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SURVEY OF ELECTRICAL RESISTIVITY MEASUREMENTS ON 16 PURE METALS IN THE TEMPERATURE RANGE O TO 273°K

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Experimental electrical resistivity data for 16 pure metals have been compiled, tabulated, and graphically illustrated for a temperature range of 0 to 273°K. A section has been prepared for each particular metal which includes references, brief comments concerned with preparation of sample, purity, and any other pertinent information, tabulated data, and graph.

Key words: electrical resistivity, compilation, low temperature, aluminum, beryllium, cobalt, copper, gold, indium, iron, lead, magnesium, molybdenum, nickel, niobium, platinum, silver, tantalum, tin.

1. INTRODUCTION

Many articles describing experimental measurements of electrical resistivity are found in the open literature. Many present results of straight-forward temperature-dependent resistivity measurements on wires or rods of high-purity metals. Some deal with the effects of irradiation, plastic deformation, magnetic fields, and alloying on resistivity, while others show the variation in resistivity due to unusual shape of the sample, e.g., whiskers or thin films. In the recent literature, superconductivity has also been studied extensively. Because the amount of literature in this field is so large, we have restricted this survey to the temperature-dependent resistivity measurements on very pure metals, with the exception of the pressure-dependent measurements by Bridgman.

All of the data from this one area of resistivity measurements have been organized into a relatively concise and useful form. For the experimentalist, we have tried to present a complete picture of what data are already available so that he may plan his work in such a manner as to fill in "gaps" in existing data or to check or "reinforce" existing measurements. For the engineer, we have presented a method of predicting the electrical

^{*} This study was supported in part by the National Aeronautics and Space Administration, Office of Advanced Research and Technology, Contract R-06-006-046.

behavior of a metallic specimen of known purity. When the purity is not known, the resistivity of the metal may be predicted by measuring its residual resistivity, which can be measured at 4.2°K, and applying Matthiessen's rule, as will be explained below. With these objectives in mind, we have reviewed carefully all of the pertinent articles and noted in a "comments" section the purity of the metals studied, their residual resistivity value, any mechanical treatment of the sample and its final form during measurements, and any other facts which might help explain the character of the experimental data.

An earlier compilation^{*} presented experimental resistivity data for 53 metallic elements. From the time of that publication to the present, the Compilation Unit of the Cryogenic Data Center has been actively acquiring electrical resistivity articles. These articles were entered into our Storage and Retrieval System together with all the other cryogenically oriented documents that have come to our attention by a systematic scanning of the primary journals, and secondary publications such as Chemical Abstracts, Physics Abstracts, NASA STAR, Nuclear Science Abstracts, DDC TAB, and International Aerospace Abstracts. A computer search of this Storage and Retrieval System was the basis for this compilation. All pertinent articles from the references listed in this search were obtained and reviewed.

2. GENERAL DISCUSSION OF RESISTIVITY**

The measured resistivity $\rho_{\rm T}$ is a function of temperature, but on approaching absolute zero it approaches a constant residual resistivity ρ_0 . The quantity ρ_0 arises from the presence of impurities, defects, and strains in the metal lattice. However, in pure annealed metals it is only a small fraction of the total resistivity at room temperature. Subtraction of ρ_0 from the measured resistivity gives a value of the resistivity appropriate for a perfectly pure, strain-free specimen. The temperature-

 [&]quot;A Compendium of the Properties of Materials at Low Temperatures (Phase II)", R. B. Stewart and V. J. Johnson, editors, Natl. Bur. Standards, Cryogenic Eng. Lab., WADD Tech. Rept. 60-56, Part IV (1961) DDC AD 272 769.

^{**} A more complete discussion of electrical resistivity can be found in <u>Electrical Resistance of Metals</u> by G. T. Meaden, Plenum Press, New York, 1965.

dependent resistivity thus obtained is called the <u>ideal</u> or <u>intrinsic</u> resistivity ρ_1 . It is caused by the interaction of the conduction electrons with the thermally induced vibrations of the lattice ions, and, if present, with the magnetic structure of the lattice. The separation of the total resistivity ρ_T into temperature dependent (ρ_1) and temperature-independent (ρ_0) contributions in this way is known as Matthiessen's rule, which may be written

$$\rho = \rho_0 + \rho_i$$

This rule is a good approximation for all engineering purposes.

The ideal resistivity due to lattice vibrations may be expressed by the Grüneisen-Bloch relation

$$\rho_{I} = \frac{C}{M\theta_{R}} \left(\frac{T}{\theta_{R}}\right)^{5} \int_{0}^{\theta_{R}/T} \frac{z^{5}dz}{(e^{z}-1)(1-e^{-z})}$$

where M is the atomic weight, C is a constant, and T is in °K. θ_R is an empirical temperature characterizing the metal's lattice resistivity in the same way the Debye temperature θ_D characterizes a solid's lattice specific heat. It is often true that $\theta_R \approx \theta_D$, typically about 300°K for most metals. Below about 0.1 θ_R this relation reduces to $\rho_1 \propto T^5$. It is found that a few of the metals follow the T^5 relation closely. The exponent of T for most nonmagnetic metals generally lies between 4.5 and 5.

A metal with a cubic crystal structure has the same resistivity whether in polycrystalline or single crystal form, apart from a small extra contribution in a polycrystal that may sometimes be caused by grain boundaries since the cubic structure is isotropic. But in a single crystal of a noncubic metal, the resistivity is often very <u>anisotropic</u>, its value depending on the direction of the flow of current. Likewise, polycrystalline specimens of such metals, if preferentially oriented, as by rolling or drawing, for instance, will have direction-dependent resistive properties.

In anisotropic metals, the electrical resistivity parallel to the principle crystalline axis is designated ρ_{II} and electrical resistivity perpendicular to the principle axis is designated ρ_{I} . When values for ρ_{II} and ρ_{I} have been determined for single crystals, one may calculate a value of $\bar{\rho}$ for a polycrystalline sample using the equation of Voigt*

$$\bar{\rho} = \frac{3\rho_{\perp} - \rho_{\parallel}}{2\rho_{\parallel} + \rho_{\perp}}$$

Superconductivity is observed in at least 30 elements. At temperatures less than their "superconducting transition temperatures, these elements lose all resistance to electric current. Articles dealing with superconductivity were not reviewed here and only the transition temperatures are noted for each metal. The curves on our graphs should not be extrapolated below this transition temperature. Some data for lead, however, do appear in the superconducting region. These measurements were made in the presence of a magnetic field, large enough to surpress the superconductivity.

* Voigt, W., Lehrbuch der Kristallphysik (Teubner, Leipzig, 1928), p. 959.

3. PRESENTATION OF DATA

A separate section has been devoted to each metal. These sections have been prepared in the format of our regular preliminary compilations and have been numbered consecutively with other worksheets dealing with other properties of materials at cryogenic temperatures. With the collection in this format, the user may easily remove any memorandum on a particular metal that he is studying from the group. The sections contain the following:

- a) Sources of data references for the articles from which we have taken the data.
- b) Additional references other articles dealing with electrical resistivity of the metal which may be of interest to the reader.
- c) Comments a concise discussion of any factors influencing the character of the experimenter's resistivity data, such as purity, heat treatment, shape of sample, crystal structure, etc.
- d) Tables tabulated experimental data. When the experimenters presented their results graphically, an attempt was made to read values from the graphs and put them into tabular form.
- e) Graph the data have been plotted as ratios $\rho_{\rm T}/\rho_{273}$, that is, the resistivity at a given temperature divided by the resistivity at 273.15°K. Many of the investigators have not given their ρ_{273} value, and in these instances we have used a value which we believed to be the most accurate value of ρ_{273} in calculating $\rho_{\rm T}/\rho_{273}$. Table 1 shows ρ_{273} values given by the investigators and the value chosen as the most accurate. The data are plotted on logarithmic coordinates which tend to emphasize the differences in the values reported by the several experimenters at the lower temperatures.

In Table 1 on pages 8 - 11, all experimental values of ρ_{273} have been tabulated for the 16 metals. The "selected" value is in most instances the lowest available value of ρ_{273} for that particular metal.

4. HOW TO USE THE DATA

As has been stated before, this is an attempt to gather all experimental data from temperature-dependent electrical resistivity measurements into a relatively concise form. The graph presents at a glance the amount of work done on a particular metal; however, for some of the more popular metals not all the tabular data are plotted because their curves would be superimposed on others. The annotated bibliography gives an insight into the character of the data.

An engineer, wishing to predict the resistivity of a particular metal, could:

- 1. review the comments section to find out if measurements have been made on a sample similar to his. If he succeeds in finding such measurements he can then refer to the tabular data and expect his metal to perform similarly.
- 2. apply Matthiessen's rule, $\rho_{T} = \rho_0 + \rho_1$. The residual resistivity, ρ_0 , could be found by measuring the resistivity at 4.2°K of the particular metal being used. The ideal resistivity, ρ_1 , would be estimated from the graph by drawing a straight line downward from the portion of the lowest curve where $\rho \propto T^5$ (shown in figure 1).



Figure 1. Relationship between ideal resistivity, ρ_i , residual resistivity, ρ_0 , and measured resistivity at a given temperature, ρ_m .

It is also possible to estimate the purity of a metal by measuring its residual resistivity at 4.2° K, finding its position on the graph, and referring to the comments section to find statements of purity for curves in the same region of the graph.

Table 1 starts on the following page.

	a p ₂₇₃ value	reported resistivity only	De Sorbo(1958) Powell et al. (1950) Ottensmeyer et al.(1954)				Radhakrishna & Nielsen(1965)	Berman & MacDonald(1952)
3 °K.	articles which did not report	reported R/Rera	Holborn(1919) Justi & Scheffers(1938) Thomas & Mendoza(1952) Caron(1953) Maimoni(1953)			Mac Donald & Mendelssohn (1950)	Schimank(1914) Semenenko et al.(1963)	Holborn(1919) Henning(1921) Meissner & Voigt(1930) de Haas et al. $(1)34$) Sekula (1959) Gniewek & Clark (1965)
mental Resistivity Values at 27	other values of resistivity at 273°K	πο πάν ^θ Οί χ q	2.50 Grüneisen & Goens(1927) 2.6 Meissner & Voigt(1930) 2.53 Aleksandrov & D'Yakov(1962) 2.46 Pawlck & Regalla(1956)		3.58 Grüneisen & Adenstedt (1938)	17.0 McJennan & Niven (1927) 5.88 Lewis (1929) 7.9 Meissner & Voigt (1930) 3.5 Denton(1947) 4.6 山、3 Mnite & Woods(1955)	5.94 Meissner & Voigt(1930) 5.57 Bridgman (1940)	1.55 Meissner(1915) 1.59 Broom(1952) 1.55 White & Woods(1959) 1.58 Domenicali & Christenson(1961) 1.58 Pawlek & Regalla(1960) 1.546 Moore et al. (1967)
Experi	ions ŧ °K	mə mdo ^{. Ə} ƏL x a GƏZLARAR Məsəfiriyə	5. 2	3.12	3.58	2.78	5.2	1.55 .
rable 1.	compilat e at 273	ns mío ⁸ 01 x q ms mío ⁸ 01 x q	0 <u>6</u> -2	3.12	3.58	5.25	5.2	1.55
	other valu	b ^ı к ТО _в орш сш Мевдел(ТЭСЕ)	5.50 5	3.12	3.58	t, ::	5.15	1.55
	our "selected" value at 273°K	ს x JC _e opum cm	∠.44 Broom(1952)	3.1~ Grüneisen & Erflinr(1940)	3.56 Erfling & Grüneisen(1942)	2.7 Powell(1953) extrapolated extrapolated value 2.74 Reich et al. (1963)	5.24 White & Woods (1959)	1.545 Powell et al. (1959)
	metal		ատուրտուհ	T _d	unț[0 ^{Poly}	сора⊥т	reqqoD

	907) Burgers(1918) gt(1930) den Berg(1936) 1(1940) : Franklin (1958)	1923,1924) Protopopescu [gt(1930) et al.(1962 [562] 1963)			dovtsov(1962) al.(1962)	1907) 1926) anz(1930) 1.2t(1930) 1.1940)
	Onnes & Clay(1 Cath, Onnes & Holborn(1919) Meissner(1925) Meissner & Voi de Haas & Van Van der Leeder Justi(1940) Van den Berg 8	Tuyn & Onnes(1 Meissner & Voi Swenson(1955) Aleksandrov(19 Orlova et al.(Holborn(1919) Semenenko & Su Semenenko et	Onnes & Clay() Holborn(1919) Onnes & Tuyn() Meissner & Fre Meissner & Vuj Meissner(1932) Van der Leeder
	2.06 Meissner(1915) 2.09 Domenicali & Christenson(1961)	<pre>8.19 Meissner et al.(1932) 8.17 Olsen(1958) interpo- lated value 8.37 Aleksandrov & D'Yakov(1962) 8.21 Kaznoff et al.(1967)</pre>			8.71 9.11 Grüneisen & Goens 9.95 Grüneisen & Goens 9.57 Kannuluik(1931) 9.66 Broom(1952) 9.28 Kemp et al.(1956) 9.27 Kemp et al.(1959) 1nterpolated value 8.80 White & Woods(1959) 8.94 Soffer et al.(1965) interpolated value	19.26 Meissner(1915) 19.3 Grüneisen(1945) 19.9 Buckel & Hilsch(1954)
_	2.0t	8.			8.71	19.3
	2 · 0†	8 9			8	19.3
	2.01	8.0	6.7	8.3	8.7.	т. 6-
	2.02 White & Woods (1959)	3.00 Powell et al. (1962)			8.7 Backlund(1961)	19.2 Aleksandrov & D'Yakov(1962)
	Cold	nwit vioq ^q	"d oul	™ d	norI	Геяд

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	rt a p ₂₇₃ value	reported resistivity only			Rosenberg(1954) Spohr & Webber (1957) Hein & Falge (1957)		Kondorsky et al. (1958) Greig & Harrison(1965)	
ı't).	articles which did not repo	reported R/R ₂₇₃	Goens & Schmid(1936)	Goens & Schmid(1936)	Dewar & Fleming(1893) Yntema(1953)	Holborn(1919) McLennan et al.(1929)	Dewar & Fleming(1900, 1904) Sudovtsov & Semenenko(1957)	Meissner et al.(1933)
Resistivity Values at 273°K (con	other values of resistivity at 273°K	wo wuqo _g ot x d			5.0 Meissner & Volgt(1930)	4.4 Blom(1919) 5.22 Meissner & Voigt(1930) 5.17 5.25 White & Wocds(1959)	7.07 Meissner & Veigt(1930) 7.37 Broom(1952) 6.2 Kemp et al.(1956) interpolated value	lé.l. Reimann & Grant(1936) 13.96 White & Woods(1957)
1mental	tions‡ 3°K	derritsen(1956) (д∂гх а ^{дб} ойт ар	3.50	4.22	3.94	5.03	6.58	یع ع
. Exper	compila ie at 27;	Gruneisen(l945) Gruneisen(l945)	3.48	4.18	3.94	5.0	6.58	
Table 1	other valı	b ^ı x I ^{O6} олт ст Меадел(1965)	3.47	4.17	3.94	4.84	ć.20	13.5
	our "selected" value at 273°K	шә шцо ₉ 0т х d	3.48 Grüneisen(1945)	4.18 Grüneisen(1945)	3.94 Gruneisen(1945)	5.00 Holmwood & Glang(1965)	6.23 White & Woods (1959)	13.96 White & Woods (1959)
	metal		" J um	¶ T≳∋	MagM Y Loq ^Q	Molybdenum	ТэйотИ	muidoiN

 Powell et al. (1907)					
Cath et al. (1917) Holborn(1919) Onnes & Tuyn(1926) Onnes & Tuyn(1926) Van der Horst et al. (1929) Henning(1926) Meissner & Grassmann(1933) de Haas & de Boer(1933-1934) Hoge & Brickwedde(1939) Van der Leeden(1940)	Onnes & Clay(1903) Holborn(1919) de Haas & Van den Berg(1935) Van der Leeden(1940)	Holborn(1919) McLennan et al.(1929)	Onnes & Tuyn(1923) Meissner(1925) Van der Leeden(1940)		18 P
9.81 Meissner(1915) 9.53*Meissner & Volgt(1930) 9.81 White & Woods(1957)	1.48 Meissner & Voigt(1930) 1.51 Kannuluik(1931) 1.48 Gerritsen & Linde (1950) 1.50 Pawlek & Rogalla(1966)	15.2 Meissner & Voigt(1930) 12.4 Burgers & Basart(1934) 12.41 Cox (1943)	<pre>ll.l5 Jaeger & Diesselhorst</pre>	L3.06 Bridgman(1933) 9.09 Bridgman(1933)	ed value. Plenum Press, New York (1965) 2 5 (1945). 20 (1950).
 9.81	1.50	12.4	10.1	60.6	e accepte <u>Metals</u> , 1 2, 137-22
 т.	1.50	12.4	10.1	9.05 9.05	than the ance of 1 turw. <u>1</u> 9
\$ \$ \$	√t.L	12.1	10.1	۰. بو م. بو	lt lower L Resist. Xakt. NE ch der P
9.50 White & Woods (1959)	1.48 White & Woods (1959)	12.3 White & Woods (1959)	10.05 Aleksandrov & D'Yakov(1963)	13.00 Aleksandrov & D'Yakov(19ó3) 9.01 Aleksandrov & D'Yakov(19ó3)	This value is quite a b: at 303°K. G. T. Meaden, <u>Electrica</u> E. Grünelsen, E <i>rf</i> ebn. ^e A. N. Gerritsen, <u>Handbu</u>
munttalq	Silver	mulstreT	rioq ^q I	I _d Т _d ГЛ	* + +

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5. ELECTRICAL RESISTIVITY DATA SHEETS

aluminum .	•	(Data	Memorandum	No.	м-9).	•	•	•	•	•	•	•	•	•	•	٠	13
beryllium	•	(Data	Memorandum	No.	M- 25)	•	•	•	•	•	•	•	•	•	•	•	21
cobalt	•	(Data	Memorandum	No.	M-10)	•	•	•	•	•	•	•	•	•	•	٠	29
copper	•	(Data	Memorandum	No.	M-ll)	•	•	•	•	•	•	•	•	•	•	•	33
gold	•	(Data	Memorandum	No.	M-1 3)	•	•	•	•	•	•	•	•	•	•	•	41
indium	•	(Data	Memorandum	No.	M-14)	•	•	•	•	•	•	•	•	•	•	•	47
iron	•	(Data	Memorandum	No.	M-1 5)	•	•	•	•	•	•	•	•	•	•	•	5 5
lead	•	(Data	Memorandum	No.	M-16)	•	•	•	•	•	•	•	•	•	•	•	63
magnesium	•	(Data	Memorandum	No.	M-17)	•	•	•	•	•	•	•	•	•	•	•	69
molybdenum	•	(Data	Memorandum	No.	M-18)	•	•	•	•	•	•	•	•	•	•	•	75
nickel	•	(Data	Memorandum	No.	M-1 9)	•	•	•	•	•	•	•	•	•	•	•	79
niobium .	•	(Data	Memorandum	No.	M- 20)	•	•	•	•	•	•	•	•	•	•	•	85
platinum .	•	(Data	Memorandum	No.	M-21)	•	•	•	•	•	•	•	•	•	•	•	89
silver	•	(Data	Memorandum	No.	M-22)	•	•	•	•	•	•	•	•	•	•	•	97
tantalum .	•	(Data	Memorandum	No.	M- 23)	•	•	•	•	٠	•	•	•	•	•	•	103
tin	•	(Data	Memorandum	No.	M- 24)	•	•	•	•	•	•	•	•	•	•	•	107

CRYOGENIC DATA MEMORANDUM

PROJECT NO. 3150123

ELECTRICAL RESISTIVITY OF ALUMINUM, AL (Atomic Number 13)

Sources of Data:

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Comments:

The data for this graph were taken from the references cited above under "Sources of Data" and are listed as ratios of electrical resistivity with respect to a datum temperature of 193°K. When the actual values of o_{273} are not available for the samples used by the investigators, a datum value reported by Broom (1952) ($o_{272} = 2.44 \times 10^{-6}$ ohm cm) is suggested for calculating values of electrical resistivity from the ratios. These curves should not be extrapolated to lower temperatures since aluminum becomes superconducting at 1.1/5°K.

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The values listed in the Landolt-Börnstein tables are those reported by Grüneisen and Goens; Holborn (1919); Justi and Scheffers; and Meissner and Voigt; and Thomas and Mendoza, while those values listed by the International Critical Tables are from Holborn (1902, 1919). These primary sources are listed above under "Other References". The original authors are used in labeling the curves on the graph.

The samples used by Holborn are reported in Landolt-Börnstein as polycrystalline with 0.47 impurities of unknown composition. The Holborn sample was annealed at 250°C. The value of $\rho_{0.70}$ to be used with Holborn data in calculating values of electrical resistivity is $\rho_{270} = 2.53 \times 10^{-6}$ chm cm. Grüneisen and Goens are reported to have used a polycrystalline sample with a small amount of impurities present. Their ρ_{273} value was 2.50 x 10⁻⁶ chm cm. The sample used by Meissner and Voigt is reported as a polycrystalline sample with undetermined impurities, which had been annealed at 300°C for 2.5 hours.

A single crystal with a small amount of impurities present is reported as the sample used by Justi and Scheffers. The sample used by Thomas and Mendoza was a polycrystalline sample with 0.005%impurities of unknown composition which had been annealed at 300°C for two hours in vacue. No other pertinent information was presented about any of the samples from the above experimenters.

Broom (1952) measured resistivities of wire samples at the annealing temperatures and the effect of deformation on the resistivity at the two higher temperatures, 0 and 100°C. His attempts to measure effects of deformation on resistivity at lower temperatures were unsuccessful because of repeated fractures of the wire between the surface of the refrigerant and the chuck. His aluminum was 99.9955°_{p} pure.

Bridgman (1952) studied pressure effects on electrical resistivity at room temperature. The results are reported as a ratio of the resistivity at the given pressure to the resistivity at one atmosphere here. His sample was annealed in vacuum to 400 °C. The purity of the sample is not given.

The samples used by Caron (1953) were 99.99 and 99.998% pure. He reported his results as the ratio R_{220}/R . As Caron did not give a value of R_{230} , the value of $\rho_{230} = 2.75 \times 10^{-6}$ ohm cm and $\rho_{273} = 2.53 \times 10^{-6}$ ohm cm from Aleksandrov and D'Yakov (1963) were used in determining the ratio R/R_{273} .

The sample of very pure aluminum, annealed at 550° C and then cooled at rates of $\beta = 3^{\circ}$ C/min., was used by De Sorbo (1958) in his initial resistivity measurements. He then studied the effects of rapid quenching on the resistivity of the specimen.

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The 3.66 mm diameter rod used by Powell et al. (1960) was initially 99.995% pure; however, the residual electrical resistivity was not as low as one would expect from a crystal of that purity. This single crystal rod was annealed in vacuum at about 400 °C for two hours.

In Maimoni (1962), data are tabulated for the resistance of eight specimens in the temperature range 2 to 26°K. Data for the specimen exhibiting the largest $R_{0.0}/R_{4.2}$ value (6,630) are given in the table below. This specimen had 1 mm square cross-section, and was machined from an ingot of 99.9999% pure 'zone-refined' aluminum. It was annealed about 100 hours at 400°C, then stored for one week at room temperature before measurements were made. No value is given for the residual resistance. These values do not appear on the Electrical Resistivity of Aluminum graph.

A cylindrical single crystal sample of 99.9998% purity was used by Aleksandrov and D'Yakov (1962) in their measurements in the temperature range 0 to 273 °K. In the lower temperature range (<4.2°K) the error in a single measurement amounted to 6 - 7%. All samples were annealed 1.5 to 2 days in air at 300°C. The residual resistivity was $\rho_0 \simeq 10^{-10}$ ohm cm.

Measurements were made by Ottensmeyer, et al. (1964) on 99.995% pure rods before and after tensile strain. Their graph shows the effect of strain on the resistivity.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

The wire sample used by Pawlek and Rogalla (1966) was 99.99% pure aluminum which had been annealed at 400 °C for one hour.

Stevenson (1967) studied the effects of strain and purity on resistance and magnetoresistance. He used aluminum wire of 59 and 69 purity which had received extensive deformation in the wire drawing process and further deformation when wound on mandrels of 1/2-inch diameter in making the samples for experiment. The mounted samples were annealed at 150°C for 4 hours. The data can be fitted to 35°K, with a maximum deviation of 6% by $p - p_0 = 7.5 \times 10^{-14} \text{ T}^3 + 7.6 \times 10^{-17} \text{ T}^5$ ohm cm. Below 20°K the 69 purity sample showed a T^{2+8} temperature variation, and the 59 sample a T^{3+1} variation. Between 20 and 35°K, they showed T^{4+1} and T^{4+4} variations respectively.

		Holborn (19	02, 1919)		
Temp. °C	100R/R273	Temp. °C	100R/R ₂₇₃	Temp. °C	100R/R ₂₇₃
- 78.3* - 80 -100 -120	64.80* 64.1 55.2 46.4	-140 -160 -180 -191.9* -192.9*	37.7 28.9 20.2 14.85* 14.49*	-200 -220 -240 -253*	12.0 7.1 4.9 4.27*

Tables of Values of Electrical Resistivity

 $\begin{array}{lll} \rho = \mbox{resistivity, (ohm cm);} & \rho_{273} = \mbox{resistivity st } 273\,^{\circ}\mbox{K, (ohm cm),} \\ R = \mbox{resistance, (ohm);} & R_{273} = \mbox{resistance at } 273\,^{\circ}\mbox{K, (ohm).} \end{array}$

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usti and Scheffers (1938)		Meissner and	Voigt (1930)	Thomas and Mendoza (1952)			
Temp. °K	ρ/ρ ₂₇₃	Temp.* °K	R/R ₂₇₃	Temp. °K	R/R ₂₇₃		
14 20	0.0014 0.0018	1.32† 4.21 20.44 77.73 273.16†	0.0067 0.0065 0.0075 0.1008 1.0000	4	0.0026		

(

Broom (1952)								
Temp.	Temp.	Resistivity	ρ/ρ ₂₇₃					
°K	°C	px10 ⁶ ohm cm						
90	-183	0.352	0.144					
194.5	- 78.5	1.55	0.635					
273	0	2.44	1.00					
373	100	3.59	1.47					

(Room Ter	nperature)
Data compared wit one atmosphere	th the resistance at taken as unity.)
Pressure	Resistance Ratio
kg/cm ²	R/R _o
0	1.000
10000	0.959
20000	0.923
30000	0.892
40000	0.865
50000	0.843
60000	0.824
70000	0.808
80000	0.794
90000	0.782
100000	0.770

Bridgman (1952)

	Caron (1953)								
(Using 1962) (Aleks	[Using $\rho_{203} = 2.75 \times 10^{-6}$ ohm cm (Aleksandrov, 1962) and $\rho_{273} = 2.53 \times 10^{-6}$ ohm cm (Aleksandrov & D'Yakov, 1963)								
Temp.	Re	sistance Ratio							
°К	R290/R	R/R ₂₉₀	R/R273						
	Pu	rity - 99.998%							
78 63 20.4 14.0	12.35 26.0 1050 1530	0.08097 0.0385 0.00095 0.00065	0.089 0.042 0.00105 0.00072						

Powel	Powell, Hall, and Roder (1960) (read from graph)								
Temp. °K	Resistivity p x 10 ⁶ ohm cm	р/Р ₂₇₃							
4	0.025	0.010							
6	0.025	0.010							
10	0.0255	0.010							
15	0.026	0.011							
20	0.0285	0.017							
30	0.041	0.019							
40	0.064	0.026							
60	0.135	0.055							
70	0.185	0.076							
75	0.22	0.090							

De	e Sorbo (195	8)			
(read from graph)					
Temp. °K	ρχ10 ⁹ ohm om	P/P273			
2 4 14 16 18 20	2.94 2.95 3.5 3.77 4.06 4.4	0.0012 0.0012 0.0014 0.0015 0.0017 0.0017			

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	Maimoni	(1962)	
Temp. °K	$\frac{R - R^{\circ}}{R_{300} - R^{\circ}} *$	Temp. °K	$\frac{R - R^{\circ}}{R_{300} - R^{\circ}}$
2 3 4 5 6 7 8 9 10	$\begin{array}{c} 1.0 \times 10^{-7} \\ 8.0 \times 10^{-7} \\ 2.7 \times 10^{-6} \\ 6.0 \times 10^{-6} \\ 1.13 \times 10^{-5} \\ 1.70 \times 10^{-5} \\ 2.46 \times 10^{-5} \\ 3.32 \times 10^{-5} \\ 4.33 \times 10^{-5} \end{array}$	11 12 13 14 15 16 17 18 19 20	5.51×10^{-5} 6.84×10^{-5} 8.38×10^{-5} 1.01×10^{-4} 1.19×10^{-4} 1.43×10^{-4} 1.69×10^{-4} 2.01×10^{-4} 2.39×10^{-4} 2.86×10^{-4}
* R ⁰ = plot Alum	residual resista ted on the Electr ninum graph.	nce. Thes ical Resis	e values are not tivity of

	Aleksandrov and D'Yakov (1962)					
Temp. °K	R/R ₂₉₃	R/R ₂₇₃	Temp. °K	R/R283	R/R ₂₇₃	
1.65 3.4 3.7	3.4 x 10 ⁻⁵ 3.4 x 10 ⁻⁵ 3.4 x 10 ⁻⁵	3.7 x 10 ⁻⁵ 3.7 x 10 ⁻⁵ 3.7 x 10 ⁻⁵	58 63.5 77.4	0.032 0.043 0.086	0.035 0.047 0.093	
4.22 14 20.4	3.4 x 10^{-5} 9.6 x 10^{-5} 2.7 x 10^{-4}	3.7×10^{-5} 10.4 x 10^{-5} 2.9 x 10^{-4}	90.31 111.6 273	0.129 0.226 0.92	0.140 0.246 1.0	
* ρ ₂₉₃ ρ ₂₇₃	= 2.75×10^{-6} = 2.53×10^{-6}	ohm cm, from Al ohm cm.	eksandrov	(1962)		

	Ottensmeyer, Bratsberg, Graham, and Hollis Hallet (1964) (read from graph - unstrained specimen)					
Temp. °K	Pide#1 / P70	"ideal resistivity" $\rho_i \times 10^9 \text{ ohm cm}$ (using $\rho_{70} = 10^{-7} \text{ ohm cm}$)	$\rho \times 10^9 \text{ ohm cm}$ $\rho = \rho_1 + \rho_0$ (where $\rho_0 = 10^{-9} \text{ ohm cm}$)	ρ/ρ ₂₇₃		
12	0.00151	0.151	1.15	0.00047		
15	0.00161	0.161	1.16	0.00048		
20	0.011	1.1	2.1	0.00086		
30	0.05	5	6	0.00246		
41	0.18	18	19	0.00779		
50	0.4	40	41	0.01680		
60	0.7	70	71	0.02910		
71	1.0	100	101	0.04139		

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Pawlek and Rogalla (1966)					
Temp. °K	Resistivity ρ x 10 ⁹ ohm cm	p/p ₂₇₃			
4.2 20.4 77 195 273	1.11 2.38 221 1440 2460	0.000451 0.000967 0.0898 0.586 1.000			

Temp.	Resistivity* ρ x 10 ⁸ ohm cm			
°К	99.999%	99 •9999%		
4.2	5.74	2.27		
5.	5.8	2.3		
15.	6.1	2.4		
20.	6.7	3.2		
25.	7.7	4.2		
34.	14.5	9.3		
300.	2512.	2349.		

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ELECTRICAL RESISTIVITY OF BERYLLIUM, Be (Atomic Number 4)

Sources of Data:

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MacDonald, D. K. C., and Mendelssohn, K., "Resistivity of pure metals at low temperatures II. The alkaline earth metals," Proc. Roy. Soc (London) <u>202</u>, 523-32 (1950).

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Meaden, G. T., Electrical Resistance of Metals, Plenum Press, New York (1965) 218 p.

Meissner, W., and Voigt, B., "Messungen mit Hilfe von flüssigem Helium. XI. Widerstand der reinen Metalle in tiefen Temperaturen," (Measurements with the help of liquid helium. XI. Resistivity of pure metals at low temperatures), Ann. Physik 7, 761-97 (1930).

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Reich, R., Kinh, V. Q., and Bonmarin, J., "Etude de la resistivite d'echantillons de beryllium de differentes puretes en fonction de la temperature et determination de la temperature de Debye de ce metal," (Study of the resistivity of samples of beryllium of different purities as a function of temperature and the determination of the Debye temperature of the metal), Compt. Rend. <u>256</u>, No. 26, 5558-61 (1963).

White, G. K. and Woods, S. B., "Thermal and Electrical Conductivities of Solids at Low Temperatures," Can. J. Phys. <u>33</u>, 58-73 (1955).

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Dyakov, I. G., Papirov, I. I., and Tikhinskiy, G. F. "Residual Electrical Resistance of Beryllium" Phys. Metals Metallog. <u>19</u>, No. 5, 135-6 (1966), transl. of Fiz. Metal. i Metalloved. <u>19</u>, No. 5, 788-90 (1965).

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Lewis, E. J., "Some Thermal and Electrical Properties of Beryllium," Phys. Rev. 34, 1575-87 (1929).

Lillie, D. W., "The physical and mechanical properties of beryllium metal," <u>The Metal Beryllium</u>, Chapt. 6, 304-27 (1955).

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Comments:

The data for this graph were taken from the references cited above under "Sources of Data". The tabular values are ratios of electrical resistivity with respect to the resistivity at 273.15 K (ρ_{273}). The ρ_{273} value used by each investigator is listed in the tables and on the graph.

Since beryllium is an anisotropic metal, resistivity values will vary according to the relation of the hexagonal c crystal axis to the direction of the resistivity measurements. Gruneisen and co-workers are the only investigators who have made measurements on single crystals. They report

 $\rho(||)_{273} = 3.56 \times 10^{-6}$ ohm cm and $\rho(\perp)_{273} = 3.12 \times 10^{-6}$ ohm cm.

The lowest values of ρ_{273} for polycrystalline beryllium were reported by Reich, et al. and Powell. They reported

$$\rho(\text{poly})_{273} = 2.7 \times 10^{-6} \text{ ohm cm}.$$

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The measurements by McLennan and Niven (1927) were made on thin sheets of beryllium. No information is given on purity or heat treatment of the sample.

Lewis (1929) used a rod of cross-sectional area 0.792 cm² made from 99.5% pure beryllium in his measurements. He found that the amount of heat treatment greatly affected the resistivity and that the best results were obtained after the sample had been slowly heated over a period of 24 hours to about 700 °C and held there for 12 hours and then cooled slowly to room temperature.

The Meissner and Voigt (1930) sample was a rod with a length of 1.5 cm and hexagonal cross-section 0.18 x 0.15 cm. The 98% pure sample was electrolytically prepared.

Grüneisen and Adenstedt (1938) measured resistivity of single crystals $Be_{||} 1$ and $Be_{||} 2$ in a direction parallel to the hexagonal c axis. The quality of crystal structure and purity of $Be_{||} 1$ were not as high as those of $Be_{||} 2$; therefore the values for $Be_{||} 1$ were not tabulated. The density of $Be_{||} 2$ was 1.84. The length was 1.55 cm and cross-section area was 0.00648 cm². The values for $Be_{||} 2$ in the tables below were taken with zero magnetic field.

The Grüneisen and Erfling (1940) measurements were made with single crystals Be₁3, Be₁4, and Be₁8 in a direction perpendicular to the hexagonal c axis (at 12°, 2°, and 30° angles to the secondary axis). Crystal sizes are: for Be₁4, $\ell_1 = 0.91$ cm and $\ell_2 = 0.83$ cm; and for Be₁8, $\ell_1 = 1.40$ cm and $\ell_2 = 0.94$ cm. Be₁3 dimensions were not given. The values in the tables below were taken with zero magnetic field. Their results show that deviation from the secondary axis has little effect on the resistivity.

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Erfling and Grüneisen (1942) made measurements on single crystals $Be_{||} 2$ and $Be_{||} 6$ in a direction parallel to the hexagonal c axis.Crystal sizes are: for $Be_{||} 2$, $l_1 = 0.55_6$ cm and $l_2 = 0.45$ cm; and for $Be_{||} 6$, $l_1 = 0.57$ cm, $l_8 = 0.33$ cm. $Be_{||} 2$ is the same sample used in the Grüneisen and Adenstedt (1938) determinations with a change in mounting. $Be_{||} 6$ sample is a six sided prism of very regular cross-section and of somewhat higher purity than $Be_{||} 2$. The values in the tables below were taken with zero magnetic field.

Powell (1953) in a literature review of experimental electrical resistivity studies cites the Denton (1947) measurements on rods 3.5 cm long and 0.3 cm diameter from a block of American G.E.C. sintered beryllium. The values in the tables below were made on the samples after a 715°C heat treatment.

The analytical purities of the samples used by MacDonald and Mendelssohn (1950) were not available but they were stated to be of comparatively high purity. The samples were in the form of thin strips. No mention is made of heat treatment.

Powell's (1953) resistivity measurements on beryllium were made on a bar 1.884 cm long by 0.865 cm diameter with a density of 1.84. This specimen was subsequently heated in a vacuum for 1 hour at 700°C and furnace cooled. The original material was from Brush Beryllium Company's crude reactor product. No chemical analysis was made on the sample. The value for ρ_{293} is 3.2 x 10⁻⁶ ohm cm.

The specimens used by White and Woods (1955), Be 1 and Be 2, were sintered polycrystalline rods (5 mm and 4 mm diameters) with approximately 2% and 0.1% impurities, respectively. Up to a temperature of about 130°K, the resistance of the two specimens may be represented by

$$\rho = (\rho_0 + 6.4 \times 10^{-8} T^{3.2}) \times 10^{-6}$$
 ohm cm.

Reich, et al. (1963) made measurements on polycrystalline beryllium wire which was annealed at 800°C for one hour in a vacuum. The beryllium was electrolytically prepared and the analysis before wiredrawing showed ~ 99.% pure beryllium. The specimen had a fine grain structure very close to the direction [1010]. ρ_0 for this sample was 0.033 x 10⁻⁶ ohm cm.

Reich (1965) studied the influence of impurities on the resistivity of polycrystalline beryllium wires at 4.2° K. In his article the type and amount of each impurity are given. His results are presented in the table below.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

Tables of Values of Electrical Resistivity

$$\label{eq:rho} \begin{array}{ll} \rho &= \mbox{Resistivity, (ohm cm)} \\ \rho_{273} &= \mbox{Resistivity at 273°K, (ohm cm)} \\ R &= \mbox{Resistance, (ohm)} \\ R_{273} &= \mbox{Resistance at 273°K, (ohm)} \end{array}$$

McLenn	an and Niven (1927)
Temp.	Specific Resistance*
°K	micro ohm
4.2	13.6
20.6	13.6
81	13.7
273	17.0**
293	17.6
* These	values are not shown on
the Ele	ctrical Resistivity of
Berylli	um graph.
** Inte	rpolated value.

	Lewis (1929)					
Temp.	Temp.	Resistivity	ρ/ρ ₂₇₃			
°C	°K	p x 10 ⁶ ohm cm				
-189	84.15	1.50	0.255			
- 77	196.15	3.22	0.548			
0	273.15	5.88	1.00			
+ 21	294.15	6.45	1.10			
+ 25	298.15	6.50	1.11			

Meissner ar	nd Voigt (1930)	
Temp. °K	p/p ₂₇₃ *	
273.16 81.73 20.44 2.38 1.35	1.00 0.3229 0.3075 0.3075 0.3075 0.3077	
* ρ ₂₇₃ = 7.	9×10^{-6} ohm cm.	

Grüneisen and Adenstedt (1938)				
Temp.	Temp.	Resistivity	p/p ₂₇₃	
°C	°K	p x 10 ⁶ ohm cm		
		Be ₁₁ 2	Be _H 2	
-252.82	20.33	0.00458	0.00128	
-194.13	79.02	0.0454	0.01268	
0.	273.15	3.58	1.00	

		Grüne	eisen and E	rfling (1940)			
Temp. Temp. °K °C		Resistivity p x 10 ⁶ ohm cm			p/p ₂₇₃		
		Be ₁ 3	^{Be} ⊥ ⁴	Be⊥8	Be ₁ 3*	^{Be} ⊥ ⁴	^{Be} ⊥ ⁸
273.15 90.29 90.17 89.86	0 -182.86 -182.98 -183.29	3.12 0.0755	3.13 0.0868 	3.12 0.0770	1.00	1.00 0.02775	1.00 0.02467
78.05 78.00 77.83	-195.10 -195.15 -195.32	0.0452	 0.0537	0.0473	0.01443	0.01717	0.01515
20.37 20.36 20.34	-252.78 -252.79 -252.81	0.0078	0.0124	0.0076	0.00251	0.00396	0.00243
* Be ₁ 3	values were plot	ted.		•	••••••••	<u> </u>	

Electrical Resistivity of Beryllium Cryogenic Data Memorandum No. M-25

Temp. Temp. °C °K		Resistivity p x 10 ⁶ ohm cm		ρ/ρ ₂₇₃	
		Be ₁₁ 2	Be _{II} б	Be ₁₁ 2*	Be _{ll} 6
-194.86 -194.20 -193.52 -183.03 0.	78.29 78.95 79.63 90.12 273.15	0.0450 0.0763 3.58	0.0404 0.04125 0.0728 3.56	0.01257 	0.0113 0.0115 0.0204 1.00

* Be_{||} 2 values were plotted.

Denton (1947)				
Temp.	Temp.	Resistivity	ρ/ρ ₂₇₃	
°C	°K	p x 10 ⁶ ohm cm		
0	273.15	3.50	1.00	
-183	90.15	0.297	0.085	
-253	20.15	0.21	0.06	

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Temp.	R/R273			
°K	Be l	Be 2*		
273	1,000	1.000		
90	0.397	0.322		
20.4	0.384	0.276		
4.2	0.384	0.276		

Powell (1953)				
Temp.	Resistivity [*]			
°C	p x 10 ⁶ ohm cm			
0	2.7**			
20	3.2			
50	4.1			
100	5.3			
200	8.1			
300	11.1			
400	13.5			
500	16.7			
600	20.4			
* These values have not been plotted on the Electrical Resistivity of Beryllium graph. ** Extrapolated value.				

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Electrical Resistivity of Beryllium Cryogenic Data Memorandum No. M-25

White and Woods (1955) (read from graph)					
Temp. °K	Resistivity p x 10 ⁶ ohm cm		p/p27	p/p273	
	Be l	Be 2	Be 1**	Be 2	
0 10 30 50 70 90 273	1.11 1.11 1.12 1.18 1.25 4.6*	1.21 1.21 1.21 1.22 1.28 1.35 1.35	0.241 0.241 0.241 0.243 0.257 0.272 1.00	0.281 0.281 0.281 0.284 0.284 0.298 0.314	
295	5.08	4.93	1.10	1.15	

Reich, Kinh, and Bonmarin (1963)				
Temp. °K	Resistivity [*] p x 10 ⁶ ohm cm	ρ/ρ ₂₇₃		
20 50 80 100 150 200 250 273.15 295	0.0334 0.0407 0.0719 0.1237 0.4690 1.184 2.189 2.743 3.283	0.0122 0.0148 0.0262 0.0451 0.1710 0.432 0.798 1.00 1.20		
* These values were actually taken from Meaden (1965) who received the experi- mental values directly from Reich. The p_0 value in Meaden (1965) should be 0.033 x 10 ⁻⁶ ohm cm.				

Reich (1965)					
Sample	Purity	Resistivity at 4.2°K* ρ x 10 ⁶ ohm cm			
	, <i>p</i>	After	After annealing in a 10 ⁻⁵ Torr vacuum		
		drawing	for 1 hour	for 150 hours	
H 1209/SR H 978/CR F 887/CR F 671/CR	99.99785 99.997586 99.987469 99.989032	0.0375 0.512 0.598 1.050	0.0332 0.465 0.399 0.938	0.0361 0.492 0.492 1.008	
* These values were not plotted on the Electrical Resistivity of Beryllium graph.					



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CRYOGENIC DATA MEMORANDUM

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FILE NO. M-10

(page 1 of 4)

ELECTRICAL RESISTIVITY OF COBALT, Co (Atomic Number 27)

Sources of Data:

International Critical Tables of Numerical Data, Physics, Chemistry, and Technology, VI, 1st Edition, Published for the National Research Council by the McGraw-Hill Book Co. Inc., 124-35 (1929).

Landolt-Börnstein Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, sechste Auflage, II Band, 6 Teil, Springer-Verlag, Berlin, 1-46 (1959).

Meaden, G. T., Electrical Resistance of Metals, Plenum Press, New York (1965) 218 p.

Meissner, W., and Voigt, B., "Messungen mit Hilfe von flüssigem Helium. XI. Widerstand der reinen metalle in tiefen Temperaturen," (Measurements with the Help of Liquid Helium. XI. Resistance of Pure Metals at Low Temperatures), Ann. Physik 7, 892-936 (1930).

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Semenenko, E. E., Sudovtsov, A. I., and Volkenshtein, N. V., "Temperature Dependence on the Electrical Resistance of Cobalt between 1.3 and 4.2°K," Soviet Phys. JETP <u>18</u>, No. 4, 957-58 (1964), Transl. from Zh. Eksperim. i Teor. Fiz. <u>45</u>, 1387-88 (1963).

White, G. K., and Woods, S. B., "Low Temperature Resistivity of the Transition Elements: Cobalt, Tungsten, Rhenium," Can. J. Phys. <u>35</u>, 656-65 (1957).

White, G. K., and Woods, S. B., "Electrical and Thermal Resistivity of the Transition Elements at Low Temperature," Phil. Trans. Roy. Soc. (London) <u>A251</u>, 273-302 (1959).

Other References:

Bridgman, P. W., "The Electric Resistance to 30,000 kg/cm² of Twenty Nine Metals and Intermetallic Compounds," Proc. Am. Acad. Arts Sci. <u>79</u>, 149-79 (1951)

Grüneisen, E., <u>Handbuch der Physik 13, 1 (1928)</u>

Grüneisen, E , "Elektrische Leitfähigkeit der Metalle bei tiefen Temperaturen," (Electrical Conductivity of Metals at Low Temperatures), Ergebn. exakt. Naturw. <u>21</u>, 50-116 (1945).

Holborn, L., Z. Physik 8, 58 (1921).

Olsen-Bär, M., Univ. of Oxford, Ph. D. Thesis (1956).

Meissner, W., Physik. Z. 29, 897-904 (1928).

Comments:

The data for this graph were taken from the references cited above under "Sources of Data" and are listed as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. When actual values of ρ_{273} for the samples used by the investigators are not available, a datum value reported by White and Woods ($\rho_{273} = 5.24 \times 10^{-6}$ ohm cm) is suggested for calculating values of electrical resistivity from these ratios.

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The values listed in the Landolt-Börnstein tables are those reported by Meissner and Voigt; and Bridgman (1951); while those values appearing in the International Critical Tables are from Holborn. These primary sources are cited above under "Other References." The original authors are used in labeling the curves on the graph.

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The Landolt-Börnstein tables list the sample used by Meissner and Voigt as an annealed, sintered polycrystalline specimen with no mention made of impurities present. The sample used by Bridgman was reported as polycrystalline with a very small amount of impurities. Bridgman reported only $\rho_{273} = 5.57 \times 10^{-6}$ ohm cm. No information is given on the amount of impurity or nature of the Holborn sample, and no further information is available on the mechanical strain or heat treatment for either of the samples.

White and Woods' (1957) measurements were with 99.999% pure cobalt rods. They report values of ideal resistivity $\rho_1 = \rho - \rho_0$ (ρ_0 = resistivity due to impurity scattering; ρ_0 values for the two cobalt samples were 0.0902 x 10⁻⁶ and 0.0907₅ x 10⁻⁶ ohm cm). Their data are reported graphically with tabular values taken from the graph. These tabular values may have an error of about $\pm 1\%$ due to uncertainty in the geometry of the specimens.

White and Woods' (1959) review paper gives values of resistivity based on their earlier measurements (1957) between 15 and 295°K and the results obtained by Olsen-Bär (1956) for temperatures below 20°K.

Semenenko, et al. (1963) used rods of 99.9984% pure cobalt. No mention is made of mechanical strain or heat treatment of the sample prior to measurement.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

A polycrystalline wire of pure cobalt was annealed at 1040°C in vacuo by Radhakrishina and Nielsen (1965) prior to resistance measurements. They do not state the percent purity of the sample. The data were presented graphically and were fitted to the expression R = $R_0 + R_1T + R_2T^2$, where $R_0 = 870.004 \times 10^{-10}$ ohm cm, $R_1 < 3.13 \times 10^{-12}$ ohm cm/°K, $R_2 = 0.9892 \times 10^{-11}$ ohm cm/(°K)². ρ_{273} (5.24 x 10⁻⁶ ohm cm) used in the resistance ratio was taken from White and Woods (1957).

Tables of Values of Electrical Resistivity

 ρ_{273} = resistivity at 273°K, (ohm cm).

Meissner and	Voigt (1930)	Holborn	(1921)
Temp. °K	R/R ₂₇₃ *	Temp. °C	100p/p ₂₇₃
1.5 4.2 20.4 77.8 86.9 273.16	0.0431 0.0426 0.0463 0.1516 0.1829 1.0000	- 80* -100* -120* -160* -180* -192	57.4 48.2 40.0 24.8 17.4 13.5

 $\rho = resistivity, (ohm cm);$

White and Woods (1957)				
Temp. °K	"Ideal Resistivity" p ₁ x 10 ⁵ ohm cm	Resistivity, $\rho \ge 10^6$ ohm cm $\rho = \rho_1 + \rho_0$ (where $\rho_0 = 0.0905 \ge 10^{-6}$ ohm cm)	p/p273	
15	0.0025	0.0930	0.0177	
20	0.0065	0.0970	0.0185	
30	0.030	0.1205	0.0230	
40	0.079	0.1695	0.0323	
50	0.150	0.2405	0.0459	
75	0.460	0.5505	0.1050	
100	0.90	0.9905	0.1890	
150	1.98	2.0705	0.3951	
200	3.23	3.3205	0.6336	
273	5.15	5.2405	1.000	
295	5.80	5.8905	1.1239	
Electrical Resistivity of Cobalt Cryogenic Data Memorandum No. M-10

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	White and Woods (1959)					
Temp. °K	"Ideal Resistivity"* $\rho_{\rm f} \ge 10^6$ ohm cm	Resistivity, $\rho \times 10^6$ ohm cm $\rho = \rho_1 + \rho_0$ (where $\rho_n = 0.089 \times 10^{-6}$ chm cm)	ρ/ρ ₂₇₃			
10	0.0011	0.0901	0.0172			
15	0.0027	0.0917	0.0175			
20	0.0066	0.0956	0.0182			
25	0.014	0.103	0.0197			
30	0.027	0.116	0.0221			
40	0.072	0.161	0.0307			
50	0.145	0.234	0.0447			
60	0.25	0.339	0.0647			
70	0.38	0.469	0.0895			
80	0.54	0.629	0.120			
90	0.72	0.809	0.154			
100	0.91	0.999	0.191			
120	1.32	1.409	0.269			
140	1.78	1.869	0.357			
160	2.26	2.349	0.448			
180	2.75	2.839	0.542			
200	3.23	3.319	0.634			
220	3.72	3.809	0.727			
250	4.50	4.589	0.876			
273	5.15	5.239	1.000			
295	5.80	5.889	1.124			

* There is uncertainty in the last digit of the resistivity data

Radhakrishna and Nielsen (1965)					
	(read from graph)				
Temp. °K	Temp. Resistivity °K ρ x 10° ohm cm				
1.4 1.9 2.3 2.8 3.2 3.6 4.0	87.145 87.160 87.175 87.200 87.220 87.220 87.246 87.282	0.01663 0.01663 0.01664 0.01664 0.01665 0.01665 0.01666			
4.6 5.1 5.5 5.9 6.2 6.4	87.336 87.380 87.423 87.465 87.495 87.495 87.520	0.01667 0.01668 0.01668 0.01669 0.01670 0.01670			

Semenenko, et al. (1963) (read from graph)					
Temp. °K	R / R ₂₇₃				
1.55 2.0 2.5 2.8 3.2 3.55 4.2	0.038196 0.038201 0.038206 0.038210 0.038215 0.038221 0.038233				



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CRYOGENIC DATA MEMORANDUM

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FILE NO. M-11

ELECTRICAL RESISTIVITY OF COPPER, Cu

(page 1 of 8)

(Atomic Number 29)

Sources of Data:

International Critical Tables of Numerical Data, Physics, Chemistry, and Technology, VI, 1st Edition, Published for the National Research Council by the McGraw-Hill Book Co. Inc., 124-35 (1929).

Landolt-Börnstein Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, sechste Auflage, II Band, 6 Teil, Springer-Verlag, Berlin, 1-46 (1959).

Berman, R., and MacDonald, D. K. C., "The Thermal and Electrical Conductivity of Copper at Low Temperatures", Proc. Roy. Soc. (London) <u>sll</u>, 122-8 (1952).

Bridgman, P. W., "The Resistance of 72 Elements, Alloys, and Compounds to 100,000 kg/cm²," Proc. Am. Acad. Arts Sci. <u>81</u>, No. 4, 165-251 (Mar 1952).

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Domenicali, C. A., and Christenson, E. L., "Effects of Transition Metal Solutes on the Electrical Resistivity of Copper and Gold Between 4 and 1300°K," J. Appl. Phys. <u>32</u>, No. 11, 2450-6 (1961).

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Moore, J. P., McElroy, D. L., and Graves, R. S., "Thermal Conductivity and Electrical Resistivity of High-Purity Copper from 78 to 400°K," Can. J. Phys. <u>45</u>, 3849-65 (1967).

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Other References:

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Back, O., "Verforming und elektrischer Widerstand von Kupfer-Einkristallen bei tiefsten Temperaturen," (The Deformation and Electrical Resistivity of Copper Single Crystals at Low Temperatures), Phys. Status Solidi 2, 535-57 (1967).

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Kovacs-Csetenyi, E., Vassel, C. R., and Kovacs, I., "The Effect of Impurity Content and Heat Treatment on the R_{273}/R_{78} Resistivity Ratio of Aluminum and Copper," Acta Phys. Acad. Sci. Hung. <u>21</u>, No. 2, 195-8 (1966).

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Pearson, W. B., "CIII. Electron Transport in Copper and Dilute Alloys at Low Temperature. III. Solid Solutions of Iron in Copper," Phil. Mag. <u>46</u>, 911 (1955).

Roder, H. M., Powell, R. L., and Hall, W. J., "Thermal and Electrical Conductivity of Pure Copper," Low Temperature Physics and Chemistry, Univ. of Wisconsin Press, p. 364-6 (Aug 1958).

Verel, D. J., "Recovery of the Resistivity of Copper Cold Worked at Low Temperatures," Physica 29, 562-64 (1963).

Comments:

The data for this graph were taken from the references cited above under "Sources of Data". The values listed in the Landolt-Börnstein tables are those reported by de Haas, de Boer and Van den Berg; Holborn; and Meissner (1928); while those values in the International Critical Tables are from Henning. These primary sources are listed above under "Other References". The original authors are used in labeling the curves on the graph.

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In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The data in the Landolt-Börnstein tables and the International Critical Tables tabulated here are listed as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. When the actual values of ρ_{273} for the samples used by the original investigators are not available, a datum value determined by Powell, et al. (1959) ($\rho_{273} = 1.545 \times 10^{-6}$ ohm cm) is suggested for calculating values of electrical resistivity from these ratios.

The Landolt-Börnstein tables report the samples used by the authors appearing in their compilation as annealed polycrystalline specimens with a small amount of impurities present. No other pertinent information is given about the data reported in Landolt-Börnstein tables or International Critical Tables.

The Meissner (1915) paper gave $\rho_{273} = 1.55 \times 10^{-6}$ ohm cm.

Onnes and Tuyn (1926) measurements were made on "natural copper crystals".

Meissner and Voigt (1930) present the same data as Meissner (1928).

Berman and Mac Donald (1952) used 99.9988% pure copper wires which were annealed for 6 hours at 450°C in helium.

Bridgman (1952) used 99.9999% pure 0.001 inch thick copper sheets to measure the effect of pressure on the electrical resistivity. He reported room temperature measurements as ratios of the resistance at a given pressure to the resistance at one atmosphere.

A 99.99% pure copper wire used by Broom (1952) was annealed for two hours at 600°C prior to resistivity measurements. The tabular data are for the specimen before deformation (wire drawing). Broom's graphs show the effect of deformation on the resistivity.

White (1953) and White and Woods (1959) used wires of 99.999% purity which were annealed in vacuum at 550 and 530 °C for three hours prior to measurement.

Sekula (1959) studied the effect of oxidizing or reducing atmosphere on the electrical resistivity minimum. The 99.999% pure copper wire specimen was first annealed in a vacuum of 2×10^{-5} mm Hg at 950°C for two hours before measurements were made. Then the specimen was reheated in 10 microns of air at 750°C for two hours before a second set of measurements was made. The resistance ratio $R/R_{20°C}$ is reported graphically for both sets of measurements; the value of $R_{20°C}$ is not given. The ratio $\rho_{293}/\rho_{273} = 1.7027/1.5527$ from White and Woods was used in determining the ratio R/R_{273} .

Powell, et al. (1959) used 99.999% pure copper rods which were annealed in vacuum at 400°C prior to measurement at 4.2°K; the resistivity of the sample was (1.01 \pm 0.02) x 10⁻⁹ ohm cm. The values in the table below are read from their graph.

The copper used by Domenicali and Christenson (1961) contains 10^{-4} to 10^{-3} % impurities. The copper was shaped in the form of square cross-section wires which were annealed at 500 °C for several hours in vacuo.

Gniewek and Clark (1965) used 99.999% pure copper in growing crystals in a 10^{-5} Torr vacuum. Their crystals were heated at 1000 °C under a pressure of 5 x 10^{-5} Torr for approximately 15 hours and then cooled at a maximum rate of 150 °C/hr.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

The samples used by Pawlek and Rogalla (1966) were 99.9943% and 99.9994% pure copper wires which had been annealed at 600°C for one hour and cooled no faster than 50°C/hr. The data in the table below are for the 99.9994% pure sample.

The Moore et al. (1967) measurements were made with 99.999% pure, polycrystalline copper rods 5 - 8 cm long.

1.40

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Tables of Values of Electrical Resistivity

 ρ_{273} = resistivity at 273°K, (ohm cm). R₂₇₃ = resistance at 273°K, (ohm). p = resistivity, (ohm cm); R = resistance, (ohm);

Meissner (1915)		Holborn (1919)		Henni	Henning (1921)		Onnes and Tuyn (1926)		
Temp. °K	p/p ₂₇₃ **	Temp. °K	R/R ₂₇₃	Temp. °C	100R/R ₂₇₃	Temp. °C	R/R273 **		
20.7 90.7 273.1*	0.0026 0.186, 1.000	81 195	0.1502 0.6602	- 76 -183 -252.8	65.739 18.868 0.6291	-184.53 -192.04 -199.98 -206.94	0.1749 0.1440 0.1103 0.0840		
* $\rho_{273} = 1.55 \times 10^{-6}$ ohm cm. ** These values are not plotted on the Electrical Resistivity of graph.					y of Copper	-218.09 -252.57 -255.07 -256.63 -258.77	0.0469 0.00154 0.00129 0.00109 0.00097		
Meissner Meissne	and Voigt (1930) er (1928)	de	Haas, et a	1. (1934)	(b	Broom (1952) efore deformation	.)		
Temp.* °K	R/R273**	Ten °ł	າp. ເ	p/p ₂₇₃	Temp. Resistivity °C p x 10 ⁶ ohm cm		P/P273		
1.32 1.97 4.20	0.00029 0.00028 0.00029	1. 4. 14.	.55 23 .26	0.00117 0.00119 0.00128	-183 - 78.5 0	0.291 1.06 1.59	0.183 0.67 1.00		

0.00176

100

2.23

1.000 273.16 * The second decimal place of the temperature values is somewhat in doubt.

20.47

0.00078

0.144

20.42 81.6

** The fifth decimal place of the electrical resistivity ratio values is somewhat in doubt.

	Berman and Mac (read from	Donald (195:) graph)	Bridgman	(1952)		
Temp. °K	Conductivity c x 10 ⁻⁶ (ohm cm) ⁻¹	Resistivity p x 10 ⁶ ohm cm	P/P273*	(room temperature) (Data compared with the resistance at atmosphere taken as unity)		
2.5 10. 16. 20.	150 154 150 135	0.0067 0.0065 0.0067 0.0074 0.0074	0.0043 0.0042 0.0043 0.0048 0.0048	Pressure kg/cm ²	R/R ₀	
24.5 30. 33. 40. 48. 53.5	79 60 36 21 15	0.009 0.013 0.017 0.028 0.048 0.037	0.0084 0.011 0.018 0.031 0.043	0 10000 20000 30000 40000 50000	1.000 0.981 0.965 0.949 0.934 0.920	
64. 72. 80. 90.	9 6 5 3	0.11 0.17 0.20 0.33	0.071 0.11 0.13 0.21	6 0030 7 0000 8 0000 9 00000	0.907 0.895 0.834 0.875 0.875	
90. 90. * These of Copp	3 e values were not plotte per graph.	0.33 ed on the Electrical	0.21 Resistivity	80000 90000 100000		

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	White (1953)					
	(read from graph)					
Temp.	P/P273					
°K	$\rho_1 \times 10^6$ ohm em	$\rho = \rho_1 + \rho_o$				
		(where $\mu_{o} = h_{\bullet} 5 \times 10^{-1}$ ohr cm)				
14	0.00035	0.00495	0.00319			
20	0.00098	0.00558	0.00360			
30	0.0030	0.0112	0.00490			
34	0.014	0.0186	0.0120			
41	0.028	0.0326	0.0210			
55	0.074	0.0786	0.0507			
62	0.11	0.1146	0.0739			
78	0.19	0.1946	0.1255			
100	0.38	0.3846	0.5780			
120	0.55	0.5546	0.3576			
190	0.98	0.9846	0.6348			

	White and Woods (1959)				
Temp. °K	"Ideal Resistivity" ρ _i x 10 ⁶ ohm cm	Resistivity, $\rho \ge 10^6$ ohm cm $\rho = \rho_1 + \rho_0$ (where $\rho_0 = 2.7 \ge 10^{-2}$ ohm cm)	ρ/ρ ₂₇₃		
15	0.00017	0.00287	0.00185		
20	0.0008	0.0035	0.0023		
25	0.0025	0.0052	0.0034		
30	0.0063	0.0090	0.0058		
40	0.022	0.0247	0.015		
50	0.050	0.0527	0.034		
60	0.095	0.0977	0.063		
70	0.153	0.1557	0.100		
80	0.215	0.2177	0.140		
90	0.280	0.2827	0.182		
100	0.350	0.3527	0.227		
120	0.490	0.4927	0.318		
140	0.635	0.6377	0.411		
160	0.775	0.7777	0.501		
180	0.92	0.9227	0.595		
200	1.06	1.0627	0.685		
220	1.20	1.2027	0.775		
250	1.40	1.4027	0.904		
273	1.55	1.5527	1.00		
295	1.70	1.7027	1.10		

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	Sekula (1959)					
	(read from graph)					
Temp.	R/F	so°c	R/R273			
°к	Vacuum Annealed	Air Annealed	Air Annealed			
1.7	8.95 x 10 ⁻⁴	3.10 x 10 ⁻⁴	0.000340			
4.6	8.85 x 10 ⁻⁴	3.18 x 10 ⁻⁴	0.000349			
6.0	8.81 x 10 ⁻⁴	3.21 x 10 ⁻⁴	0.000352			
7.6	8.81 x 10 ⁻⁴	3.27 x 10 ⁻⁴	0.000359			
9.0	8.85 x 10 ⁻⁴	3.31 x 10 ⁻⁴	0.000363			
11.1	9.00 x 10 ⁻⁴	3.46 x 10 ⁻⁴	0.000379			
13.5	9.37 x 10 ⁻⁴	3.90 x 10 ⁻⁴	0.000428			
15.0	9.70 x 10 ⁻⁴	4.28 x 10 ⁻⁴	0.000469			
16.5	10.10 x 10 ⁻⁴	4.80 x 10 ⁻⁴	0.000526			
18.0	11.00 x 10 ⁻⁴					
* using the ratio ρ ₂₉₃ /ρ ₂₇₃ = 1.7027/1.5527 from White and Woods (1959).						

	Powell, et al. (1959) (read from graph)				
Temp. °K	Resistivity pxl ⁶ ohm em	P/P275			
4.2	0.00101	0.000654			
5.0	0.00105	0.000680			
6.5	0.0011	0.000712			
7.7	0.00115	0.000744			
10.3	0.0013	0.000744			
20.4	0.0021	0.00136			
22.0	0.0030	0.00194			
78.0	0.190	0.123			
273.15	1.545	1.000			

Domenicali and Christenson (1961) (read from graph)					
Temp. °K	Resistivity p x 10 ⁶ ohm cm	ρ/ρ ₂₇₃ *			
1 25 50 75 100	0.01 0.02 0.05 0.2 0.35	0.0063 0.013 0.032 0.13 0.22			
150 200 250 273 300	0.7 1.05 1.4 1.58 1.75	0.40 0.66 0.89 1.00 1.11			
* These values were not plotted on the Electrical Resistivity of Copper graph.					

	Gniewek and Clark (1965)					
	Crystal	R300°K /R4.0°K	R4.0°K /R273°K			
А	polycrystalline	20000	0.0000548			
В	single	23000	0.0000477			
с	single	15600	0.0000703			
*	Calculated using	the values of W	hite and Woods			

f	Calculated	using	the v	alues	of	Whi	te	and	Woods
	(1959) for	ρ ₂₉₃ =	1.70	27 x 1	0 -e :	∋hm	em	and	
	$\rho_{273} = 1.5$	527 x 10	⁻⁶ ohm	cm.					

Pawlek and Rogalla (1966)				
Temp.Resistivity ρ/ρ_{273} °K $\rho \ge 10^9$ ohm. cm				
4.2 20.4 77 195 273	0.330 1.11 192 990 1580	0.000213 0.000703 0.122 0.630 1.000		

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Moore, McElroy and Graves (1967)			
Temp. °K	Resistivity p x 10 ⁶ ohm cm	p/p ₂₇₃ *	
4.2	0.00172	0.0011	
85	0.248	0.160	
90	0.282	0.182	
100	0.350	0.226	
110	0.418	0.270	
120	0.488	0.316	
130	0.558	0.361	
140	0.631	0.408	
150	0.702	0.454	
175	0.876	0.567	
200	1.047	0.677	
225	1.219	0.788	
250	1.389	0.898	
273.16	1.546	1.000	
*These values have not been plotted on the Electrical Resistivity of Copper graph.			

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CRYOGENIC DATA MEMORANDUM

PROJECT NO. 3150123

ELECTRICAL RESISTIVITY of GOLD, Au (Atomic Number 79)

(page 1 of 6)

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Comments:

The data for this graph were taken from the references cited above under "Sources of Data" and are listed as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. When the actual values of ρ_{273} are not available for the samples used by the various investigators, a datum value reported by White and Woods (1959) ($\rho_{273} = 2.02 \times 10^{-6}$ ohm cm) is suggested for calculating values of electrical resistivity from these ratios.

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The values listed in the Landolt-Börnstein tables are those reported by Holborn, Justi, and Meissner, while the values appearing in the International Critical Tables are those from Cath, Onnes, and Burgers. These primary sources are listed above under "Other References". The original authors are used in labeling the curves on the graph. The Cath et al.measurements were made on "pure minting gold" wires. Meissner (1915) reported $\rho_{273} = 2.065 \times 10^{-6}$ ohm cm.

Onnes and Clay (1907) made their measurements on 0.1 mm diameter wires which were heated in an "annealing furnace for a long time and slowly cooled". The purity of the samples follows; Au_{III} was ~ 99.985%, Au_{IV} and Au_V were ~ 99.995%. Their 1908 measurements were on Au_V.

Onnes and Tuyn (1926) list values taken by Meissner (1925) see other references on single crystal gold. Onnes and Tuyn give no other information about the sample.

Meissner and Voigt (1930) present the same data as that found in the earlier Meissner paper (1926).

The 99.9999% pure gold used by de Haas and Van den Berg (1936) was in the form of a wire which was annealed at 480°C for 5 hours prior to measurement.

Van der Leeden (1940) measured the resistivity of single crystal wires which were annealed at 480°C for 2 hours. The purity was not stated.

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The material used by Bridgman (1952) was specified as "highest purity" but with no analysis. The sample was rolled to 0.001 inch thickness and annealed. The measurements were made at room temperature and the resistance ratio is the resistance at the given pressure compared to the resistance at one atmosphere.

The purity of the two single crystal samples used by Van den Berg and Franken (1958) was 99.998%. These single crystal samples were not prepared in high vacuum and were not annealed.

White and Woods (1959) used wire samples of 99.99% purity which had been previously annealed in vacuo at 530 and 700 °C.

The gold used by Domenicali and Christenson (1961) contains 10^{-4} to 10^{-3} % impurities. The gold was shaped in the form of square cross-section wires which were annealed at 500 °C for several hours in vacuo.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

Tables of Values of Electrical Resistivity

 ρ = resistivity, (ohm cm); R = resistance, (ohm); ρ_{273} = resistivity at 273°K, (ohm cm).

, (ohm); R_{273} = resistance at 273°K, (ohm).

Onnes and Clay (1907)				
Temp.	Temp.	R/R _o		
°C	°K	AuIII	AuIV	Au *
0 -103.83 -183.00 -197.87 -205.01 -215.34 -252.93 -255.13 -258.81 -261 -262	273.09 169.26 90.09 75.22 68.08 57.75 20.16 17.96 14.28 12.09 11.09	1. 0.59601 0.27653 0.21456 0.14058 0.01602 0.01095	1. 0.59389 0.27177 0.20963 0.13407 0.008743 0.004265 0.003257	1. 0.59306 0.27096 0.20871 0.17897 0.13337 0.008103 0.005691 0.003601 0.002713 0.002526
* These are the values plotted on the Electrical Resistivity of Gold graph.				

Meissner (1915)		
Temp. °K	R/R ₂₇₃ **	
21.5 91.5 273.1*	0.00836 0.2764 1.0000	
* P273 = 2	2.06 ₅ x 10 ⁻⁶	

ohm cm. ** These values are not plotted on the Electrical Resistivity of Gold graph.

Holborn (1919)		
°K	R/R ₂₇₃	
81 195	0.2375 0.6955	

Cath, Onnes and Burgers (1918)			
Temp. °C	Temp. °K	100R/R ₂₇₃	
0.0	273.09	100.	
- 84.97	188.12	66.443	
-102.22	170.87	59.628	
-130.28	142.81	48.507	
-145.86	127.23	42.273	
-164.37	108.72	34.764	
-183.95	89.14	26.660	
-195.88	77.21	21.622	
-205.31	67.78	17.596	
-208.18	64.91	16.365	
-216.26	56.83	12.906	
-222.78	50.31	10.130	
-228.73	44.36	7.680	
-233.62	39.47	5.804	
-236.80	36.29	4.667	
-240.25	32.84	3.538	
-243.68	29.41	2.553	
-245.80	27.29	2.039	
-252.57	20.52	0.845	
-255.01	18.08	0.594	
-258.35	14.74	0.379	
-268.88	4.21	0.223	
-269.57	3.52	0.223	
-271.61	1.48	0.223	

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Meissner (1925)			
Temp. °C	R/R ₂₇₃		
-191.37 -193.14 -200. * -220. * -240. *	0.2320 0.2252 0.195 * 0.109 * 0.033 *		
-252.69 0.00642 -260. * 0.0010* -268.89 0.00039 -269.38 0.00038 -271.48 0.00039			
* Interpolated values.			

Meissner and Voigt (1930) Meissner (1926)			
Temp. °K	R/R ₂₇₃		
1.61 4.20 20.41 81.75 84.87 273.16	0.00109 0.00109 0.00707 0.2341 0.2480 1.0000		

Justi (1940)		
Temp. °K	R/R ₂₇₃	
4.2 14.0 20.4 79.0	0.00085 0.00227 0.00709 0.219	

de Haas and Van den Berg (1936)				
Temp. °K	100R/R _{o°c}	Temp. °K	loor/R _{c°c}	
20.44 18.08 17.03 16.05 15.17 12.10 11.95 11.84 10.00 9.95	0.9048 0.6573 0.5730 0.5076 0.4564 0.3386 0.3348 0.3320 0.2967 0.2959	9.38 8.83 7.28 6.54 6.08 4.81 4.23 3.77 3.12 2.39 1.63	0.2890 0.2826 0.2714 0.2685 0.2674 0.2651 0.2644 0.2644 0.2646 0.2652 0.2666	

Van der Leeden (1940)			
Au	1	Au 2	
Temp. °K	100R/R	Temp. °K	100R/Ro*
20.43 18.23 17.38 16.32 15.18 14.13	0.9960 0.7537 0.6767 0.5964 0.5240 0.4720	20.41 18.215 17.365 16.61 15.37 14.23	2.108 1.854 1.774 1.721 1.624 1.560
* These values were not plotted on the Electrical Resistivity of Gold graph.			

Bridgman (1952)				
(room temperature)				
(Data compared with the resistance at one atmosphere taken as unity)				
Pressure R/R _o Pressure R/R _o				
kg/cm ²		kg/cm ²		
0 10000 20000 30000 40000 50000	1.000 0.971 0.944 0.919 0.896 0.874	60000 70000 80000 90000 100000	0.855 0.840 0.829 0.821 0.816	

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Van den Berg and Franken (1958)					
Temp. °K	R _I x 10 ⁶ ohn	R _{II} x 10 ⁶ ohm	R _I /R ₂₇₃	R _{II} /R ₂₇₃	
1.365 1.762 1.968 2.229	1.1684 1.1659 1.1648 1.1633	2.4227 2.4217 2.4211 2.4209	0.003686 0.003678 0.003674 0.003670	0.005953 0.005950 0.005949 0.005948	
2.719 3.196 3.713 4.240	1.1619 1.1602 1.1604 1.1599	2.4207 2.4205 2.4214 2.4223	0.003665 0.003660 0.003661 0.003659	0.005948 0.005947 0.005949 0.005952	
273.0	317.0	407.0	1.0	1.0	

White and Woods (1959)					
Temp.	"Ideal Resistivity"	Resistivity, $p \ge 10^6$ ohm cm	р/р ₂₇₃		
°К	$\rho_i \times 10^5$ ohm cm	$\rho = \rho_1 + \rho_0$			
		(where $p_0 = 6.23 \times 10^{-9}$ ohm cm)			
10	0.0006	0.0068	0.00337		
15	0.0037	0.0099	0.00491		
20	0.0125	0.0197	0.00977		
25	0.027	0.0332	0.0165		
30	0.050	0.0562	0.0279		
40	0.12	0.1262	0.0626		
50	0.20	0.2062	0.102		
60	0.29	0.2962	0.147		
70	0.38	0.3862	0.192		
80	0.460	0.4662	0.231		
90	0.545	0.5512	0.273		
100	0.630	0.6362	0.316		
120	0.790	0.7962	0.395		
140	0.955	0.9612	0.477		
160	1.12	1.1262	0.559		
180	1.28	1.2862	0.638		
200	1.44	1.4462	0.717		
220	1.60	1.6062	0.797		
250	1.83	1.8362	0.911		
273	2.01	2.0162	1.000		
295	2.20	2.2062	1.094		

Domenicali and Christenson (1961) (read from graph)				
Temp. °K	Resistivity p x 10 ⁶ ohm cm	0/0 ₂₇₃		
1	0.01	0.005		
10	0.01	0.005		
25	0.04	0.020		
50	0.2	0.099		
75	0.4	0.20		
100	0.6	0.30		
150	1.08	0.53		
200	1.45	0.71		
250	1.86	0.92		
273	2.02	1.00		
300	2.3	1.14		

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ELECTRICAL RESISTIVITY of INDIUM, In (Atomic Number 49) (page 1 of 7)

Sources of Data:

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Comments:

The data for this graph were taken from the references cited above under "Sources of Data". The values listed in the Landolt-Börnstein tables are those reported by Meissner, Franz, and Westerhoff; and Meissner and Voigt; while those values appearing in the International Critical Tables are from Tuyn and Onnes. These primary sources are listed above under "Other References". The original authors are used in labeling the three curves on the graph. The curves chould not be extrapolated to lower temperatures since indium becomes a superconductor between 3.374 and 3.432 °K.

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The data in the Landolt-Börnstein tables and the International Critical Tables, tabulated here, are listed as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. The actual values of c_{273} were not available for the samples used by Meissner and Voigt; and Tuyn and Onnes, so a datum value reported by Powell, Woodman, and Tye ($\rho_{273} = 8.00 \times 10^{-6}$ ohm cm) is suggested for calculating values of electrical resistivity from these ratios.

The Landolt-Börnstein tables list the samples of both references as polycrystalline with 0.2% impurities in the sample used by Meissner and Voigt and a very small amount of impurity in the samples used by Meissner, Franz and Westerhoff. No mention is made of the amount of impurities in the sample used by Tuyn and Onnes, and no information was given on the mechanical strain or heat treatment for any of the samples from any of the above authors.

Bridgman (1952) studied the effect of pressure on electrical resistivity. The sample was rolled and cut into strips and was believed to be 99.9% pure.

The purity of the indium wire samples used by Swenson (1955) was 99.9%. The wires were extruded and not annealed. The values of resistance ratio in the table below for 50, 40, 20, and 4.2° K are extrapolated; all others are experimental.

Olsen's (1958) measurements were made on ten wire specimens with diameters varying from 0.2 to 2.54 mm in diameter from three different sources. No statement of purity was made. Below 3.37°K, where indium becomes superconducting, the zero field resistance was obtained by extrapolating from measurements in fields greater than the critical. The values in the table below are for the 2.0 mm diameter wire; this wire having the lowest residual resistivity $\rho_0 = 0.27 \times 10^{-9}$ ohm cm.

Electrical Resistivity of Indium Cryogenic Data Memorandum No. M-14

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The cylindrical indium samples used by Aleksandrov (1962) had a purity of 99.9993% and were annealed 1-2 days at 25-50°C before measurements were made. He observed the effect of sample size on the resistivity of indium and estimates the error in a single measurement on the thickest and purest sample at 4.2°K to be 1.5%. He found $\rho_{203} = 9 \times 10^{-6}$ ohm cm. The samples of indium used by Aleksandrov and D'Yakov (1962) were the same as those of Aleksandrov (1962) with the exception that they were all polycrystalline. They found $\rho_{273} = 8.37 \times 10^{-6}$ ohm cm, $\rho_0 = 3 \times 10^{-10}$ ohm cm.

Powell, et al. (1962) used 99.9997% pure rods in their measurements. No mention is made of heat or mechanical treatment to the sample. The experimental data were plotted on a graph and the following tabular values are taken from that graph.

Protopopescu, et al. (1962) reported the influence of purity on the electrical resistivity of indium. The samples range from 96.05 to 99.998% pure. The table below presents values for the four purest samples.

Wire samples of 99.9994% purity were used by Orlova, et al. (1963) in constructing resistance thermometers. The thermometers were annealed at $\sim 100\,^\circ\text{C}$ for 3 hours prior to resistivity measurements.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

Kaznoff et al. (1967) used 99.99% pure polycrystalline rods which were 0.3" in diameter. The table below gives smoothed values.

Tables of Values of Electrical Resistivity

ρ = Resistivity, (ohm cm); R = Resistance, (ohm);

 P_{273} = Resistivity at 273°K, (ohm cm). R_{273} = Resistance at 273°K, (ohm).

Tuyn and Onnes (1923, 1924)						
Temp. °C	Temp. °K	100R/R ₂₇₃	Temp. °C	Temp. °K	100R/R ₂₇₃	
-182.79	90,30	28.75	-254.95	18.14	5.173	
-194.06	79,03	24.92	-256.61	16.48	4.796	
-202.07	71,02	22.20	-258.89	14.20	4.317	
-209.98	63.11	19.52	-268.87	4.22	3•394	
-218.30	54.79	16.71	-269.49	3.60	3•392	
-252.65	20.44	5.739	-269.61	3.48	3•387	

Meissner and	Voigt (1930)
Temp. °K	R/R ₂₇₃
4.21 20.46 77.82 88.90 273.16	0.00387 0.0256 0.2177 0.2567 1.0000

Meissner, Franz and Westerhoff (1932)		
Temp. °K	R/R ₂₇₃	
4.23 20.4 77.8 273.16*	0.0015 0.0216 0.212 1.000	
* $\rho_{273} = 8.19 \times 10^{-6}$ ohm cm.		

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Bridgman (1952)			
	R/R _o (At Room Temperature)		
Pressure kg/cm ²	(Taking the Resistance at Atmospheric Pressure as R_0)		
0	1.000		
10000	0.891		
20000	0.810		
30000	0.746		
40000	0.694		
50000	0.650		
60000	0.610		
70000	0.578		
80000	0.548		
90000	0.520		
100000	0.493		

Swenson (1955)			
Temp. °K	R/R _{273.2} °k		
4.2	0.0010		
20.0	0.0200		
40.0	0.0820		
60.0	0.1520		
77.7	0.2189		
117.6	0.3607		
143.0	0.4549		
160.5	0.5214		
180.7	0.6023		
194.7	0.6576		
210.8	0.7224		
227.0	0.7929		
242.0	0.8603		
257.3	0.9286		
272.2	0.9942		

	Olsen (1958)	
Temp. °K	ρχ10 ⁹ ohm cm	ρ/ρ ₂₇₃ *
1.45	.277	3.39 x 10 ⁻⁵
1.6	.277	3.39 x 10 ^{-Б}
2.0	. 295	3.61 x 10 ^{-б}
2.5	.321	3.93 x 10 ^{-Б}
3.0	.356	4.36 x 10 ^{-б}
3.5	•435	5.32 x 10 ⁻⁵
4.0	.567	6.94 x 10 ^{-Б}
4.2	.620	7.59 x 10 ⁻⁵
	8.17 x 10^{-6} ohm cm sen's $\rho_{293} = 8.79$ Aleksandrov and I	was calculated x 10 ⁻⁶ ohm cm Yakov ratio

Electrical Resistivity of Indium Cryogenic Data Memorandum No. M-14

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Aleksandrov (1962)				
Temp. °K	Type of Crystal	R /R ₂₉₃	R /R ₂₇₃	
4.2 3.4 4.2	Polycrystal Polycrystal Single crystal	0.000073 0.000048	0.000079 0.000052	

Temp.		
°К	R / R_{293}^{*}	R /R [*] 273
3.4	4.8×10^{-5}	5. 2 x 10 ^{-s}
3.7	5.4 x 10^{-5}	5.8 x 10^{-5}
4.22	7.3×10^{-5}	7.8×10^{-5}
4.46	8.6 x 10 ⁻⁵	9.2 x 10 ⁻⁵
14.0	6.7×10^{-3}	7.2×10^{-3}
20.4	0.018	0.019
58.0	0.128	0.138
77.4	0.193	0.207
90.31	0. 232	0, 249
111.6	0.309	0.332
273.0	0.93	1.000

Powell, et al. (1962)				
Temp. °C	Temp. °K	Resistivity p x 10 ⁶ ohm cm	P/P273	
-200	73.15	1.65	0, 206	
-150	123.15	3.08	0, 385	
-100	173.15	4.60	0. 575	
- 50	223.15	6.22	0.778	
0	273.15	8.00	1,000	
50	323.15	10,00	1.250	
100	373.15	12.15	1, 519	
120	393.15	13.00	1.625	

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Protopopescu, et al. (1962)						
SamplePurity $\rho_{0.0.5} \times 10^6$ $\rho_{0.0} \times 10^6$ $\rho_{0.0} / \rho_{2.0.3}$ $\rho_{0.0} / \rho_{2.0.3}$ Number%ohm cmohm cm $\rho_{m.cm}$ $\rho_{0.0} / \rho_{2.0.3}$						
5 (electrically refined)	99.99	8.16	1.62	0.199	0.216	
6 (zone refined)	99.988	8.28	1.69	0.204	0.221	
7 (zone refined)	99.996	7.92	1.33	0,168	0.182	
8 (zone refined)	99.998	7.49	1.23	0.164	0.178	

* These values are not plotted on the Electrical Resistivity of Indium graph.

Orlova, et al. (1963)				
Thermometer	Resistan	ce Ratios [*]		
Number	R20.4/R273	$R_{4.2}/R_{273}$		
1	0, 02123	0.0004216		
2	0.02103	0.0004066		
3	0.02105	0.0002968		
4	0.02103	0,0002792		
6	0.02101	0.0002704		
8	0.01289	0,0002887		

* These values are not plotted on the Electrical Resistivity of Indium graph.

Kaznoff et al. (1967)					
Temp. °K	ρ x 10 ⁶ ohm cm	P/ P273	Temp. °K	p x 10 ⁶ ohm cm	P/P273
80 100 120 140 160	1.826 2.431 3.038 3.647 4.257	0.222 0.296 0.370 0.444 0.518	180 200 220 240 260	4.869 5.499 6.155 6.894 7.694 8.211	0.593 0.670 0.750 0.840 0.937



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CRYOGENIC DATA MEMORANDUM

FILE NO. M-15

ELECTRICAL RESISTIVITY OF IRON, Fe (Atomic Number 26)

(page 1 of 7)

Sources of Data:

International Critical Tables of Numerical Data, Physics, Chemistry, and Technology, VI, 1st Edition, Published for the National Research Council by the McGraw-Hill Book Co. Inc. 124-35 (1929).

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Comments:

The data for this graph were taken from the references cited above under "Sources of Data". The values listed in the Landolt-Börnstein tables are those reported by Meissner; and Cleaves and Hiegel; while those values appearing in the International Critical Tables are from Holborn. These primary sources are cited above under "Other References." The original authors are used in labeling the curves on the graph.

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The data in the Landolt-Börnstein tables and the International Critical Tables, tabulated here, are listed as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. When the actual values of ρ_{273} for the samples used by the several investigators are not available, a datum value reported by Backlund (1961) ($\rho_{273} = 8.7 \times 10^{-6}$ ohm cm) is suggested for calculating values of electrical resistivity from these ratios. The value $\rho_{273} = 8.7 \times 10^{-6}$ ohm cm will be used for all data sets, except those investigations which measured ρ_{273} .

The Landolt-Börnstein tables list the sample used by Cleaves and Hiegel as an annealed polycrystalline specimen with less than 0.01% impurities. Their value for resistivity at 29°K was 9.71×10^{-6} ohm cm. The sample used by Meissner is reported as an annealed polycrystalline specimen with a very small amount of impurities present.

The Holborn (1919) sample contained 0.009% impurity and was heated to 500 °C for several minutes, then annealed at 380 °C for 3 hours.

Grüneisen and Goens (1927) report the following information about their iron samples: Iron 1 - double electrolytically refined, first hammered, then tempered; Iron 2 - electrolytically separated many crystals, technically "pure", not tempered; Iron 3 - electrolytic, hammered many times, tempered for one hour at 500°C.

Meissner and Voigt (1930) presented the same data as Meissner (1928).

Kannuluik (1931) used a 99.88% pure iron wire.

The samples used by Broom (1952) were 99.993% pure and were annealed at 600°C for two hours before measurements were made. The tabular values below are for resistivity measurements before deformation. Broom's graphs show the effect of deformation on resistivity.

Kemp, et al. (1956) made resistivity measurements on 2 mm diameter rods (99.9% purity) which were annealed at 750 °C for four hours in vacuo. White and Woods (1959) presented a table of smoothed values based on the Kemp, et al. (1956) work and the subsequent work of White and Woods (1959).

The iron wires used by Kondorsky (1958) were made from chemically pure material. The specimens were heated in a vacuum at 900°C for one hour and then cooled slowly within the furnace. The residual resistivity was 1.458 x 10^{-6} ohm cm.

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Electrical Resistivity of Iron Cryogenic Data Memorandum No. M-15

> Kemp, et al. (1959) used iron specimens, believed to be from the same material as that of Grüneisen and Goens which was described as follows: "Doubly refined electrolytic iron, not melted in vacuo but cut out of a precipitated plate, annealed at 950°C to remove H₂ then compressed to destroy the precipitation structure and reannealed in vacuo at 950°C". However, the residual resistivity found by Kemp, et al. indicates that the samples were not as pure as the ones used by Grüneisen and Goens. The Kemp samples were cut into the shape of bars and measurements were made without any further treatment. The values listed in the table below are for Kemp's second sample, a slightly modified bar with projections of the same iron as the sample on which the potential and thermometer connections were made.

Backlund (1961) used very pure iron bars (cross section of about 15 mm^2 and length of 100 mm) which were annealed at about 500 °C for 10 hours to remove the cold-work effects.

The iron specimen used by Semenenko and Sudovtsov (1962) was grown by distillation in vacuum in the form of a needle, having a grain size approximately equal to the specimen diameter. The purity of the sample was greater than 99.9% and compensation was made for the earth's magnetic field during the measurements. They give two equations to represent their data in the temperature ranges of their investigations:

- 1) for 1.23 to 4.2°K, $R/R_0 \circ_C = 3.9606 \times 10^{-3} + 3.1 \times 10^{-6}T + 1.10 \times 10^{-6}T^2$; and
- 2) for 14 to 20 °K, $R/R_0 \circ_c = 3.9606 \times 10^{-3} + 1.64 \times 10^{-6} T^2 + 4.02 \times 10^{-11} T^5$.

The values in the table below have been read from their graph.

Semenenko, et al.(1962) found "the residual resistance of the iron was $R(0^{\circ}K)/R(0^{\circ}C) = 3.9606 \times 10^{-3}$ in a compensated earth's field, for a measuring current of 150 mA; $R(0^{\circ}K) = 1.2595 \times 10^{-3} \Omega$. The temperature was determined accurate to $10^{-2} {}^{\circ}K$ from the helium vapor pressure". No information is given about the sample. They found the equation $R = 3.9606 \times 10^{-3} + 3.1 \times 10^{-6} T + 1.1 \times 10^{-6} T^2$ to represent their data.

The iron rectangular plate sample used by Soffer et al. (1965) was made from an ingot of zone-refined iron with a purity of 99.999815%. The sample was cold rolled and annealed to minimize strains. The sample size was 10 cm x 1 cm x 1 mm.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

Tables of Values of Electrical Resistivity

 ρ = Resistivity, (ohm cm)

 ρ_{273} = Resistivity at 273°K, (ohm cm)

Holborn (1919)					
Temp., °C	100R/R273	Temp., °C	100R/R ₂₇₃		
- 78.1 - 80 * -100 *	57.86 55.9 47.3	-192.7 -200 * -220 *	8.48 6.2 2.7		
-120 * -140 * -160 *	38.1 29.2 20.7	-240 * -253	1.4 1.13		
ł	* Values from interpolation				

Electrical Resistivity of Iron Cryogenic Data Memorandum No. M-15

	Grüneisen and Goens (1927)						
Sample Number	Р _{273.2} x 10 ⁶ ohm om	0 _{83.2} х 10 ⁶ оhm с m	ρ _{21.2} x 10 ⁶ ohm cm	ρ _{83.2} /ρ _{273.2}	P21.2/P273.2		
1	8.71	0.776	0.0681	0.0893	0.00782		
2	9.11	0.929	0.143,	0.1020	0.01120		
3	9•95	1.917	1.060	0.1927	0.01937		

Meissner and Voigt (1930) Meissner (1928)				
Temp. °K*	ρ/ρ ₂₇₃ **			
1.98† 4.21 20.40 78.24 273.16†	0.00618 0.00620 0.00761 0.0741 1.000			
* The second decimal place is in doubt.				
** The fifth decimal place is in doubt.				

† $\rho_{273} = 9.11 \times 10^{-6}$ ohm cm $\rho_{1,98} = 0.0563 \times 10^{-6}$ ohm cm

Kannuluik (1931)					
Temp. Temp. Specific Resistance ρ/ρ_{273} * °C °K $\rho \times 10^6$ ohm cm					
-183 - 78.5 0	90.15 194.65 273.15	1.531 5.74 9.57	0.160 0.600 1.00		
* These values were not plotted on the Electrical Resistivity of Iron graph.					

	Broom (1952)					
Temp. °C	Temp. °K	Resistivity px10 ⁶ ohm em	P/6272			
-183.0	90.15	1.09	0.120			
- 78.5	194.65	5.78	0.638			
0.0	273.15	9.06	1.000			
100.0	373.15	14.73	1.648			

	Kemp, Klemens, and White (1956) (read from graph)				
Temp. °K	"Ideal resistivity" $\rho_1 \ x \ 10^6 \ \text{ohm cm}$	Resistivity, $\rho \times 10^6$ ohm cm $\rho = \rho_1 + \rho_0$ where $\rho_0 = 2.48 \times 10^{-7}$ ohm cm	P/ P273		
16	0.010	0.258	0.0289		
23	0.014	0.262	0.0293		
30	0.028	0.276	0.0309		
35	0.041	0.289	0.0323		
40	0.050	0.298	0.0333		
58	0.19	0.438	0.0490		
80	0.45	0.698	0.0781		
100	0.98	1.228	0.137		
130	2.0	2.248	0.251		
200	5.0	5.248	0.587		
273	9.0	9.248	1.000		
293	10.0	10.248	1.146		

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Kondorsky, Galkina, and Tchernikova (1958) (read from graph)				
Temp. °K	Resistivity p x 10 ⁶ ohm cm	P/P273		
2 20 40 60 73	1.46 1.5 1.6 1.9 2.3	0.168 0.172 0.184 0.218 0.264		

Kemp, K	Kemp, Klemens, and Tainsh (1959)					
Temp.	Resistivity	P/ P273				
۰ĸ	px10 ⁶ ohm cm					
4.2 15.2 20.8 26.1 32.5	0.092 0.097 0.100 0.106 0.120	0.0103 0.0109 0.0112 0.0119 0.0134				
54.4 61.2 74.2 79.1 90.2 273.0* 293.0	0.269 0.368 0.631 0.744 1.06 9.27* 10.3	0.0301 0.0412 0.0706 0.0832 0.119 1.000 1.152				

* Interpolated value.

White and Woods (1959)				
Temp. °K	"Ideal Resistivity" ρ, x 10 ⁶ ohm cm	Resistivity, $\rho \ge 10^6$ ohm cm $\rho = \rho_1 + \rho_0$ where $\rho_0 = 0.095 \ge 10^{-6}$ ohm cm	P/ P273	
10	0.001 ₆	0.0965	0.0110	
15	0.0034	0.0984	0.0112	
20	0.007	0.102	0.0116	
25	0.012 ₆	0.1075	0.0122	
30	0.022	0.117	0.0133	
40	0.06 ₀	0.155	0.0176	
50	0.13 ₅	0.230	0.0262	
60	0.25	0.345	0.0392	
70	0.42	0.515	0.0586	
80	0.64	0.735	0.0836	
90	0.92	1.015	0.115	
100	1.24	1.335	0.152	
120	1.95	2.045	0.233	
140	2.73	2.825	0.321	
160	3.55	3.645	0.414	
180	4.4₀	4, 495	0.511	
200	5.3	5, 395	0.613	
220	6.2	6, 295	0.716	
250	7.5₅	7, 645	0.869	
273	8.7	8, 795	1.000	
295	9.8	9, 895	1.125	

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	Backlund (1961)				
	(read from graph	1)			
Temp. °K	Resistivity p x 10 ⁶ ohm cm	P/ P273			
90 195 273 293	1.1 5.1 8.7 9.8	0.123 0.570 1.000 1.096			

Semenenko a	and Sudovtsov (1962)
(read	d from graph)
Temp.	Resistance Ratio
°K	R /R ₀ °c
2.0	0.00397
4.0	0.00399
9.2	0.00410
12.0	0.00421
13.8	0.00430
16.0	0.00442
17.0	0.00450
20.0	0.0047!!

Semenenko, Sudovtsov and Shvets (1962) (read from graph)				
Temp. °K	Resistance R x 10 ⁶ ohm	R/R ₂₇₃ *		
0.38 1. 2. 3. 4. 273.0	1261.35 1263.9 1270.7 1279.6 1291.1 318000.	0.00396 0.00397 0.00399 0.00402 0.00406 1.000		
* These values are almost identical to the Semenenko and Sudovtsov (1962) values and are therefore not plotted on the Electrical Resistivity of Iron graph.				

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Soffer, Dreesen, and Pugh (1965) (read from graph)				
Temp. °K	Resistivity $\rho \ge 10^6$ ohm cm	ρ/ρ ₂₇₃ *		
77 112 169 231 273 300 * These the E Iron coinc plotta	0.6 1.8 4.0 6.9 8.94 10.7 values are not plue lectrical Resistiv graph because these ide with others pr- ed.	0.067 0.20 0.45 0.77 1.00 1.20 otted on ity of e points eviously		



CRYOGENIC DATA MEMORANDUM

FILE NO. M-16

ELECTRICAL RESISTIVITY OF LEAD, Pb (Atomic Number 82)

(page 1 of 5)

Sources of Data:

Landolt-Börnstein Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, sechste Auflage, II Band, 6 Teil, Springer-Verlag, Berlin, 1-46 (1959).

Aleksandrov, B. N., "Size Effect in Electrical Resistivity of High-Purity Metals," Soviet Phys. JETP <u>16</u>, No. 2, 286-94 (1963), Transl. of Zh. Eksperim. i Teor. Fiz. <u>43</u>, 399-410 (1962).

Aleksandrov, B. N., and D'Yakov, I. G., "Variation of the Electrical Resistance of Pure Metals with Decrease of Temperature," Soviet Phys. JETP <u>16</u>, No. 3, 603-08 (1963), Transl. of Zh. Eksperim. i Teor. Fiz. <u>43</u>, 852-59 (1962).

Bridgman, P. W., "The Resistance of 72 Elements, Alloys and Compounds to 100,000 kg/cm²," Proc. Am. Acad. Arts Sci. <u>81</u>, No. 4, 165-251 (1952).

Buckel, W., and Hilsch, R., "Einfluss der Kondensation bei tiefen Temperaturen auf den elektrischen Widerstand und den Supraleitung fur verschiedene Metalle," (Effect on the Electrical Resistance and Superconduction of Various Metals of Condensation at Low Temperatures), Z. Physik <u>138</u>, 109-20 (1954).

Meaden, G. T., Electrical Resistance of Metals, Plenum Press, New York (1965) 218 p.

Meissner, W., Ann. Physik (4) 47, 1001-58 (1915)

Onnes, H. K., and Clay, J., "On the Change of the Resistance of the Metals at Very Low Temperatures and the Influence Exerted on It by Small Amounts of Admixtures," Communs. Phys. Lab. Univ. Leiden No. 99c (1907).

Van der Leeden, P., "Geleiding van warmte en electriciteit door metalen," (Conduction of heat by metals), Gedrukt Bij Drukherig Waltman, Koornmarkt 62, Te Delft 11-76 (July 1940).

Other References:

Bridgman, P. W., "Miscellaneous Measurements of the Effect of Pressure on Electrical Resistance," Proc. Am. Acad. Arts Sci. <u>82</u>, No. 2, 83-100 (1953).

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Meissner, W., Ann. Physik (5) 13, 641 (1932).

Meissner, W., and Franz, H., Z. Physik 65, 30 (1930).

Onnes, H. K., and Tuyn, W., Communs. Kamerlingh Onnes Lab. Univ. Leiden Suppl. No. 58 (1926).

Onnes, H. K., and Tuyn, W., Communs. Kamerlingh Onnes Lab. Univ. Leiden No. 160b (1922).

Van den Berg, G. J., "The Electric Resistance of Potassium, Tungsten, Copper, Tin, and Lead at Low Temperatures," Physica <u>14</u>, 111-38 (Apr 1948), also Communs. Kamerlingh Onnes Lab. Univ. Leiden No. 274a (1948).

Comments:

The data for this graph were taken from the references cited above under "Sources of Data". The data listed in the Landolt-Börnstein tables are those reported by Meissner and Franz; Meissner; Onnes and Tuyn; and Van den Berg; listed above under "Other References". The original authors are used in labeling the curves on the graph.

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The curves on the graph should not be extrapolated to lower temperatures as lead becomes a superconductor at 7.22°K. It will be noted, however, that the data of Van den Berg; Aleksandrov and D'Yakov; and Meissner extend into the superconducting region. These data below the transition temperature were based on observations of the electrical resistance with the lead subjected to a super-critical magnetic field to maintain electrical resistance.

The data tabulated here are ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. When the actual values of p_{273} are not available for the samples used by the original investigators, a datum value reported by Aleksandrov and D'Yakov ($p_{273} = 19.2 \times 10^{-6}$ ohm cm) is suggested for calculating values of electrical resistivity from these ratios.

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The Landolt-Börnstein tables report the samples used by all of the investigators in their compilation as polycrystalline with a very small amount of impurities present.

Yaeger and Diesselhorst (1900) report the sample used in determining ρ_{273} as polycrystalline with less than 0.05% impurities. Their value at 273°K was 19.2 x 10⁻⁶ ohm cm.

The purity of the lead strip used by Onnes and Clay (1907) was 99.985%. No other information is given about the preparation of the sample. The values listed in the table below are resistances compared with the resistance at 0°C.

Meissner (1915) reported $\rho_{273} = 19.2_6 \times 10^{-8}$ ohm cm.

Van der Leeden (1940) used a polycrystalline lead wire (0.025 cm diameter) in his electrical resistivity measurements. The purity of the sample was not stated.

The purity of Bridgman's (1952) sample was 99.999%. His measurements show the effect of pressure on electrical resistivity at room temperature.

Buckel and Hilsch (1954) prepared metal layers for their measurement by low temperature condensation (4°K). They report only one measurement at 273°K of 19.9 x 10^{-6} ohm cm.

Aleksandrov (1962) used polycrystalline samples of 99.99964% purity. The samples were in the form of 0.5 to 2.5 mm diameter rods. He estimated the error to be << 1%. Measurements were made in a magnetic field of H = 540 Oe in addition to H = 0 at 4.2°K. He used $\rho_{273} = 19.3 \times 10^{-6}$ ohm cm.

Aleksandrov and D'Yakov (1962) used the same lead samples as Aleksandrov (1962). However, they did not reduce the diameters so much so that the resistance would be affected. The measurements for temperatures below 7.22°K were made in the presence of a magnetic field. Using a quadratic dependence of ρ on H, they obtained values of ρ for H = 0. Their $\rho_0 \approx 4 \times 10^{-10}$ ohm cm.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

Electrical Resistivity of Lead Cryogenic Data Memorandum No. M-16

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Tables of Values of Electrical Resistivity

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 ρ = resistivity, (ohm cm); R = resistance, (ohm);

Р 273 В	=	resistivity at 273°K,	(ohm cm).
1273	-	resistance at $2/3$ K,	(onm).

Onnes and Clay (1907)					
Temp.	Temp.	Resistance ratio			
°K	°C	R/R ₂₇₃			
14.39	-258.70	0.01311			
18.02	-255.07	0.02314			
20.31	-252.78	0.03032			
56.48	-216.61	0.17129			
68.57	-204.52	0.21742			
77.94	-195.15	0.25257			
89.44	-183.65	0.29439			
169.46	-103.63	0.59548			
273.09	- 0.0	1.000			
289.42	16.33	1.0652			

Meissner (1915)				
Temp. °K	p/p273			
21.8 91.7 273.1*	0.035 ₀ 0.303 1.000			
 * ρ₂₇₃ = 19.2₆ x 10⁻⁶ ohm cm. ** These values are not plotted on the Electrical Resistivity of Lead graph. 				

Onnes and Tuyn (1926)		Meissner an Meissner an	ner and Voigt (1930) mer and Franz (1930)		issner (1932)	
Temp* °K	R/R ₂₇₃	Temp* °K	R/R ₂₇₃	Temp. °K	R/R ₂₇₃	
7.26 14.32 20.52 73.11 88.56	0.0010 0.0113 0.0301 0.2321 0.2895	7.26 14.02 20.32 273.16	0.0007 0.0104 0.0292 1.0000	1.3 4.2	1.55 x 10 ^{-4**} 1.75 x 10 ^{-4**}	
 * The second decimal place of the temperature values is somewhat in doubt. ** These measurements were made with the aid of a supercritical magnetic field at temperatures at which lead is normally a superconductor. 						

	Van der Leeden (1940)				
Temp. °K	100R/R ₀ *	Temp. °K	100R/R ₀ *		
90.33 82.06 73.16 67.09 55.33	29.65 26.51 23.19 20.92 16.51	20.40 19.35 18.21 17.29 16.00 15.03 14.10	3.015 2.639 2.272 1.988 1.620 1.356 1.118		
* These values have not been plotted on the Electrical Resistivity of Lead graph.					

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Van den Berg (1948) Bridgman (1952)					
Temp* °K	R/R_{273}	(Resistance compared with the resistance at room temperature and one atmosphere pressure.)			
2.30 3.22	0.00013 † 0.00015 †	Pressure kg/cm ²	R/R _o	Pressure kg/cm ²	R/R _o
4.24 7.22 9.38 20.32	0.00019 f 0.00083 0.0025 0.0301	0 10000 20000 30000 40000 50000	1.000 0.873 0.779 0.704 0.647 0.603	60000 70000 80000 90000 100000	0.570 0.543 0.521 0.502 0.487
* The s ** The f some	second decimal p fifth decimal pl what in doubt.	lace of the temp ace of the elect	perature va prical resi	lues is somev stivity ratio	what in doubt.

[†] These measurements were made with the aid of a supercritical magnetic field at temperatures at which lead is normally a superconductor.

Aleksandrov (1962)					
Sample	Temp. °K	R/R ₂₉₃ †	R/R273 [†]		
Polycrystal H = 640 Oe	4.2	0.00007	80000.0		
Polycrystal H = O	4.2	0.000063	830000.0		
Polycrystal	20.4	0.00268	0.00290		
† $\rho_{293} = 20.9 \times 10^{-6}$ ohm cm and $\rho_{273} = 19.3 \times 10^{-6}$ ohm cm.					

	Aleksandrov and D'Yakov (1962)						
Temp. °K	R/R ₂₉₃	R/R ₂₇₃	Temp. °K	R/R₂⊕3	R/R ₂₇₃		
0.0 1.9 3.6 3.8 4.0 4.22 4.46	$\begin{array}{c} 1.9 \times 10^{-5} \\ 2.15 \times 10^{-5} \\ 3.8 \times 10^{-5} \\ 4.52 \times 10^{-5} \\ 5.3 \times 10^{-5} \\ 6.28 \times 10^{-5} \\ 7.8 \times 10^{-5} \\ \end{array}$	$\begin{array}{c} 2.1 & \times 10^{-5} \\ 2.33 \times 10^{-5} \\ 4.1 & \times 10^{-5} \\ 4.90 & \times 10^{-5} \\ 5.7 & \times 10^{-5} \\ 6.80 & \times 10^{-5} \\ 8.4 & \times 10^{-5} \end{array}$	7.2 14.0 20.4 58.0 77.4 90.31 273.0	6.3 x 10 ⁻⁴ † 9.5 x 10 ⁻³ 0.027 0.106 0.230 0.272 0.917	$\begin{array}{c} 6.8 \times 10^{-4} \\ 10.3 \times 10^{-3} \\ 0.029 \\ 0.180 \\ 0.249 \\ 0.295 \\ 1.00 \end{array}$		
* Usir Alek † Meas	 * Using p₂₉₃ = 20.9 x 10⁻⁶ ohm cm and p₂₇₃ = 19.2 x 10⁻⁶ ohm cm from Aleksandrov (1962). † Measurements below 7.22°K were made in the presence of a magnetic field. 						


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CRYOGENIC DATA MEMORANDUM

PROJECT NO. 3150123

FILE NO. M-17

ELECTRICAL RESISTIVITY OF MAGNESIUM, Mg (Atomic Number 12)

(page 1 of 5)

Sources of Data:

Landolt-Börnstein Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, sechste Auflage, II Band, 6 Teil, Springer-Verlag, Berlin, 1-46 (1959).

International Critical Tables of Numerical Data, Physics, Chemistry, and Technology, VI, 1st Edition, Published for the National Research Council by the McGraw-Hill Book Co., Inc., 124-35 (1929).

Bridgman, P. W., "The Resistance of 72 Elements, Alloys and Compounds to 100,000 kg/cm²," Proc. Am. Acad. Arts Sci. <u>81</u>, No. 4, 165-251 (1952).

Goens, E., and Schmid, E., "Elastische Konstanten, electrischer Widerstand und thermische Ausdehnung des Magnesiumkristalls," (Elastic Constants, Electrical Resistance and Thermal Expansion of Magnesium Crystals), Physik. Z. <u>37</u>, 385-91 (1936).

Grüneisen, E., "Elektrische Leitfahigkeit der Metalle bei tiefen Temperaturen," (Electrical Conductivity in Metals at Low Temperatures), Ergebn. exakt. Naturw. <u>21</u>, 50-116 (1945).

Hein, R. A., and Falge, R. L., "Resistance Minimum of Magnesium: Electrical Resistivity Below 1°K," Phys. Rev. <u>105</u>, 1433-34 (1957).

Meaden, G. T., Electrical Resistance of Metals, Plenum Press, New York (1965) 218 p.

Spohr, D. A., and Webber, R. T., "Resistance Minimum of Magnesium: Electrical and Thermal Resistivities," Phys. Rev. <u>105</u>, 1427-33 (1957).

Other References:

Bridgman, P. W., "Electrical Resistance Under Pressure, Including Certain Liquid Metals," Proc. Am. Acad. Arts Sci. 56, 61-154 (1921).

Bridgman, P. W., "The Electric Resistance to 30,000 kg/cm² of Twenty Nine Metals and Intermetallic Compounds," Proc. Am. Acad. Arts Sci. <u>79</u>, 149-79 (1951).

Das, K. B., and Gerritsen, A. N., J. Appl. Phys. 33, 3301 (1962).

Dewar, J., and Fleming, J. A., Phil. Mag. (5) 36, 271 (1893).

Kan, L. S., and Lazarev, B. G., "On the Resistance Minimum of Magnesium at Low Temperatures," Akad. Nauk. SSSR Doklady 81, 1027-29 (1951).

MacDonald, D. K. C., and Mendelssohn, K., Proc. Roy. Soc. (London) A202, 523-33 (1950).

Meissner, W., and Voigt, B., "Messungen mit Hilfe von flüssigem Helium. XI. Widerstand der reinen Metalle in tiefen Temperaturen," (Measurements with the Help of Liquid Helium. XI. Resistance of Pure Metals at Low Temperatures), Ann. Physik (5) 7, 761-97 (1930).

Niccolai, G., "Über den elektrischen Widerstand der Metalle zwischen sehr höhen und sehr tiefen Temperaturen," (Concerning the electrical resistance of metals between very high and very low temperatures), Physik. Z. 9, 367 (1908).

Nichols, J. L., J. Appl. Phys. 26, 470 (1955).

Rorschach, H. E., and Herlin, M. A., "The Resistance Minimum in Magnesium at Low Low Temperatures," Phys. Rev. <u>87</u>, 193 (Jul 1952).

Rosenberg, H. M., "The Thermal and Electrical Conductivity of Magnesium at Low Temperatures," Phil. Mag. <u>45</u>, 73-9 (1954).

Stager, R. A., and Drickamer, G. H., "Effect of Temperature and Pressure on the Electrical Resistance of Four Alkaline Earth Metals," Phys. Rev. <u>131</u>, No. 6, 2524-27 (1963).

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Yntema, G. B., "Magnetoresistance of Mg, Cu, Sb, and Al at Liquid Helium Temperatures," Phys. Rev. <u>91</u>, 1388-94 (Sept 1953).

Comments:

The data for this graph were taken from the references cited above under "Sources of Data" and are listed as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. Since magnesium is an anisotropic metal, we list suggested values of ρ_{273} for Mg||, MgL, and polycrystalline magnesium to be used in calculating electrical resistivity from these

ratios. These values are: and $p_{(1)_{273}} = 3.48 \times 10^{-6} \text{ ohm cm}, \quad p_{(1)_{273}} = 4.18 \times 10^{-6} \text{ ohm cm},$ $p_{(1)_{273}} = 4.18 \times 10^{-6} \text{ ohm cm},$

These values are from Grüneisen (1945).

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The values listed in the Landolt-Börnstein tables are those reported by Meissner and Voigt; Niccolai: Rosenberg; and Yntema; while those values listed in the International Critical Tables are from Dewar and Fleming. Those primary sources are listed above under "Other References". The original authors are used in labeling the curves on the graph.

The sample used by Meissner and Voigt is reported by Landolt-Börnstein as polycrystalline and annealed in a vacuum at 250°C for 2.5 hours. The sample used by Yntema was of a polycrystalline nature with less than 0.02% impurities present. The Yntema sample was also annealed but no mention is made of conditions. The sample used by Niccolai was reported as polycrystalline with very few impurities present. Rosenberg's sample was a 1.5 mm diameter rod (99.95% pure) which was annealed in vacuo at 500°C for six hours.

The Goens and Schmid (1936) measurements were made with cylindrical shaped single crystals which were grown from the melt of 99.95% pure starting material. Only two resistivity values are given for a temperature of 18.0°C:

 $\begin{array}{l} \rho_{\parallel 1} = 3.77_{\textrm{B}} \times 10^{-6} \ \textrm{ohm cm and} \\ \rho_{\perp} = 4.53_{\textrm{O}} \times 10^{-6} \ \textrm{ohm cm.} \end{array}$

Grüneisen (1945) uses Goens and Schmid's data to determine the resistivity values at 0°C:

$$\rho_{\parallel} = 3.48 \times 10^{-6}$$
 ohm cm and
 $\rho_{\perp} = 4.18 \times 10^{-6}$ ohm cm

and by averaging the two using Voigt's equation, he calculates for the quasiisotrope:

$\rho_{273} = 3.94 \times 10^{-6}$ ohm cm.

Bridgman (1952) measured the effect of pressure on electrical resistivity. His sample was from "old single crystal stock" rolled to a thickness of 0.002 inch with widths varying from 0.013 to 0.039 inch.

Spohr and Webber (1957) measured the resistivity of two specimens in the shape of rods about 9 cm long and 3 mm in diameter. The first specimen Mg(Fe) was 99.984 % pure with iron as the major contaminant and the second Mg(Mn) was 99.954 % pure with manganese as the only significant contaminant. Prior to measurements Mg(Fe) was cold-worked and Mg(Mn) was annealed for 24 hours at 300°C and rapidly quenched in water at 40°C. The data in the table below have been read from their graph.

Hein and Falge (1957) extended the measurements of Spohr and Webber to temperatures below l^{κ} . They used the same specimens, Mg(Fe) and Mg(Mn). The values in the table below were taken from their graph.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

Tables of Values of Electrical Resistivity

$$\rho$$
 = Resistivity, (ohm cm)

 ρ_{273} = Resistivity at 273°K, (ohm cm)

Dewar and F	leming (1893)	Meissner and	Voigt (1930)	Yntem	a (1953)
Temp. °C	100 p/p ₂₇₃	Temp.** °K	R/R ₂₇₃	Temp. °K	R/R ₂₇₃
- 78.3* - 80 -100 -120 -140 -160 -180 -182.9*	68.2* 67.4 59.0 50.5 41.9 33.2 24.4 23.0*	1.27 † 3.16 4.20 20.46 77.61 88.19 273.16 †	0.0329 0.0326 0.0323 0.0344 g 0.1576 0.2006 1.0000	1.30 4.21	0.00537 0.00516
* Results of actual observations. All other values from interpolations. ** The second decimal place is in doubt. † $\rho_{273} = 5.00 \times 10^{-6}$ ohm cm; $\rho_{1,27} = 0.164 \times 10^{-8}$ ohm cm.					

Temp.	Temp.	Resistance Ratio, R/Ro*	
°C	°K	Mgli	Mgi
+100	373.15	1.429	1.421
0	273.15	1.000	1.000
-183.1	90.05	0.182,	0.1796
-195.25	77.90	0.1319	0.127
-252.8	20.35	0.0010	0.001

(page 4 of 5)

Electrical Resistivity of Magnesium Cryogenic Data Memorandum No. M-17

	Rosenberg (1954)		
	Temp. °K	ρ/ρ ₂₇₃	
	2.5 5 10	0.00630* 0.00623* 0.00632*	
	15 25	0.0068 0.0096	
*	The fifth decimal place is in doubt.		

Bridgman (1952)			
(Resistance compared to resistance at room temperature and one atmosphere pressure.)			
Pressure kg/cm ²	r/r _o	Pressure kg/cm ²	r/r _o
0 10000 20000 30000 40000 50000	1.000 0.953 0.916 0.886 0.859 0.837	60000 70000 80000 90000 100000	0.817 0.800 0.786 0.776 0.767

Temp.Resistivity, $\circ \times 10^{8}$ ohm cm ρ/ρ_{273} °KMg(Fe)Mg(Mn)Mg(Fe)Mg(N1 6.624 14.79 0.0168 0.01 3 6.50 13.21 0.0165 0.01 5 6.46 12.70 0.0164 0.01	
°K Mg(Fe) Mg(Mn) Mg(Fe) Mg(N 1 6.624 14.79 0.0168 0.01 3 6.50 13.21 0.0165 0.01 5 6.46 12.70 0.0164 0.01	
1 6.624 14.79 0.0168 0.01 3 5.50 13.21 0.0165 0.01 5 6.45 12.70 0.0164 0.01	(Mn)
$ \begin{vmatrix} 7 & 6.47 & 12.24 & 0.0164 & 0.03 \\ 10 & 5.53 & 12.00 & 0.0166 & 0.03 \\ \end{vmatrix} $	0375 03 3 5 0322 0311 0305
12 6.61 11.90 0.0166 0.03 15 6.78 11.87 0.0172 0.03 17 6.95 11.95 0.0176 0.03 20 7.25 12.20 0.0184 0.03 22 12.40 0.01 0.01	0302 0301 0303 0310 0315

	Hein and Falge (1957) *				
Temp.	Resistivity, $\rho \ge 10^8$ ohm cm		ρ/ρ273		
°К	Mg(Fe)	Mg(Mn)	Mg(Fe)	Mg(Mn)	
0.2 0.4 0.8 1.2 1.6 2.0	6.92 6.86 6.75 6.70 6.66 6.60	16.90 16.40 15.66 15.18 14.78 14.48	0.0176 0.0174 0.0171 0.0170 0.0170 0.0169 0.0168	0.0429 0.0416 0.0397 0.0385 0.0375 0.0368	
2.4 2.8 3.2 3.6 4.0	6.60 6.59 6.59 6.58 6.58	14.20 13.96 13.72 13.60 13.48	0.0168 0.0167 0.0167 0.0167 0.0167 0.0167	0.0360 0.0354 0.0348 0.0345 0.0342	
* read	* read from graph.				



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CRYOGENIC DATA MEMORANDUM

ELECTRICAL RESISTIVITY OF MOLYBDENUM, Mo (Atomic Number 42)

(page 1 of 4)

Sources of Data:

International Critical Tables of Numerical Data, Physics, Chemistry, and Technology, VI, 1st Edition, Published for the National Research Council by the McGraw-Hill Book Co., Inc., 124-35 (1929).

Landolt-Börnstein Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, sechste Auflage, II Band, 6 Teil, Springer-Verlag, Berlin, 1-46 (1959).

Holmwood, R. A., and Glang, R., "Resistivity and Temperature Coefficient of Pure Molybdenum," J. Chem. Eng. Data <u>10</u>, 162-3 (1965).

Kannuluik, W. G., "The Thermal and Electrical Conductivities of Several Metals Between -183°C and 100°C," Proc. Roy. Soc. (London) <u>A141</u>, 159-68 (1931).

McLennan, J. C., Howlett, L. E., and Wilhelm, J. O., "On the Electrical Conductivity of Certain Metals at Low Temperatures," Trans. Roy. Soc. (Canada) <u>23</u>, 287-306 (1929).

Meaden, G. T., Electrical Resistance of Metals, Plenum Press, New York (1965) 218 p.

White, G. K., and Woods, S. B., "Electrical and Thermal Resistivity of the Transition Elements at Low Temperatures," Phil. Trans. Roy. Soc. (London) <u>A251</u>, 273-302 (1959).

Other References:

Elom, E. C., "Temperature Coefficient of Resistance of Molybdenum," Phys. Rev. 13, 308 (1919).

Bridgman, P. W., "The Electric Resistance to 30,000 kg/cm² of Twenty Nine Metals and Intermetallic Compounds," Proc. Am. Acad. Arts Sci. <u>79</u>, 149-79 (1951).

Goree, W. S., "Electrical Conductivity of Metals at High Pressures and Low Temperatures," Univ. of Florida, Gainesville, Ph.D. Thesis (1964), (Avail. from Univ. Microfilms, Ann Arbor, Mich., Order No. 65-5985).

Holborn, L., Ann. Physik 59, 145 (1919).

Meissner, W., Physik. Z. 29, 897-904 (1928).

Meissner, W., and Voigt, B., "Messungen mit Hilfe von flüssigem Helium. XI. Widerstand der reinen Metalle in tiefen Temperaturen," (Measurements with the Help of Liquid Helium. XI. Resistance of Pure Metals at Low Temperatures), Ann. Physik 7, 892-936 (1930).

Northcott, L , Molybdenum, Butterworths, London (1956)

Taylor, R. E., and Finch, R. A., "The Specific Heats and Resistivities of Molybdenum, Tantalum, and Rhenium from Low to Very High Temperatures," North Am. Aviation Inc., Atomics Intern. Div., Canoga Park, Calif., NAA-SR-6034 (1961) Contr. AT(11-1)-Gen-8, 32 pp.

Taylor, R. E., and Finch, R. A., "The Specific Heats and Resistivities of Molybdenum, Tantalum, and Rhenium," J. Less Common Metals <u>6</u>, No. 4, 283-94 (Apr 1964).

Tye, R. P., "Preliminary Measurements on the Thermal and Electrical Conductivities of Molybdenum, Niobium, Tantalum and Tungsten," J. Less Common Metals <u>3</u>, No. 1, 13-18 (Feb 1961).

Volkenshtein, N. V., Romanov, E. P., Starostina, L. S., et al., "Temperature Dependence of Electric Resistance of Molybdenum Single Crystals," Fiz. Metal. 1 Metalloved <u>17</u>, No. 4, 627-9 (1964).

Volkenshteyn, N. V., Starostina, L. S., Startsev, V. Ye., and Romanov, Ye. P., "Temperature Dependence of the Low-Temperature Electrical Conductivity of Molybdenum and Tungsten Single Crystals," Phys. Metals Metallog. <u>18</u>, 85-90 (1964), Transl. of Fiz. Metal. i Metalloved. <u>18</u>, No. 6, 888-94 (1964).

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(page 2 of 4)

Worthing, A. G., "Physical Properties of Well Seasoned Molybdenum and Tantalum as a Function of Temperature," Phys. Rev. 28, 190-201 (1920).

Comments:

The data for this graph were taken from the references cited above under "Sources of Data" and are listed as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. When the actual values of ρ_{273} for the samples used by the several investigators are not available, a datum value reported by Holmwood and Glang ($\rho_{273} = 5.0 \times 10^{-6}$ ohm cm) is suggested for calculating values of electrical resistivity from these ratios.

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The values listed in the Landolt-Börnstein tables are those reported by Meissner and Voigt; and Blom; while the values listed by the International Critical Tables are from Holborn. The samples used by both authors are listed as polycrystalline with no mention made of impurities present. No reference is made as to the nature of the sample used by Holborn, and no information is available on mechanical strain or heat treatment for any of the samples from any of the above sources of data. Meissner Voigt gave $p_{273} = 5.22 \times 10^{-6}$ ohm cm. Blom gave $p_{273} = 4.4 \times 10^{-6}$ ohm cm.

The McLennan et al. (1929) wire sample was "baked in vacuo at a high temperature for a number of hours" prior to measurement. They do not list the purity of the sample.

Kannuluik (1931) used a 99.83% pure wire sample.

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The three samples used by White and Woods (1959) were 99.9% pure wires. One sample was vacuum annealed at 1350°C prior to measurement, but the other two were not given any further treatment. The tabular data are smoothed values obtained from large-scale graphs.

Holmwood and Glang (1965) measured the resistivity of a 99.999% molybdenum bar, zone purified in vacuum and nearly single crystalline.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

Tables of Values of Electrical Resistivity

- ρ = Resistivity, (ohm cm)
- ρ_{273} = Resistivity at 273°K, (ohm cm)
 - = Resistance, (ohm)
- R_{273} = Resistance at 273°K, (ohm)

Holborn (1919)		
Temp. °C	100R/R ₂₇₃	
- 78.2 - 80* -100* -120*	66.60 65.9 57.4 48.9	
-140* -160* -180* -192.5	40.5 32.2 24.2 19.11	
* Values from interpolation		

Mc Lennan, Howlett	t, and Wilhelm (1929)
Temp. °K	Resistance Ratio R/R _O •c
2.3 4.2 20.6 84.1	0.079 0.079 0.079 0.079 0.206
273.1 298.6	1.00

Electrical Resistivity of Molybdenum Cryogenic Data Memorandum No. M-18

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Meissner and Voigt (1930)		
Temp. °K	p/ p ₂₇₃ *	
1.5 4.2 20.4 77.8 86.9 273.16	0.0462* 0.0455 0.0448 0.1370 0.1701 1.0000	
* ρ ₂₇₃ = 5.22 x 10 ⁻⁶ ohm cm; ρ _{1.6} = 0.241 x 10 ⁻⁶ ohm cm.		

Kannuluik (1931)				
Sample	Temp. °C	Temp. °K	Specific Resistance ρ x 10 ⁶ ohm cm	р/р ₂₇₃
Mo l	-183.0	90.15	0.952	0.181
	- 78.5	194.65	3.39	0.646
	0.	273.15	5.25	1.00
	100.	373.15	7.67	1.46
Mo 2	-183.0	90.15	0.882	0.171
	78.5	194.65	3.33	0.644
	0.	273.15	5.17	1.00
	100.	373.15	7.56	1.46

	White and Woods (1959)			
Temp. °K	"Ideal resistivity" $\rho_1 \propto 10^6$ ohm cm	Resistivity, $\rho \times 10^{6}$ ohm cm $\rho = \rho_{1} + \rho_{0}$ where $\rho_{0} = 0.227 \times 10^{-6}$ ohm cm	р/ р ₂₇₃	
25	$0.00^{4_{6}}$	0.232	0.0458	
30	0.01_{2}	0.239	0.0472	
40	$0.0^{4_{7}}$	0.274	0.0541	
50	0.11_{3}	0.340	0.0671	
60	0.21_{6}	0.443	0.0874	
70	0.354	0.581	0.1147	
80	0.515	0.742	0.1464	
90	0.714	0.941	0.1857	
100	0.92	1.147	0.2264	
120	1.36	1.587	0.3132	
140	1.8 ₂	2.047	0.4040	
160	2.2 ₇	2.497	0.4928	
180	2.1 ₃	2.957	0.5836	
200	3.1 ₈	3.407	0.6724	
220	3.64	3.867	0.7632	
250	4•32	4.547	0.8974	
273	4•84	5.067	1.0000	
295	5•33	5.557	1.0967	

Holmwood and Glang (1965)			
Temp. °C	Temp. °K	Resistivity* $\rho \ge 10^6$, ohm cm	
-196 0 25 50 75 100	77.15 273.15 298.15 323.15 348.15 373.15	0.486 5.00 5.57 6.17 6.78 7.40	
* These values are not plotted on the Electrical Resistivity of Molybdenum graph.			

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CRYOGENIC DATA MEMORANDUM

PROJECT NO. 3150123

FILE NO. M-19

ELECTRICAL RESISTIVITY OF NICKEL, Ni (Atomic Number 28) (page 1 of 5)

Sources of Data:

International Critical Tables of Numerical Data, Physics, Chemistry, and Technology, VI, 1st Edition, Published for the National Research Council by the McGraw-Hill Book Co. Inc., 124-35 (1929).

Landolt-Börnstein Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, sechste Auflage, II Band, 6 Teil, Springer-Verlag, Berlin, 1-46 (1959).

Broom, T., "The Effect of Temperature of Deformation on the Electrical Resistivity of Cold-Worked Metals and Alloys," Proc. Phys. Soc. (London) B65, 871-81 (1952).

Greig, D., and Harrison, J. P., "The Low Temperature Electrical Transport Properties of Nickel and Dilute Nickel-Copper Alloys," Phil. Mag. <u>12</u>, No. 115, 71-79 (1965).

Kemp, W. R. G., Klemens, P. G., and White, G. K., "Thermal and Electrical Conductivities of Iron, Nickel, Titanium, and Zirconium at Low Temperatures," Australian J. Phys. 9, 180-88 (1956).

Kondorsky, E., Galkina, O. S., and Tchernikova, L. A., "Nature of Electrical Resistivity of the Ferromagnetic Metals at Low Temperatures," J. Appl. Phys. <u>29</u>, No. 3, 243-6 (1958), also Zh. Eksperim. 1 Teor. Fiz. 34, No. 5, 1070-6 (1958).

Meaden, G. T., Electrical Resistance of Metals, Plenum Press, New York (1965) 218 p.

Meissner, W., and Voigt, B., "Messungen mit Hilfe von flussigem Helium, XI. Widerstand der reinen Metalle in tiefen Temperaturen," (Measurements with the Help of Liquid Helium, XI. Resistance of Pure Metals at Low Temperatures), Ann. Physik (5) 7, 892 (1930).

Sudovtsov, A. I., and Semenenko, E. E., "Peculiarities of the Temperature Dependence of the Electrical Resistance of Ferromagnetic Metals at Low Temperatures," Zh. Eksptl. i Teor. Fiz. <u>31</u>, 525 (1956), Soviet Phys. JETP <u>4</u>, 592 (1957).

White, G. K., and Woods, S. B., "Electrical and Thermal Resistivity of the Transition Elements at Low Temperatures," Phil. Trans. Roy. Soc. (London) <u>A251</u>, 273-302 (1959).

Other References:

Bridgman, P. W., "The Electric Resistance to 30,000 kg/cm² of Twenty Nine Metals and Intermetallic Compounds," Proc. Am. Acad. Arts Sci. <u>79</u>, 149-79 (1951).

Dewar, J., Proc. Roy. Soc. (London) 73, 244 (1904).

Fleming, J. A., Proc. Roy. Soc. (London) 66, 50 (1900).

Grüneisen, E., "Elektrische Leitfahigkeit der Metalle bei tiefen Temperaturen," (Electrical Conductivity of Metals at Low Temperatures), Ergebn. exakt. Naturw. <u>21</u>, 50-116 (1945).

Meissner, W., Physik. Z. 27, 725 (1926).

Mott, N. F., "Resistance and Thermoelectric Properties of Transition Metals," Proc. Roy. Soc. (London) <u>A156</u>, 368-82 (1936).

Schwerer, F.C., and Silcox, J., "Electrical Resistivity of Nickel at Low Temperatures," Phys. Rev. Letters 20, No. 3, 101-3 (Jan 1968).

Volvick, G., "Influence de la pression d'un gaz neutre sur la resistance d'un fil de nickel," (Effect of the Pressure of a Neutral Gas on the Resistance of Nickel Wire), Compt. Rend. <u>252</u>, 1285-87 (1961).

Wise, E. M., Proc. Inst. Radio Engrs. 25, 714 (1937).

Comments:

The data for this graph were taken from the references cited above under "Sources of Data" and are presented here as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273° K. When the actual values of ρ_{273} for the samples used by the several investigators are not available, a datum value reported by White and Woods (1959) ($\rho_{273} = 6.23 \times 10^{-6}$ ohm cm) is suggested for calculating values of electrical resistivity from these ratios.

(page 2 of 5)

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The values listed in the Landolt-Bornstein tables are those reported by Meissner and Wise; while those values appearing in the International Critical Tables are from Dewar and Fleming. These primary references are cited above under "Other References". The original authors are used in labeling both curves on the graph.

The Landolt-Bornstein tables list the sample used by Wise as polycrystalline with 0.01% impurities of unknown composition. A value of 6.14×10^{-6} ohm cm was reported by Wise for 273°K. The sample used by Meissner is reported as polycrystalline and was annealed in a hydrogen atmosphere.

Meissner and Voigt (1930) report the same data as Meissner (1926).

Broom's sample (1952) was 99.8% pure nickel wire and was annealed for two hours at 600 °C before measurements were made. The values in the table below were before deformation.

The purity of the nickel sample used by Kemp, et al. (1956) was greater than 99.9%. The sample was in the form of a 2 mm diameter rod which was annealed four hours in vacuo at 750 °C prior to measurement.

The Sudovtsov and Semenenko (1957) paper available to us was the Russian version and therefore I could not find out anything about the sample.

The nickel wires used by Kondorsky et al. (1958) were made from chemically pure material. The specimens were heated in a vacuum at 900 °C for one hour and then cooled slowly within the furnace. The residual resistivity was 0.20 x 10^{-6} ohm cm.

White and Woods (1959) used 99.997% pure nickel rods which were annealed in vacuo at 800°C prior to measurement. These smoothed tabular values were read from a large-scale graph.

Greig and Harrison (1965) used 99.998% pure nickel rod with 2 mm diameter which had been annealed for 12 hours at 850°C. The values in the table below were read from their graph.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

Tables of Values of Electrical Resistivity

 ρ = Resistivity, (ohm cm)

 ρ_{273} = Resistivity at 273°K, (ohm cm)

Temp. °C	Temp. °K	100 p/ p27 3	Temp. °C	Temp. °K	100 9/ P273
- 78.3	194.85	61.3	-180 †	93.15	21.7
- 80 †	193.15	60.5	-182.9	91.25	20.8
-100 †	173.15	51.8	-200 †	73.15	15.6-
-120 †	153.15	43.7	-220 †	53.15	11.2
-140 †	133.15	36.1	-240 †	33.15	8.9
-160 †	113.15	28.7	-252.7	20.45	8.5

Electrical Resistivity of Nickel Cryogenic Data Memorandum No. M-19

Meissner a	Meissner and Voigt (1930)		
Meissn	Meissner (1926)		
Temp.* R/R ₂₇₃ ** °K			
1.34†	0.00503		
4.21	0.00508		
20.40	0.00662		
78.8	0.0919		
87.4	0.1179		
273.16†	1.0000		
* The second decimal place is in doubt. ** The fifth decimal place is in doubt. † $\rho_{1.34} = 0.035 \times 10^{-6}$ ohm cm. $\rho_{273} = 7.07 \times 10^{-6}$ ohm cm.			

Broom (1952)				
Temp. °C	Temp. °K	Resistivity p x 10 ⁶ ohm cm	P/ P273	
-183.0	90.15	1.77	0.24	
- 78.5	194.65	4.59	0.62	
0.0	273.15	7.37	1.00	
100.0	373.15	11.56	1.57	

(read from graph)				
Temp. °K	"Ideal Resistivity" p _i xlo ⁶ ohm em	Resistivity, $\rho \ge 10^6$ ohm cm $\rho = \rho_1 + \rho_0$ (where $\rho_0 = 0.0347 \ge 10^{-6}$ ohm cm)	P, P273	
12	0.0043	0.0390	0.0063	
15	0.0055	0.0402	0.0065	
17	0.0075	0.0422	0.0068	
27	0.024	0.0587	0.0095	
38	0.066	0.101	0.0163	
57	0.20	0.235	0.0379	
78	0.45	0.485	0.0782	
110	1.3	1.33	0.215	
160	2.5	2.53	0.408	
293	7.2	7.22*	1.166	

Sudovtsov and Semenenko (1957) (read from graph)		
Temp. R/R ₂₇₃ °K		
1.2	0.010105	
1.6	0.010108	
2.0		
2.6	0.010120	
3.0	0.010125	
3.6	0.010136	
4.0	0.010144	
4.2	0.010148	

Kondorsky, Galkina and Tchernikova (1958) (read from graph)			
Temp. °K	p/p273		
2 20 40 60 73	0.20 0.25 0.35 0.50 0.71	0.032 0.040 0.056 0.081 0.11	

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Electrical Resistivity of Nickel Cryogenic Data Memorandum No. M-19

White and Woods (1959)			
Temp. °K	"Ideal Resistivity" p; x 10 ⁶ ohm cm	Resistivity, $\rho \propto 10^6$ ohm cm $\rho = \rho_1 + \rho_0$ (where $\rho_0 = 0.0280 \times 10^{-8}$ ohm cm)	р/ Р ₂₇₃
15	0.0045	0.0325	0.0052
20	0.009	0.037	0.0059
25	0.017	0.045	0.0072
30	0.030	0.058	0.0093
40	0.073	0.101	0.0162
50	0.15	0.178	0.0286
60	0.24 ₅	0.273	0.0438
70	0.38	0.408	0.0655
80	0.55	0.578	0.0928
90	0.75	0.778	0.125
100	1.00	1.028	0.165
120	1.46	1.488	0.239
140	1.97	1.998	0.321
160	2.52	2.548	0.409
180	3.10	3.128	0.502
200	3.7_2	3.748	0.602
220	4.3_6	4.388	0.705
250	5.4_0	5.428	0.872
273	6.2_0	6.228	1.00
295	7.0_4	7.068	1.13

Greig and Harrison (1965) (read from graph)				
Temp.Resistivity $\rho/\rho_{27.3}$ °K $\rho \ge 10^6$ ohm cm				
7.5	0.001	0.00016		
10.05	0.002	0.00032		
15.05	0.005	0,00081		
21.0	0.01	0.0016		
26.0	0.02	0.0032		
35.0	0.05	0.0081		



CRYOGENIC DATA MEMORANDUM

PROJECT NO. 3150123

ELECTRICAL RESISTIVITY OF NIOBIUM, Nb (Atomic Number 41)

(page 1 of 4)

Sources of Data:

Landolt-Börnstein Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, sechste Auflage, II Band, 6 Teil, Springer-Verlag, Berlin, 1-46 (1959).

Bridgman, P. W., "The Resistance of 72 Elements, Alloys and Compounds to 100,000 kg/cm²," Proc. Am. Acad. Arts Sci. <u>81</u>, No. 4, 165-251 (1952).

Meaden, G. T., <u>Electrical Resistance of Metals</u>, Plenum Press, New York (1965) 218 p.

White, G. K., and Woods, S. B., "Low Temperature Resistivity of Transition Elements: Vanadium, Niobium, and Hafnium," Can. J. Phys. <u>35</u>, 892-900 (1957).

White, G. K., and Woods, S. B., "Electrical and Thermal Resistivity of the Transition Elements at Low Temperatures," Phil. Trans. Roy. Soc. (London) <u>A251</u>, No. 995, 273-302 (1959).

Other References:

Argent, B. B., and Milne, G. J. C., "The Physical Properties of Niobium, Tantalum, Molybdenum and Tungsten," J. Less Common Metals <u>2</u>, 154-62 (1960).

Bridgman, P. W., "The Electric Resistance to 30,000 kg/cm² of Twenty Nine Metals and Intermetallic Compounds," Proc. Am. Acad. Arts Sci. <u>79</u>, 149-79 (1951).

Mc Lennan, J. C., Howlett, L. E., and Wilhelm, J. O., "On the Electrical Conductivity of Certain Metals at Low Temperatures," Trans. Roy. Soc. Can. Sect. III, <u>23</u>, 287-306 (1929).

Meissner, W., Franz, H., and Westerhoff, H., Ann. Physik (5) 17, 593 (1933).

Potter, H. H., "Electrical Resistance and Thermoelectric Power of the Transition Metals," Proc. Phys. Soc. (London) 53, 695-705 (1941).

Reimann, A. L., and Grant, K., Phil. Mag. (7) 22, 34 (1936).

Tye, R. P., "Preliminary Measurements on the Thermal and Electrical Conductivities of Molybdenum, Niobium, Tantalum and Tungsten," J. Less Common Metals <u>3</u>, No. 1, 13-18 (1961).

Comments:

The data presented here were taken from the references cited above under "Sources of Data" and are listed as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. The value of the electrical resistivity at 273°K (ρ_{273}) for niobium to be used in calculating values of electrical resistivity (ρ) is 13.96 x 10⁻⁶ ohm cm from White and Woods (1959). These data should not be extrapolated to lower temperatures as niobium becomes a superconductor at about 9.3°K.

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The values listed in the Landolt-Börnstein tables are those reported by Meissner, Franz and Westerhoff; and Reimann and Grant, cited above under "Other References". The Landolt-Börnstein tables list the samples used by Meissner, et al. as polycrystalline with 0.08% O_2 and 0.02% Ta impurities present. No other pertinent information is given about either of the samples. Reimann and Grant reported a value of $\rho_{273} = 16.1 \times 10^{-6}$ ohm cm.

Bridgman (1952) measured the effect of pressure on electrical resistivity of metal sheets of 0.0012 inch thickness. The purity of the sample was not given. His reported values are ratios of resistance at the given pressure to resistance at room temperature and one atmosphere pressure.

The niobium samples used by White and Woods (1957) were 99.7 and 99.7% pure and were in the form of rods and wires. Their table of values "may be regarded as somewhat tentative below 30°K, Mattheissen's rule not being strictly valid". They found that niobium becomes superconducting at 9.25°K.

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Electrical Resistivity of Niobium Cryogenic Data Memorandum No. M-20

White and Woods (1959) cite their 1957 work as the basis for their tabular values. These values differ from the earlier ones in the lower temperature region. They note that there is appreciable uncertainty in the value of ρ_0 .

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

Tables of Values of Electrical Resistivity

 ρ = Resistivity, (ohm cm)

 ρ_{273} = Resistivity at 273°K, (ohm cm)

Meissner, Franz a	nd Westerhoff (1933)
Temp.	R /R273
-K	
· 9•33	0.035
20.4	0.0617
78	0.2416
273.16	1.0000

Bridgman (1952)			
Pressure kg/cm ²	R/R _o (Resistance compared with the resistance at room temperature and 1 atmosphere)		
0	1.000		
10000	0.986		
20000	0.973		
30000	0.961		
40000	0.950		
50000	0.938		
60000	0.928		
7000b	0.918		
80000	0.909		
90000	0.901		
100000	0.894		

	White and Woods (1957)				
Temp. °K	"Ideal Resistivity" p _i x 10 ⁶ ohm cm	Resistivity, $\rho \propto 10^6$ ohm cm $\rho = \rho_1 + \rho_0$ (where $\rho_0 = 0.46 \times 10^6$ ohm cm)	P/ P273		
15	0.03 ₈	0.498	0.0357		
20	0.084	0.544	0.0390		
30	0.25	0.71	0.0508		
40	0.56	1.02	0.0730		
50	0.97	1.43	0.102		
75	2.36	2.82	0.202		
1.00	3.90	4.36	0.312		
150	7.0	7.46	0.534		
200	9.8	10.26	0.735		
250	12.3	12.76	0.914		
273	13.5	13.96	1.00		
295	14.5	14.96	1.07		

Electrical Resistivity of Niobium Cryogenic Data Memorahdum No. M-20

White and Woods (1959)				
Temp. °K	"Ideal Resistivity" _{f1} x10 ⁶ ohm cm	Resistivity, $\rho \ge 10^6$ ohm cm $\rho = \rho_1 + \rho_0$ (where $\rho_0 = 0.46 \ge 10^6$ ohm cm)	P/P273	
15	0.035	0.495	0.0354	
20	0.08	0.54	0.0387	
25	0,15	0.61	0.0437	
30	0.25	0.71	0.0508	
40	0.56	1.02	0.0730	
50	0.97	1.43	0.102	
60	1.5	1.96	0.140	
70	2.07	2.53	0.181	
80	2.68	3.14	0.225	
90	3.30	3.76	0.269	
100	3.9б	4.41	0.316	
120	5.2	5.66	0.405	
140	6.4	6.86	0.491	
160	7.5 ₅	8.01	0.574	
180	8.7	9.16	0.656	
200	9.8	10.26	0.735	
220	10.8	11.26	0.806	
250	12.3	12.76	0.914	
273	13.5	13.96	1.00	
295	14.5	14.96	1.07	

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CRYOGENIC DATA MEMORANDUM

PROJECT NO. 3150123

FILE NO. M-21

ELECTRICAL RESISTIVITY OF PLATINUM, Pt (Atomic Number 78)

(page 1 of 7)

Sources of Data:

International Critical Tables of Numerical Data, Physics, Chemistry, and Technology, VI, 1st Edition, Published for the National Research Council by the McGraw-Hill Book Co. Inc., 124-35 (1929).

Landolt-Börnstein Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, sechste Auflage, II Band, 6 Teil, Springer-Verlag, Berlin, 1-46 (1959).

Cath, P. G., Onnes, H. K., and Burgers, J. M., "On the Measurement of Very Low Temperatures. XXVIII. Comparison of the Platinum and the Gold Resistance Thermometers with the Helium Thermometer," Communs. Phys. Lab. Univ. Leiden No. 152c (1917).

de Haas, W. J., and de Boer, J., "The Electrical Resistance of Platinum at Low temperatures," Physica <u>1</u>, 609-16 (1933-1934); Communs. Kamerlingh Onnes Lab. Univ. Leiden No. 231c.

Hoge, H. J., and Brickwedde, F. G., "Establishment of a Temperature Scale for the Calibration of Thermometers between 14° and 83° K," J. Res. Natl. Bur. Std. <u>22</u>, 351-73 (1939).

Meaden, G. T., Electrical Resistance of Metals, Plenum Press, New York (1965) 218 p.

Meissner, W., and Voigt, B., "Messungen mit Hilfe von flüssigem Helium. XI. Widerstand der reinen Metalle in tiefen Temperaturen," (Measurements with the Help of Liquid Helium. XI. Resistance of Pure Metals at Low Temperatures), Ann. Physik (5) 7, 892 (1930).

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White, G. K., and Woods, S. B., "Thermal and Electrical Conductivity of Rhodium, Iridium, and Platinum," Can. J. Phys. 35, 248-57 (1957).

White, G. K., and Woods, S. B., "Electrical and Thermal Resistivity of the Transition Elements at Low Temperature," Phil. Trans. Roy. Soc. (London) <u>A251</u>, No. 995, 273-302 (1959).

Other References:

Berry, R. J., "Relationship between the Real and Ideal Resistivity of Platinum," Can. J. Phys. <u>41</u>, No. 6, 946-82 (Jun 1963).

Berry, R. J., "Ideal Resistivity of Platinum below 20°K," Can. J. Phys. 45, No. 5, 1693-708 (May 1967).

Bridgman, P. W., "The Electric Resistance to 30,000 kg/cm² of Twenty Nine Metals and Intermetallic Compounds," Proc. Am. Acad. Arts Sci. 149-79 (1951).

Grüneisen, E., "Electrische Leitfahigkeit der Metalle bei tiefen Temperaturen", (Electrical Conductivity of Metals at Low Temperatures), Ergebn. exakt. Naturw. <u>21</u>, 50-116 (1945).

Hatton, J., "Effect of Pressure on the Electrical Resistance of Metals at Liquid Helium Temperatures," Phys. Rev. 100, No. 2, 681-4 (1955).

Henning, F., Handbuch der Physik IX, Berlin, Springer-Verlag (1926).

Holborn, L., Ann. Physik 59, 145 (1919).

Kos, J. F., and Lamarche, J. L. G., "The Electrical Resistivity of Thermometrically Pure Platinum below 11°K," Can. J. Phys. <u>45</u>, No. 2, Part 1, 339-54 (1967).

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Meissner, W., "Thermische und elektrische Leitfähigkeit einiger Metalle zwischen 20 und 373° abs." (Thermal and Electrical Conductivity of Some Metals between 20 and 373°K), Ann. Physik <u>47</u>, No. 16, 1001-58 (1915).

Meissner, W., Physik. Z. 27, 725 (1926).

Meissner, W., and Grassmann, P., Physik. Z. <u>34</u>, 516 (1933).

Onnes, H. K., and Tuyn, W., Communs. Phys. Lab. Univ. Leiden Suppl. No. 58 (1926).

Powell, R. W., Tye, R. P., and Woodman, M. J., Platinum Metals Rev. 6, 138 (1962).

Sharevshaya, D. I., and Strelkov, P. G., "The Resistance of Thermometric Platinum in the Liquid Helium Temperature Range," Izmeritel. Tekhn. No. 2, 18-19 (1960).

Van der Horst, H. D., Tuyn, W. and Onnes, H. K., Private communication with the editors of the International Critical Tables of Numerical Data, Physics, Chemistry, and Technology, VI, (1929).

Comments:

The data for this graph were taken from the references cited above under "Sources of Data" and are listed as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. The value of electrical resistivity at 273°K (ρ_{273}) for platinum to be used in calculating values of electrical resistivity (ρ) is 9.60 x 10⁻⁶ ohm cm. This value is taken from White and Woods (1959).

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The values listed in the Landolt-Börnstein tables are those reported by Holborn; Meissner; and Meissner and Grassmann; while those values appearing in the International Critical Tables are from Henning; Onnes and Tuyn; and Van der Horst, Tuyn and Onnes. These primary sources are listed above under "Other References". The original authors are used in labeling the several curves on the graph. The sample used by Holborn is reported in the Landolt-Börnstein tables as cast polycrystalline with a very small amount of impurities present. The Meissner sample from the 1915 reference is reported to have been annealed. Meissner found $\rho_{273} = 9.81 \times 10^{-6}$ ohm cm. The sample used by Meissner and Grassmann is reported as an annealed polycrystalline sample with less than 0.001% of Cu and Pb impurities present.

The Cath et al. (1917) measurements were made with "extremely pure" platinum wires with 1/10 mm diameter. The wires are designated Pt-21 and Pt-26.

Meissner and Voigt (1930) report the same data as that found in the earlier Meissner paper (1928). The calculated value of ρ_{273} from the (1930) paper is 9.53 x 10⁻⁶ ohm cm.

The samples used by de Haas and de Boer (1933-1934) were 99.999% pure wires (6mm diameter) which had been previously tempered for 20 minutes at 750 °C.

Hoge and Brickwedde (1939) measured the resistance of several platinum resistance thermometers in an effort to establish a method for measuring temperature below 83°K by a means other than the gas thermometer. The data for thermometer L6 was used to construct a table of smoothed values. The purity of the platinum was not stated.

Van der Leeden's (1940) measurements were made with 0.15 mm diameter wire which had been vacuum annealed at 840°C for 2 hours. The purity of the sample was not stated.

White and Woods (1957) used 99.99% pure rods which had been annealed at 1050°C prior to measurement. White and Woods (1959) used their 1957 measurements plus some additional measurements to obtain their table of smoothed values.

Powell et al. (1962) used 99.9997% pure platinum polycrystalline rods which were annealed at ~ 1000 °C prior to measurement. They report one value at 273 °K, $\rho_{273} = 9.85 \times 10^{-6}$ ohm cm.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

Electrical Resistivity of Platinum Cryogenic Data Memorandum No. M-21

Powell et al.(1967) measured the resistivity of polycrystalline rods which were annealed at 1273°K prior to measurement. The purity of the sample was ~99.999995%.

Tables of Values of Electrical Resistivity

p = resistivity, (ohm cm); R = resistance, (ohm); ρ₂₇₈ = resistivity at 273°K, (ohm cm). R₂₇₃ = resistance at 273°K, (ohm).

Meissner (1915)				
Temp. ρ/ρ ₂₇₃ °K				
20.7	0.00631			
91.4	0.250			
273.1 1.000				
* $\rho_{273} = 9.81 \times 10^{-6}$ ohm cm				

Cath, Onnes, and Burgers (1917)				
Pt-	21	Pt-	26	
Temp. °K	R/R _o *	Temp. °K	R/R _o *	
273.09 250.08 230.07 211.79 170.07 160.37	1.00000 0.90890 0.82907 0.75545 0.58615 0.54627	273.09 250.08 230.07 211.79 170.07 160.37	1.00000 0.90867 0.82839 0.75453 0.58468 0.54469	
152.26 142.72 129.44 89.14 85.98 77.21	0.51277 0.47313 0.41762 0.24605 0.23249 0.19475	152.26 142.72 129.44 89.14 85.98 77.21	0.51111 0.47132 0.41570 0.24375 0.23014 0.19233	
67.78 64.91 61.04 56.83 50.31 44.38	0.15459 0.14261 0.12667 0.10959 0.084278 0.063510	67.78 64.91 61.04 56.83	0.15210 0.14011 0.12419 0.10704	
43.83 43.78 43.09 41.39 39.48 36.29	0.061757 0.061566 0.059297 0.054016 0.048324 0.039554			
36.25 32.83 31.32 29.88 29.42 28.40	0.039425 0.031219 0.027921 0.025195 0.024253 0.022524	36.28 32.83 31.31 29.88	0.037087 0.028743 0.025470 0.022698	
27.30 20.62 20.52 20.50 19.04 18.08	0.020618 0.012535 0.012415 0.012412 0.012412 0.011235 0.010559	27.30 20.58 20.52 20.52 20.50 20.31	0.018208 0.010172 0.010103 0.010098 0.010093 0.010015	
16.94 15.36 14.20	0.0098758 0.0090808 0.0085984	20.25 18.08 14.18	0.0098924 0.0083504 0.0065589	
* These values are almost identical with the values of Van der Horst et al. and therefore were not plotted on the Electri- cal Resistivity of Platinum graph.				

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Holborn (1919)		Meissner and Meissner	Meissner and Voigt (1930) Meissner (1926)		Meissner and Grassmann (1933)	
Temp. °K	R/R 273	Temp.* °K	R /R 273 **	Temp.* °K	ρ/ρ ₂₇₃ **	
20 81 195	0.0060 0.2060 0.6860	1.35 † 4.21 20.4 91.4	0.00165 0.00168 0.00607 0.250	1.35 4.2 20.4	0.00031 0.00031 0.00425	
* The s ** The f	econd decimal pl ifth decimal pla	ace is in doubt.	t.000 † p _{1.35} = ρ ₂₇₃ ⇒	0.016 x 10 ⁻⁶ ohn 9.53 x 10 ⁻⁸ ohn	n cm, cm.	

	Onnes and Tuyn (1926)	Van der Horst et al. (1929)	Henning (1926)
Temp., °C	100R/R273	100R/R273	100P/P273
- 80	68.158	68.017	67.782
- 90	64.113	63.955	63.688
-100	60.053	59.874	59.576
-120	51.863	51.650	51.295
-140	43.595	43.337	42.928
-160	35.213	34.904	34.463
-180 -200 -210	26.709 18.176 14.009	26.356 17.750 13.563	25.885 17.268
-220		9.587	
-230		6.030	
-240		3.252	
-250 -255 -260	1.5885 1.335	1.571 1.1263 0.894	0.5706
-265	1.239	0.810	
-270	1.225	0.7863	

	de Haas and de Boer (1933 - 1934)					
Temp. R/R _{O°C}		Temp. R/R _{O°C} Temp.				
°K		°K °K				
0.00	0.0003621	9.07	0.0005770			
1.07	0.0003638	9.96	0.0006500			
1.68	0.0003664	11.01	0.0007641			
2.49	0.0003712	13.14	0.0011129			
3.36	0.0003791	14.09	0.0013335			
4.25	0.0003902	15.31	0.0017107			
5.28	0.0004098	16.47	0.0021656			
6.75	0.0004535	17.45	0.0026332			
7.41	0.0004797	18.51	0.0031913			
8.51	0.0005387	19.60	0.0038916			
8.82	0.0005598	20.44	0.0045148			

Electrical Resistivity of Platinum Cryogenic Data Memorandum No. M-21

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Hoge and Brickwedde (1939) (smoothed values based on thermometer L6)				
Temp. °K	R∕R _{o∘c}			
10	0.002789			
13	0.003298			
15	0.003868			
20	0.006513			
25	0.011539			
30	0.019454			
35	0.030348			
40	0.043967			
50	0.077525			
60	0,116550			
70	0.158396			
80	0.201338			
90	0.244716			

	Van der Leeden (1940)					
Temp. 100R/Ro Temp. 100R/Ro Temp. 100R/Ro °K °K °K °K °K 100R/Ro						
4.24 3.72 3.15 2.70 0.00	0.068474 0.067781 0.067178 0.066786 0.065760	20.43 19.42 18.26 18.23 17.38	0.4664 0.3918 0.3204 0.3215 0.2742	17.37 16.32 15.18 14.13	0.2731 0.2265 0.1839 0.1535	

White and Woods (1957)						
Temp. °K	"Ideal Resistivity" r, x 10 ⁶ ohm cm	Resistivity, $\rho \ge 10^6$ ohm cm $\rho = \rho_i + \rho_0$ (where $\rho_0 = 0.0125 \ge 10^6$ ohm cm)	ρ/ P273*			
6	0.0006	0.0131	0.00134			
10	0.0031	0.0156	0.00159			
15	0.0155	0.0280	0.00286			
20	0.044	0.057	0.0058			
30	0.180	0.193	0.0197			
40	0.45	0.46	0.047			
50	0.76	0.77	0.079			
75	1.72	1.73	0.176			
100	2.8 ₀	2.81	0.287			
150	4.8 ₀	4.81	0.491			
200	6.8 ₀	6.81	0.695			
273	9.8 ₀	9.81	1.00			
295	10.65	10.66	1.09			
* These	 These values were not shown on the Electrical Resistivity Ratio for					
Plati	Platinum graph which is found on the last page of this Data Memoran-					
dum N	dum No. M-21.					

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Electrical Resistivity of Platinum Cryogenic Data Memorandum No. M-21

White and Woods (1959)					
Temp. °K	"Ideal Resistivity" p ₁ x 10 ⁶ ohm cm	Resistivity, $\rho \propto 10^6$ ohm cm $\rho = \rho_1 + \rho_0$	P/ P273		
		(where $p_0 = 0.0125 \times 10^6$ ohm cm)			
4	0.00024	0.01274	0.001325		
6	0.00065	0.01315	0.001368		
8	0.0014	0.0139	0.001446		
10	0.0029	0.0154	0.00160		
15	0.0116	0.0241	0.00251		
20	0.0359	0.0484	0.00503		
25	0.0837	0.0962	0.01000		
30	0.160	0.173	0.0180		
40	0.396	0.409	0.0425		
50	0.719	0.732	0.0761		
60	1.094	1.107	0.115		
70	1.497	1.510	0.157		
80	1.90 ₉	1,922	0.200		
90	2.326	2.339	0.243		
100	2.742	2.755	0.287		
120	3.565	3.578	0.372		
140	4.375	4.387	0.456		
160	5.18	5.19	0.540		
180	5.97	5.98	0.622		
200	6.76	6.77	0.704		
220	7.54	7.55	0.785		
250	8.70	8.71	0.906		
273	9•59	9.60	1.00		
295	10.42	10.43	1.08		

Powell, Tye, and Woodman (1967)					
Temp. Resistivity* °K ρ x 10 ⁶ ohm cm					
100 200 300 400 500	2.8 6.9 10.92 14.72 18.4				
* These values are not plotted on the Electrical Resistivity of Platinum graph.					

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Electrical Resistivity of Platinum

CRYOGENIC DATA MEMORANDUM

PROJECT NO. 3150123

FILE NO. M-22

ELECTRICAL RESISTIVITY OF SILVER, Ag (Atomic Number 47)

(page 1 of 5)

Sources of Data:

International Critical Tables of Numerical Data, Physics, Chemistry, and Technology, VI, 1st Edition, Published for the National Research Council by the McGraw-Hill Book Co., Inc., 124-35 (1929).

Landolt-Börnstein Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, sechste Auflage, II Band, 6 Teil, Springer-Verlag, Berlin, 1-46 (1959).

Bridgman, P. W., "The Resistance of 72 Elements, Alloys and Compounds to 100,000 kg/cm²," Proc. Am. Acad. Arts Sci. <u>81</u>, No. 4, 165-251 (1952).

Gerritsen, A. N., and Linde, J. O., "Thermal Conductivity of Some Dilute Silver Alloys," Communs. Kamerlingh Onnes Lab. Univ. Leiden No. 305b (1956).

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Meissner, W., and Voigt, B., "Messungen mit Hilfe von flüssigem Helium. XI. Widerstand der reinen Metalle in tiefen Temperaturen," (Measurements with the Help of Liquid Helium. XI. Resistivity of Pure Metals at Low Temperatures), Ann. Physik (5) 7, 761-97 (1930).

Pawlek, F., and Rogalla, D., "The Electrical Resistivity of Silver, Copper, Aluminum, and Zinc as a Function of Purity in the Range 4 - 298°K," Cryogenics <u>6</u>, No. 1, 14-20 (1966) and Metall. <u>20</u>, No. 9, 949-56 (1966).

Van der Leeden, P., "Geleiding van warmte en electriciteit door metalen," (Conduction of heat by metals), Gedrukt Bij Drukherig Waltman, Koornmarkt 62, Te Delft 11-76 (July 1940).

White, G. K., and Woods, S. B., "Electrical and Thermal Resistivity of the Transition Elements at Low Temperatures," Phil. Trans. Roy. Soc. London <u>A251</u>, No. 995, 273-302 (1959).

Other References:

de Haas, W. J., and Van den Berg, G. J., Physica <u>3</u>, 440-9 (1936) and Communs. Kamerlingh Onnes Lab. No. 241-D (1936).

Dewar, J., and Fleming, J. A., Phil. Mag. (5) 36, 271 (1893).

Fenton, E. W., Rogers, J. S., and Woods, S. B., "Lorenz Numbers of Pure Aluminium, Silver, and Gold at Low Temperatures," Can. J. Phys. <u>41</u>, 2026-33 (1963).

Goree, W. S., "Electrical Conductivity of Metals at High Pressures and Low Temperatures," Univ. of Florida, Gainesville, Ph.D. Thesis (1964) 166 pp., (Avail. from Univ. Microfilms Order No. 65-5985).

Goree, W. S., and Scott, T. A., "Pressure Dependence of Electrical Conductivity of Metals at Low Temperatures," J. Phys. Chem. Solids <u>27</u>, 835-48 (1966).

Hatton, J., "Effect of Pressure on the Electrical Resistance of Metals at Liquid Helium Temperatures," Phys. Rev. 100, No. 2, 681-4 (1955).

Holborn, L., Ann. Physik 59, 145 (1919).

Knook, B., and Van den Berg, G. J., "The Electrical Resistance of Pure Gold and Silver at Low Temperatures," Physica <u>26</u>, 505-12 (1960), Communs. Kamerlingh Onnes Lab. Univ. Leiden No. 321c (1960).

Meissner, W., Physik. Z. 27, 725 (1926).

Onnes, H. K., and Clay, J., Proc. Acad. Sci. Amsterdam <u>10</u>, 207 (1908) and Communs. Phys. Lab. Univ. Leiden No. 99c (1907).

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(page 2 of 5)

Comments:

The data for this graph were taken from the references cited above under "Sources of Data" and are listed as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. When the actual values of ρ_{273} are not available for the samples used by the several investigators, a datum value reported by White and Woods (1959) ($\rho_{273} = 1.476 \times 10^{-6}$ ohm cm) is suggested for calculating values of electrical resistivity from these ratios.

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The values listed in the Landolt-Börnstein tables are those reported by Dewar and Fleming; Holborn; de Haas and Van den Berg; and Meissner; while those values appearing in the International Critical Tables are from Onnes and Clay. These primary sources are listed above under "Other References". The original authors are used in labeling the curves on the graph. The samples used by the investigators appearing in Landolt-Börnstein are all reported as polycrystalline with a small amount of impurities present. The samples used by Holborn, and de Haas and Van den Berg were annealed. The sample used by Meissner was aged. The Onnes and Clay sample was 99.82% pure silver wire. Dewar and Fleming reported one value $\rho_{273} = 1.47 \times 10^{-6}$ ohm cm.

Meissner and Voigt (1930) present the same data as Meissner (1926).

The purity of the Kannuluik (1931) sample was not given.

The samples used by Van der Leeden (1940) were 0.2 cm and 0.6 cm diameter wires designated Ag 1 and Ag 2, respectively. They were annealed at 500°C for 2 hours prior to measurement.

The purity of the Bridgman (1952) sample is not stated nor is there any mention of heat treatment made. The samples were in the form of thin sheets, 0.001 inch thick.

The samples Ag 2t and Ag 4t used by Gerritsen and Linde (1956) were annealed in "the gas" (assume air) for 4 hours at 740°K and 750°K, respectively. They were in the form of rectangular rods. No chemical analysis was available.

White and Woods (1959) rod specimens were 99.999% pure and were annealed in vacuum at 650° and 530°C. The smoothed values in the table below were taken from large-scale graphs.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

The sample used by Pawlek and Rogalla (1966) was 99.9964% pure silver wire. The wire was annealed one hour in argon at 500 °C and cooled at less than 50 °C/hr.

Tables of Values of Electrical Resistivity

 $\begin{array}{ll} \rho = \mbox{resistivity, (ohm cm);} & \rho_{273} = \mbox{resistivity at 273°K, (ohm cm).} \\ R = \mbox{resistance, (ohm);} & R_{273} = \mbox{resistance at 273°K, (ohm cm).} \end{array}$

Temp. °C	100R/R273	Temp. °C	100 R/R ₂₇₃	Temp. °C	100R/R273	
- 80 t	67.8	-1 ¹ 40 †	43.2	-204.67	15.528	
-100 †	59.6	-160 †	34.8	-220 †	9.2	
-103.81	58.087	-180 †	26.3	-240 †	2.6	
-120	51.4	-183 .57	24.679	-252.92	0.8913	
-139.87†	43.282	-195.17	19.703	-259.22	0.6942	
		-200 †	17.6			

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Holbo	Holborn (1919) Meissner & Voigt (1930) Meissner (1926)		de Haas and Van den Berg							
Temp.	P/P273	Temp.*	ρ/ρ273**	Temp.	P/P273					
°K		°K		°K						
20	0.0054	1.34 †	0.00679	4.2	0.00266					
81	0.2071	4.21	0.00682	6.0	0.00268					
195	0.6841	20.40	0.01000	8.4	0.00274					
		78.85	0.1974	10.8	0.00288					
		87.42 273.16†	0.2349	20.4	0.00543					
* The	e second decimal p	lace of the tem	perature values is	s somewhat in doul	ot.					
** The dou	** The fifth decimal place of the electrical resistivity ratio values is somewhat in doubt.									
† p ₂₇	$3 = 1.48 \times 10^{-6}$ or	m cm; p _{1.34} =	0.010 x 10 ⁻⁶ ohm	$\rho_{273} = 1.48 \times 10^{-6}$ ohm cm; $\rho_{1.34} = 0.010 \times 10^{-6}$ ohm cm.						

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Kannuluik (1931)				
Sample	Temp. °C	Temp. °K	Specific Resistance ρ x 10 ⁶ ohm cm	ρ/ρ ₂₇₃ **
Ag	-183.0 - 78.5 0. 100.	90.15 194.65 273.15 373.15	0.377 1.036 1.509 2.121	0.250 0.687 1.00 1.41
Ag*	-183.0 - 78.5 0. 100.	90.15 194.65 273.15 373.15	0.341 1.035 1.510 2.123	0.226 0.685 1.00 1.41
* Measurements were repeated after the silver wire had re- ceived a prolonged annealing at 500 °C.				
**These values were not plotted on the Electrical Resistivity				

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of	Sil	ver	grap	h.

Van der Leeden (1940) Temp. Ag 1 Ag 2 *K 100 B/B.* 100 B/B.			
20.45 0.337 1.180 19.41 0.2815 1.124 18.23 0.232 1.058 17.28 0.199 1.0215 15.80 0.1605 0.959 14.01 0.130 0.929 0.00 0.079 0.830			
* Only the Ag 1 values were plotted on the Electrical Resisti- vity of Silver graph.			

	Gerritsen and Linde (1956)				
Temp. °K	Resistivity pxl0 ⁶ ohm cm		/م	°273	
	Ag 2t	Ag 4t	Ag 2t*	Ag 4t	
14 16 18 20	0.00447 0.00519 0.00619 0.00743	0.00694 0.00758 0.00852 0.00983	0.00304 0.00353 0.00421 0.00505	0.00469 0.00512 0.00576 0.00664	
70 80 90 273	0.238 0.297 0.359 1.47	0.235 0.299 0.363 1.48	0.162 0.202 0.244 1.00	0.159 0.202 0.245 1.00	
* Ag 2t values were plotted.					

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	Bridgman (1952)				
(Resistance i	(Resistance is compared with resistance at room temperature and one atmosphere pressure)				
Pressure kg/cm ²	R/R _o	Pressure kg/cm ²	R/R _o		
0	1.000	50000	0.683		
10000	0.910	60000	0.647		
20000	0.837	70000	0.618		
30000	0.775	80000	0.592		
40000	0.724	90000	0.569		
		100000	0.548		

White and Woods (1959)			
Temp. °K	"Ideal Resistivity" c, x 10 ⁿ ohm cm	Resistivity, $\rho \ge 10^6$ ohm cm $\rho = \rho_0 + \rho_1$ (where $\rho_0 = 5.53 \ge 10^{-9}$ ohm cm)	P/ P273
10	0.0002	0.0058	0.0039
15	0.0011	0.0067	0.0045
20	0.0038	0.0094	0.0064
25	0.010	0.0156	0.0106
30	0.020	0.0256	0.0173
40	0.058	0.0636	0.0431
50	0.11	0.1156	0.0783
60	0.17	0.1756	0.1190
70	0.230	0.2356	0.1597
80	0.290	0.2956	0.2003
90	0.35%	0.3606	0.2444
100	0.420	0.4256	0.2884
120	0.545	0.5506	0.3731
140	0.675	0.6806	0.4612
160	0.795	0.8005	0.54 2 6
180	0.92	C.9:56	0.6273
200	1.04	1.0456	0.7086
220	1.16	1.1656	0.7899
250	1.34	1.3456	0.9119
273	1.47	1.4756	1.0000
295	1.61	1.6156	1.0949

Pawlek and Rogalla (1966)			
Temp. Resistivity °K ρ x 10 ⁵ ohm cm		P/ P273	
4.2 20.4 77.0 195.0 273.0	0.739 4.33 276.0 991.0 1500.0	0.000493 0.00289 0.184 0.661 1.000	

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FILE NO. M-23

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ELECTRICAL RESISTIVITY OF TANTALUM, Ta (Atomic Number 73)

(page 1 of 4)

Sources of Data:

International Critical Tables of Numerical Data, Physics, Chemistry, and Technology, VI, 1st Edition, Published for the National Research Council by the McGraw-Hill Book Co. Inc., 124-35 (1929).

Landolt-Börnstein Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, sechste Auflage, II Band, 6 Teil, Springer-Verlag, Berlin, 1-46 (1959).

Bridgman, P. W., "The Resistance of 72 Elements, Alloys, and Compounds to 100,000 kg/cm²," Proc. Am. Acad. Arts Sci. <u>81</u>, No. 4, 165-251 (1952).

Cox, M., "Thermal and Electrical Conductivities of Tungsten and Tantalum," Phys. Rev. 64, 241-47 (1943).

Meaden, G. T., Electrical Resistance of Metals, Plenum Press, New York (1965) 218 p.

White, G. K., and Woods, S. B., "Electrical and Thermal Resistivity of the Transition Elements at Low Temperatures," Phil. Trans. Roy. Soc. (London) <u>A251</u>, No. 995, 273-302 (1959).

Other References:

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Goree, W. S., "Electrical Conductivity of Metals at High Pressures and Low Temperatures," Univ. of Florida, Gainesville, Ph.D. Thesis (1964), 166 p., Univ. Microfilms Order No. 65-5985.

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Comments:

The data for this graph were taken from the references cited above under "Sources of Data" and are listed as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. When actual values of p_{273} are not available for the samples used by the investigators, a datum value reported by White and Woods (1959) ($p_{273} = 12.3 \times 10^{-6}$ ohm cm) is suggested for calculating values of electrical resistivity from these ratios. The curves on this graph should not be extrapolated to lower temperatures as tantalum becomes a superconductor at 4.2° K.

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

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The values listed in the Landolt-Börnstein tables are those reported by Burgers and Basart; McLennan, Howlett and Wilhelm; and Meissner and Voigt; while those values appearing in the International Critical Tables are from Holborn. These primary sources are cited above under "Other References". The names of the original authors are used in labeling the curves on the graph. The samples used by the investigators appearing in Landolt-Börnstein are reported as polycrystalline with no mention made of impurities. Burgers and Basart reported $\rho_{273} = 12.4 \times 10^{-6}$ ohm cm.

The wire sample used by Cox (1943) was 99.9% pure tantalum. No mention is made of any heat treatment prior to measurements.

Bridgman (1952) measured the effect of pressure on the resistivity of thin sheets (0.003 inch thick). No additional information is given about the sample.

White and Woods (1959) used 99.9% pure tantalum rods which were annealed in vacuo at 2500°C.

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

Tables of Values of Electrical Resistivity

 $\begin{array}{ll} \rho = \mbox{resistivity, (ohm cm);} & \rho_{273} = \mbox{resistivity at } 273\,^{\circ}\!K, \mbox{ (ohm cm).} \\ R = \mbox{resistance, (ohm);} & R_{273} = \mbox{resistance at } 273\,^{\circ}\!K, \mbox{ (ohm).} \end{array}$

Holborn (1919)			
Temp. °C	100R/R ₂₇₃	Temp. °C	10CR/R273
- 78.2 - 80 † -100 † -120 †	72.98 72.4 64.9 57.3	-140 † -160 † -180 † -192.6	49.6 41.9 34.3 29.55
t Values from interpolation.			

McLennar and Will	n, Howlett Nelm (1929)
Temp.	R/R273
°K	
4.3	0.029
20.6	0.033
80.0 273.1	0.230 1.00

Meissner and	Voigt (1930)		
Temp.*	R/R273		
°K			
4.29 ^{**}	0.00019		
4.49	0.0099		
20.44	0.0140		
77.61	0.2037		
88.30	0.2511		
273.16**	1.0000		
* The second decimal place of the temperature values is somewhat			
** $p_{273} = 15.2 \times 10^{-10}$ $p_{4.29} = 0.0029$	0 ⁻⁶ ohm cm x 10 ⁻⁶ ohm cm		

Cox (1943)			
Temp. °K	Resistivity ρ x 10 ^e ohm cm	P/P273	
77.33	2.46	0.1982	
273.2	12.41	1.000	
373.4	17.18	1,384	

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	Bridgman (1952)				
(Resistance compared	(Resistance compared with resistance at room temperature and 1 atmosphere pressure)				
Pressure kg/cm ²	R/R _o	Pressure kg/cm ²	R/R _o		
0	1.000	60000	0.918		
10000	0.984	70000	0.908		
20000	0.968	80000	0.898		
30000	0.954	90000	0.890		
40000	0.941	100000	0.882		
50000	0.929				

	White and Woods (1959)				
Temp. °K	"Ideal Resistivity" ρ ₁ x 10 ⁶ ohm cm	Resistivity, $\rho \times 10^6$ ohm cm $\rho = \rho_1 + \rho_0$ (where $\rho_0 = 0.1881 \times 10^6$ ohm cm)	ρ/ ρ ₂₇₃		
10	0.0032	0.1913	0.01557		
15	0.017	0.2051	0.01669		
20	0.051	0.2391	0.01946		
25	0.12	0.3081	0.02507		
30	0.23	0.4181	0.03402		
40	0.54	0.7281	0.05925		
50	0.95	1.138	0.09262		
60	1.4 $_{3}$	1.618	0.1317		
70	1.96	2.148	0.1748		
80	2.50	2.688	0.2187		
90	3.0 ₃	3.218	0.2619		
100	3.5 ₅	3.738	0.3042		
120	4.6	4.788	0.3896		
140	5.6	5.788	0.4710		
160	6.6 ₅	6.838	0.5565		
180 200 250 273 295	7.65 8.6 9.6 11.0 12.1 13.1	7.838 8.788 9.788 11.188 12.288 13.288	0.6379 0.7152 0.7965 0.9105 1.000 1.081		

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CRYOGENIC DATA MEMORANDUM

PROJECT NO. 3150123

FILE NO. M-24

ELECTRICAL RESISTIVITY OF TIN, Sn (Atomic Number 50) (page 1 of 5)

Sources of Data:

International Critical Tables of Numerical Data, Physics, Chemistry, and Technology, VI, 1st Edition, Published for the National Research Council by the McGraw-Hill Book Co. Inc., 124-35 (1929).

Landolt-Börnstein Zahlenwerte und Funktionen aus Physik, Chemie, Astronomie, Geophysik und Technik, sechste Auflage, II Band, 6 Teil, Springer-Verlag, Berlin, 1-46 (1959).

Aleksandrov, B. N., "Size Effect in Electrical Resistivity of High-Purity Metals," Soviet Phys. JETP <u>16</u>, No. 2, 286-94 (1963).

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Bridgman, P. W., "The Resistance of 72 Elements, Alloys and Compounds to 100,000 kg/cm²," Proc. Am. Acad. Arts Sci. <u>81</u>, No. 4, 165-251 (1952).

Kunzler, J. E., and Renton, C. A., "Size Effect in Electrical Resistivity Measurements on Single Crystals of High-Purity Tin at Liquid Helium Temperatures," Phys. Rev. 108, No. 6, 1397 (1957).

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Other References:

Bridgman, P. W., "The Effect of Pressure on the Electrical Resistance of Single Metal Crystals at Low Temperature," Proc. Am. Acad. Arts Sci. <u>68</u>, 95-123 (1933).

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Goree, W. S., "Electrical Conductivity of Metals at High Pressures and Low Temperatures," Univ. of Florida, Gainesville, Ph.D. Thesis (1964), 166 p., Univ. Microfilms Order No. 65-5985.

Goree, W. S., and Scott, T. A., "Pressure Dependence of Electrical Conductivity of Metals at Low Temperatures," J. Phys. Chem. Solids 27, 835-48 (1966).

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Jaeger, W., and Diesselhorst, H., Wiss. Abhandl. physik. tech. Reichsanstalt 3, 269 (1900).

Kan, L. S., and Lazarev, B. G., "Effect of Hydrostatic Compression on the Electrical Conductivity of Metals at Low Temperatures," Soviet Phys. JETP 7, No. 1, 180-81 (1958).

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Comments:

The data for this graph were taken from the references cited above under "Sources of Data" and are listed as ratios of electrical resistivity with respect to the resistivity at a datum temperature of 273°K. Since tin is an anisotropic metal, we list suggested values of ρ_{273} for SnH , SnL, and polycrystalline tin to be used in calculating electrical resistivity from these ratios. These

 $P(||)_{273} = 13.084 \times 10^{-6} \text{ ohm cm},$ $P(poly)_{273} = 10.05 \times 10^{-6} \text{ ohm cm}.$ $^{\rho}(\perp)_{273} = 9.01275 \times 10^{-6}$ ohm cm, and values are:

The first and second values are from Aleksandrov and D'Yakov (1963) and the third value was calculated from their data using Voigt's equation:

 $\frac{1}{\rho_{\text{(poly)}}} = \frac{1}{3} \left[\frac{1}{\rho_{\text{H}}} + \frac{2}{\rho_{\text{L}}} \right].$

The curves on the graph should not be extrapolated to lower temperatures as tin becomes a superconductor at 3.74°K.

In instances where data points were quite widely separated or areas where data did not exist, symbols were used to show the available data points so that the reader will know where arbitrary position or shape of the graph was made.

The values listed in the Landolt-Börnstein tables are those reported by Jaeger and Diesselhorst; and Meissner; while those values appearing in the International Critical Tables are from Onnes and Tuyn. These primary sources are listed above under "Other References". The Landolt-Börnstein tables list the samples of Meissner as polycrystalline with no mention of impurities present. The sample used by Onnes and Tuyn is reported as polycrystalline with less than 0.01% impurities of unknown composition. Jaeger and Diesselhorst reported less than 0.03% Pb impurities of unknown sample used in the determination of ρ_{273} . Their value was $\rho_{273} = 11.15 \times 10^{-6}$ ohm cm. No information was given on the mechanical or heat treatment of any of the above samples.

The Bridgman (1933) measurements were made with a 1 mm diameter single crystal rod at four crystal orientations; 82°, 17°, 90°, and 0° angles between axis and length of rod. The rod was formed in pyrex tubing by slowly lowering from a furnace.

Van der Leeden (1940) measured the resistivity of a 0.2 mm diameter wire. The wire was presumably polycrystalline with purity not stated.

Bridgman (1952) measured the effect of pressure on the resistivity of thin sheets of 0.001 inch thickness.

Kunzler and Renton (1957) made measurements on single crystals of high purity. The values in the table are for the specimen before it was reduced in cross section; the initial thickness was 4 mm.

Aleksandrov (1963) used 99.99985% pure tin in the form of rods of 2.7 mm diameter. Aleksandrov and D'Yakov (1963), using the same samples as Aleksandrov, obtained values for resistivity of tin from 3.7 to 273°K, using wire diameters which do not affect the resistivity values. Their samples were single crystals with the principal axis parallel to the sample axis (SnH), and with the principal axis at right angles to the sample axis (SnH). They state that the error of a single measurement of R/R_{293} at T = 4.2°K amounted to 2 - 2.5% for tin. The $\rho_0(SnH) \simeq 10^{-10}$ ohm cm and $\rho_0(SnH) \simeq 7 \times 10^{-11}$ ohm cm.

Electrical Resistivity of Tin Cryogenic Data Memorandum No. M-24

The "ideal" resistivity values tabulated in the lower right-hand corner of the graph were taken from Meaden (1965). His book presents a comprehensive review of the literature dealing with experimental determinations of electrical resistivity together with a relatively concise account of the modern theory of the electrical resistance of metals and alloys.

Tables of Values of Electrical Resistivity

 $R_o = \text{Resistance at O}^\circ C$, (ohm)

Onnes and Tuyn (1923)				Ме		
Temp. °C	Temp. °K	100p/p ₂₇₃	Temp. °C	Temp. °K	100p/p ₂₇₃	Tem °K
102.13 115.14 127.50	171.02 158.01 145.65	57.36 52.16 47.25	-209.98 -218.30 -252.65	63.17 54.85 20.50	14.67 11.45 1.162	4. 20. 88.
141.06 158.74 182.80	132.09 114.41 90.35	41.90 34.91 25.44	-254.95 -256.61 -258.89	18.30 16.54 14.26	0.836 0.637 0.409	L
194.07 202.07	79.08 71.08	20.98 17.79	-269.33	3.82	0.099	

Meissn	er (1925)
Temp. °K	ρ/ρ ₂₇₃
4.2 20.4 88.2	0.00078 0.0120 0.2457

Van der Leeden (1940)		
Temp. °K	100R/R _o	
14.29	0.443	
16.31	0.672	
17.48	0.813	
19.46	1.107	
20.40	1.266	
69.05	17.52	
77.50	20.93	
78.15	21.40	
84.15	23.66	
90.30	26.08	

Bridgman (1952)			
Pressure kg/cm ²	R/R _o *	Pressure kg/cm ²	R∕R₀*
0 10000 20000 30000 40000 50000	1.000 0.910 0.837 0.775 0.724 0.683	60000 70000 80000 90000 100000	0.647 0.618 0.592 0.569 0.548
* Resistance compared with resistance at room temperature and one atmos- phere pressure.			

Bridgman (1933)				
Temp.	Angle between axis and length			
°K	90°	0 °	90°	0°
	Resist p x 10 ⁶	ivity ohm cm	p/p	* 273
90.35 194.85 273.15	3.255 8.736 13.08	2.404 6.147 9.088	0.2489 0.6678 1.000	0.2646 0.6764 1.000
* These values were not plotted on the Electrical Resistivity of Tin graph.				

Kunzler and Renton (1957)			
Temp. °K	Resistivity ρ x 10 ⁶ ohm cm	ρ/ρ ₂₇₃ *	
4.2	0.000525	0.000035	
273.0	15.0	1.0	
*These values were not plotted on			

*These values were not plotted on the Electrical Resistivity of Tin graph.

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Aleksandrov (1963)					
Temp. °K	Resistance Ratio R/R ₂₉₃				
	Sn∥	Sn⊥			
4.2	1.45	1.55			
* For Sn H , ρ_{293} = 14.3 x 10^{-6}ohm cm. For Sn \pm , ρ_{293} = $9.85x10^{-6}\text{ohm}$ cm.					

Aleksandrov and D'Yakov (1963)					
Temp. °K	Resistance Ratio R/R [*] 295		Resistance Ratio R/R [*] ₂₇₃		
	Sn∥	Sn1	Sn II	SnL	
3.7 4.22 4.46 7.2 14.0 20.4	$\begin{array}{c} 1.13 \times 10^{-6} \\ 1.45 \times 10^{-5} \\ 1.64 \times 10^{-5} \\ 1.05 \times 10^{-4} \\ 3.2 \times 10^{-3} \\ 0.0111 \end{array}$	1.17×10^{-6} 1.55×10^{-5} 1.81×10^{-6} 1.23×10^{-4} 2.54×10^{-3} 8.68×10^{-3}	$1.23 \times 10^{-5} \\ 1.58 \times 10^{-5} \\ 1.79 \times 10^{-5} \\ 1.15 \times 10^{-4} \\ 3.5 \times 10^{-3} \\ 0.0121$	$\begin{array}{c} 1.28 \times 10^{-5} \\ 1.70 \times 10^{-5} \\ 1.99 \times 10^{-5} \\ 1.35 \times 10^{-4} \\ 2.79 \times 10^{-3} \\ 9.52 \times 10^{-3} \end{array}$	
58.0 63.5 77.4 90.31 111.6 273.0	0.119 0.140 0.199 0.244 0.331 0.915	0.109 0.128 0.182 0.23 0.316 0.915	0.130 0.153 0.217 0.267 0.362 1.000	0.120 0.140 0.200 0.252 0.347 1.000	
* For SnII ; $\rho_{293} = 14.3 \times 10^{-6}$ ohm cm, $\rho_{273} = 13.084 \times 10^{-6}$ ohm cm. For SnI ; $\rho_{293} = 9.85 \times 10^{-6}$ ohm cm, $\rho_{273} = 9.01275 \times 10^{-6}$ ohm cm.					

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