#### **Trilinos Advanced Capabilities, Extensibility and Future Directions** Michael A. Heroux Sandia National Laboratories





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Sandia is a multiprogram laboratory operated by Sandia Corporation, a Lockheed Martin Company, for the United States Department of Energy under contract DE-AC04-94AL85000.

#### Trilinos Contributors (past 3 years)

Chris Baker Developer of Anasazi, RBGen

Ross Bartlett Lead Developer of MOOCHO, Stratimikos, RTOp, Thyra Developer of Rythmos

Pavel Bochev Lead Developer Intrepid

Paul Boggs Developer of Thyra

Erik Boman Lead Developer Isorropia Developer Zoltan

Todd Coffey Lead Developer of Rythmos

Karen Devine Lead Developer Zoltan

Clark Dohrmann Lead Developer of CLAPS

Carter Edwards Lead Developer phdMesh

Michael Gee Developer of ML, Moertel, NOX

Bob Heaphy Lead developer of Trilinos SQA Developer Zoltan Mike Heroux Trilinos Project Leader Lead Developer of Epetra, AztecOO, Kokkos, IFPACK, Tpetra Developer of Amesos, Belos, EpetraExt

Ulrich Hetmaniuk Developer of Anasazi

Robert Hoekstra Lead Developer of EpetraExt Developer of Epetra

Russell Hooper Developer of NOX

Vicki Howle Lead Developer of Meros

Jonathan Hu Developer of ML

Joe Kotulski Lead Developer of Pliris

**Rich Lehoucq** Developer of Anasazi and Belos

Kevin Long Developer of Thyra

Roger Pawlowski Lead Developer of NOX

Michael Phenow Trilinos Webmaster Developer WebTrilinos

Eric Phipps Lead developer Sacado Developer of LOCA, NOX Dennis Ridzal Lead Developer of Aristos, Intrepid

Marzio Sala Lead Developer of Didasko, Galeri, IFPACK, WebTrilinos Developer of ML, Amesos

Andrew Salinger Lead Developer of LOCA, Capo

Paul Sexton Developer of Epetra and Tpetra

**Bob Shuttleworth** Developer of Meros.

Chris Siefert Developer of ML

Bill Spotz Lead Developer of PyTrilinos Developer of Epetra, New\_Package

Ken Stanley Lead Developer of Amesos and New\_Package

Heidi Thornquist Lead Developer of Anasazi, Belos, RBGen and Teuchos

Ray Tuminaro Lead Developer of ML and Meros

Jim Willenbring Developer of Epetra and New\_Package. Trilinos library manager

Alan Williams Lead Developer Isorropia, FEI Developer of Epetra, EpetraExt, AztecOO, Tpetra

# **Take Home Messages**

- Trilinos is both:
  - A development community
  - A collection of software
- OO techniques lead to:
  - Extensibility at many levels.
  - Scalable infrastructure.
  - Interoperability of independently developed capabilities.
  - Ability to adjust to architecture changes.
- Project is growing:
  - Including more of "vertical software stack".
  - Adapting to broader user base.
- We are seeking collaborations with broader DOE community.



# **Background/Motivation**



### **Target Problems: PDES and more...**



#### **Target Platforms: Any and All** (Now and in the Future)

- Desktop: Development and more...
- Capability machines:
  - Redstorm (XT3), Clusters
  - Roadrunner (Cell-based).
  - Large-count multicore nodes.
- Parallel software environments:
  - MPI of course.
  - UPC, CAF, threads, vectors,...
  - Combinations of the above.
- User "skins":
  - C++/C, Python
  - Fortran.
  - Web, CCA.



# **Motivation For Trilinos**

- Sandia does LOTS of solver work.
- When I started at Sandia in May 1998:
  - Aztec was a mature package. Used in many codes.
  - FETI, PETSc, DSCPack, Spooles, ARPACK, DASPK, and many other codes were (and are) in use.
  - New projects were underway or planned in multi-level preconditioners, eigensolvers, non-linear solvers, etc...
- The challenges:
  - Little or no coordination was in place to:
    - Efficiently reuse existing solver technology.
    - Leverage new development across various projects.
    - Support solver software processes.
    - Provide consistent solver APIs for applications.
  - ASCI (now ASC) was forming software quality assurance/engineering (SQA/SQE) requirements:
    - Daunting requirements for any single solver effort to address alone.



# **Evolving Trilinos Solution**

- Trilinos<sup>1</sup> is an evolving framework to address these challenges:
  - Fundamental atomic unit is a *package*.
  - Includes core set of vector, graph and matrix classes (Epetra/Tpetra packages).
  - Provides a common abstract solver API (Thyra package).
  - Provides a ready-made package infrastructure (new\_package package):
    - Source code management (cvs, bonsai).
    - Build tools (autotools).
    - Automated regression testing (queue directories within repository).
    - Communication tools (mailman mail lists).
  - Specifies requirements and suggested practices for package SQA.
- In general allows us to categorize efforts:
  - Efforts best done at the Trilinos level (useful to most or all packages).
  - Efforts best done at a package level (peculiar or important to a package).
  - Allows package developers to focus only on things that are unique to their package.







# **Trilinos Package Concepts**

Package: The Atomic Unit



## **Trilinos Packages**

- Trilinos is a collection of *Packages*.
- Each package is:
  - Focused on important, state-of-the-art algorithms in its problem regime.
  - Developed by a small team of domain experts.
  - Self-contained: No explicit dependencies on any other software packages (with some special exceptions).
  - Configurable/buildable/documented on its own.
- Sample packages: NOX, AztecOO, ML, IFPACK, Meros.
- Special package collections:
  - Petra (Epetra, Tpetra, Jpetra): Concrete Data Objects
  - Thyra: Abstract Conceptual Interfaces
  - Teuchos: Common Tools.
  - New\_package: Jumpstart prototype.



# **Trilinos Package Summary**

	Objective	Package(s)
Discretizations	Meshing & Spatial Discretizations	phdMesh, Intrepid
	Time Integration	Rythmos
Methods	Automatic Differentiation	Sacado
	Mortar Methods	Moertel
Core	Linear algebra objects	Epetra, Jpetra, Tpetra
	Abstract interfaces	Thyra, Stratimikos, RTOp
	Load Balancing	Zoltan, Isorropia
	"Skins"	PyTrilinos, WebTrilinos, Star-P, ForTrilinos
	C++ utilities, (some) I/O	Teuchos, EpetraExt, Kokkos, Triutils
Solvers	Iterative (Krylov) linear solvers	AztecOO, Belos, Komplex
	Direct sparse linear solvers	Amesos
	Direct dense linear solvers	Epetra, Teuchos, Pliris
	Iterative eigenvalue solvers	Anasazi
	ILU-type preconditioners	AztecOO, IFPACK
	Multilevel preconditioners	ML, CLAPS
	Block preconditioners	Meros
	Nonlinear system solvers	NOX, LOCA
	Optimization (SAND)	MOOCHO, Aristos

## What Trilinos is not

- Trilinos is not a single monolithic piece of software. Each package:
  - Can be built independent of Trilinos.
  - Has its own self-contained CVS structure.
  - Has its own Bugzilla product and mail lists.
  - Development team is free to make its own decisions about algorithms, coding style, release contents, testing process, etc.
- Trilinos top layer is not a large amount of source code: < 2% total SLOC.
- Trilinos is not "indivisible":
  - You don't need all of Trilinos to get things done.
  - Any collection of packages can be combined and distributed.
  - Current public release contains only 30 of the 40+ Trilinos packages.



#### **Insight from History** A Philosophy for Future Directions

- In the early 1800's U.S. had many new territories.
- Question: How to incorporate into U.S.?
  - Colonies? No.
  - Expand boundaries of existing states? No.
  - Create process for self-governing regions. Yes.
  - Theme: Local control drawing on national resources.
- Trilinos package architecture has some similarities:
  - Asynchronous maturation.
  - Packages decide degree of interoperations, use of Trilinos facilities.
- Strength of each: Scalable growth with local control.



# **Trilinos Strategic Goals**

- Scalable Computations: As problem size and processor counts increase, the cost of the computation will remain nearly fixed.
- Hardened Computations: Never fail unless problem essentially intractable, in which case we diagnose and inform the user why the problem fails and provide a reliable measure of error.
- **Full Vertical Coverage:** Provide leading edge enabling technologies through the entire technical application software stack: from problem construction, solution, analysis and optimization.
- Grand Universal Interoperability: All Trilinos packages will be interoperable, so that any combination of packages that makes sense algorithmically will be possible within Trilinos and with compatible external software.
- Universal Accessibility: All Trilinos capabilities will be available to users of major computing environments: C++, Fortran, Python and the Web, and from the desktop to the latest scalable systems.
- Universal Solver RAS: Trilinos will be:
  - Integrated into every major application at Sandia (Availability).
  - The leading edge hardened, efficient, scalable solution for each of these applications (**Reliability**).
  - Easy to maintain and upgrade within the application environment (Serviceability).

Algorithmic Goals

Software Goals



#### **Trilinos Statistics**



Stats: Trilinos Download Page 10/16/2007.

# **External Visibility**



- Awards: R&D 100, HPC SW Challenge (04).
- www.cfd-online.com:

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A project led by Sandia to develop an object-oriented software framework for scientific computations. This is an active project which includes several state-of-the-art solvers and lots of other nice things a software engineer writing CFD codes would find useful. Everything is freely available for download once you have registered. Very good!

- Industry Collaborations: Boeing, Goodyear, ExxonMobil.
- Linux distros: Debian, Mandriva.
- Star-P Interface.
- SciDAC TOPS-2 partner.
- Over 5000 downloads since March 2005.
- Occasional unsolicited external endorsements such as the following two-person exchange on mathforum.org:
  - > The consensus seems to be that OO has little, if anything, to offer
  - > (except bloat) to numerical computing.
  - I would completely disagree. A good example of using OO in numerics is
  - Trilinos: http://software.sandia.gov/trilinos/



#### **Trilinos Presentation Forums**

- Next Trilinos User Group Meeting:
  - Nov 6-8, 2007.
  - At Sandia National Laboratories, Albuquerque, NM, USA.
- ACTS "Hands-on" Tutorial:
  - Aug 19-21, 2008.
  - At Lawrence Berkeley Lab, Berkeley, CA, USA.



# Website

- http:trilinos.sandia.gov
  Developer content on software.sandia.gov.
- Always looking to improve layout, content.
- Site was recently redesigned.









# **Whirlwind Tour of Packages**

**Discretizations Methods Core Solvers** 





Interoperable Tools for Rapid Development of Compatible Discretizations

Intrepid offers an **innovative software design** for compatible discretizations:

- allows access to FEM, FV and FD methods using a common API
- supports hybrid discretizations (FEM, FV and FD) on unstructured grids
- supports a variety of cell shapes:
  - standard shapes (e.g. tets, hexes): high-order finite element methods
  - arbitrary (polyhedral) shapes: low-order mimetic reconstructions

 enables optimization, error estimation, V&V, and UQ using fast invasive techniques (direct support for cell-based derivative computations or via automatic differentiation)





# **Rythmos**

- Suite of time integration (discretization) methods
- Includes: backward Euler, forward Euler, explicit Runge-Kutta, and implicit BDF at this time.
- Native support for operator split methods.
- Highly modular.
- Forward sensitivity computations will be included in the first release with adjoint sensitivities coming in near future.









# **Whirlwind Tour of Packages**

**Discretizations Methods Core Solvers** 





- Capabilities for nonconforming mesh tying and contact formulations in 2 and 3 dimensions using Mortar methods.
- Mortar methods are types of Lagrange Multiplier constraints that can be used in contact formulations and in non-conforming or conforming mesh tying as well as in domain decomposition techniques.
- Used in a large class of nonconforming situations such as the surface coupling of different physical models, discretization schemes or nonmatching triangulations along interior interfaces of a domain.



# Sacado: Automatic Differentiation

- Efficient OO based AD tools optimized for element-level computations
- Applies AD at "element"-level computation
  "Element" means finite element, finite volume, network device,...
- Template application's element-computation code
  - Developers only need to maintain one templated code base
- Provides three forms of AD
  - Forward Mode:  $(x, V) \longrightarrow \left(f, \frac{\partial f}{\partial x}V\right)$ 
    - Propagate derivatives of intermediate variables w.r.t. independent variables forward
    - Directional derivatives, tangent vectors, square Jacobians,  $\partial f/\partial x$  when  $\mathbf{m} \ge \mathbf{n}$ .
  - Reverse Mode:  $(x, W) \longrightarrow \left(f, W^T \frac{\partial f}{\partial x}\right)$ 
    - Propagate derivatives of dependent variables w.r.t. intermediate variables backwards
    - Gradients, Jacobian-transpose products (adjoints),  $\partial f/\partial x$  when **n > m**.
  - Taylor polynomial mode:  $x(t) = \sum_{k=0}^{d} x_k t^k \longrightarrow \sum_{k=0}^{d} f_k t^k = f(x(t)) + O(t^{d+1}), \quad f_k = \frac{1}{k!} \frac{d^k}{dt^k} f(x(t))$
  - Basic modes combined for higher derivatives.

**Developers: Eric Phipps, David Gay** 







# **Whirlwind Tour of Packages**

**Discretizations Methods Core Solvers** 





# **Teuchos**

- Portable utility package of commonly useful tools:
  - ParameterList class: key/value pair database, recursive capabilities.
  - LAPACK, BLAS wrappers (templated on ordinal and scalar type).
  - Dense matrix and vector classes (compatible with BLAS/LAPACK).
  - FLOP counters, timers.
  - Ordinal, Scalar Traits support: Definition of 'zero', 'one', etc.
  - Reference counted pointers / arrays, and more...
- Takes advantage of advanced features of C++:
  - Templates
  - Standard Template Library (STL)
- ParameterList:
  - Allows easy control of solver parameters.
  - XML format input/output.

Developers: Roscoe Barlett, Kevin Long, Heidi Thorquist, Mike Heroux, Paul Sexton, Kris Kampshoff, Chris Baker









- Collection of several sparse/dense kernels that affect the performance of preconditioned Krylov methods
- Goal:
  - Isolate key non-BLAS kernels for the purposes of optimization.
- Kernels:
  - Dense vector/multivector updates and collective ops (not in BLAS/Teuchos).
  - Sparse MV, MM, SV, SM.
- Serial-only for now.
- Reference implementation provided (templated).
- Mechanism for improving performance:
  - Default is aggressive compilation of reference source.
  - BeBOP: Jim Demmel, Kathy Yelick, Rich Vuduc, UC Berkeley.
  - Vector version: Cray.



**Developer: Mike Heroux** 



# Trilinos Common Language: Petra

- Petra provides a "common language" for distributed linear algebra objects (operator, matrix, vector)
- Petra<sup>1</sup> provides distributed matrix and vector services.
- Exists in basic form as an object model:
  - Describes basic user and support classes in UML, independent of language/implementation.
  - Describes objects and relationships to build and use matrices, vectors and graphs.
  - Has 3 implementations under development.



#### **Petra Implementations**

- Epetra (Essential Petra):
  - Current production version.
  - Restricted to real, double precision arithmetic.
  - Uses stable core subset of C++ (circa 2000).
  - Interfaces accessible to C and Fortran users.
- Tpetra (Templated Petra):
  - Next generation C++ version.
  - Templated scalar and ordinal fields.
  - Uses namespaces, and STL: Improved usability/efficiency.
- Jpetra (Java Petra):
  - Pure Java. Portable to any JVM.
  - Interfaces to Java versions of MPI, LAPACK and BLAS via interfaces.





Developers: Mike Heroux, Rob Hoekstra, Alan Williams, Paul Sexton

# **EpetraExt: Extensions to Epetra**

- Library of useful classes not needed by everyone
- Most classes are types of "transforms".
- Examples:
  - Graph/matrix view extraction.
  - Epetra/Zoltan interface.
  - Explicit sparse transpose.
  - Singleton removal filter, static condensation filter.
  - Overlapped graph constructor, graph colorings.
  - Permutations.
  - Sparse matrix-matrix multiply.
  - Matlab, MatrixMarket I/O functions.
- Most classes are small, useful, but non-trivial to write.





# Thyra

- High-performance, abstract interfaces for linear algebra
- Offers flexibility through abstractions to algorithm developers
- Linear solvers (Direct, Iterative, Preconditioners)
  - Abstraction of basic vector/matrix operations (dot, axpy, mv).
  - Can use any concrete linear algebra library (Epetra, PETSc, BLAS).
- Nonlinear solvers (Newton, etc.)
  - Abstraction of linear solve (solve Ax=b).
  - Can use any concrete linear solver library:
    - AztecOO, ML, PETSc, LAPACK
- Transient/DAE solvers (implicit)
  - Abstraction of nonlinear solve.
  - ... and so on.



Developers: Roscoe Bartlett, Kevin Long



# **PyTrilinos**



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- PyTrilinos provides Python access to Trilinos packages.
- Uses SWIG to generate bindings.
- Epetra, AztecOO, IFPACK, ML, NOX, LOCA, Amesos and NewPackage are support.
- Possible to:
  - Define RowMatrix implementation in Python.
  - Use from Trilinos C++ code.
- Performance for large grain is equivalent to C++.
- Several times hit for very fine grain code.







# **WebTrilinos**

- WebTrilinos: Web interface to Trilinos
  - Generate test problems or read from file.
  - Generate C++ or Python code fragments and click-run.
  - Hand modify code fragments and re-run.









# **Whirlwind Tour of Packages**

**Discretizations Methods Core Solvers** 


## **IFPACK: Algebraic Preconditioners**

- Overlapping Schwarz preconditioners with incomplete factorizations, block relaxations, block direct solves.
- Accept user matrix via abstract matrix interface (Epetra versions).
- Uses Epetra for basic matrix/vector calculations.
- Supports simple perturbation stabilizations and condition estimation.
- Separates graph construction from factorization, improves performance substantially.
- Compatible with AztecOO, ML, Amesos. Can be used by NOX and ML.

Developers: Marzio Sala, Mike Heroux





### : Multi-level Preconditioners

- Smoothed aggregation, multigrid and domain decomposition preconditioning package
- Critical technology for scalable performance of some key apps.
- ML compatible with other Trilinos packages:
  - Accepts user data as Epetra\_RowMatrix object (abstract interface). Any implementation of Epetra\_RowMatrix works.
  - Implements the Epetra\_Operator interface. Allows ML preconditioners to be used with AztecOO, Belos, Anasazi.
- Can also be used completely independent of other Trilinos packages.





### Amesos

- Interface to direct solvers for distributed sparse linear systems (KLU, UMFPACK, SuperLU, MUMPS, ScaLAPACK)
- Challenges:
  - No single solver dominates
  - Different interfaces and data formats, serial and parallel
  - Interface often changes between revisions
- Amesos offers:
  - A single, clear, consistent interface, to various packages
  - Common look-and-feel for all classes
  - Separation from specific solver details
  - Use serial and distributed solvers; Amesos takes care of data redistribution
  - Native solvers: KLU and Paraklete



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Developers: Ken Stanley, Marzio Sala, Tim Davis



# **AztecOO**

- Krylov subspace solvers: CG, GMRES, Bi-CGSTAB,...
- Incomplete factorization preconditioners
- Aztec is the workhorse solver at Sandia:
  - Extracted from the MPSalsa reacting flow code.
  - Installed in dozens of Sandia apps.
  - 1900+ external licenses.
- AztecOO improves on Aztec by:
  - Using Epetra objects for defining matrix and RHS.
  - Providing more preconditioners/scalings.
  - Using C++ class design to enable more sophisticated use.
- AztecOO interfaces allows:
  - Continued use of Aztec for functionality.
  - Introduction of new solver capabilities outside of Aztec.





Developers: Mike Heroux, Alan Williams, Ray Tuminaro

# **Belos and Anasazi**

- Next generation linear solvers (Belos) and eigensolvers (Anasazi) libraries, written in templated C++.
- Provide a generic interface to a collection of algorithms for solving large-scale linear problems and eigenproblems.
- Algorithm implementation is accomplished through the use of abstract base classes (mini interface) and traits classes. Interfaces are derived from these base classes to:
  - operator-vector products
  - status tests
  - orthogonalization
  - any arbitrary linear algebra library.
- Includes <u>block</u> linear solvers and eigensolvers.

Developers: Heidi Thornquist, Mike Heroux, Chris Baker, Rich Lehoucq, Ulrich Hetmaniuk





- Suite of nonlinear solution methods
- NOX uses abstract vector and "group" interfaces:
  - Allows flexible selection and tuning of various strategies:
    - Directions.
    - Line searches.
  - Epetra/AztecOO/ML, LAPACK, PETSc implementations of abstract vector/group interfaces.
- Designed to be easily integrated into existing applications.







- Library of continuation algorithms
- Provides
  - Zero order continuation
  - First order continuation
  - Arc length continuation
  - Multi-parameter continuation (via Henderson's MF Library)
  - Turning point continuation
  - Pitchfork bifurcation continuation
  - Hopf bifurcation continuation
  - Phase transition continuation
  - Eigenvalue approximation (via ARPACK or Anasazi)



**Developers: Andy Salinger, Eric Phipps** 



- MOOCHO: Multifunctional Object-Oriented arCHitecture for Optimization
  - Large-scale invasive simultaneous analysis and design (SAND) using reduced space SQP methods.

**Developer: Roscoe Bartlett** 

- Aristos: Optimization of large-scale design spaces
  - Invasive optimization approach based on full-space SQP methods.
  - Efficiently manages inexactness in the inner linear system solves.



**Developer: Denis Ridzal** 

# Full "Vertical" Solver Coverage <u>Trilinos Packages</u>

Optimization Problems:		
• Unconstrained:	Find $u \in \Re^n$ that minimizes $f(u)$	MOOCHO,
• Constrained:	Find $y \in \Re^m$ and $u \in \Re^n$ that	Aristos
	minimizes $f(y, u)$ s.t. $c(y, u) = 0$	
Transient Problems:	Solve $f(\dot{x}(t), x(t), t) = 0$	
· DAEs/ODEs:	$t \in [0,T], \ x(0) = x_0, \ \dot{x}(0) = x'_0$	Rythmos
	for $x(t) \in \Re^n$ , $t \in [0,T]$	
Nonlinear Problems:	Given nonlinear op $c(x, u) \in \mathfrak{K}^{n+m} \to \mathfrak{K}^{n}$	
• Nonlinear equations:	Solve $c(x) = 0$ for $x \in \Re^n$	NOX
• Stability analysis:	For $c(x, u) = 0$ find space $u \in U \ni \frac{\partial c}{\partial x}$ singular	LOCA
Implicit Linear Problems:	Given linear ops (matrices) $A, B \in \Re^{n \times n}$	AztecOO, Belos,
• Linear equations:	Solve $Ax = b$ for $x \in \Re^n$	Ifpack,ML,etc.
• Eigen problems:	Solve $Av = \lambda Bv$ for (all) $v \in \Re^n$ , $\lambda \in \Re$	Anasazi
Explicit Linear Problems:		Epotro Tpotro
• Matrix/graph equations:	Compute $y = Ax$ ; $A = A(G)$ ; $A \in \Re^{m \times n}$ , $G \in \square^{m \times n}$	
• Vector problems:	Compute $y = \alpha x + \beta w$ ; $\alpha = \langle x, y \rangle$ ; $x, y \in \Re^n$	<b>ID</b> National Laboratories

# Algorithms Research: Truly Useful Multi-level Methods

- Fly-through of next 4 slides.
- Theme:

Multi-level preconditioning has come of age across broad spectrum of problems.





#### **ASC SIERRA** Applications

#### SIERRA/Fuego/Syrinx

- Helium plume V&V Project
- > 260K, 16 processor run

ML/GMRES is ~25% faster than without ML

As problem size increase, ML expected to be more beneficial

#### **SIERRA/Aria Multiphysics**

coupled potential/thermal/displacement DP MEMS problem

ML reduced solve time (40%) from ~20 minutes to ~12 minutes

compared to actual ANSYS runs & ARIA re-creation ANSYS scheme







time = 22.67 s



# Compressible flow to determine aerodynamic characteristics for the Nuclear Weapons Complex

- Additional Issues that have been addressed
  - FEI/Nox/Trilinos interface development
  - Block Algorithm Improvements
  - Block Gauss-Seidel, Block Grid Transfers

- B61 problem (6.5 million dofs, 64 procs)
- Pseudo-transient + Newton
- Euler flow, Mach .8

- Linear solver: 173 solves, tolerance= 10<sup>-4</sup>
  - GMRES/ILU → 7494 sec
- GMRES/MG → 3704 sec





- Falcon problem (13<sup>+</sup> Million dofs, 150 procs)
- Pseudo-transient + Newton
- Euler flow, Mach .75
- Linear solver: 109 solves, tolerance= 10<sup>4</sup>
- GMRES/ILU → 7620 sec
- GMRES/MG → 3787 sec
- 10x improvement on final linear solve.
- > 5x gains on some problems
   over entire sequence



- New Grid Transfers (220<sup>+</sup>K Falcon, 1 proc)
- Pseudo-transient + Newton, Euler flow @ Mach .75
- Last linear solve, tolerance= 10<sup>-9</sup>
  - GMRES/MG/old transfers  $\rightarrow$  47 its, 49 sec
  - GMRES/MG/new transfers  $\rightarrow$  24 its, 26 sec



# **Multi-level Methods Summary**

- Solving <u>hard, real</u> problems <u>fast, scalably</u>.
- Still need more...



# Algorithms Research: Specialized Solvers

- Next wave of capabilities: Specialized solvers.
- Examples in Trilinos:
  - Optimal domain decomposition preconditioners for structures: CLAPS
  - Mortar methods for interface coupling: Moertel.
  - Segregated Preconditioners for Navier-Stokes: Meros.
- Examples in Applications:
  - EMU (with Boeing).
  - Tramonto.





Lipid Bi-Layer Problem: One example (of many variations)





### **Preconditioner for** *S*





# **Tramonto Solver Summary**

- 3-level linear operator structure.
- Matlab to fully parallel: 1 month.
- Complex orchestration:
  - Preconditioner: 100+ distributed Epetra matrices used in sequence.
  - ML, IFPACK, Amesos used on subproblems.
- Utilizes 8 Trilinos packages in total.
- 566 Lines of Code (Polymer Solver).
- Polymorphic Design.



#### **3D Polymer Results**





## **Properties of New Solver**

- Uniform distributed mesh  $\rightarrow$  uniform distributed work.
- Preconditioner sub-steps naturally parallel:
  - $\rightarrow$  Results invariant to processor count up to round-off.
- Preconditioner requires almost no extra memory:
  - $\rightarrow$  4-10X reduction over previous approach.
- GMRES subspace and storage reduced 6X 10X or more Laurie's Favorite Properties!
- Speedup 20-2X.
  - Solver has:
    - No tuning parameters.
    - Near linear scaling.

Michael A. Heroux, Laura J. D. Frink, and Andrew G. Salinger. Schur complement based approaches to solving density functional theories for inhomogeneous fluids on parallel computers. SIAM J. Sci. Comput. 2007.



## **Extending Capabilities: Preconditioners, Operators, Matrices**

Illustrated using AztecOO as example



## **Epetra User Class Categories**

- Sparse Matrices: *RowMatrix*, (CrsMatrix, VbrMatrix, FECrsMatrix, FEVbrMatrix)
- Linear Operator: *Operator*: (AztecOO, ML, Ifpack)
- Dense Matrices: DenseMatrix, DenseVector, BLAS, LAPACK, SerialDenseSolver
- Vectors: Vector, MultiVector
- Graphs: CrsGraph
- Data Layout: Map, BlockMap, LocalMap
- Redistribution: Import, Export, LbGraph, LbMatrix
- Aggregates: LinearProblem
- Parallel Machine: Comm, (SerialComm, MpiComm, MpiSmpComm)
- Utilities: Time, Flops



### **LinearProblem Class**

- •A linear problem is defined by:
  - Matrix A :
    - An Epetra\_RowMatrix or Epetra\_Operator object. (often a CrsMatrix or VbrMatrix object.)
  - Vectors *x*, *b* : Vector objects.
- •To call AztecOO, first define a LinearProblem:
  - Constructed from *A*, *x* and *b*.
  - Once defined, can:
    - Scale the problem (explicit preconditioning).
    - Precondition it (implicitly).
    - Change *x* and *b*.



## **AztecOO**

- Aztec is the previous workhorse solver at Sandia:
  - Extracted from the MPSalsa reacting flow code.
  - Installed in dozens of Sandia apps.
- AztecOO leverages the investment in Aztec:
  - Uses Aztec iterative methods and preconditioners.
- AztecOO improves on Aztec by:
  - Using Epetra objects for defining matrix and RHS.
  - Providing more preconditioners/scalings.
  - Using C++ class design to enable more sophisticated use.
- AztecOO interfaces allows:
  - Continued use of Aztec for functionality.
  - Introduction of new solver capabilities outside of Aztec.



### A Simple Epetra/AztecOO Program

// Header files omitted...
int main(int argc, char \*argv[]) {
 MPI\_Init(&argc,&argv); // Initialize MPI, MpiComm
 Epetra\_MpiComm Comm( MPI\_COMM\_WORLD );

// \*\*\*\*\* Map puts same number of equations on each pe \*\*\*\*\*

int NumMyElements = 1000 ; Epetra\_Map Map(-1, NumMyElements, 0, Comm); int NumGlobalElements = Map.NumGlobalElements();

// \*\*\*\*\* Create an Epetra Matrix tridiag(-1,2,-1) \*\*\*\*\*

Epetra\_CrsMatrix A(Copy, Map, 3); double negOne = -1.0; double posTwo = 2.0;

for (int i=0; i<NumMyElements; i++) {
 int GlobalRow = A.GRID(i);
 int RowLess1 = GlobalRow - 1;
 int RowPlus1 = GlobalRow + 1;
 if (RowLess1!=-1)
 A.InsertGlobalValues(GlobalRow, 1, &negOne, &RowLess1);
 if (RowPlus1!=NumGlobalElements)
 A.InsertGlobalValues(GlobalRow, 1, &negOne, &RowPlus1);
 A.InsertGlobalValues(GlobalRow, 1, &posTwo, &GlobalRow);
}</pre>

A.FillComplete(); // Transform from GIDs to LIDs

// \*\*\*\*\* Create x and b vectors \*\*\*\*\*
Epetra\_Vector x(Map);
Epetra\_Vector b(Map);
b.Random(); // Fill RHS with random #s

// \*\*\*\*\* Create Linear Problem \*\*\*\*\*
Epetra\_LinearProblem problem(&A, &x, &b);

// \*\*\*\*\* Create/define AztecOO instance, solve \*\*\*\*\*
AztecOO solver(problem);
solver.SetAztecOption(AZ\_precond, AZ\_Jacobi);
solver.Iterate(1000, 1.0E-8);

MPI\_Finalize() ; return 0;

### **AztecOO Extensibility**

- AztecOO is designed to accept externally defined:
  - **Operators** (both *A* and *M*):
    - The linear operator *A* is accessed as an Epetra\_Operator.
    - Users can register a preconstructed preconditioner as an Epetra\_Operator.
  - RowMatrix:
    - If *A* is registered as a RowMatrix, Aztec's preconditioners are accessible.
    - Alternatively *M* can be registered separately as an Epetra\_RowMatrix, and Aztec's preconditioners are accessible.
  - StatusTests:
    - Aztec's standard stopping criteria are accessible.
    - Can override these mechanisms by registering a StatusTest Object.



# AztecOO understands Epetra\_Operator

- AztecOO is designed to accept externally defined:
  - Operators (both *A* and *M*).
  - RowMatrix (Facilitates use of AztecOO preconditioners with external A).
  - StatusTests (externallydefined stopping criteria).





# AztecOO Understands Epetra\_RowMatrix



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# AztecOO UserOp/UserMat Recursive Call Example

#### Trilinos/packages/aztecoo/example/AztecOO\_RecursiveCall

- 1. Poisson2dOperator A(nx, ny, comm); // Generate nx by ny Poisson operator
- 2. Epetra\_CrsMatrix \* precMatrix = A.GeneratePrecMatrix(); // Build tridiagonal approximate Poisson
- 3. Epetra\_Vector xx(A.OperatorDomainMap()); // Generate vectors (xx will be used to generate RHS b)
- 4. Epetra\_Vector x(A.OperatorDomainMap());
- 5. Epetra\_Vector b(A.OperatorRangeMap());
- 6. xx.Random(); // Generate exact x and then rhs b
- 7. A.Apply(xx, b);
- 8. // Build AztecOO solver that will be used as a preconditioner
- 9. Epetra\_LinearProblem precProblem;
- 10. precProblem.SetOperator(precMatrix);
- 11. AztecOO precSolver(precProblem);
- 12. precSolver.SetAztecOption(AZ\_precond, AZ\_ls);
- 13. precSolver.SetAztecOption(AZ\_output, AZ\_none);
- 14. precSolver.SetAztecOption(AZ\_solver, AZ\_cg);
- 15. AztecOO\_Operator precOperator(&precSolver, 20);
- 16. Epetra\_LinearProblem problem(&A, &x, &b); // Construct linear problem
- 17. AztecOO solver(problem); // Construct solver
- 18. solver.SetPrecOperator(&precOperator); // Register Preconditioner operator
- 19. solver.SetAztecOption(AZ\_solver, AZ\_cg);
- 20. solver.Iterate(Niters, 1.0E-12);



# Ifpack/AztecOO Example

#### Trilinos/packages/aztecoo/example/IfpackAztecOO

- 1. // Assume A, x, b are define, LevelFill and Overlap are specified
- 2. Ifpack\_IlukGraph IlukGraph(A.Graph(), LevelFill, Overlap);
- 3. IlukGraph.ConstructFilledGraph();
- 4. Ifpack\_CrsRiluk ILUK (IlukGraph);
- 5. ILUK.InitValues(A);
- 6. assert(ILUK->Factor()==0); // Note: All Epetra/Ifpack/AztecOO method return int err codes
- 7. double Condest;
- 8. ILUK.Condest(false, Condest); // Get condition estimate
- 9. if (Condest > tooBig) {
- 10. ILUK.SetAbsoluteThreshold(Athresh);
- 11. ILUK.SetRelativeThreshold(Rthresh);
- 12. Go back to line 4 and try again
- 13.
- 14. Epetra\_LinearProblem problem(&A, &x, &b); // Construct linear problem
- 15. AztecOO solver(problem); // Construct solver
- 16. solver.SetPrecOperator(&ILUK); // Register Preconditioner operator
- 17. solver.SetAztecOption(AZ\_solver, AZ\_cg);
- 18. solver.lterate(Niters, 1.0E-12);
- 19. // Once this linear solutions complete and the next nonlinear step is advanced,
- 20. // we will return to the solver, but only need to execute steps 5 on down...



# **Multiple Stopping Criteria**

- Possible scenario for stopping an iterative solver:
  - Test 1: Make sure residual is decreased by 6 orders of magnitude. And
  - Test 2: Make sure that the inf-norm of <u>true</u> residual is no more 1.0E-8.

But

- Test 3: do no more than 200 iterations.
- Note: Test 1 is *cheap*. Do it before Test 2.



### **AztecOO StatusTest classes**

- AztecOO\_StatusTest:
  - Abstract base class for defining stopping criteria.
  - Combo class: OR, AND, SEQ



AztecOO\_StatusTest Methods



# AztecOO/StatusTest Example

Trilinos/packages/aztecoo/example/AztecOO

- 1. // Assume A, x, b are define
- 2. Epetra\_LinearProblem problem(&A, &x, &b); // Construct linear problem
- 3. AztecOO solver(problem); // Construct solver
- 4. AztecOO\_StatusTestResNorm restest1(A, x, bb, 1.0E-6);
- 5. restest1.DefineResForm(AztecOO\_StatusTestResNorm::Implicit, AztecOO\_StatusTestResNorm::TwoNorm);
- 6. restest1.DefineScaleForm(AztecOO\_StatusTestResNorm::NormOfInitRes, AztecOO\_StatusTestResNorm::TwoNorm);
- 7. AztecOO\_StatusTestResNorm restest2(A, x, bb, 1.0E-8);
- 8. restest2.DefineResForm(AztecOO\_StatusTestResNorm::Explicit, AztecOO\_StatusTestResNorm::InfNorm);
- 9. restest2.DefineScaleForm(AztecOO\_StatusTestResNorm::NormOfRHS, AztecOO\_StatusTestResNorm::InfNorm);
- 10. AztecOO\_StatusTestCombo comboTest1(AztecOO\_StatusTestCombo::SEQ, restest1, restest2);
- 11. AztecOO\_StatusTestMaxIters maxItersTest(200);
- 12. AztecOO\_StatusTestCombo comboTest2(AztecOO\_StatusTestCombo::OR, maxItersTest1, comboTest1);
- 13. solver.SetStatusTest(&comboTest2);
- 14. solver.SetAztecOption(AZ\_solver, AZ\_cg);
- 15. solver.lterate(Niters, 1.0E-12);



# **Summary: Extending Capabilities**

- Trilinos packages are designed to interoperate.
- All packages (ML, IFPACK, AztecOO, ...) that can provide linear operators:
  - Implement the Epetra\_Operator interface.
  - Are available to any package that can use an linear operator.
- All packages (ML, AztecOO, NOX, Belos, Anasazi, ...) that can use linear operators:
  - Accept linear operator via Epetra\_Operator interface.
  - Support easy user extensions.
- All packages (ML, IFPACK, AztecOO, ...) that need matrix coefficient data:
  - Can access that data from Epetra\_RowMatrix interface.
  - Can use any concrete Epetra matrix class, or any user-provided adapter.



## **Summary: Extending Capabilities**

AztecOO is one example:

- Flexibility comes from abstract base classes:
  - Epetra\_Operator:
    - All Epetra matrix classes implement.
    - Best way to define A and M when coefficient info **not** needed.
  - Epetra\_RowMatrix:
    - All Epetra matrix classes implement.
    - Best way to define A and M when coefficient info is needed.
  - AztecOO\_StatusTest:
    - A suite of parametrized status tests.
    - An abstract interface for users to define their own.
    - Ability to combine tests for sophisticated control of stopping.


#### **A Few More Useful Things**



#### **Fortran Interface**

- Presently Trilinos has no full-featured Fortran interface.
- Plans in place to develop OO Fortran interface.
- Developed as part of SciDAC TOPS-2 effort.
- Just ramping up now.



# **Stratimikos**

- New package in Trilinos 7.0.
- Single point of access to Trilinos preconditioners/solvers:
  - Common interface all preconditioners.
  - Common interface to all solvers.
  - Selection of preconditioner/solver via parameter list.
- Simplest way to access the suite of Trilinos capabilities.
- Simple driver code available on website.
- Will be the focus of Fortran access to Trilinos.



# **Dynamic External Package Support**

- New directory Trilinos/packages/external.
- Supports seamless integration of externally developed packages via package registration.
- Your package: "WorldsBestPreconditioner"
  - Understands configure/make.
  - Can have its own options: --enable-superfast-mode
- Copy source into Trilinos/packages/external.
- In Trilinos/packages/external, type:
   ./CustomizeExternal.csh WorldsBestPreconditioner
- Build Trilinos in the usual way using configure/make.
  - Include arguments such as --enable-superfast-mode: They will be passed down to your package.



# **Software Quality**



# SQA/SQE

- Software Quality Assurance/Engineering is important.
- Not sufficient to say, "We do a good job."
- Trilinos facilitates SQA/SQE development/processes for packages:
  - 10 of 30 ASC SQE practices are directly handled by Trilinos (no requirements on packages).
  - Trilinos provides infrastructure support for the remaining 20.
  - Trilinos Dev Guide Part II: Specific to ASC requirements.
  - Trilinos software engineering policies provide a ready-made infrastructure for new packages.
  - Trilinos philosophy: Few *requirements*. Instead mostly *suggested practices*. Provides package with option to provide alternate process.



Trilinos Service	SQE Practices Impact
Yearly Trilinos User Group Meeting (TUG) and Developer Forum: Once a year gathering for tutorials, package feature updates, user/developer requirements discussion and developer training.	<ul> <li>All Requirements steps: gathering, derivation, documentation, feasibility,etc.</li> <li>User and Developer training.</li> </ul>
Monthly Trilinos leaders meetings: Trilinos leaders, including package development leaders, key managers, funding sources and other stakeholders participate in monthly phone meetings to discuss any timely issues related to the Trilinos Project.	<ul> <li>Developer Training.</li> <li>Design reviews.</li> <li>Policy decisions across all development phases.</li> </ul>
<b>Trilinos and package mail lists:</b> Trilinos lists for leaders, announcements, developers, users, checkins and similar lists at the package level support a variety of communication. All lists are archived, providing critical artifacts for assessments and audits.	<ul> <li>—Developer/user/client communication.</li> <li>—Requirements/design/testing artifacts.</li> <li>—Announcement/documenting of releases.</li> </ul>
<b>Trilinos and Trilinos3PL source repositories:</b> All source code, development and user documentation is retained and tracked. In addition, reference versions of all external software, including BLAS, LAPACK, Umfpack, etc. are retained in Trilinos3PL.	<ul><li>—Source management.</li><li>—Versioning.</li><li>—Third-party software management.</li></ul>
<b>Bugzilla Products:</b> Each package has its own Bugzilla Product with standard components.	—Requirements/faults capturing and tracking.
<b>Trilinos configure script and M4 macros:</b> The Trilinos configure script and related macros support portable installation of Trilinos and its packages	—Portability. —Software release.
<b>Trilinos test harness:</b> Trilinos provides a base testing plan and automated testing across multiple platforms, plus creation of testing artifacts. Test harness results are used to derive a variety of metrics for SQE.	<ul><li>—Pre-checkin and regression testing.</li><li>—Software metrics.</li></ul>

# **Software Lifecycles**



# (Typical) Project Lifecycle

Consider this lifecycle





# Scientific Research and Life Cycle Models

- Life Cycle Models are generally developed from the point of view of business software.
- Little consideration is given to algorithmic development.
- Traditional business execution environment is traditional mainframe or desktop, not parallel computers.
- Traditional development "techniques" are assumed.



# Research Software needs a different model

- Research should be "informal":
  - Allow external collaborators, students, post-docs, etc.
  - Allow changes of direction without seeking permission
  - Should use modern software development paradigms
    - i.e. Lean/Agile methods
  - Must be verified more than validated
- Production code must:
  - Have formality appropriate to risks,
  - Be Complete (documentation, testing, ...),
  - Be "user proofed",
  - Be platform independent (as necessary),
  - Be validated not just verified.



#### "Promotional" Model



- •Lower formality
- •Fewer Artifacts
- •Lean/Agile

- •Higher formality
- •Sufficient Artifacts
- •Bullet proof
- •Maintainable



# Trilinos Software Lifecycle Model

*The Trilinos Software Lifecycle Model*, James M. Willenbring and Michael A. Heroux and Robert T. Heaphy, *Proceeding of the 29th International Conference on Software Engineering*, May 2007



# Trilinos Lifecycle Phases

- Three phases:
  - Research.
  - Production Growth.
  - Production Maintenance.
- Each phase contains its own lifecycle model.
- Promotional events:
  - Required for transition from one phase to next.
  - Signify change in behaviors and attitude.
- Phase assigned individually to each package.



# Lifecycle Phase 1: Research

- Conducting research is the primary goal.
- Producing software is potentially incidental to research.
- Any software that is produced is typically a "proof of concept" or prototype.
- Software that is in this phase may only be released to selected internal customers to support their research or development and should not be treated as production quality code.



# Phase 1 Required Practices

- The research proposal is the project plan.
- Software is placed under configuration control as needed to prevent loss due to disaster.
- Peer reviewed published papers are primary verification and validation.
- The focus of testing is a proof of correctness, not software.
- Periodic status reports should be produced, presentation is sufficient.
- A lab notebook, project notebook, or equivalent is the primary artifact.



#### **Multicore Efforts**



### **Test Platform: Clovertown**

- Intel: Clovertown, Quad-core (actually two dual-cores)
- Performance results are based on 1.86 GHz version





# **LAMMPS Strong Scaling**





#### **HPC Conjugate Gradient**







- Trilinos/Epetra MPI Results
- Bandwidth Usage vs. Core Usage





- SpMV MPI+pthreads
- Theme: Programming model doesn't matter if algorithm is the same.





- Double-double dot product MPI+pthreads
- Same theme.





- Classical DFT code.
- Parts of code: Speedup is great.
- Parts: Speedup negligible.





- Closer look: 4-8 cores.
- 1 core: Solver is 12.7 of 289 sec (4.4%)
- 8 cores: Solver is 7.5 of 16.8 sec (44%).



# **Summary: Multicore**

- MPI-only is sometimes enough:
  - LAMMPS
  - Tramonto (at least parts), and threads might not help solvers.
- Introducing threads into MPI:
  - Not useful if using same algorithms.
  - Same conclusion as 12 years ago.
- Increase in bandwidth requirements:
  - Decreases effective core use.
  - Independent of programming model.
- Opportunities for effective use of threading:
  - Change of algorithm.
  - Better load balancing.



# **Solver Algorithms for Multicore**

- Block Krylov methods: Belos, Anasazi
- Block data structures: VbrMatrix
- Hybrid DMP/SMP preconditioners: Another talk.
- Tpetra focus:
  - Hybrid data strucures.
  - Hybrid parallel machine model.



# **To Come**

#### **Opportunities and Challenges**



# **Themes for FY08/09**

- Redefinition of Trilinos scope beyond solvers.
- Next steps in packaging and distribution.
- Continued outreach to other communities
- Rethinking source management.



# **Scope of Trilinos**

- Addition of Sacado, Zoltan, FEI, Intrepid, phdMesh: Not solvers.
- Framework support natural.
- Rephrasing of project goals, descriptions underway.
- Grouping of packages into meta-packages: At least conceptually.



# **Packaging and Distribution**

- Mac and Windows are ever more popular development environments.
- Goal: Provide click-install capabilities for Mac OS, MS Visual Studio, Linux COE.



# Outreach

- Trilinos packages part of SciDAC:
  - ITAPS, CSCAPES, TOPS-2.
  - Opportunity to serve broader DOE community.
- Trilinos popular in universities:
  - Single largest sector of users.
- Trilinos part of several industrial efforts.
  - Improves capabilities.
  - Amortizes costs over broader funding sources.
- Elevates certain activities:
  - Fortran accessibility.
  - Packaging & distribution.



# **Source Management**

- Think of repository as a database.
- Logical collections gathered dynamically.
- Consider use of multiple source management tools:
  - Local vs. global management.
  - Fully distributed.
- Certainly svn is option, but looking at all options.



# **Take Home Messages**

- Trilinos is both:
  - A development community
  - A collection of software
- OO techniques lead to:
  - Extensibility at many levels.
  - Scalable infrastructure.
  - Interoperability of independently developed capabilities.
  - Ability to adjust to architecture changes.
- Project is growing:
  - Including more of "vertical software stack".
  - Adapting to broader user base.
- We are seeking collaborations with broader DOE community.



# **Trilinos Availability/Information**

- Trilinos and related packages are available via LGPL.
- Current release (8.0) is "click release". Unlimited availability.
- More information:
  - http://trilinos.sandia.gov
  - http://software.sandia.gov
  - Additional documentation at my website: http://www.cs.sandia.gov/~mheroux.
- 5<sup>th</sup> Annual Trilinos User Group Meeting:

November 6-8, 2007 at Sandia National Laboratories, Albuquerque, NM, USA.

