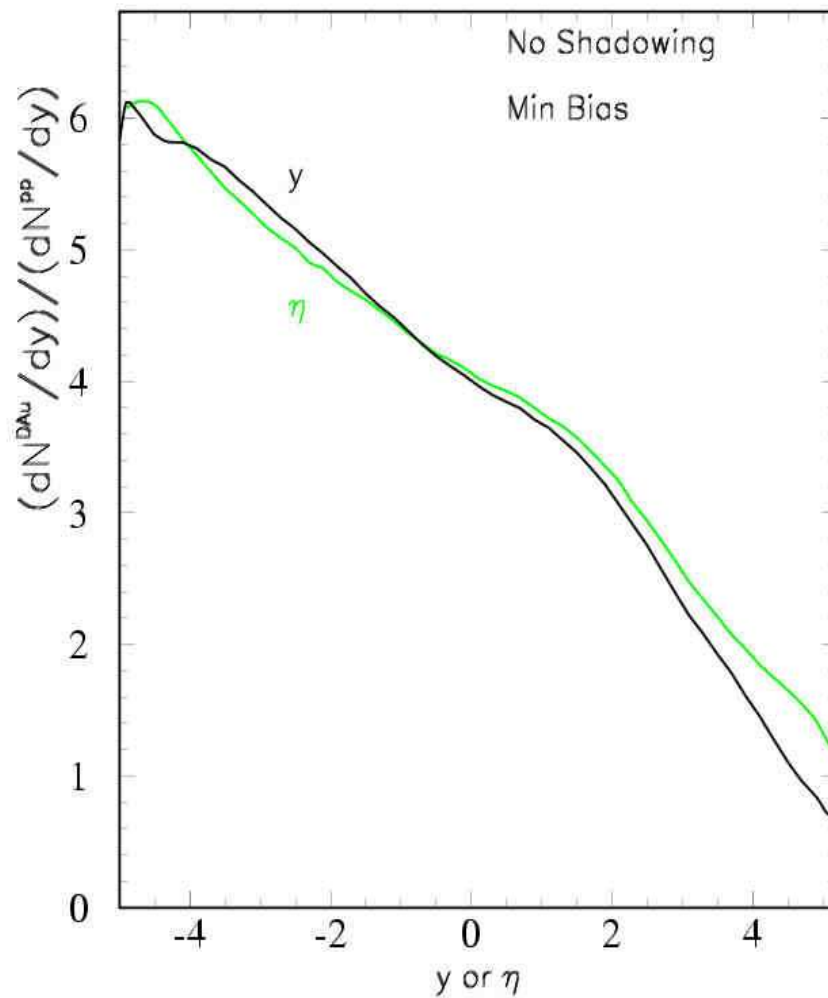
# Beam Fragmentation Dominates $y > 3$

200 AGeV m.b. D+Au, pp  $\rightarrow$   $h^{ch}$  HIJING1.383 ys



# The D+Au Triangle in HIJING

200 AGeV m.b. D+Au/pp  $\rightarrow$   $h^{+/-}$  HIJING1.383



Brodsky, Gunion, Kuhn, PRL39(77)1120

## Color Neutralization (Multi-Soft) Model

DPM: Capella et al

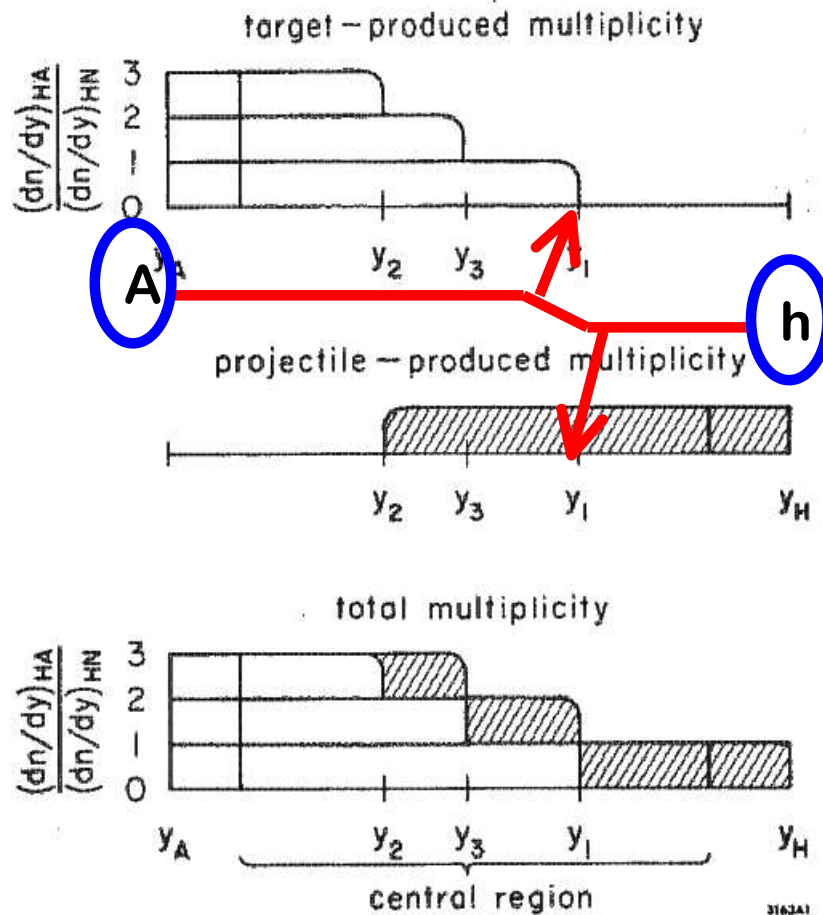
LUND: Anderson et al

HIJING: Wang, MG

Triangle Distribution  
Consequence of

1) Conservation of  
Valence quarks, i.e. B

2)  $\sim 1/x$  Feynman Wee

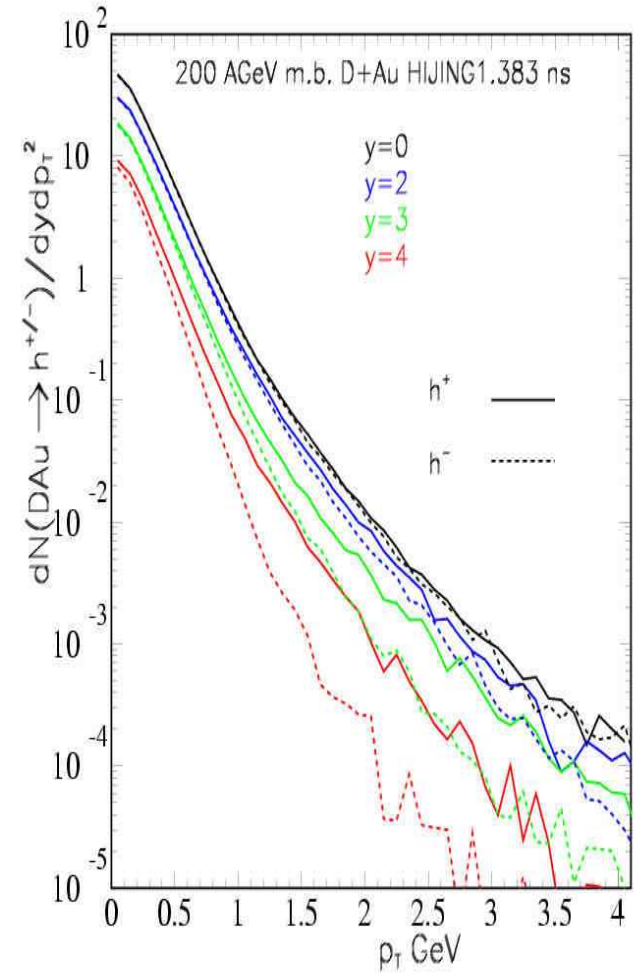
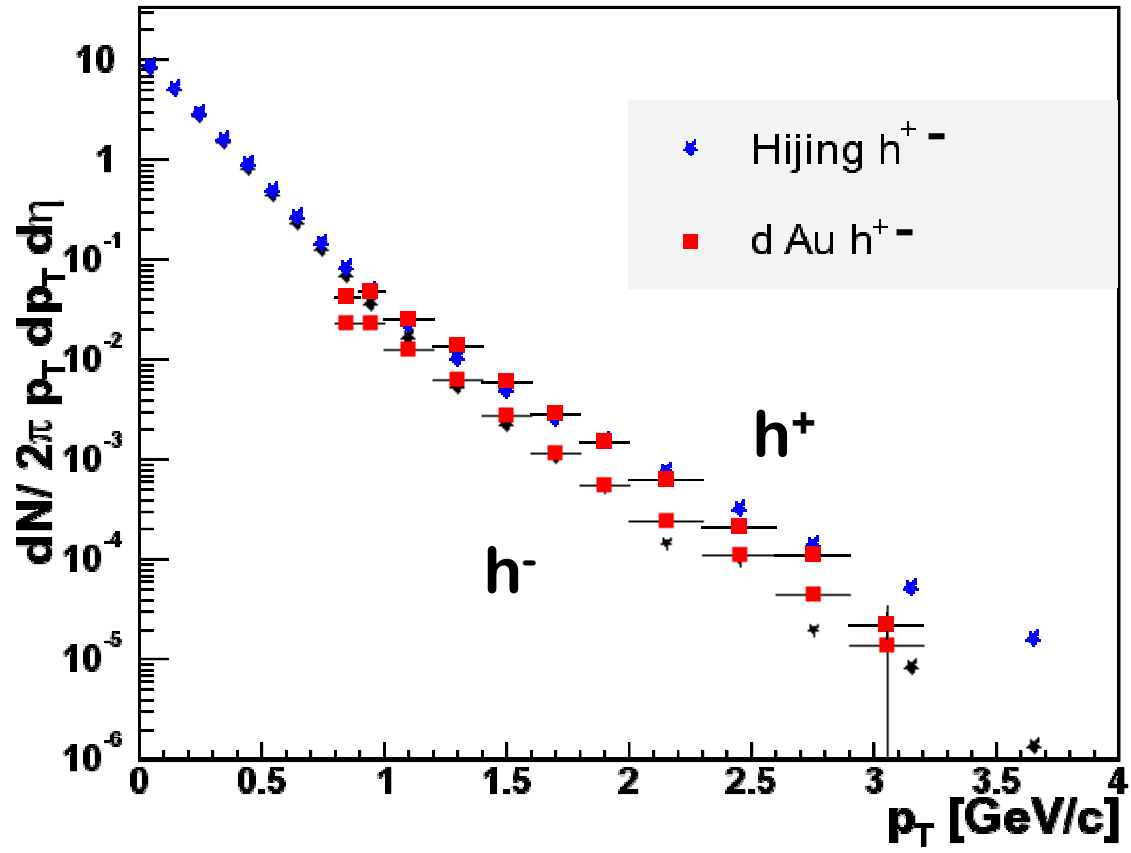


Predicted Triangle pA distribution

*Preliminary* BRAHMS  $\eta=3$

**$h^+ > h^-$  Clear evidence of Valence quark fragment**

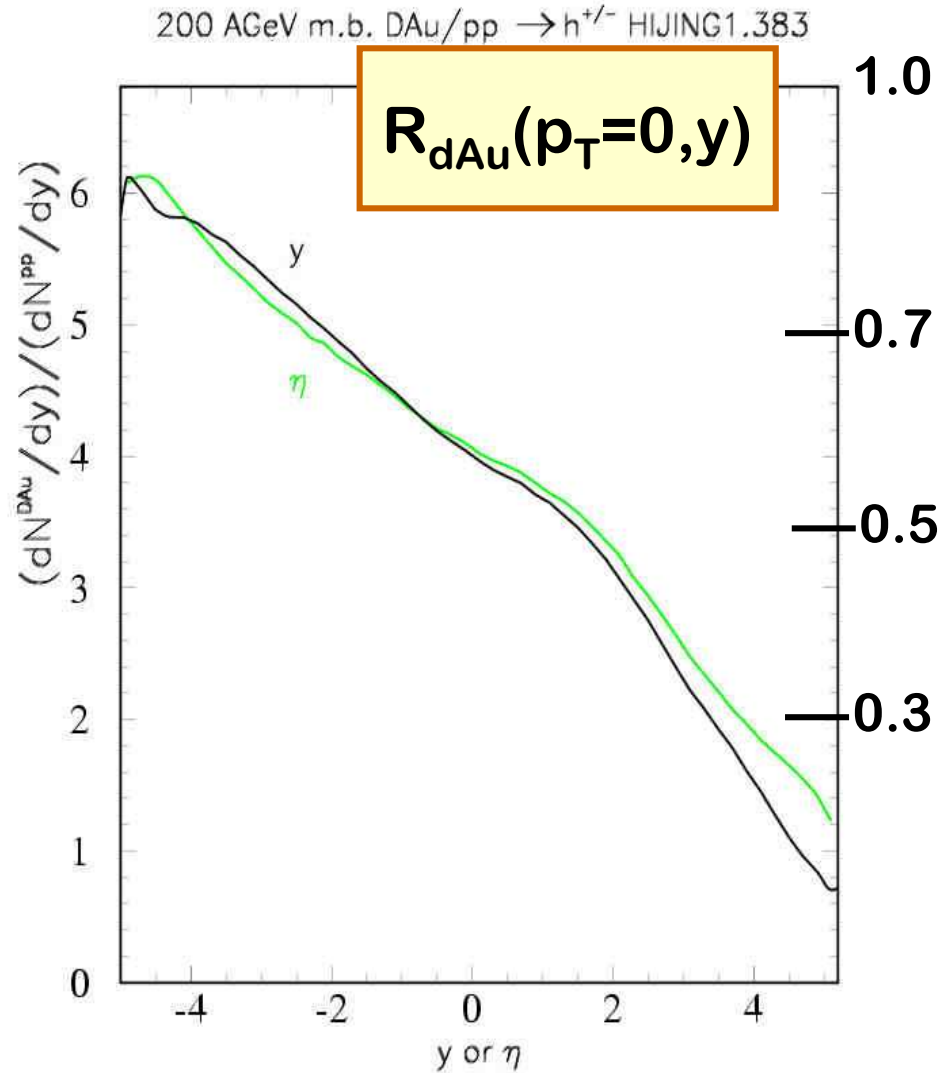
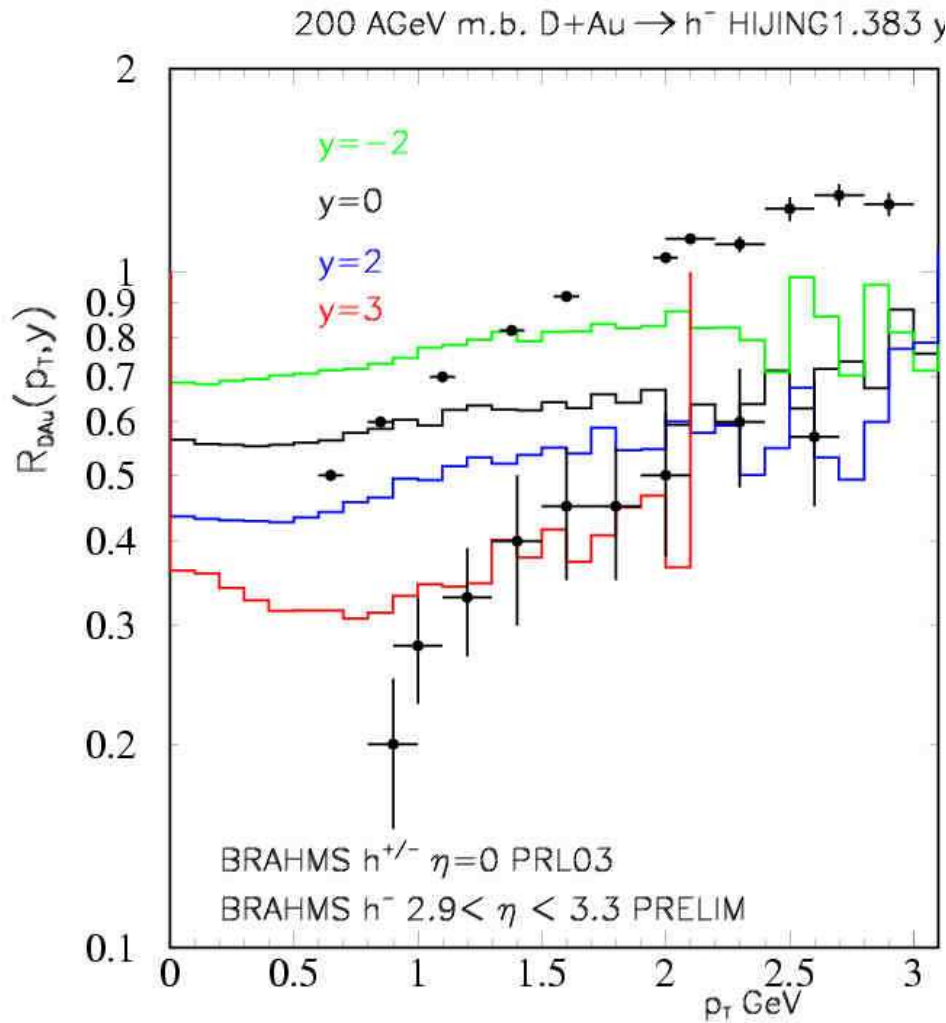
d Au positives at 4 degrees rees



Debbe et al, DNP 10/31/2003

Low  $p_T < 0.5$  *Triangle* boundary controls  
 forward  $R_{dA}(y_d) \sim 1/N_{\text{coll}}$  !!

The D+Au triangle



THE SMALL X COLLABORATION @ LUND

Bo Andersson<sup>1</sup>, Sergei Baranov<sup>2</sup>, Jochen Bartels<sup>3</sup>,  
 Marcello Ciafaloni<sup>4</sup>, John Collins<sup>5</sup>, Mattias Davidsson<sup>6</sup>,  
 Gösta Gustafson<sup>1</sup>, Hannes Jung<sup>6</sup>, Leif Jönsson<sup>6</sup>, Martin Karlsson<sup>6</sup>,  
 Martin Kimber<sup>7</sup>, Anatoly Kotikov<sup>8</sup>, Jan Kwiecinski<sup>9</sup>,  
 Leif Lönnblad<sup>1</sup>, Gabriela Miu<sup>1</sup>, Gavin Salam<sup>10</sup>, Mike H. Seymour<sup>11</sup>,  
 Torbjörn Sjöstrand<sup>1</sup>, Nikolai Zotov<sup>12</sup>

DGLAP, BFKL, CCFM



CASCADE, LDCMC, ARIADNE



PYTHIA  
HIJING

2  $k_t$ -factorization versus higher order processes in collinear factorization

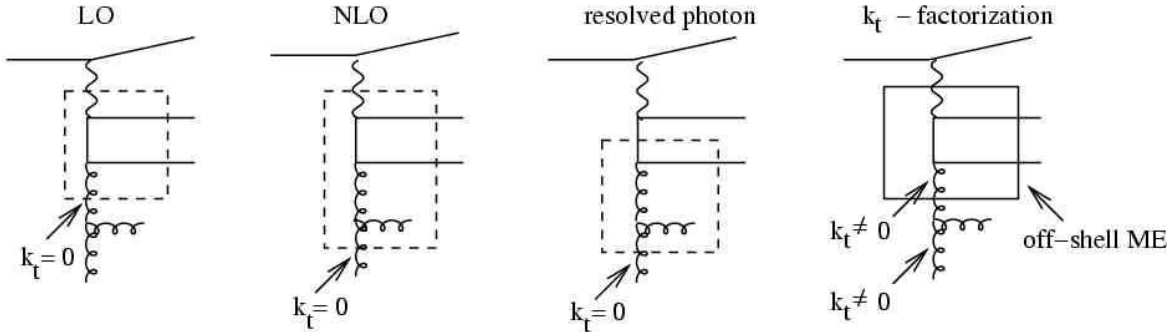


Figure 1. Diagrammatic representation of LO, NLO and resolved photon processes in the collinear approach compared to the  $k_t$ -factorization approach.

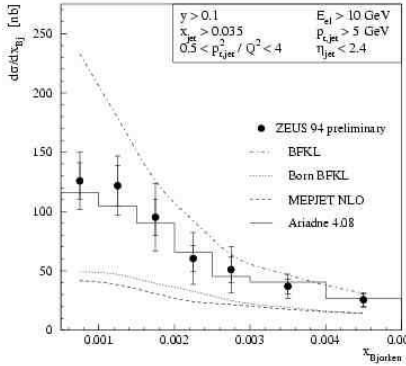


FIGURE 2. Forward jet cross section vs.  $x_{Bj}$ ; a qualitative comparison between ZEUS data, QCD calculations and Ariadne Monte Carlo. Inner error bars are statistical errors only, the outer are the quadratic sum of statistical and systematic errors.



# Four independent calibrations of Initial QGP density

$$\epsilon(\tau_0) \approx 100 \epsilon_0 = 15 \text{ GeV} / \text{fm}^3$$

## 1. Bjorken Backward extrapolation

$$\begin{aligned} E_T / N_\pi &= 0.5 \text{ GeV}, \quad dN_\pi / dy = 1000, \\ \tau_0 &= 1/p_0 = 0.2 \text{ fm}/c, \quad V = (0.2 \text{ fm})\pi R^2 = 30 \text{ fm}^3 \\ \epsilon_{\text{Bj}} &= 500 \text{ GeV} / 30 \text{ fm}^3 = 100 \epsilon_0 \end{aligned}$$

## 2. Hydrodynamic initial condition needed for $v_2(p_T)$

$$\epsilon_{\text{Hydro}} > 2 \epsilon_{\text{Bj}} = 500 \text{ GeV} / 30 \text{ fm}^3 = 100 \epsilon_0$$

KHH  
TS  
HN

## 3. Jet Tomography: $dN_g/dy = 1000$

$$\epsilon_{\text{Jets}} \approx \epsilon_{\text{Bj}} \approx 100 \epsilon_0$$

GLV  
WW

## 4. Gluon saturation $p_T < Q_s$ predicted

$$dN_g/dy = 1000 \text{ at } Q_{\text{sat}} = 1 \text{ GeV at } y=0$$

MB  
McV  
EKRT

**The END of searching for the QGP**

**The BEGINNING of measuring its properties**

- 12D Correlations
- Heavy Quarks
- Direct Photons
- Leptons

## Experimental To Do List

- $Y = \pm 4$  dAu pt to kinematic bounds
- $C_2(\phi_1, \phi_2, p_{t1}, p_{t2}, \eta_1, \eta_2, f_{l1}, f_{l2}, \text{Mult}, A, B, E_{cm})$
- Heavy Quark tomography
- Open Charm (enhancement?); J/Psi (suppression?)
  - Charm Flow?
- Need Direct Photons thermometer
  - and tagged direct photon -quark jets!
- Excitation function  $E_{cm} \sim 50-100$ ,  $A = 20-100$

## Theory To Do List

- HBT source  $E_{cm}$  invariance?  
why No time-delay? Is Lin-Ko the answer?
- $E_T/N$   $E_{cm}$  invariance,  $N_{part}$  invariance?
- $V_2(p_T > 2, m)$  source of Flat High  $p_T$  saturation
- $V_2(y)$  *NON* Bjorken boost invariant 3+1 D
- Baryon transport dynamics
- Thermalization, QGP Transport theory