Uncertainties in SUSY Precision Calculations

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CERN, 10/2004

1. Introduction
2. Precision Observables in the MSSM
3. Status and Perspectives
4. Conclusions

1. Introduction

Q: Which Lagrangian describes the world?

Q': What describes the world better: SM or MSSM ?
A: Two possible ways:

- Search for new SUSY particles

new SUSY particles found $\Updownarrow$ SM ruled out

  Problem:
  SUSY particles are too heavy for todays colliders, only upper limits of $\mathcal{O}$(100 GeV).

  $\to$ waiting for Tevatron (2005. . . ?)
  $\to$ waiting for LHC (2007. . . ?)

- Search for indirect effects of SUSY
  via Precision Observables

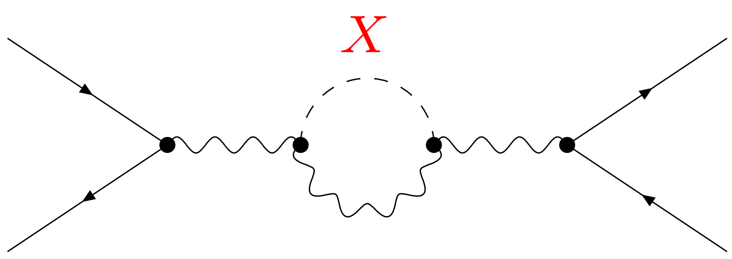
Precision Observables (POs):

Comparison of electro-weak precision observables with theory:

EW Precision data:		Theory:
$M_W, \sin^2\theta_{\text{eff}}, a_\mu$	$\leftrightarrow$	SM, MSSM , . . .

$\Downarrow$

Test of theory at quantum level: Sensitivity to loop corrections

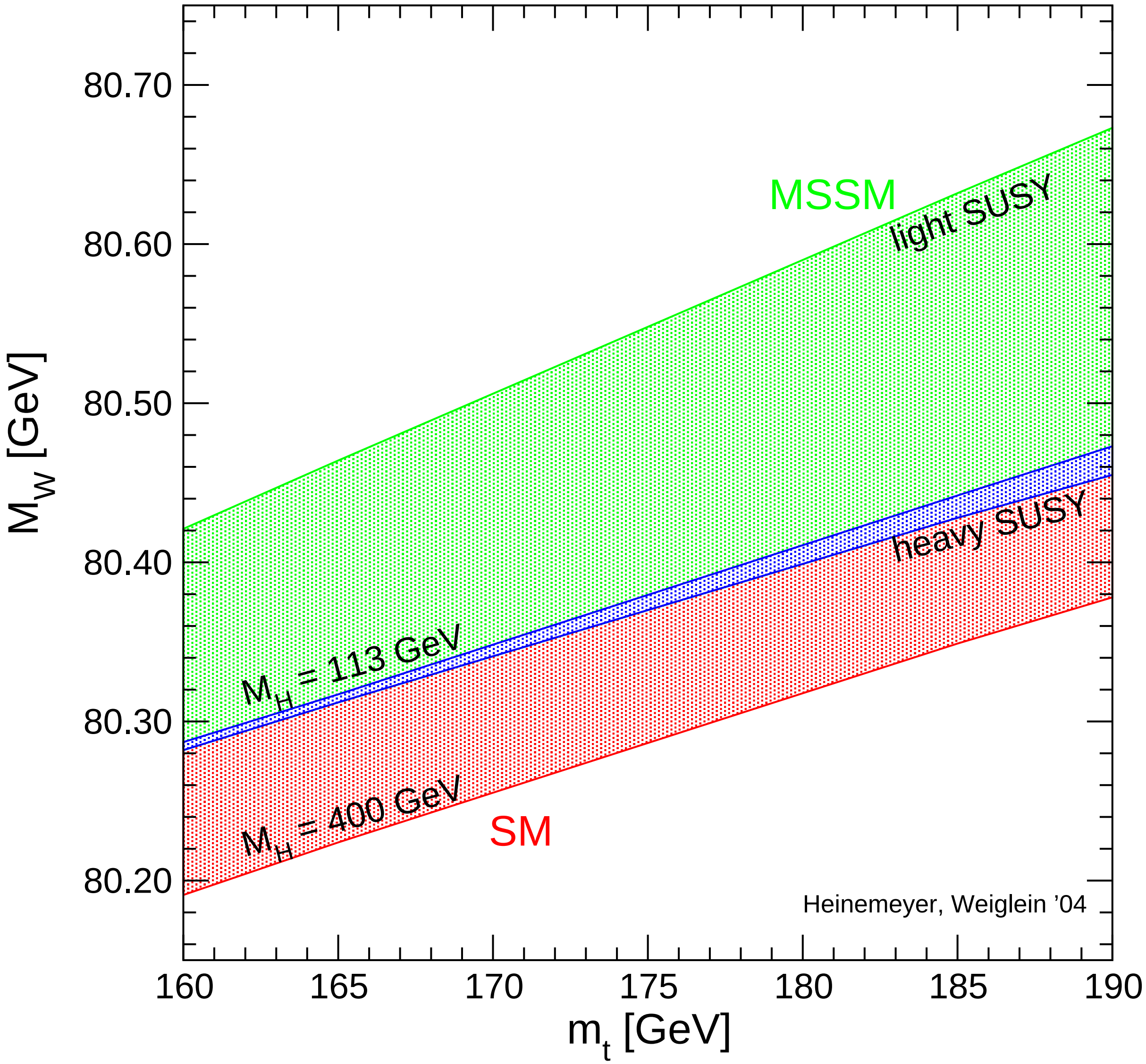


$\Downarrow$

Very high accuracy of measurements and theoretical predictions needed

- Which model fits better?
- Does the prediction of a model contradict the experimental data?

Example: Prediction for M_W in the SM and the MSSM :



MSSM uncertainty:
unknown masses
of SUSY particles

SM uncertainty:
unknown Higgs mass

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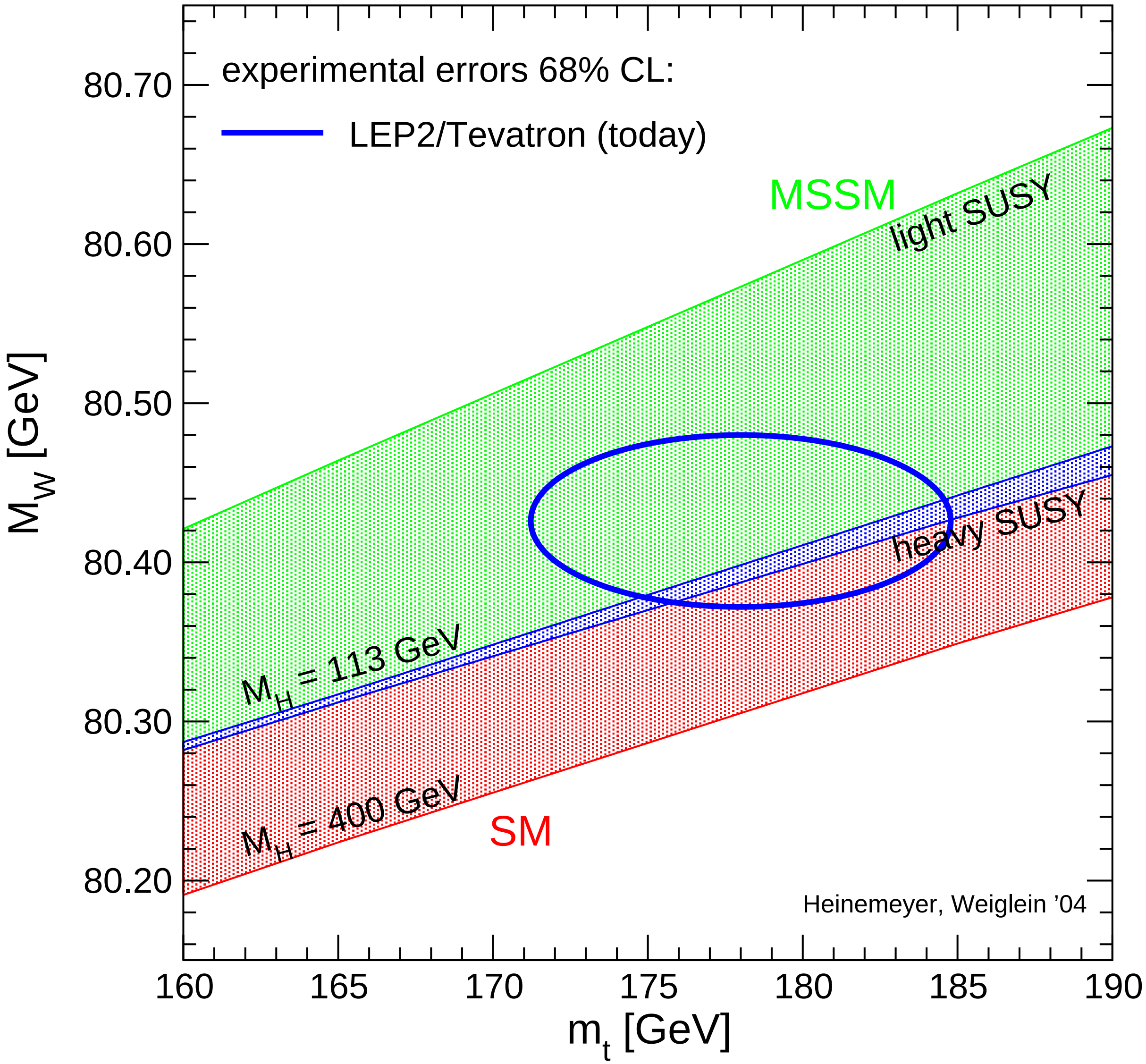

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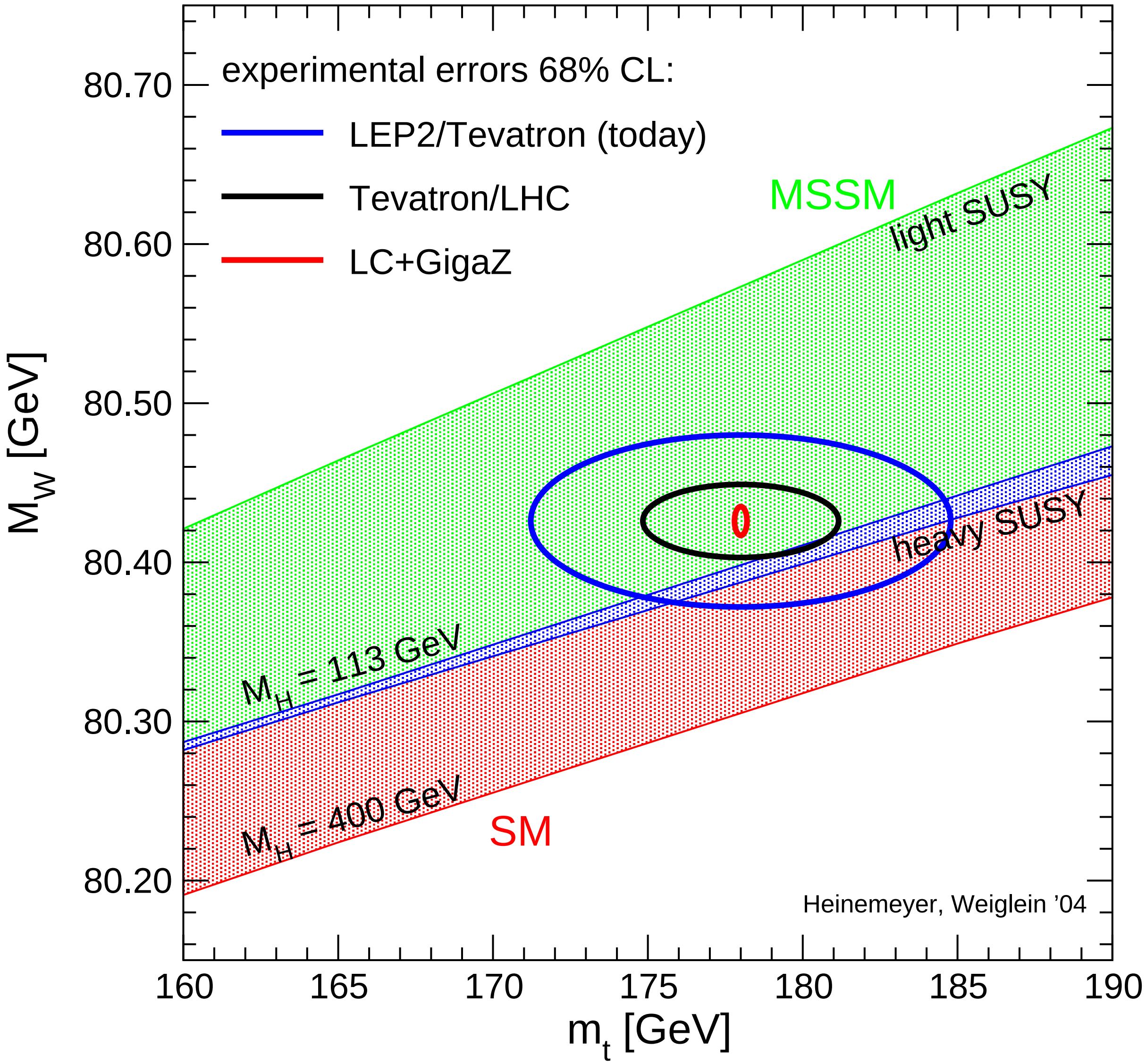

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The Minimal Supersymmetric Standard Model (MSSM)

Superpartners for Standard Model particles

$$\Big[u, d, c, s, t, b\Big]_{L,R} \quad \Big[e, \mu, \tau\Big]_{L,R} \quad \Big[\nu_{e,\mu,\tau}\Big]_{L} \qquad \text{Spin } \tfrac{1}{2}$$

$$\Big[\tilde{u}, \tilde{d}, \tilde{c}, \tilde{s}, \tilde{t}, \tilde{b}\Big]_{L,R} \quad \Big[\tilde{e}, \tilde{\mu}, \tilde{\tau}\Big]_{L,R} \quad \Big[\tilde{\nu}_{e,\mu,\tau}\Big]_{L} \qquad \text{Spin } 0$$

$$g \quad \underbrace{W^{\pm}, H^{\pm}} \quad \underbrace{\gamma, Z, H_1^0, H_2^0} \qquad \text{Spin 1 / Spin 0}$$

$$\tilde{g} \quad \tilde{\chi}^{\pm}_{1,2} \quad \tilde{\chi}^{0}_{1,2,3,4} \qquad \text{Spin } \frac{1}{2}$$

Enlarged Higgs sector: Two Higgs doublets

physical states: $h^0, H^0, A^0, H^{\pm}$

Goldstone bosons: $G^0, G^{\pm}$

Input parameters: $\tan\beta = \frac{v_2}{v_1}$, $\quad M_A^2$ or $M_{H^{\pm}}^2$

Problem in the MSSM: many scales

$\tilde{t}$ sector of the MSSM: (scalar partner of the top quark)

Mass matrix for $\tilde{t}_L, \tilde{t}_R$:

$$(\tilde{t}_L, \tilde{t}_R) \begin{pmatrix} M^2_{\tilde{t}_L} + m_t^2 + DT_{1t} & m_t X_t \\ m_t X_t & M^2_{\tilde{t}_R} + m_t^2 + DT_{2t} \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix}$$

$$\Big\Downarrow \quad \leftarrow \text{Diagonalization}, \theta_{\tilde{t}}$$

$$(\tilde{t}_1, \tilde{t}_2) \begin{pmatrix} m^2_{\tilde{t}_1} & 0 \\ 0 & m^2_{\tilde{t}_2} \end{pmatrix} \begin{pmatrix} \tilde{t}_1 \\ \tilde{t}_2 \end{pmatrix}$$

$X_t = A_t - \mu \cot\beta$; large mixing possible

$\Rightarrow$ Physical parameters: $m_{\tilde{t}_1}$, $m_{\tilde{t}_2}$, $\theta_{\tilde{t}}$

$\Rightarrow$ Soft SUSY-breaking parameters: $M_{\tilde{t}_L}$, $M_{\tilde{t}_R}$, A_t

$\Rightarrow$ Soft SUSY-breaking parameters determine SUSY mass patterns

Possible extensions:

cMSSM (complex MSSM):

Possibly complex parameters:

– μ : Higgsino mass parameter

– $A_{t,b,\tau}$: trilinear couplings $\Rightarrow X_{t,b,\tau} = A_{t,b} - \mu^* \{\cot\beta, \tan\beta\}$ complex

– $M_{1,2}$: gaugino mass parameter (one phase can be eliminated)

– $m_{\tilde{g}}$: gluino mass

$\Rightarrow$ can induce $\mathcal{CP}$-violating effects

NMFV MSSM (non-minimal flavor violation):

$\rightarrow$ Mixing of scalar quark families (beyond CKM)

e.g. sbottom/sstrange mixing :

$$\left(\tilde{b}_L, \tilde{b}_R, \tilde{s}_L, \tilde{s}_R\right) \begin{pmatrix} \widetilde{B} & 0 \\ 0 & \widetilde{S} \end{pmatrix} \begin{pmatrix} \tilde{b}_L \\ \tilde{b}_R \\ \tilde{s}_L \\ \tilde{s}_R \end{pmatrix} \rightarrow \left(\tilde{b}_L, \tilde{b}_R, \tilde{s}_L, \tilde{s}_R\right) \begin{pmatrix} \widetilde{B} & \neq 0 \\ \neq 0 & \widetilde{S} \end{pmatrix} \begin{pmatrix} \tilde{b}_L \\ \tilde{b}_R \\ \tilde{s}_L \\ \tilde{s}_R \end{pmatrix}$$

NMSSM, . . .

2. Precision Observables in the MSSM

Precision observables: M_W, $\sin^2\theta_{\rm eff}$, m_h, $(g-2)_\mu$, b physics, ...

1.) Theoretical prediction for M_W in terms of $M_Z, \alpha, G_\mu, \Delta r$:

$$M_W^2\left(1-\frac{M_W^2}{M_Z^2}\right) = \frac{\pi\,\alpha}{\sqrt{2}\,G_\mu}\left(\frac{1}{1-\Delta r}\right)$$

$\Updownarrow$

loop corrections

2.) Effective mixing angle:

$$\sin^2\theta_{\rm eff} = \frac{1}{4\,|Q_f|}\left(1-\frac{\mathrm{Re}\,g_V^f}{\mathrm{Re}\,g_A^f}\right)$$

Higher order contributions:

$$g_V^f \to g_V^f + \Delta g_V^f, \quad g_A^f \to g_A^f + \Delta g_A^f$$

Corrections to M_W, $\sin^2\theta_{\rm eff}$

$\longrightarrow$ can be approximated with the **ρ-parameter:**

ρ measures the relative strength between
neutral current interaction and charged current interaction

$$\rho = \frac{1}{1 - \Delta\rho} \qquad\qquad \Delta\rho = \frac{\Sigma_Z(0)}{M_Z^2} - \frac{\Sigma_W(0)}{M_W^2}$$

(leading, process independent terms)

$\Delta\rho$ gives the main contribution to EW observables:

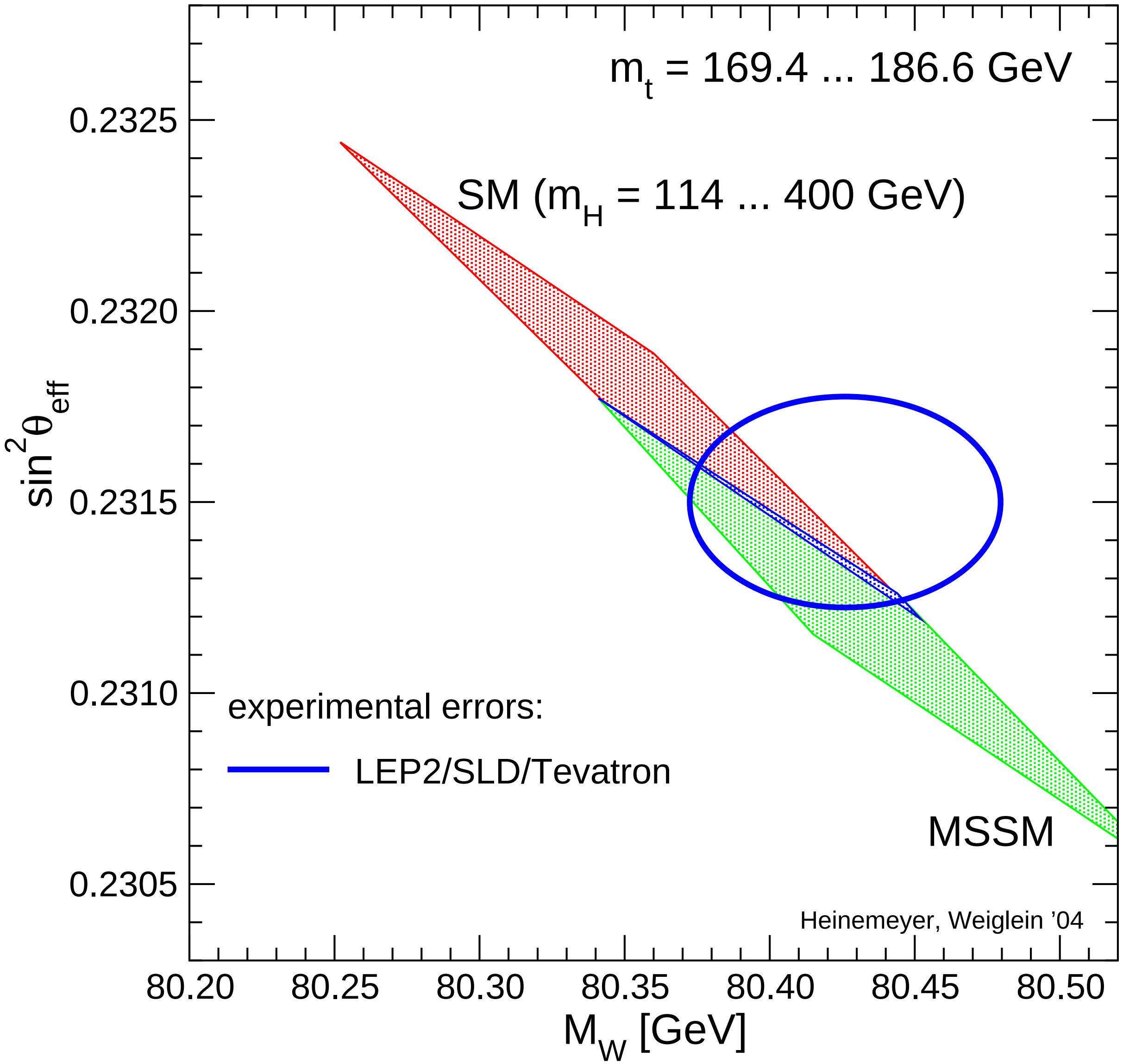
$$\Delta M_W \approx \frac{M_W}{2}\frac{c_{\rm W}^2}{c_{\rm W}^2 - s_{\rm W}^2}\Delta\rho,$$

$$\Delta \sin^2\theta_W^{\rm eff} \approx -\frac{c_{\rm W}^2 s_{\rm W}^2}{c_{\rm W}^2 - s_{\rm W}^2}\Delta\rho$$

$\Rightarrow$ Experimental bound: $\Delta\rho \lesssim 2 \times 10^{-3}$

Example of application:

Prediction for M_W and $\sin^2\theta_{\rm eff}$ in the SM and the MSSM :



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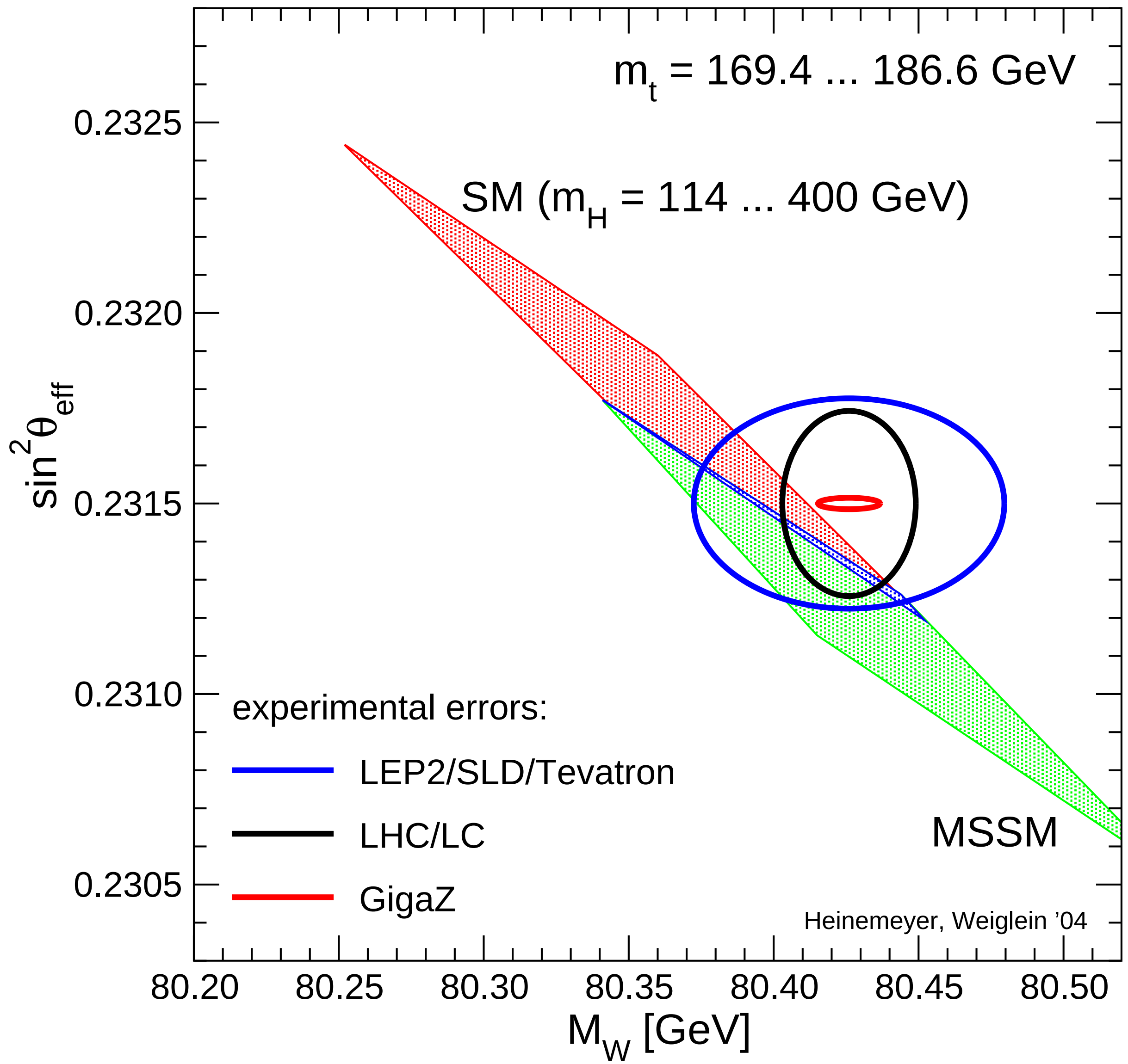

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3.) Theoretical prediction of the lightest MSSM Higgs boson mass: m_h

Contrary to the SM: m_h is not a free parameter

MSSM tree-level bound: $m_h < M_Z$, excluded by LEP Higgs searches

Large radiative corrections:

Dominant one-loop corrections: $\sim G_\mu m_t^4 \ln \left(\frac{m_{\tilde{t}_1} m_{\tilde{t}_2}}{m_t^2} \right)$

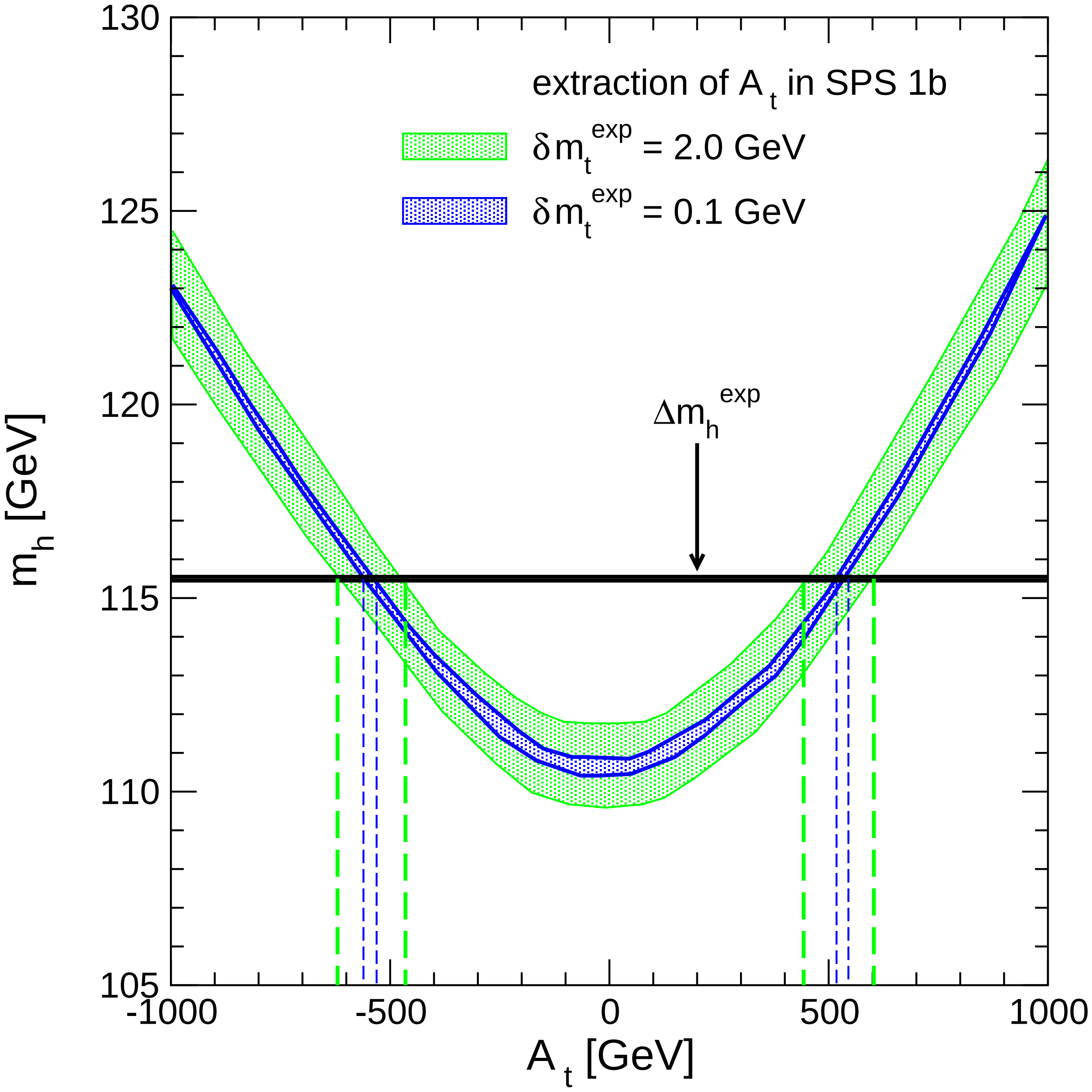
The MSSM Higgs sector is connected to all other sector via loop corrections (especially to the scalar top sector)

Measurement of m_h, Higgs couplings $\Rightarrow$ test of the theory

LHC: $\Delta m_h \approx 0.2$ GeV, LC: $\Delta m_h \approx 0.05$ GeV

$\Rightarrow$ m_h will be (the best?) electroweak precision observable

Example of application: m_h prediction as a function of A_t



SPS1b:

$m_{\tilde{t}_1}, m_{\tilde{t}_2}, m_{\tilde{b}_1}, m_{\tilde{b}_2}$ known,

A_t unknown

$\tan\beta, M_A$ known,

realistic experimental errors assumed

$\Rightarrow$ extraction of A_t possible

but theory errors neglected!

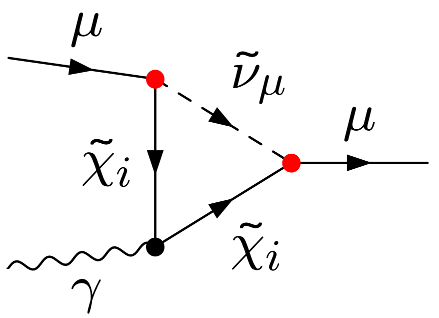
4.) Prediction of the anomalous magnetic moment of the muon: $(g-2)_\mu$

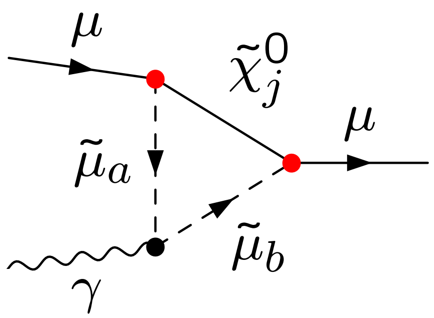
(→ see talk by Dominik Stöckinger on Friday for more details)

Coupling of muon to magnetic field : $\mu - \mu - \gamma$ coupling

$$\bar{u}(p')\left[\gamma^\mu F_1(q^2) + \frac{i}{2m_\mu}\sigma^{\mu\nu}q_\nu F_2(q^2)\right]u(p)A_\mu \qquad F_2(0) = (g-2)_\mu$$

Feynman diagrams for MSSM 1L corrections:

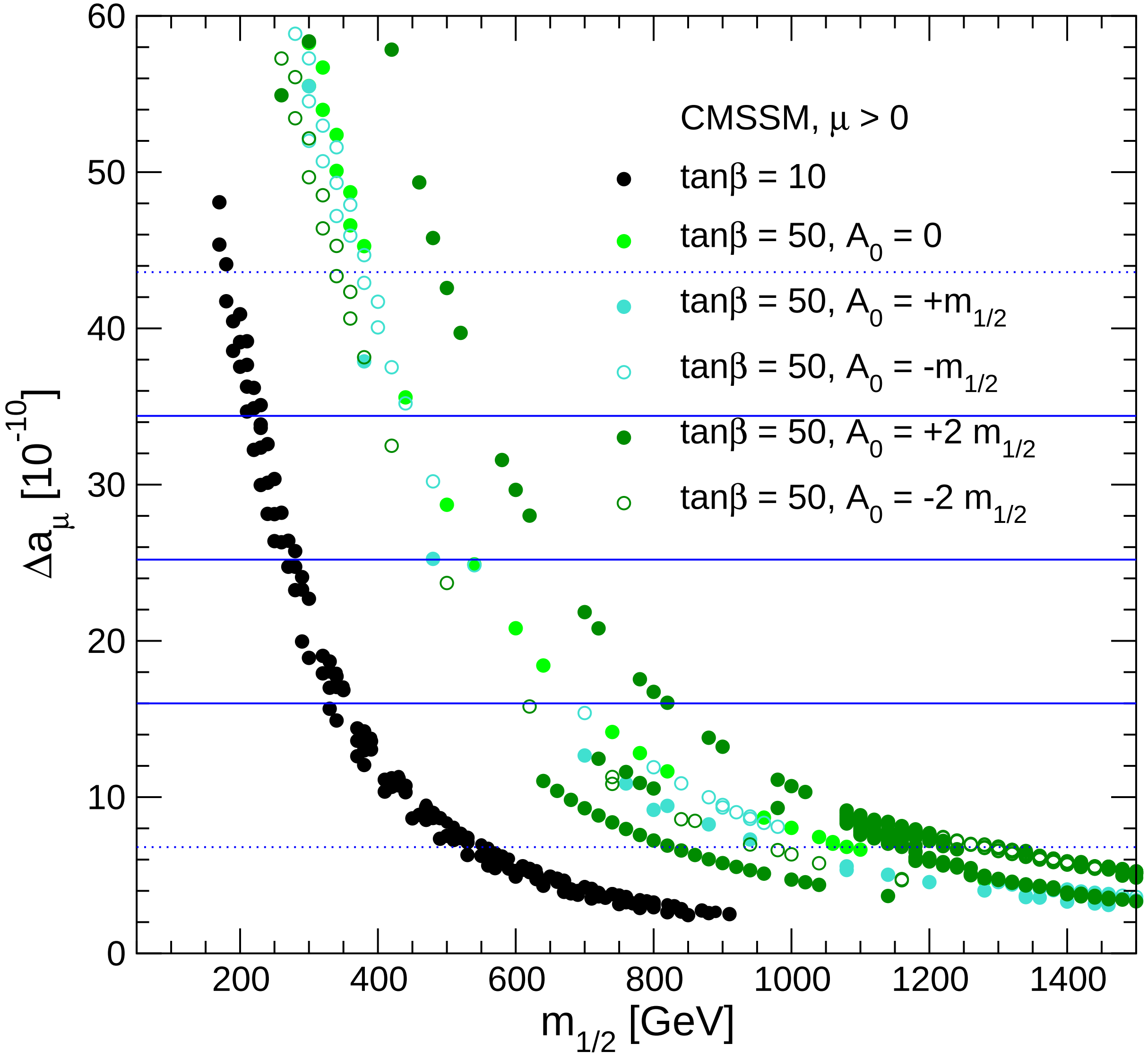




Enhancement factor as compared to SM:

$$\mu - \tilde{\chi}_i^\pm - \tilde{\nu}_\mu \quad : \quad \sim m_\mu \tan\beta$$
$$\mu - \tilde{\chi}_j^0 - \tilde{\mu}_a \quad : \quad \sim m_\mu \tan\beta$$

Example: Investigation of mSUGRA with cold dark matter constraint



Scan over $m_{1/2}$, m_0, A_0
$\tan\beta = 10, 50$
selected points give correct amount of cold dark matter

[*Ellis, S.H., Olive, Weiglein '04*]

Severe bounds on e.g. $m_{1/2}$

3. Status and Perspectives

Experimental error:

– current error

– future expectations

$\Rightarrow$ sets the scale, has to be matched by other errors

Theory error:

– what higher-order corrections are available

– what is missing

$\Rightarrow$ error due to missing higher order corrections

($\rightarrow$ focus on SUSY, no detailed SM results)

Parametric error:

– current uncertainty in the prediction due to error in the input parameters

– future uncertainty

$\Rightarrow$ focus on SM parameters

$\Rightarrow$ derive information about (unknown) SUSY parameters

(SUSY parametric uncertainties highly model dependent)

Status and Perspectives (A) Prediction of M_W and $\sin^2\theta_{\text{eff}}$:

Done:

- MSSM, Δr: full one-loop corrections
  [*P. Chankowski, A. Dabelstein, W. Hollik, W. Mösle, S. Pokorski, J. Rosiek '94*]
  [*D. Garcia, J. Solà '94*]

- MSSM: Z-boson observables, one-loop
  [*D. Garcia, R. Jiménez, J. Solà '95*] [*D. Garcia, J. Solà '95*]
  [*A. Dabelstein, W. Hollik, W. Mösle '95*] [*P. Chankowski, S. Pokorski '96*]

- MSSM, $\Delta\rho$: leading $\mathcal{O}(\alpha\alpha_s)$ corrections
  [*A. Djouadi, P. Gambino, S.H., W. Hollik, C. Jünger, G. Weiglein '97*]
  [*S.H., W. Hollik, G. Weiglein '98*]

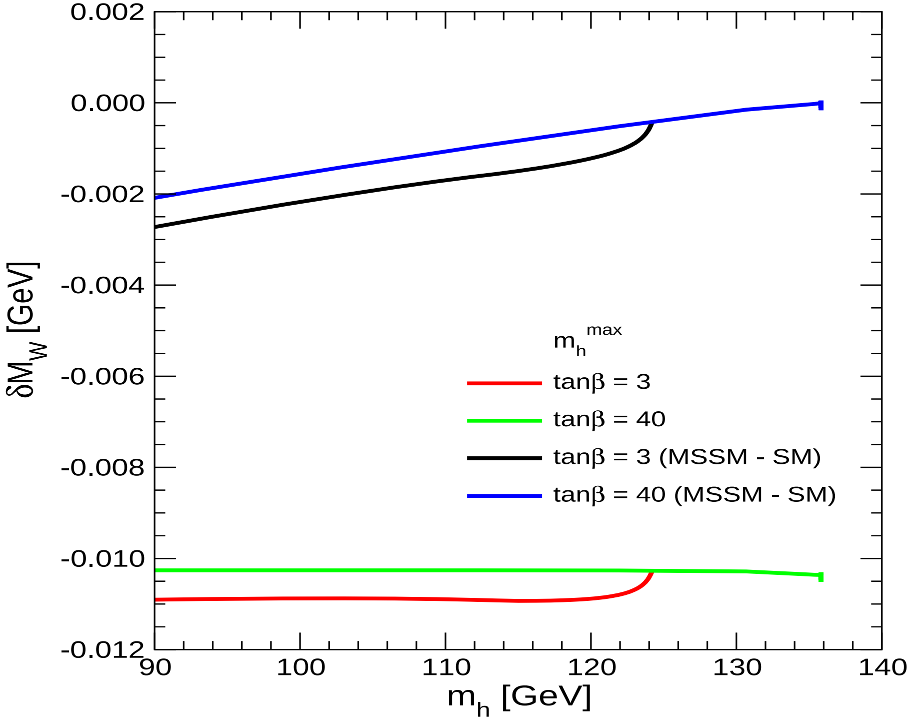
- MSSM, Δr: leading gluonic $\mathcal{O}(\alpha\alpha_s)$ corr.
  [*S.H. '98*]

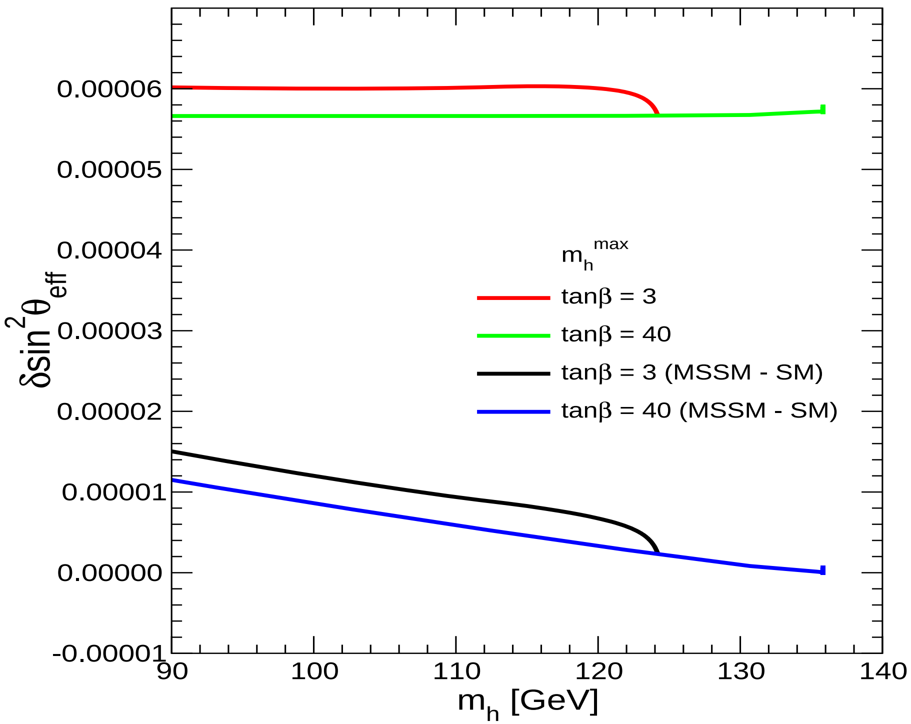
- MSSM, $\Delta\rho$: leading $\mathcal{O}\left(\alpha_t^2, \alpha_t\alpha_b, \alpha_b^2\right)$ corrections ($M_{\text{SUSY}} \to \infty$)
  [*S.H., G. Weiglein '02, '03*]

Missing:

- MSSM, $\Delta\rho$: leading $\mathcal{O}\left(\alpha_t^2, \alpha_t\alpha_b, \alpha_b^2\right)$ corrections ($M_{\text{SUSY}} \neq \infty$)
- MSSM, Δr, $\sin^2\theta_{\text{eff}}$: subleading $\mathcal{O}\left(G_\mu^2 m_t^2\right)$

Effect of latest corrections:





Corrections to M_W up to -12 MeV , $|\delta M_W^{\text{MSSM}-\text{SM}}| \lesssim 3$ MeV

Corrections to $\sin^2\theta_{\text{eff}}$ up to 6×10^{-5} , $\delta\sin^2\theta_{\text{eff}}^{\text{MSSM}-\text{SM}} \lesssim 2 \times 10^{-5}$

Current and future errors:

Current:

$$\delta M_W^{\rm theory} \approx \pm 10 \text{ MeV}, \qquad \delta \sin^2\theta_{\rm eff}^{\rm theory} \approx \pm 10 \times 10^{-5}$$

$$\delta m_t: \quad \delta M_W^{\rm para} \approx \pm 26 \text{ MeV}, \qquad \delta \sin^2\theta_{\rm eff}^{\rm para} \approx \pm 14 \times 10^{-5}$$

$$\delta(\Delta\alpha_{\rm had}): \quad \delta M_W^{\rm para} \approx \pm 6.5 \text{ MeV}, \qquad \delta \sin^2\theta_{\rm eff}^{\rm para} \approx \pm 13 \times 10^{-5}$$

$$\delta M_W^{\rm exp} \approx \pm 34 \text{ MeV}, \qquad \delta \sin^2\theta_{\rm eff}^{\rm exp} \approx \pm 16 \times 10^{-5}$$

Future:

$$\delta M_W^{\rm theory} \gtrsim \pm 2 \text{ MeV}, \qquad \delta \sin^2\theta_{\rm eff}^{\rm theory} \gtrsim \pm 2 \times 10^{-5}$$

$$\delta m_t: \quad \delta M_W^{\rm para} \approx \pm 1 \text{ MeV}, \qquad \delta \sin^2\theta_{\rm eff}^{\rm para} \approx \pm 0.4 \times 10^{-5}$$

$$\delta(\Delta\alpha_{\rm had}): \quad \delta M_W^{\rm para} \approx \pm 1 \text{ MeV}, \qquad \delta \sin^2\theta_{\rm eff}^{\rm para} \approx \pm 1.8 \times 10^{-5}$$

$$[\text{GigaZ}]: \quad \delta M_W^{\rm exp} \approx \pm 7 \text{ MeV}, \qquad \delta \sin^2\theta_{\rm eff}^{\rm exp} \approx \pm 1.3 \times 10^{-5}$$

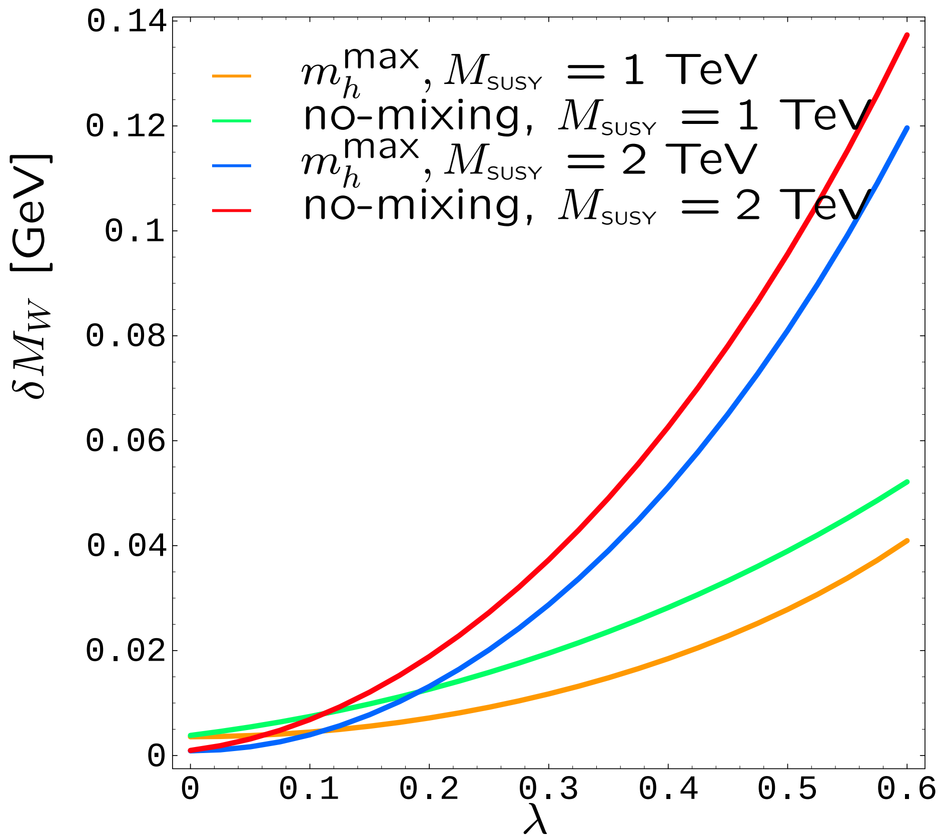
(SUSY parametric errors depend strongly on the scenario)

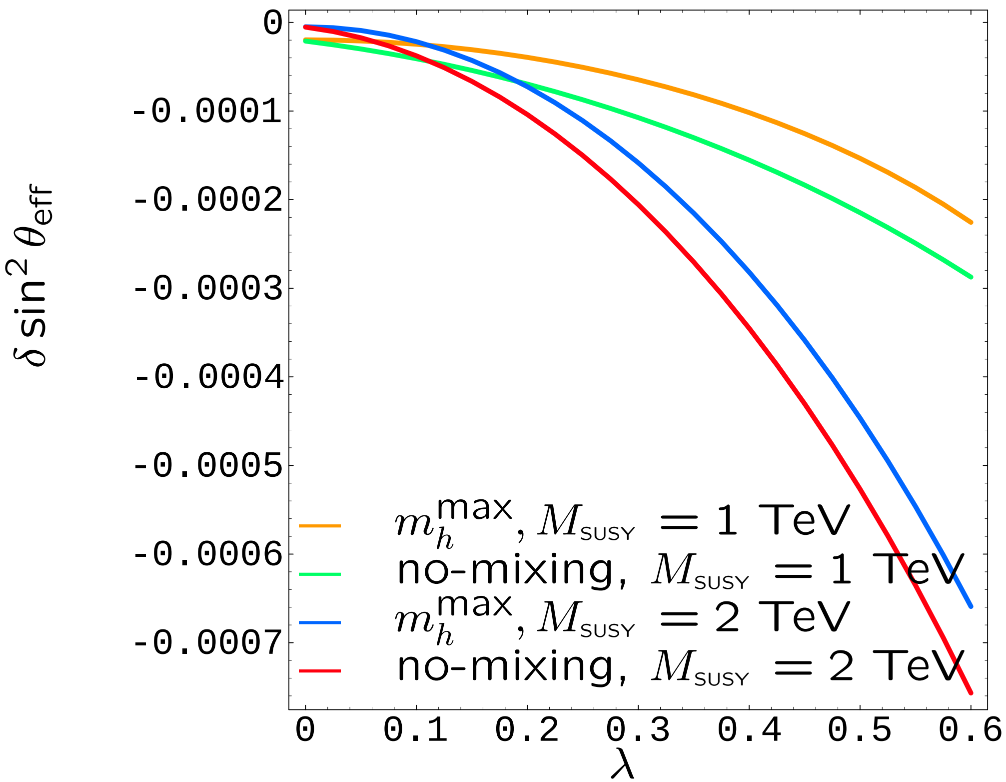
$\Rightarrow M_W$ under control, $\sin^2\theta_{\rm eff}$ barely precise enough

Most recently: Leading corrections in the NMFV MSSM

[S.H., W. Hollik, F. Merz, S. Peñaranda '04]

→ mixing of $\tilde{t}/\tilde{c}$ and $\tilde{b}/\tilde{s}$: LL mixing $\sim \lambda \times M^2_{\text{SUSY}}$ (corresponds to $(\delta_{LL})_{23}$):





⇒ large NMFV mixing λ can be strongly constrained

Status and Perspectives (B) Prediction of m_h in the r/cMSSM:

More recently done (this millennium):

– subleading (non)-log $\mathcal{O}\left(\alpha_t^2\right)$ terms
$\Rightarrow \delta m_h \lesssim 1-4$ GeV
[A. Brignole, G. Degrassi, P. Slavich, F. Zwirner '01] *[J. Espinosa, R. Zhang '01]*

– "Δm_b" effects $\Rightarrow$ leading $\mathcal{O}\left(\alpha_b \alpha_s\right)$ terms
$\Rightarrow \delta m_h$ for large $\tan\beta$
[M. Carena, D. Garcia, U. Nierste, C. Wagner '00]

– Remaining $\mathcal{O}\left(\alpha_b \alpha_s\right)$ corrections
$\Rightarrow \delta m_h \lesssim 0-3$ GeV for very large μ, $\tan\beta$
[A. Brignole, G. Degrassi, P. Slavich, F. Zwirner '01]
[S.H., W. Hollik, H. Rzehak, G. Weiglein '04]

– Leading $\mathcal{O}\left(\alpha_t \alpha_b, \alpha_b^2\right)$ corrections
$\Rightarrow \delta m_h \lesssim 0-3$ GeV for "extreme" parameters
[A. Dedes, G. Degrassi, P. Slavich '03]

– "Full" 2-loop EP (not for OS calculation)
[S. Martin '02, '03]

More recently done (cont.'):

- evaluation of the Higgs sector of the (c)MSSM:
  full 1-loop, $q^2 \neq 0$ (+ leading/subleading 2-loop) $\Rightarrow \delta m_h \lesssim 1 - 7$ GeV
  [*M. Frank, S.H., W. Hollik, G. Weiglein '02*]
- full 1-loop corrections for charged Higgs sector
  [*M. Frank, S.H., W. Hollik, G. Weiglein '02*]
- New renormalization ($\overline{\text{MS}}$/OS)
  for 1-loop result $\Rightarrow \delta m_h \approx 1 - 2$ GeV
  [*M. Frank, S.H., W. Hollik, G. Weiglein '02*]
- Renormalization at $\mathcal{O}(\alpha_b \alpha_s)$
  $\Rightarrow \delta m_h \lesssim 1 - 2$ GeV for very large μ, $\tan\beta$
  [*S.H., W. Hollik, H. Rzehak, G. Weiglein '04*]
- evaluation of the Higgs sector of the NMFV MSSM
  [*S.H., W. Hollik, F. Merz, S. Peñaranda '04*]

Missing:

- full 2-loop (incl. full renormalization)
- leading 3-loop ($\rightarrow$ possible, but technical difficulties . . .)

Remaining higher-order uncertainties:

[*G. Degrassi, S.H., W. Hollik, P. Slavich, G. Weiglein '02*]

2-loop momentum independent:

remaining 2-loop, $q^2 = 0$: $\Delta m_h \lesssim 1.5$ GeV

- subleading $\mathcal{O}(\alpha_t \alpha_s)$
- subleading $\mathcal{O}\left(\alpha_t^2\right)$
- $\mathcal{O}\left(\alpha_\tau^2\right)$
- 2-loop gaugino contributions $\rightarrow$ T

2-loop momentum dependent:

Formally of $\mathcal{O}\left(\alpha_s \alpha_t m_t^2 m_h^2 / M_W^2\right)$
(i.e. like the "remaining 2-loop" corrections)

1-loop: $\Delta m_h \lesssim 2$ GeV

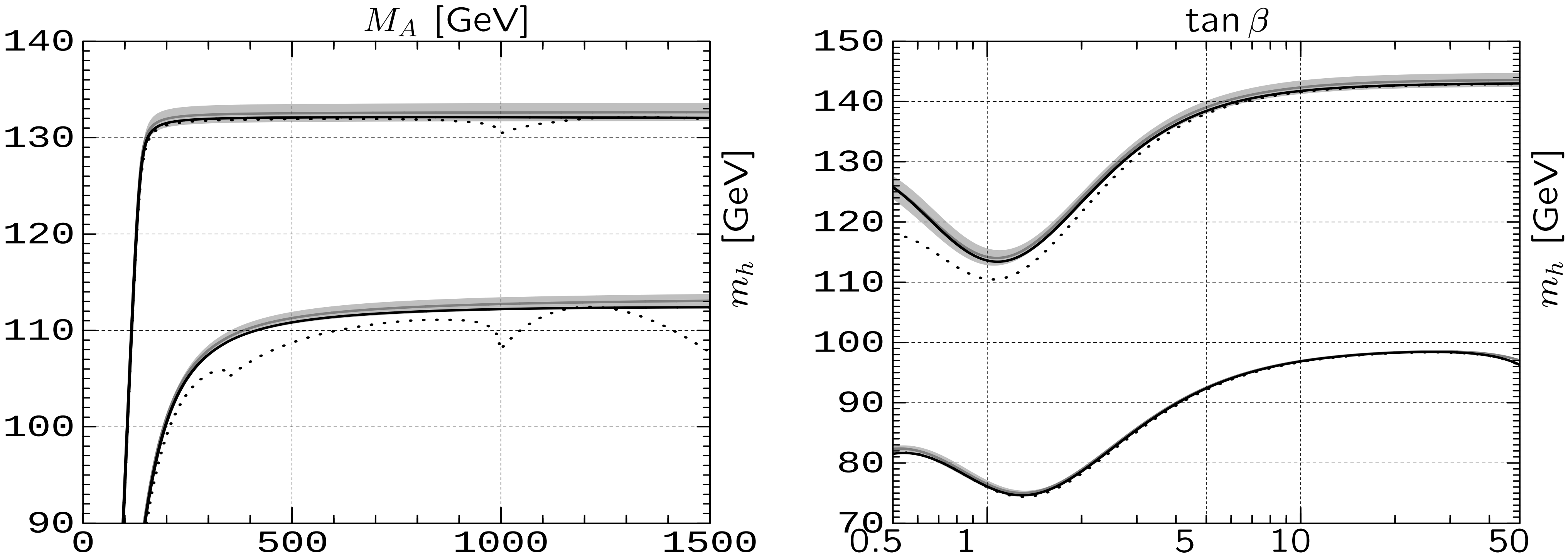
2-loop: $\Delta m_h \lesssim 1$ GeV

Variation of $\overline{\text{MS}}$ renormalization constant:

m_h^{max} scenario, $\mu_{\text{dim}} = 0.5\, m_t \ldots 2\, m_t$

[*M. Frank, S.H., W. Hollik, G. Weiglein '02*]

$\tan\beta = 2, 20$ $\qquad\qquad$ $M_A = 100, 500$ GeV



$t/\tilde{t}$: 3-loop, 4-loop, . . . :

1) changing renormalization of m_t at 2-loop: → T
$\Rightarrow \Delta m_h \lesssim 1.5$ GeV from leading 3-loop corrections

2) explicit formula for simplified case:

$$\Delta m_h^2 = \frac{3\alpha_t \overline{m}_t^2}{\pi^3} \log^3\left(\frac{M_{\text{SUSY}}^2}{m_t^2}\right)\left[\frac{23}{6}\alpha_s^2 - \frac{5}{4}\alpha_s\alpha_t - \frac{33}{64}\alpha_t^2\right]$$

$(M_A = m_{\tilde{g}} = m_{\tilde{t}_1} = m_{\tilde{t}_2} \equiv M_{\text{SUSY}}, \tan\beta \to \infty) \Rightarrow \Delta m_h \lesssim 1.5$ GeV

3) iterative numerical solution of RGEs: [*A. Hoang '97*] $\Rightarrow \Delta m_h \lesssim 1.5$ GeV

$b/\tilde{b}$: 3-loop, 4-loop, . . . :

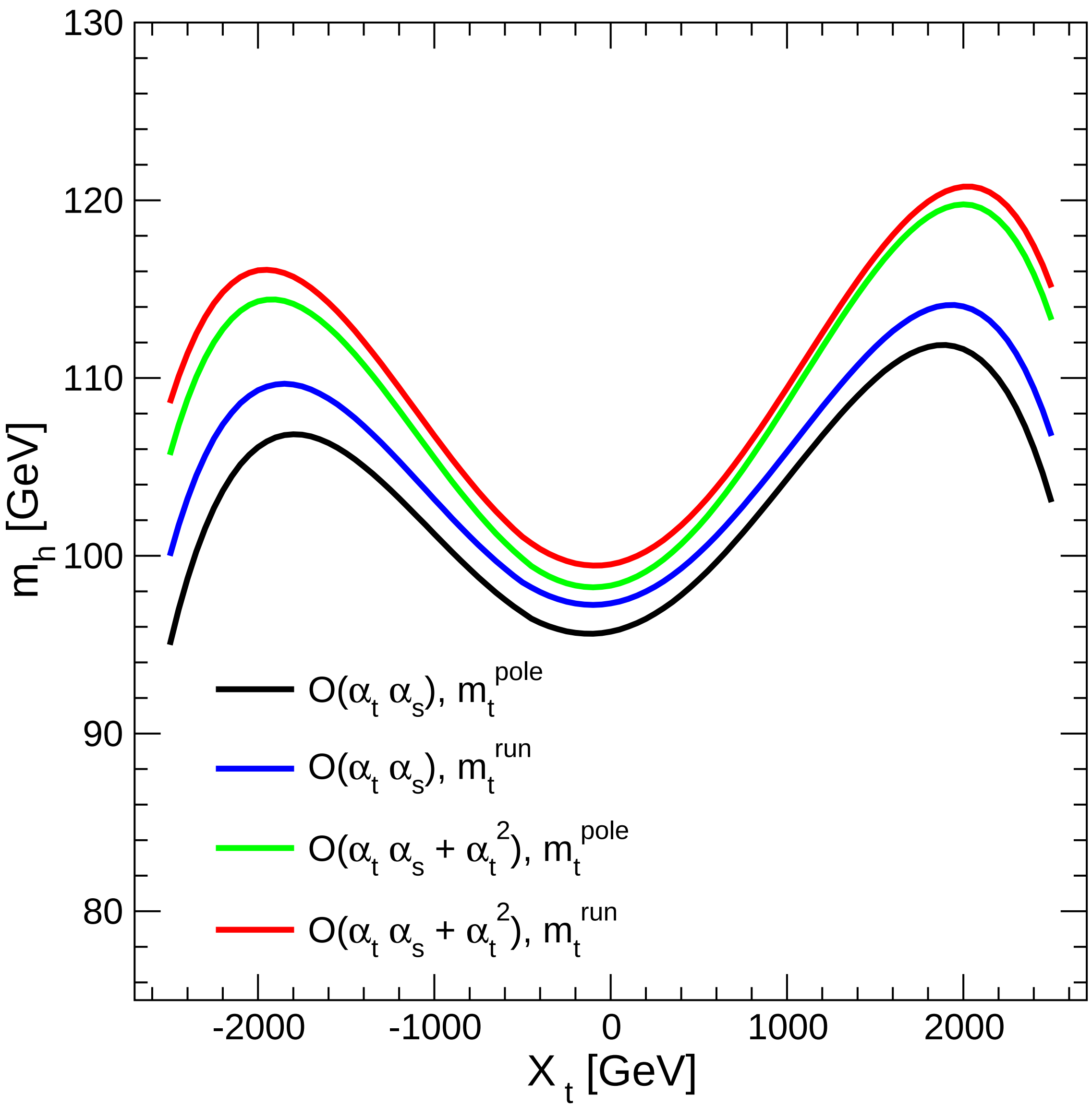
changing the renormalization scheme → T
$\Rightarrow \Delta m_h \lesssim 0 - 3$ GeV (depending on parameter space)

full intrinsic error: (from unknown higher-order corrections)

today: $\Delta m_h^{\text{intr}} \approx 3$ GeV (depending on parameter space)
needed for future: $\Delta m_h^{\text{intr}} \lesssim 0.5 - 0.1$ GeV

$t/\tilde{t}$: 3-loop, 4-loop, ... : changing renormalization of m_t at 2-loop:

[*G. Degrassi, S.H., W. Hollik, P. Slavich, G. Weiglein '02*]



Parameter:

$M_A = M_{\text{SUSY}} = 1$ TeV,

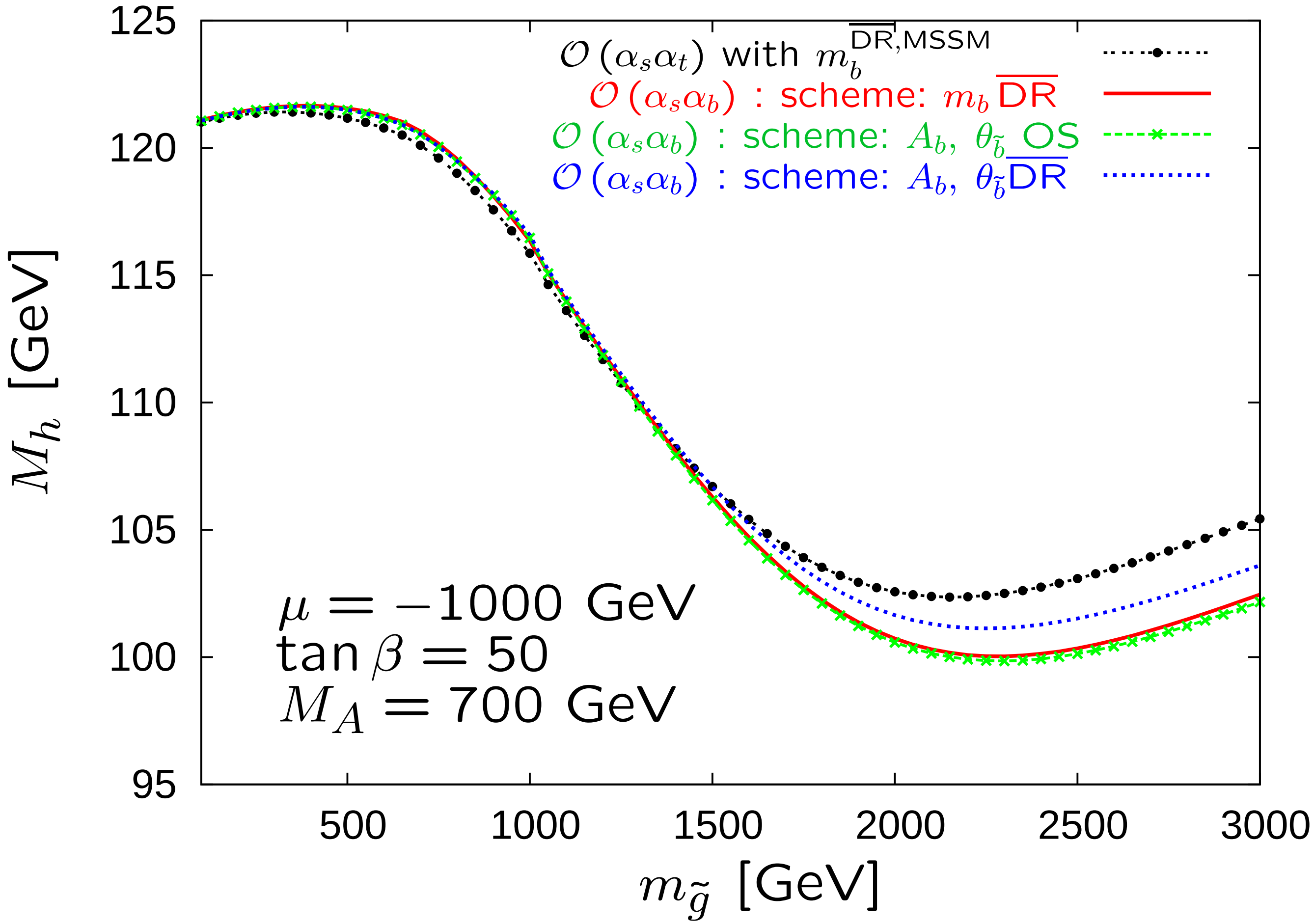
$\tan\beta = 3$

compare: m_t^{pole} vs. m_t^{run}

$\Rightarrow$ $\Delta m_h \lesssim 1.5$ GeV from leading 3-loop corrections

$b/\tilde{b}$: 3-loop, 4-loop, . . . : changing renormalization of $b/\tilde{b}$ sector at 2-loop:

[*S.H., W. Hollik, H. Rzehak, G. Weiglein '04*]



Parameter:

$M_{\text{SUSY}} = 1$ TeV,

$A_t = A_b = 2$ TeV

compare: 3 schemes

$\Rightarrow$ $\Delta m_h \lesssim 0 - 3$ GeV from leading 3-loop corrections depending on parameter space!

($\to$ see talk by S.H. in the PhenClub tomorrow for more details)

Parametric uncertainties:

m_t:

today: $\delta m_t^{\text{Tevatron}} \approx 4$ GeV $\Rightarrow \Delta m_h^{m_t} \approx 4$ GeV

future: $\delta m_t^{\text{LHC}} \approx 1 - 2$ GeV $\Rightarrow \Delta m_h^{m_t} \approx 1 - 2$ GeV $\Rightarrow$ not sufficient!

$\delta m_t^{\text{LC}} \approx 100$ MeV $\Rightarrow \Delta m_h^{m_t} \approx 100$ MeV

m_b: $\delta m_b \lesssim 100$ MeV $\Rightarrow$ negligible

M_W:

today: $\delta M_W = 34$ MeV $\Rightarrow \Delta m_h^{M_W} \approx 100$ MeV

future: $\delta M_W^{\text{GigaZ}} \approx 7$ MeV negligible

α_s:

today: $\delta \alpha_s(M_Z) \approx 0.002 \Rightarrow \Delta m_h^{\alpha_s} \approx 0.3$ GeV

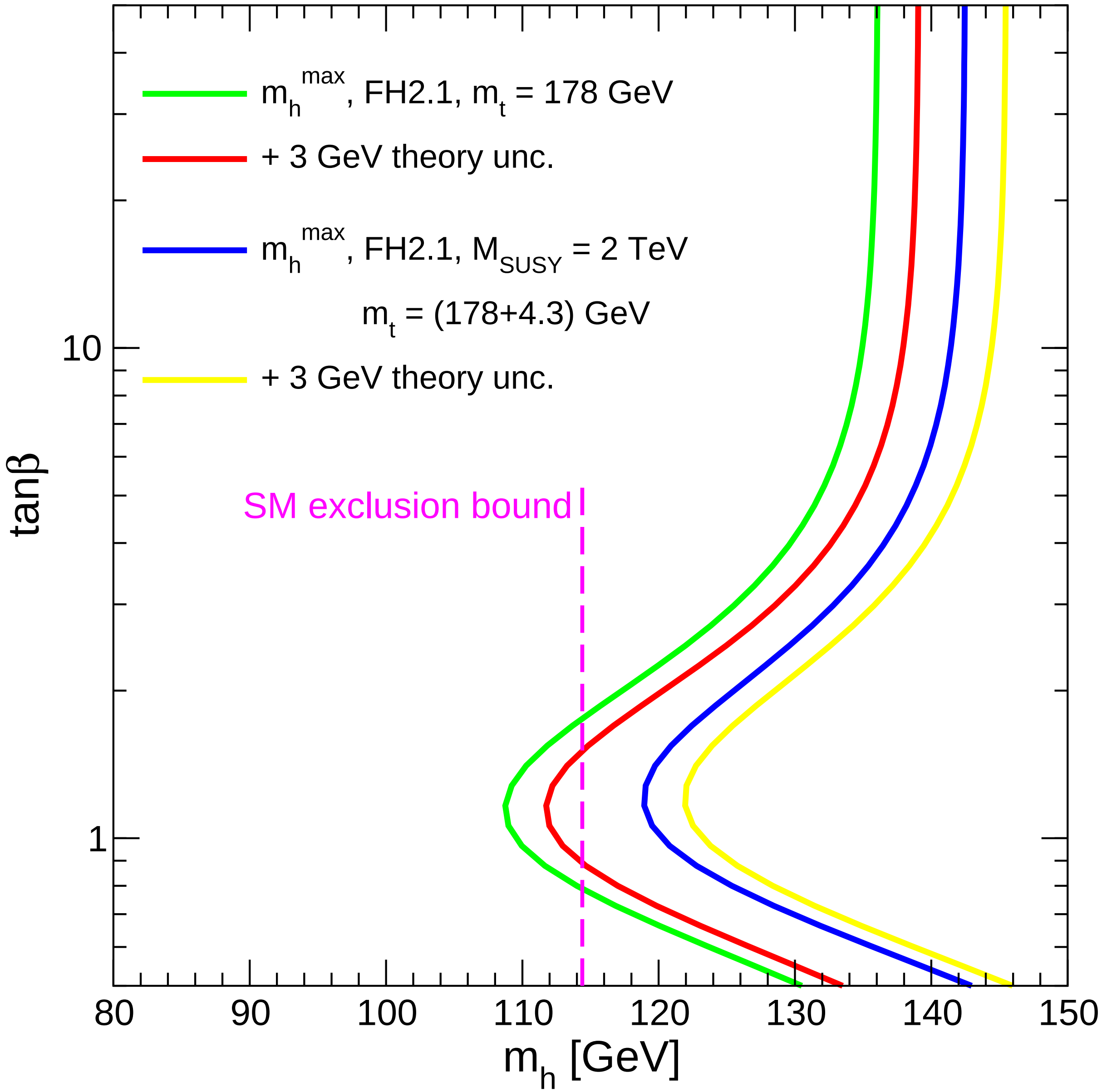
future: $\delta \alpha_s(M_Z) \lesssim 0.001 \Rightarrow \Delta m_h^{\alpha_s} \approx 0.1 - 0.2$ GeV

Experimental uncertainties:

$\Delta m_h^{\text{exp,LHC}} \approx 200$ MeV

$\Delta m_h^{\text{exp,LC}} \approx 50$ MeV $\Rightarrow$ can hardly be matched (we do our best!)

Example I: effect on $\tan\beta$ exclusion:



compare:

m_h^{max} scenario, *FeynHiggs*2.1, $m_t = 178$ GeV

m_h^{max} scenario, *FeynHiggs*2.1, 3 GeV theory unc.

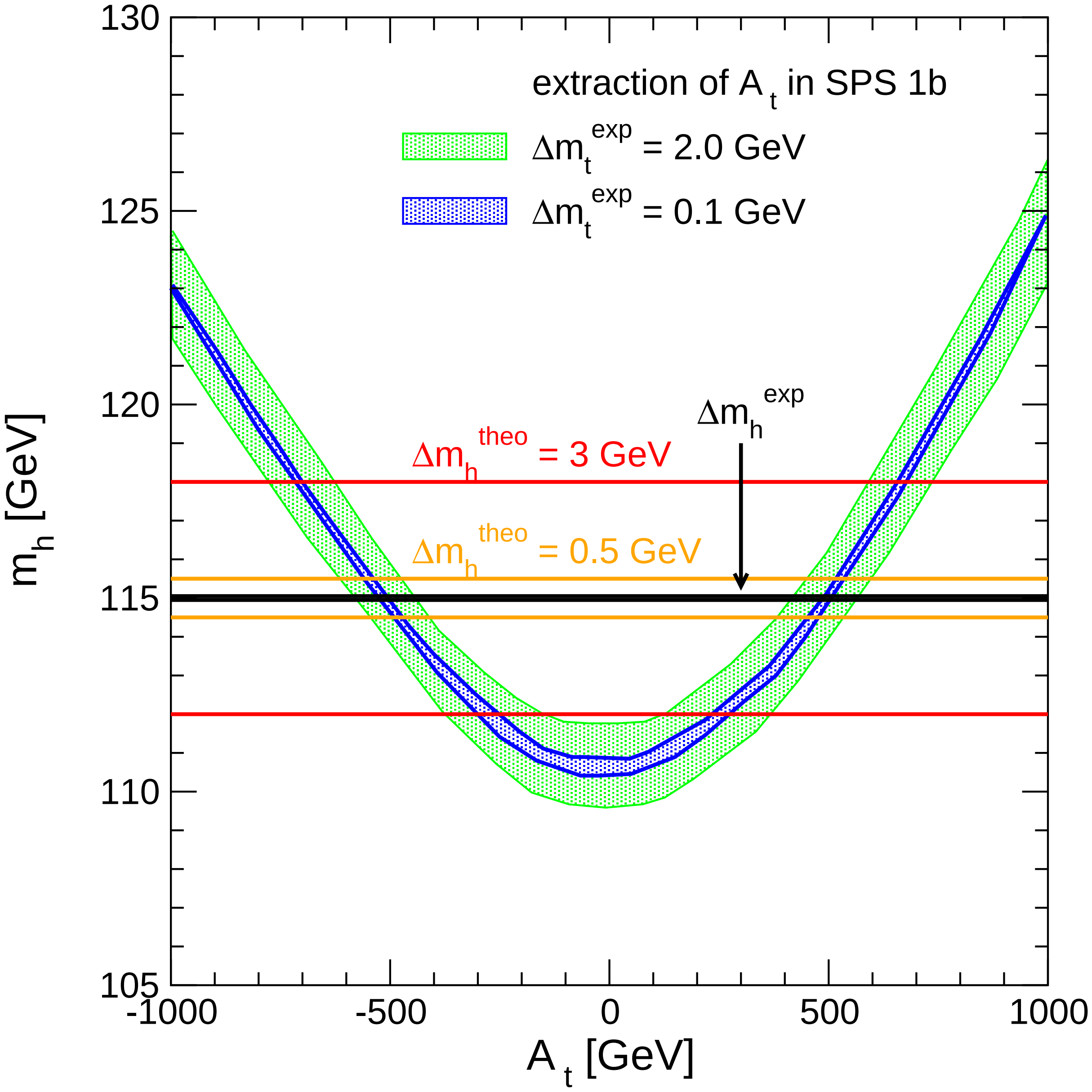
$\Rightarrow$ $\tan\beta$ bound considerably weakened

even worse:

m_h^{max} scenario with $m_t = 182.3$, $M_{SUSY} = 2$ TeV

m_h^{max} scenario with $m_t = 182.3$, $M_{SUSY} = 2$ TeV + 3 GeV theory unc.

Example II: m_h prediction as a function of A_t



SPS1b:

$m_{\tilde{t}_1}, m_{\tilde{t}_2}, m_{\tilde{b}_1}, m_{\tilde{b}_2}$ known,

A_t unknown

$\tan\beta, M_A$ known,

realistic experimental errors assumed

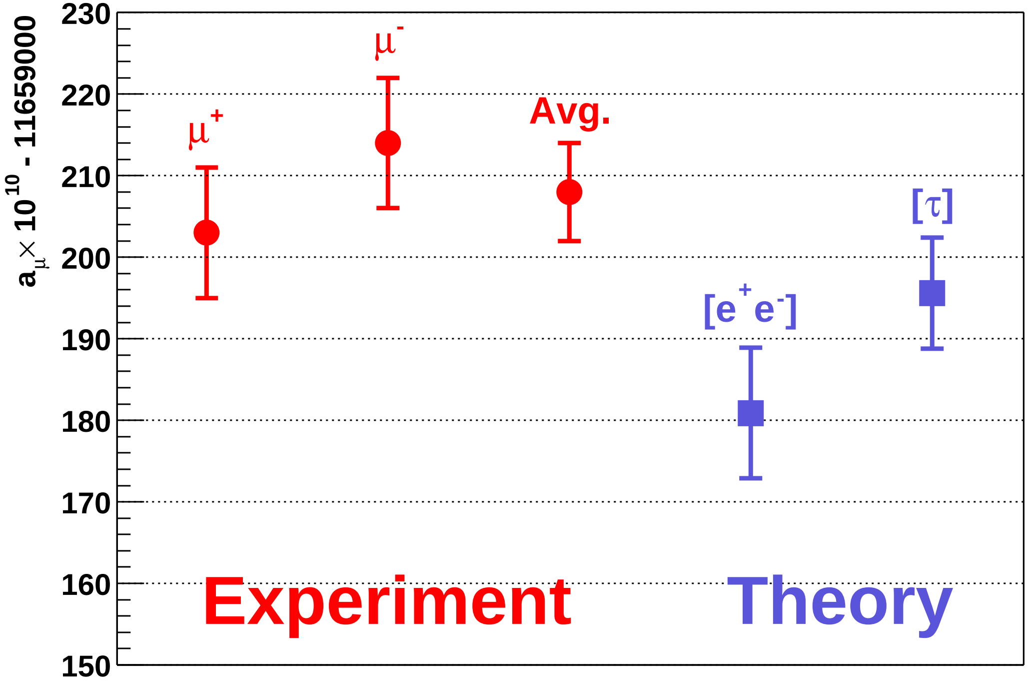
$\Rightarrow$ extraction of A_t possible

$\Rightarrow$ Δm_h^{theo} has to be under control

Status and Perspectives (C)

$$a_\mu \equiv (g-2)_\mu/2$$

Overview about the current experimental and SM (theory) result:
[*g-2 Collaboration, hep-ex/0401008*]



$a_\mu^{\rm exp} - a_\mu^{\rm theo,SM} \approx (25.2 \pm 9.2) \times 10^{-10}$

long history . . .

Overview of the SM theory evaluation:

Source	contr. to $a_\mu[10^{-10}]$	
LO hadr.	$\sim 695 \pm 7$ (e^+e^-)	[*Davier et al, Hagiwara et al. '03*]
		[*Ghozzi, Jegerlehner '03*]
	711.0 ± 6 (τ)	[*Davier, Eidelman, Höcker, Zhang '03*]
LBL	8 ± 4	[*Knecht, Nyffeler '02*]
	13.6 ± 2.5 tbc	[*Melnikov, Vainshtein '03*]
EW 1L	19	
EW 2L	-4	[*Czarnecki, Krause, Marciano '98*]
exp. res.	6	[*BNL E821 '04*]

→ "Isospin breaking effects" in τ data problematic [*Ghozzi, Jegerlehner '03*]

→ KLOE data (radiative return) agrees with e^+e^- data

⇒ general agreement at ICHEP'04 Beijing: discard τ data

$$a_\mu^{\rm exp} - a_\mu^{\rm theo,SM} \approx (25.2 \pm 9.2) \times 10^{-10}$$

Prediction of $(g-2)_\mu$ in the MSSM:

Done:

- full 1-loop corrections
  [T. Moroi '95]

- leading QED log at $\mathcal{O}\left(\alpha^2\right)$ $\Rightarrow$ -8% for $M_{\text{SUSY}} \approx 500$ GeV
  [G. Degrassi, G. Giudice '98]

- some leading parts of Barr-Zee diagrams at 2-loop
  [C. Chen, C. Geng '01] [A. Arhrib, S. Baek '01]
  $\rightarrow$ disagreement by a factor of 4

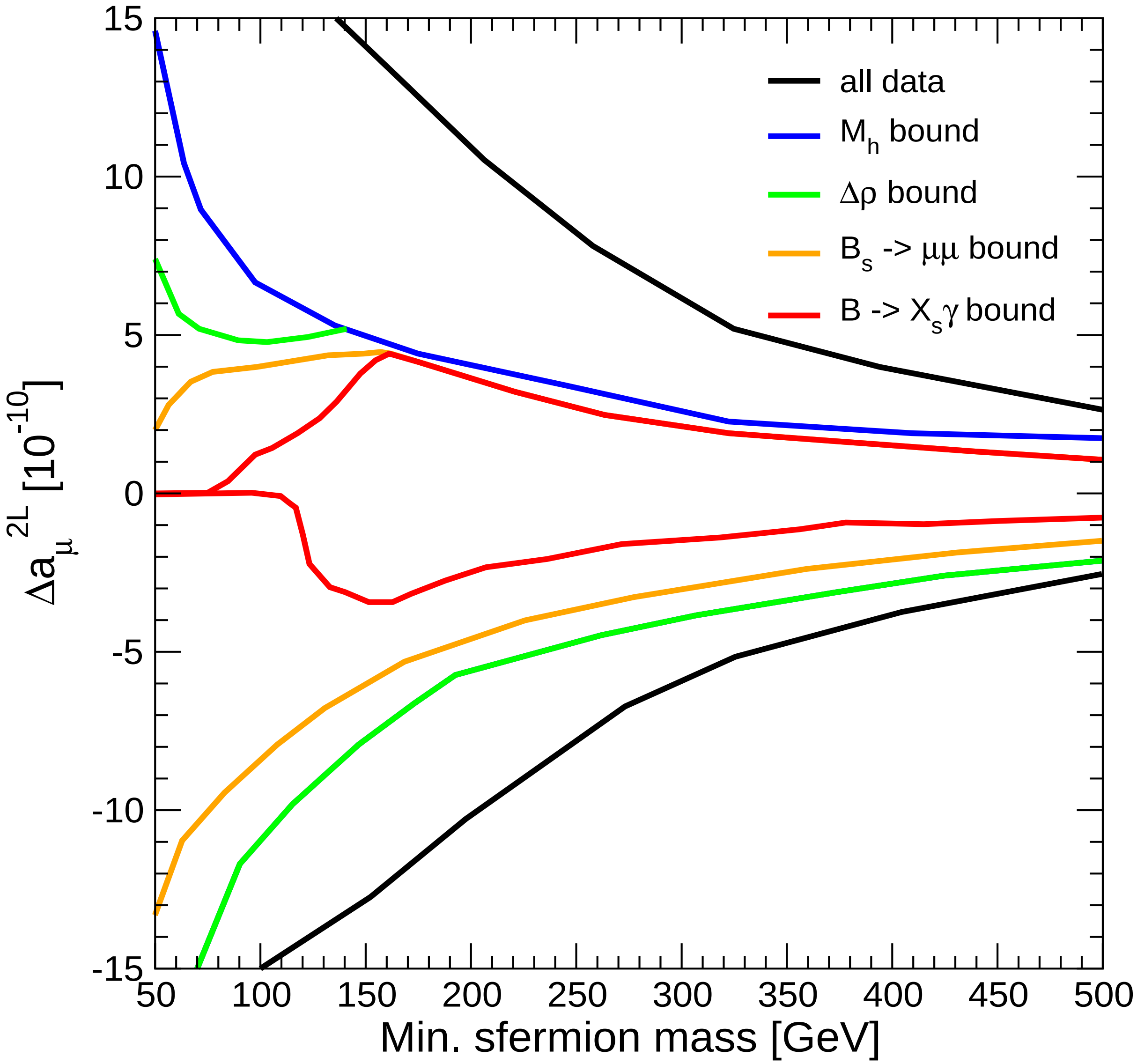
- all 2-loop diagrams with closed SM fermion/sfermion or chargino/neutralino loop
  [S.H., D. Stöckinger, G. Weiglein '03 '04]

Missing:

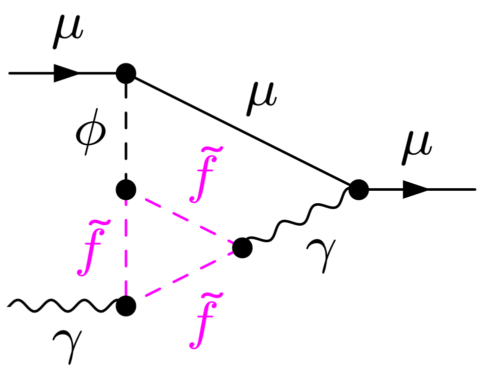
- remaining 2-loop contributions ($\rightarrow$ under way)

Still problematic: SM evaluation, $\Delta\alpha_{\text{had}}$, . . .

Effects of latest corrections: $f/\tilde{f}$ loops (I)



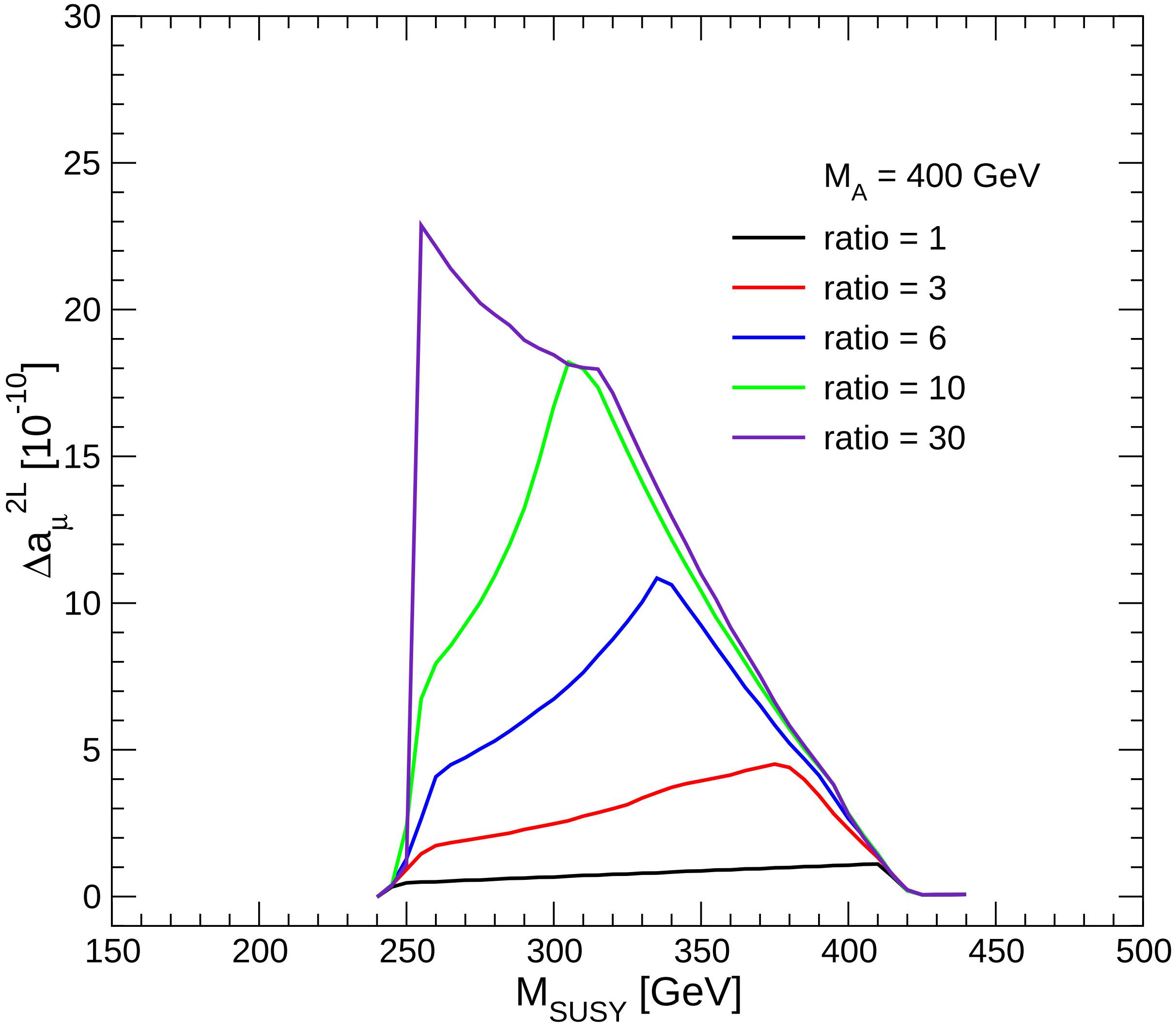
– largest contributions from $(\tilde{f}V\phi)$ (Barr-Zee diag.)



– no constraints
$\Rightarrow$ corrections up to 20×10^{-10} possible

– constraints
$\Rightarrow |\Delta a_\mu^{2L}| \lesssim 5 \times 10^{-10}$

Effects of latest corrections: $f/\tilde{f}$ loops (II)



relaxed universality:

$M_{\text{SUSY}} = M_Q = M_U \neq M_D$

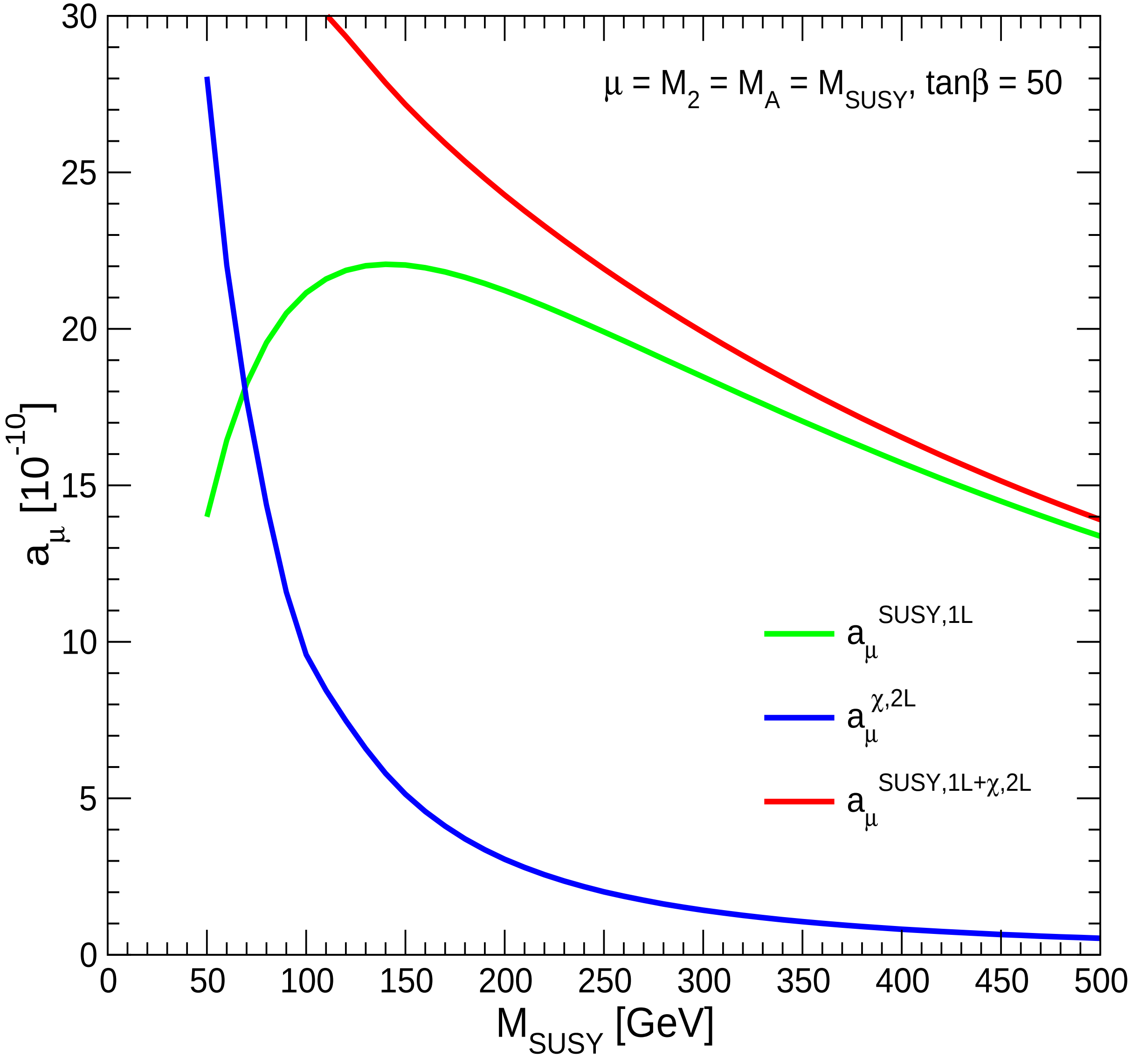
ratio $:= M_D/M_U$

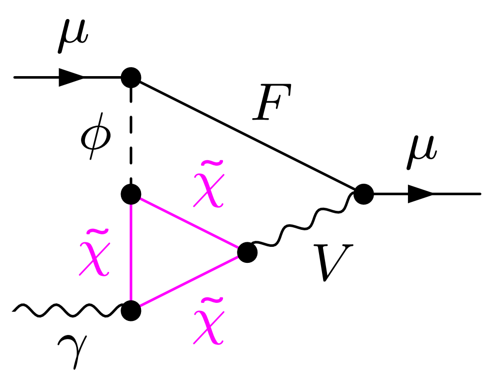
current experimental error:

$\delta a_\mu^{\text{exp}} = \pm 6 \times 10^{-10}$

$\Rightarrow$ huge corrections possible

Effects of latest corrections: chargino/neutralino loops





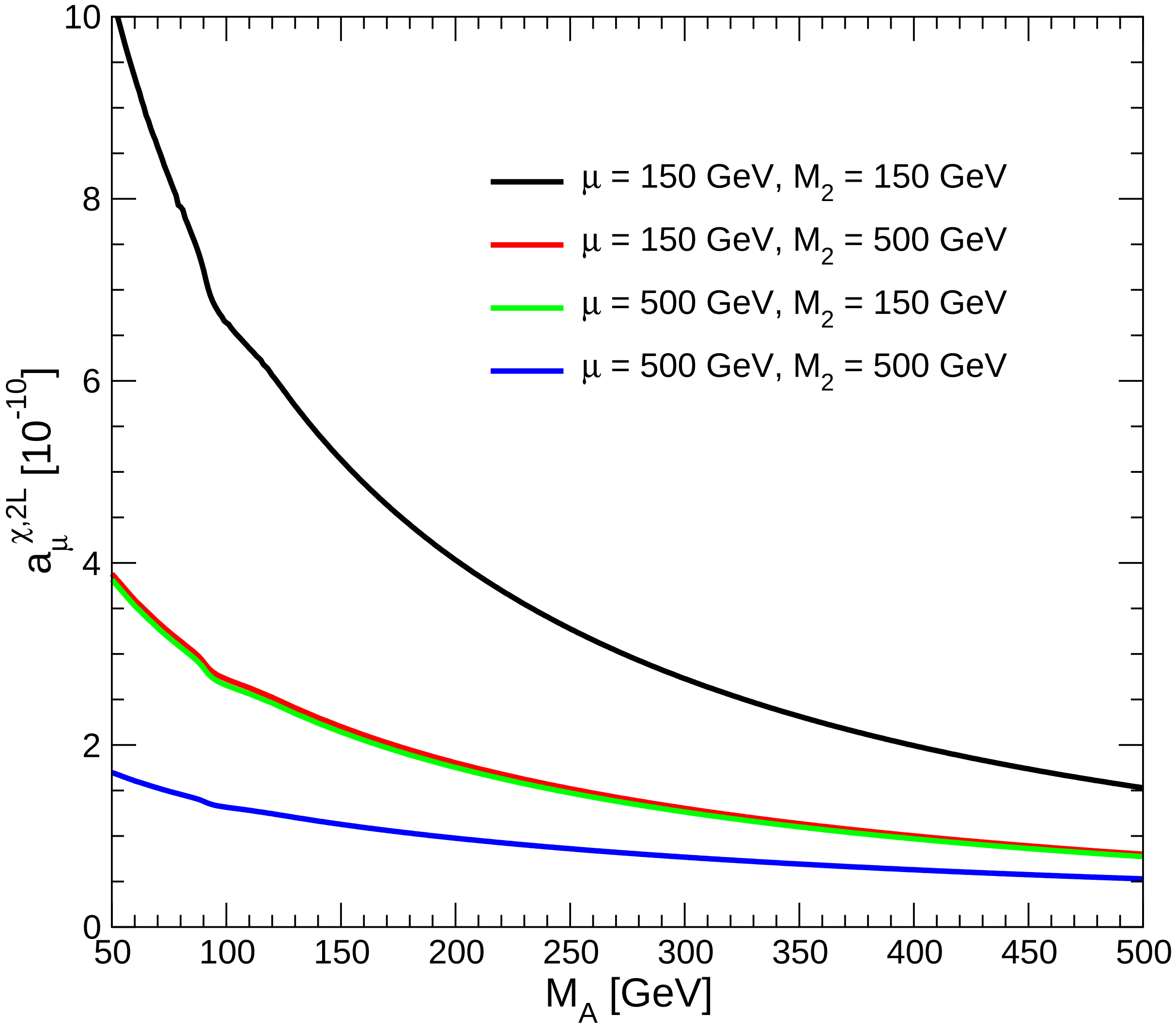
here: 1L suppressed:

$m_{\tilde{\mu}} = m_{\tilde{\nu}} = 1$ TeV

$\Rightarrow$ 2L can be sizable

$\gtrsim 5 \times 10^{-10}$

Results in Split SUSY:



Split SUSY:

[*Arkani-Hamed, Dimopoulos '04*]

[*Giudice, Romanino '04*]

– scalar masses large ($\gtrsim 10^9$ GeV)

– fermion masses "normal"

only non-vanishing contribution to $(g-2)_\mu$: $(\tilde{\chi} V \phi)$

$\Rightarrow$ no sizable contribution survives
result as in the SM

$\Rightarrow$ Split SUSY "excluded" at 95% C.L.

Remaining uncertainties:

1. SUSY 1L diagrams with a mixed $f/\tilde{f}$ loop

$\longrightarrow$ same enhancement factors as
SM 1L diagrams with a closed $f/\tilde{f}$ loop attached

$\Rightarrow$ possibly of similar order

2. THDM corrections to SUSY 1L diagrams

Already known:

QED corrections to $a_\mu^{\text{SUSY}}(1\text{L})$: $\sim -8\%$ for $M_{\text{SUSY}} = 500$ GeV
[*G. Degrassi, G. Giudice '98*]

$\longrightarrow$ only evaluated for a common SUSY mass scale
$\Rightarrow$ non-negligible corrections possible

$\Rightarrow$ Remaining uncertainties estimated to $\sim 6 \times 10^{-10}$
[*S.H., D. Stöckinger, G. Weiglein '04*]

4. Conclusinos

- Precision observables
  - can give valuable information about the "true" Lagrangian
  - can provide bounds on SUSY parameter space

- M_W, $\sin^2\theta_{\text{eff}}$:

$$\text{today}: \quad \delta M_W^{\text{theory}} \approx \pm 10 \text{ MeV}, \qquad \delta\sin^2\theta_{\text{eff}}^{\text{theory}} \approx \pm 10 \times 10^{-5}$$

$$\text{future}: \quad \delta M_W^{\text{theory}} \gtrsim \pm 2 \text{ MeV}, \qquad \delta\sin^2\theta_{\text{eff}}^{\text{theory}} \gtrsim \pm 2 \times 10^{-5}$$

$$\text{[GigaZ]}: \quad \delta M_W^{\text{exp}} \approx \pm 7 \text{ MeV}, \qquad \delta\sin^2\theta_{\text{eff}}^{\text{exp}} \approx \pm 1.3 \times 10^{-5}$$

$\Rightarrow$ M_W under control, $\sin^2\theta_{\text{eff}}$ barely precise enough

- m_h:

$$\text{today}: \quad \delta m_h^{\text{theo}} \approx \pm 3 \text{ GeV}, \quad \delta m_h^{\text{para}} \gtrsim \pm 4 \text{ GeV}, \quad \delta m_h^{\text{exp}} = ???$$

$$\text{future}: \quad \delta m_h^{\text{theo}} \lesssim \pm 0.5 \text{ GeV}, \quad \delta m_h^{\text{para}} \gtrsim \pm 0.1 \text{ GeV}, \quad \delta m_h^{\text{exp}} = 0.05 \text{ GeV}$$

$\Rightarrow$ huge effort necessary to exploit physics potential

- $(g-2)_\mu$: under control with full 2-loop result; $\delta a_\mu^{\text{theo}} \lesssim 6 \times 10^{-10}$

$\Rightarrow$ still problematic: SM evaluation, $\Delta\alpha_{\text{had}}$, ...

Experimental situation:

Current/future Experiments
$\rightarrow$ provide high accuracy measurements !

Theory situation:

measured observables have to be compared with theoretical predictions (of your favorite model)

Measured data is only meaningful if it is matched with theoretical calculations at the same level of accuracy

We have to start **NOW** to achieve necessary accuracy in time

Theoretical calculations should be viewed as an essential part of all future High Energy Physics programs