

Weak decays, CP violation and CKM: Theoretical Status

João P. Silva

ISEL and CFIF - Lisbon

Apologies

- I have chosen only a few subjects
- I quote only a few references

(so many articles... so little time...)

- $(\alpha, \beta, \gamma) = (\varphi_2, \varphi_1, \varphi_3)$

Outline

1 – CKM, unitarity triangle and all that

2 – Provocations

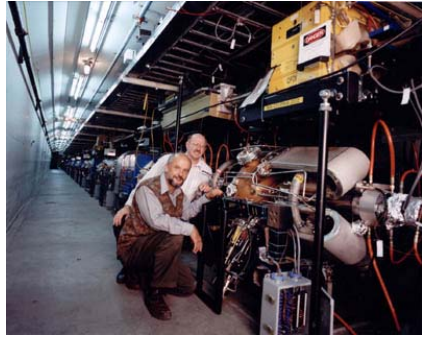
3 – Some current issues

4 – Conclusions

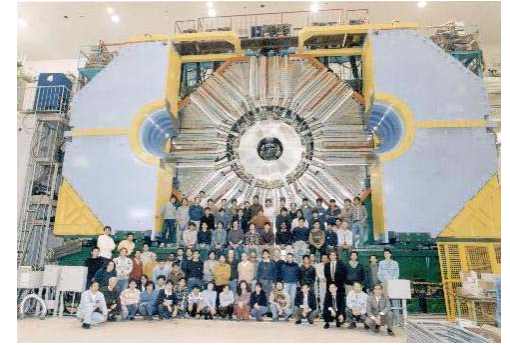
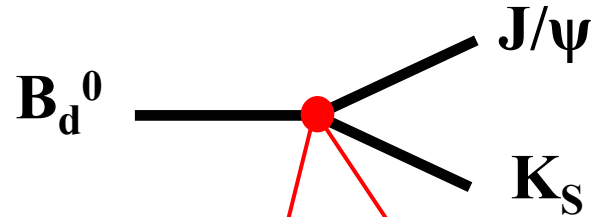
1 – CKM, Unitarity triangle and all that

- **Theory, Phenomenology and Experiment**
hadronic “messy” elements
- **The (ρ, η) plane**
the goal: detect or constrain New Physics
- **The unitary triangle**
gives only one of many tests

Generic analysis



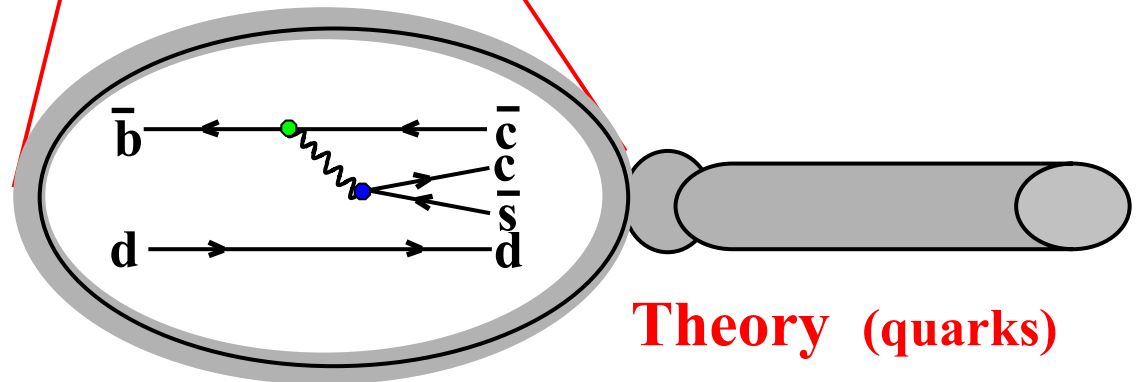
Phenomenology (hadrons)



Produce initial state

Detect final state

Experiment



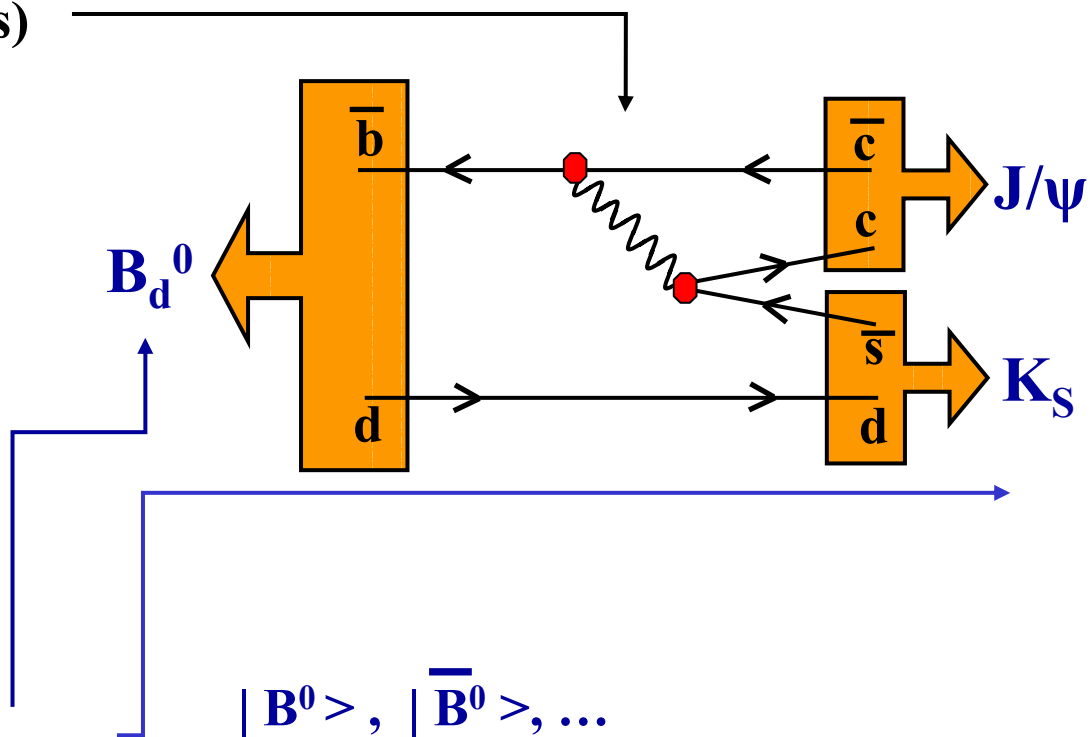
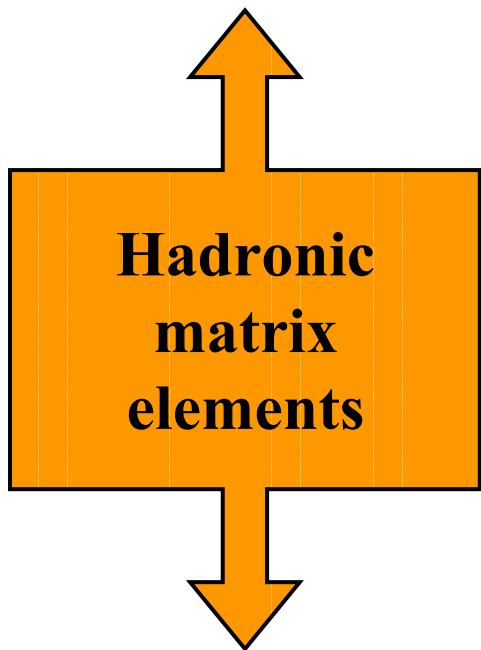
Theory (quarks)

The big problem: hadronic “messy” elements

u, d, s, c, b, t, ...

Operator rephasing: $\hat{\psi} \rightarrow e^{i\varphi_{quark}} \hat{\psi}$

Theory (quark operators)



$|B^0\rangle, |\bar{B}^0\rangle, \dots$

Phenomenology (hadron states)

State rephasing: $|B^0\rangle \rightarrow e^{i\alpha_{hadrons}} |B^0\rangle$

CPV observables: phenomenology

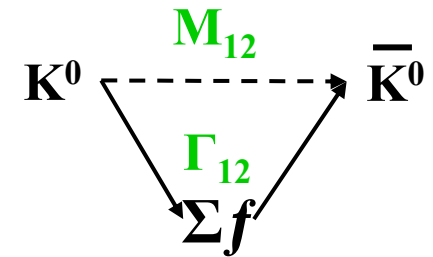
$|B^0\rangle \rightarrow e^{i\alpha} |B^0\rangle$ freedom

\implies CPV observables require clash of two phases

1. Clash mixing M_{12} with Γ_{12} : $|q/p|-1$

CPV in mixing

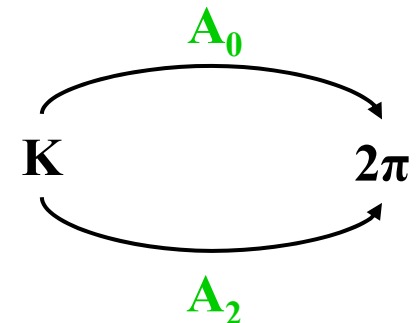
Measured in kaon system through ϵ_K



2. Clash two direct decay paths: $|\bar{A}/A|-1$

CPV in decay

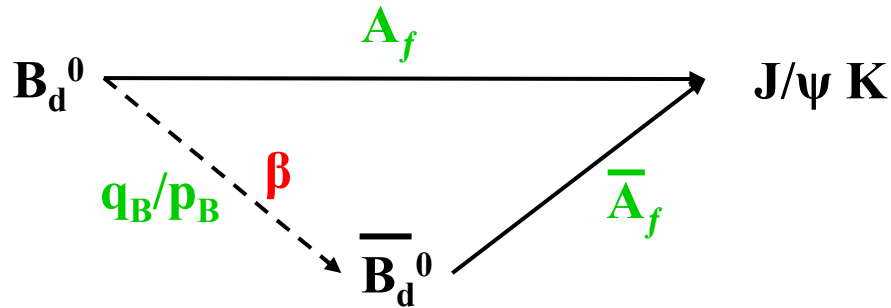
Measured in kaon system through ϵ'_K



3. Clash direct path with mixing path; first mix, then decay

$$\lambda_f = q_B/p_B \bar{A}_f/A_f$$

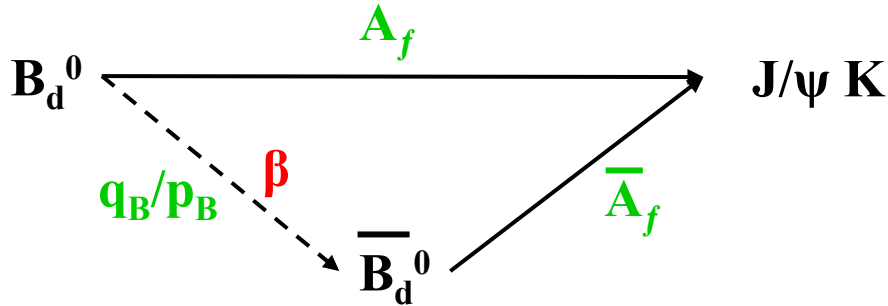
Measured in B_d system through $\sin 2\beta$



3. Clash direct path with mixing path; first mix, then decay

$$\lambda_f = q_B/p_B \bar{A}_f/A_f$$

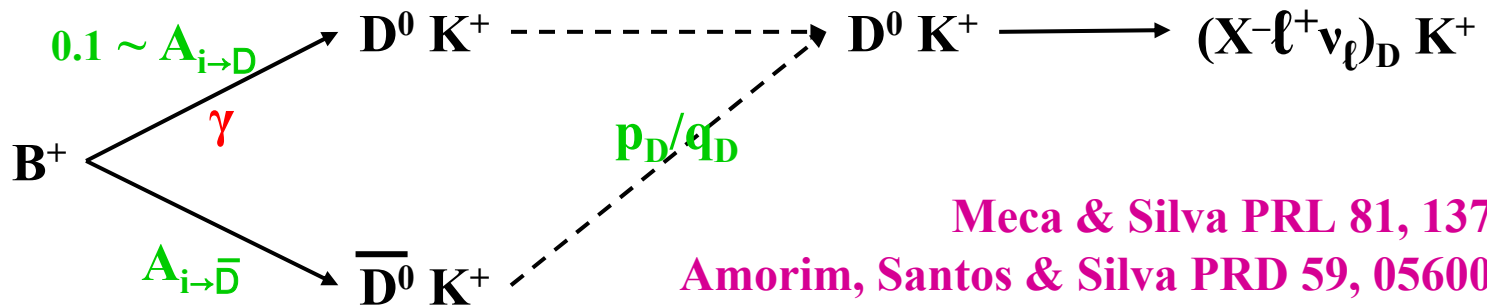
Measured in B_d system through $\sin 2\beta$



4. Clash direct path with mixing path; first decay, then mix

$$\xi_i = A_{i \rightarrow D}/A_{i \rightarrow \bar{D}} p_D/q_D$$

Never measured; but can affect measurements of γ in $B \rightarrow D$



Meca & Silva PRL 81, 1377 (1998)

Amorim, Santos & Silva PRD 59, 056001 (1999)

In the SM $|q/p|^2 - 1 \sim 10^{-3}$

The other CPV observables are measured in

$$\Gamma[B^0(t) \rightarrow f] \sim e^{-\Gamma t} [1 + C_f \cos(\Delta m t) - S_f \sin(\Delta m t)]$$

$$\Gamma[\bar{B}^0(t) \rightarrow f] \sim e^{-\Gamma t} [1 - C_f \cos(\Delta m t) + S_f \sin(\Delta m t)]$$

Direct CPV $C_f \equiv \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} \xrightarrow{\text{if } \lambda_f \approx e^{-2i\varphi}} 0$

Interference CPV $S_f \equiv \frac{2\text{Im}(\lambda_f)}{1 + |\lambda_f|^2} \xrightarrow{\text{if } \lambda_f \approx e^{-2i\varphi}} -\sin(2\varphi)$

CPV observables: theory

1. Phases can come from $\Delta B=2$ terms

phases in the mixing

2. Phases can come from $\Delta B=1$ terms

phases in the decay

In the SM all effects arise from a single CPV phase in the charged current interactions

Wolfenstein parametrization of the CKM matrix

$1 - \lambda^2/2$	λ	$A \lambda^3 (\rho - i\eta)$
$-\lambda$	$1 - \lambda^2/2$	$A \lambda^2$
$A \lambda^3 (1 - \rho - i\eta)$	$-A \lambda^2$	1

Wolfenstein PRL51, 1945 (1983)

$$\lambda = 0.2196 \pm 0.0026$$

from $s \rightarrow u$ transitions

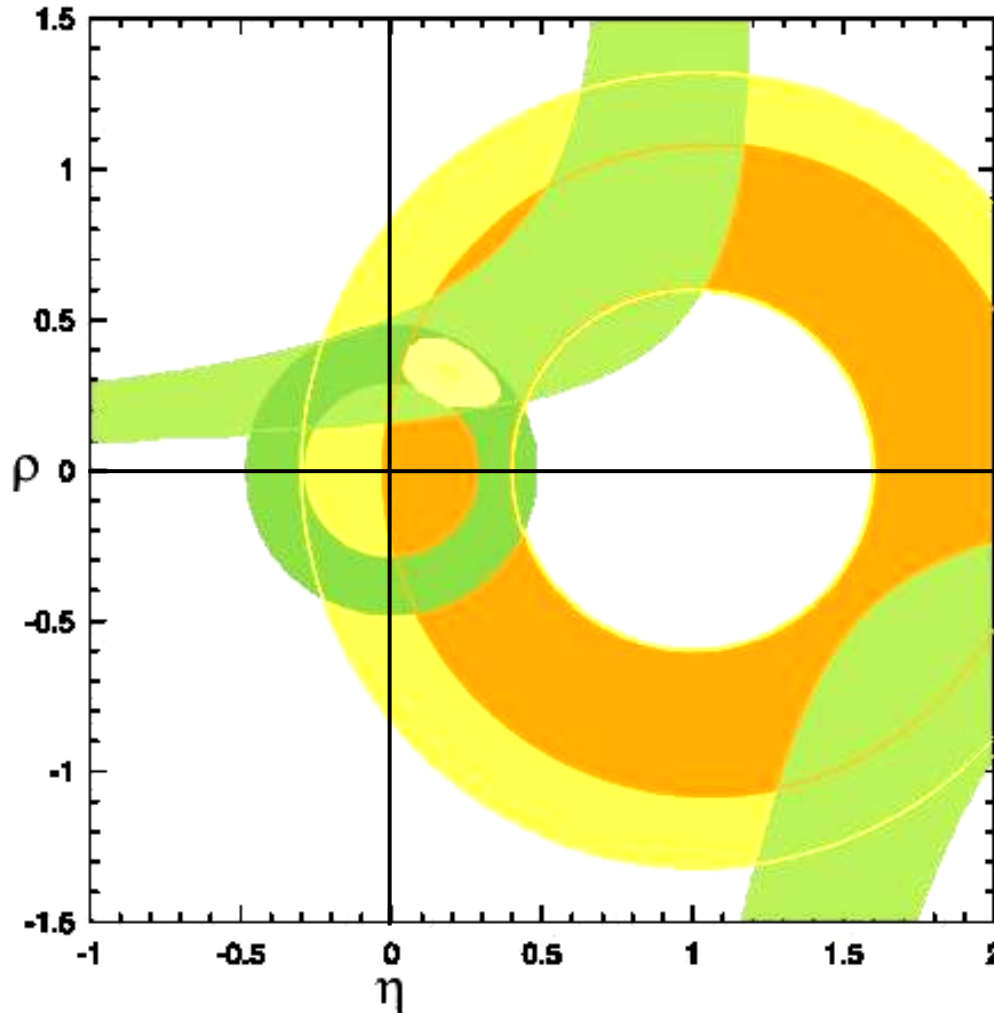
$$A = 0.85 \pm 0.06$$

from $b \rightarrow c$ transitions

“All” other experiments probe some combination of ρ and η

Our main goal is to detect new physics

Look for a lack of overlap among different constraints in



Thanks to Laplace

Redundant “parametrization” of the CKM matrix

1	$\lambda e^{i\chi'}$	$A R_b \lambda^3 e^{-i\gamma}$
$-\lambda$	1	$A \lambda^2$
$A R_t \lambda^3 e^{-i\beta}$	$-A \lambda^2 e^{i\chi}$	1

- In the SM**

$$R_t e^{-i\beta} \approx 1 - \rho - i \eta$$

$$R_b e^{-i\gamma} \approx \rho - i \eta$$

$$\chi \approx \lambda^2 \eta$$

$$\chi' \approx A^2 \lambda^4 \eta$$

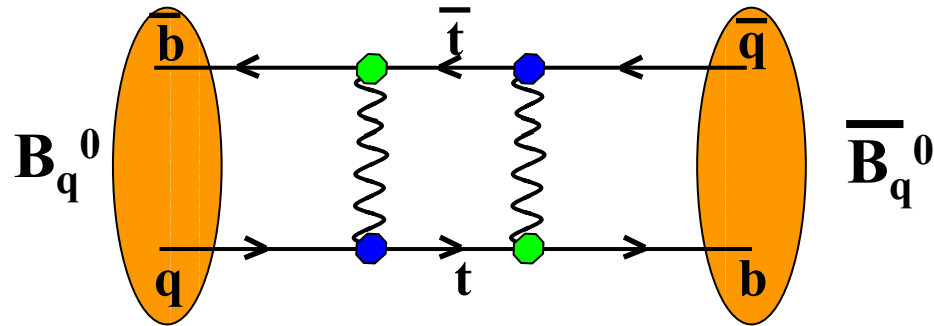
Aleksan, Kayser & London
PRL73, 18 (1994)

- Beyond the SM**

- there are nine independent magnitudes
- but there are only four independent phases: $\beta, \gamma, \chi, \chi'$

Branco, Lavoura & Silva
“CP violation”

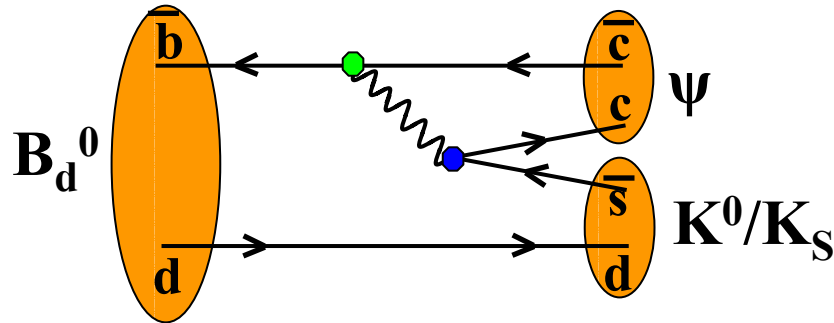
Mixing in the SM



$$\mathbf{B}_d^0 \implies (V_{tb}^* V_{td})^2 = \mathbf{1} (AR_t \lambda^3 e^{-i\beta})^2 \implies \mathbf{q/p} = e^{-2i\tilde{\beta}}$$

$$\mathbf{B}_s^0 \implies (V_{tb}^* V_{ts})^2 = \mathbf{1} (-A\lambda^2 e^{i\chi})^2 \implies \mathbf{q/p} = e^{2i\tilde{\chi}}$$

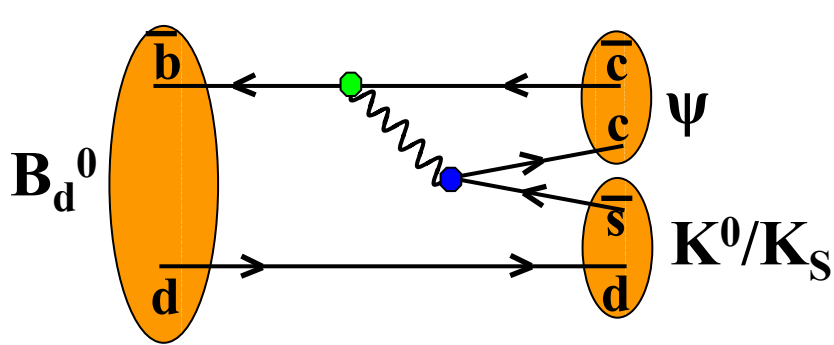
B → ψ K_S



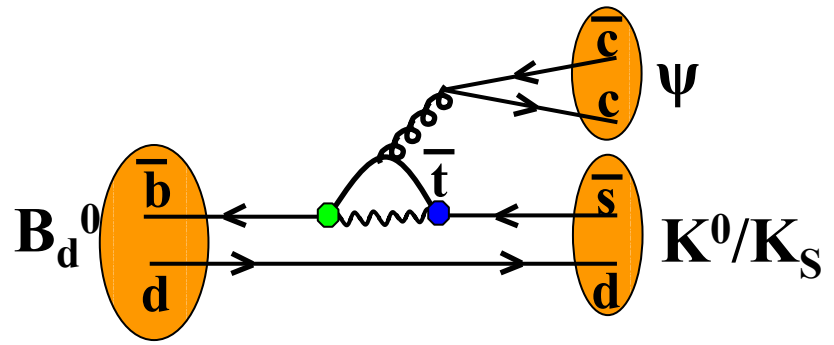
$$V_{cb}^* V_{cs} = A \lambda^2 \mathbf{1}$$

$$\lambda_{\psi K_S} = \frac{q}{p} \frac{A(\bar{B} \rightarrow \psi K_S)}{A(B \rightarrow \psi K_S)} = e^{-2i\beta} \frac{\cancel{\text{h.m.e.}}}{\cancel{\text{h.m.e.}}} = - e^{-2i\tilde{\beta}}$$

$B \rightarrow \psi K_S$



$$V_{cb}^* V_{cs} = A\lambda^2 \mathbf{1}$$



$$V_{tb}^* V_{ts} = \mathbf{1} (-A\lambda^2 e^{i\chi})$$

- $S_{\psi K_S} = \sin(2\beta)$ at LP'03:

- Belle 140 fb^{-1} $0.733 \pm 0.057 \pm 0.028$

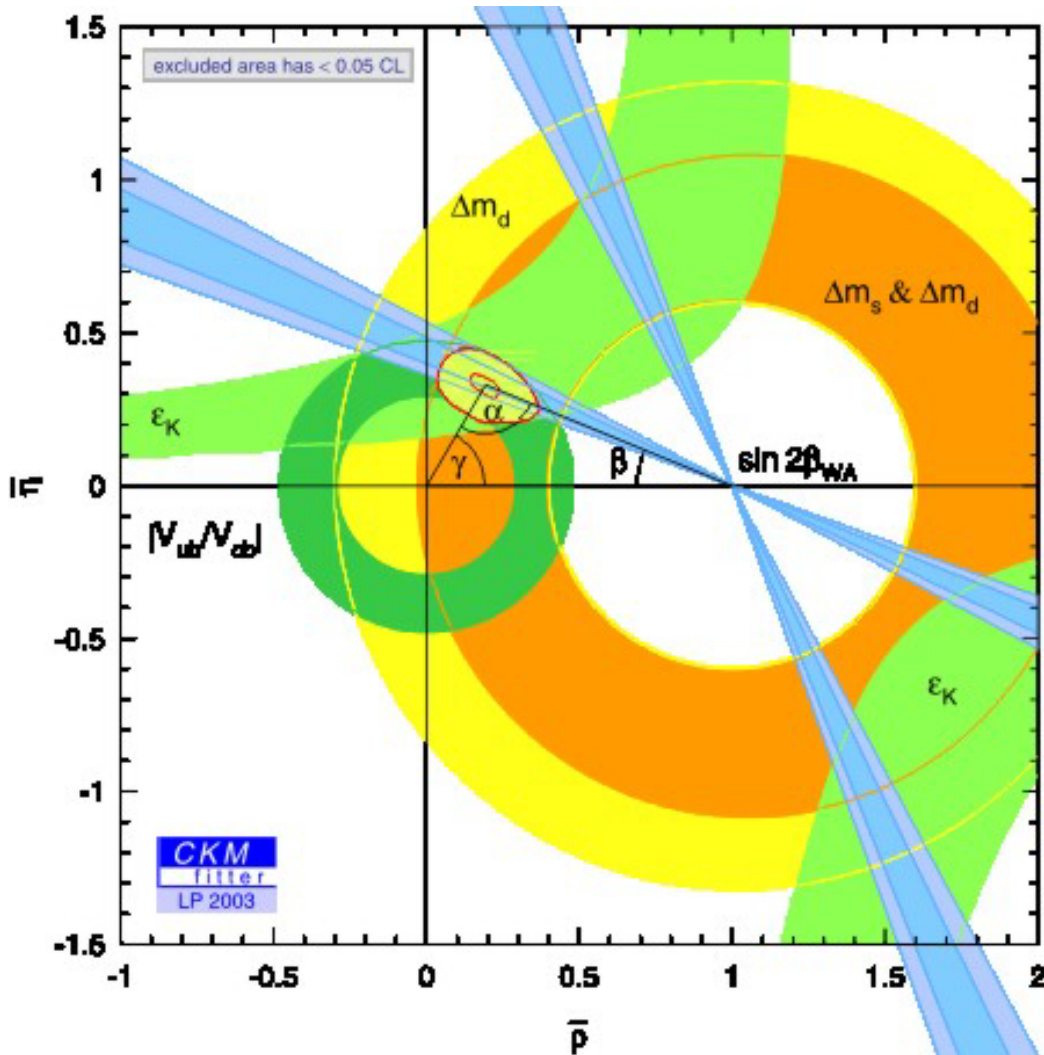
- BaBar 81 fb^{-1} $0.741 \pm 0.067 \pm 0.033$

- New World Average (**Browder** from **Höcker**):

$$\sin(2\beta) = 0.736 \pm 0.049$$

Precision Measurement

Constraints on the ρ - η plane



<http://ckmfitter.in2p3.fr>

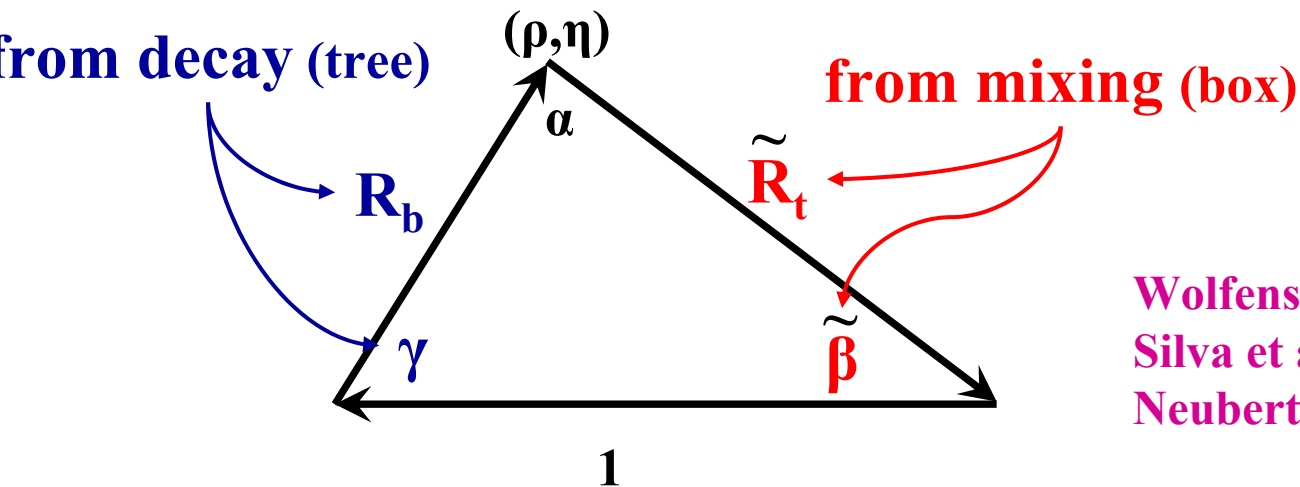
Höcker et al.

EPJ C21, 225 (2001)

Unitarity triangle

1	$\lambda e^{i\chi}$	$A R_b \lambda^3 e^{-i\gamma}$
$-\lambda$	1	$A \lambda^2$
$A R_t \lambda^3 e^{-i\beta}$	$-A \lambda^2 e^{i\chi}$	1

$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0 \quad \implies \quad R_b e^{+i\gamma} + R_t e^{-i\beta} = 1$$



Wolfenstein since 1964
 Silva et al. PRD67, 036004 (2003)
 Neubert ph/0308224

2 – Provocations

- goal is to **uncover NP**; not to test the SM
- **4th type** of CPV to be measured
- unitary triangle
 - compares **mixing versus decay**
 - is **only one** of many tests of the SM picture of CPV

- $\alpha + \beta + \gamma = \pi$ **by definition**
- **only two large phases in the CKM: β and γ**
- **testing this relation makes exactly the same sense as testing the relation $\beta = \beta$**

3 – Some current issues

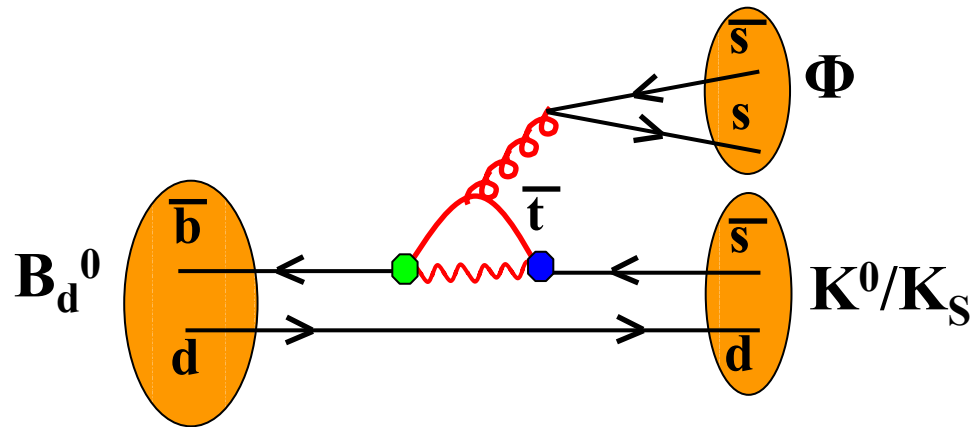
- Hints from $B \rightarrow \Phi K_S$
- $B \rightarrow \pi\pi$ and penguin pollution
- Usefulness of $B \rightarrow \pi^0\pi^0$
- Hints from $B \rightarrow K\pi$ decays

“Testing the relation $\beta=\beta$ ”

The angle β can be probed in a variety of channels:

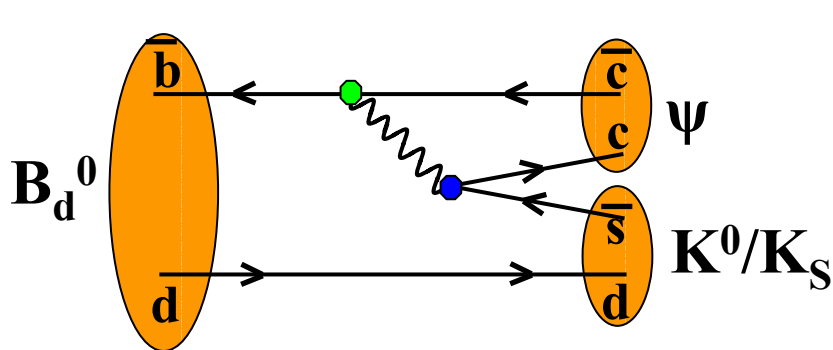
- $B_d \rightarrow \Phi K_S$, $B_d \rightarrow \eta' K_S$ and $(-) B_d \rightarrow K^+ K^- K_S$
should yield the same angle β found in $B_d \rightarrow \psi K_S$
- $b \rightarrow ccd$ decays, $B_d \rightarrow \psi \pi^0$ and $B_d \rightarrow D^{(*)+} D^{(*)-}$
 $(b \rightarrow ccd) \sim \lambda (b \rightarrow ccs)$ could be more sensitive to $b \rightarrow d$ penguins
than $(b \rightarrow ccs)$ is to $b \rightarrow s$ penguins
- $B_d \rightarrow A K_S$, with $A = \chi_1 \eta_c$
comparison with $B_d \rightarrow \psi K_S$ tests models which break P and CP
Atwood & Hiller ph/0307251
- $B_d \rightarrow J/\psi K_L$
comparison with $B_d \rightarrow J/\psi K_S$ tests CPT and exotic $B \rightarrow \bar{K}$ decays
Lavoura PRD62, 056002 (2000)
Grossman et al. PLB538, 327 (2002)

$B \rightarrow \Phi K_S$ is a penguin decay

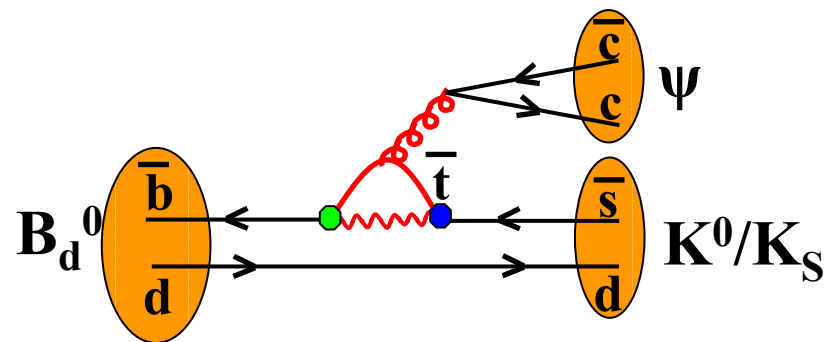


$$V_{tb}^* V_{ts} = 1 (-A\lambda^2 e^{i\alpha})$$

- Recall



$$V_{cb}^* V_{cs} = A\lambda^2 1$$



$$V_{tb}^* V_{ts} = 1 (-A\lambda^2 e^{i\alpha})$$

Simple predictions

- A “prediction” of the SM is
Phase β ($b \rightarrow s$ penguin) = Phase β ($b \rightarrow c\bar{c}s$)
- Since $B_d \rightarrow \Phi K_S$ and $B_d \rightarrow \eta' K_S$ are $b \rightarrow s$ penguin decays, they are more likely to be affected by NP
- Due to the different hadronic matrix elements, the impact may be different in the two decays

Measurements of $B \rightarrow \Phi K_S$

Obs.	Date	BaBar	Belle	Average
$S_{\Phi K_S}$	previous	$-0.18 \pm 0.51 \pm 0.07$	$-0.73 \pm 0.64 \pm 0.22$	-0.38 ± 0.41
	LP'03	$+0.45 \pm 0.43 \pm 0.07$	$-0.96 \pm 0.50 \pm 0.10$	-0.14 ± 0.33
$C_{\Phi K_S}$	previous	$-0.80 \pm 0.38 \pm 0.12$	$+0.56 \pm 0.41 \pm 0.16$	-0.19 ± 0.30
	LP'03	$-0.38 \pm 0.37 \pm 0.12$	$+0.15 \pm 0.29 \pm 0.08$	-0.04 ± 0.24

- Table from **LP'03** talks, specially **Browder**, and **HFAG**
- Compare with $\sin(2\beta) = 0.736 \pm 0.049$
- BaBar came closer to $S_{\psi K_S}$
- Belle's disagreement worsened
- Overall same 2.7σ with $S_{\psi K_S}$ remained

\implies Possibility of New Physics

What would be needed to explain

$$S_{\Phi K_s} = -0.14 ?$$

- **New Physics in $b \rightarrow s$ penguins**
- **with amplitude comparable to the SM**
- **and, with a large relative CP phase**

One possibility: Non-SM sZb couplings

$$L_Z^{\text{new}} = \frac{g^2}{4\pi} \frac{g}{2\cos\theta_W} \left[\mathbf{Z}_{sb} \bar{b}_L \gamma_\mu s_L + \mathbf{Z}'_{sb} \bar{b}_R \gamma_\mu s_R \right] Z^\mu + h.c.$$

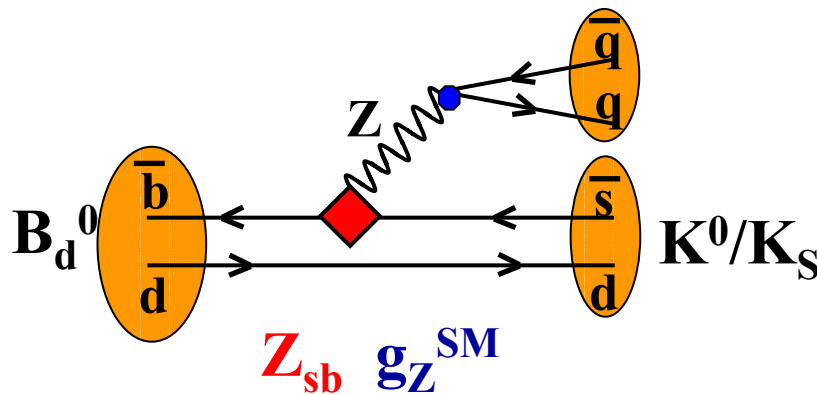
- **Experimental constraint from inclusive $B_d \rightarrow X_s e^+ e^-$ decays**

$$\sqrt{|\mathbf{Z}_{sb} + \mathbf{Z}_{sb}^{\text{SM}}|^2 + |\mathbf{Z}'_{sb}|^2} \leq 0.08 \quad \text{with} \quad \mathbf{Z}_{sb}^{\text{SM}} = -V_{tb}^* V_{ts} \sin^2 \theta_W C_{10}^* \approx -0.04$$

imply that new Z penguins are at most 2-3 larger than SM

- **These new vertices also affect BR and A_{FB} in $b \rightarrow s \ell^+ \ell^-$ (\sim SM), $B_s \rightarrow \mu^+ \mu^-$ (~ 10 SM), Δm_s (~ 0.5 SM), while $b \rightarrow s \gamma$ remains SM-like.**

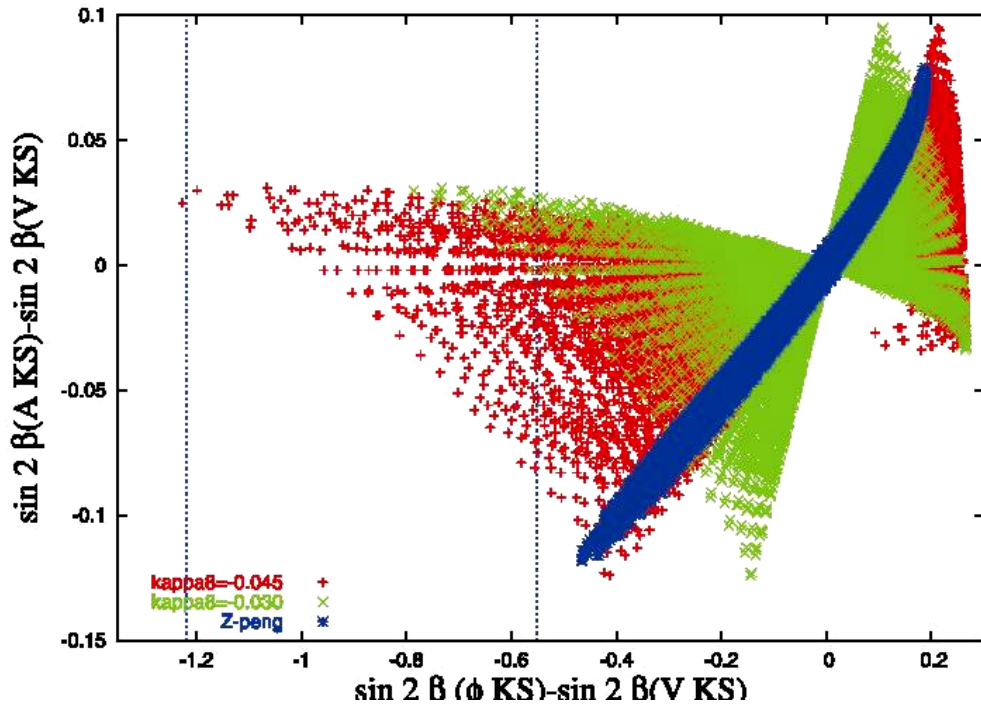
Non-SM sZb couplings



$$g_Z^{SM,V}(ss) = -0.35 \quad g_Z^{SM,A}(ss) = +0.5$$

$$g_Z^{SM,V}(\psi, \psi') = +0.19 \quad g_Z^{SM,A}(\eta_c, \chi_1) = -0.5$$

Atwood & Hiller ph/0307251



Experimentally

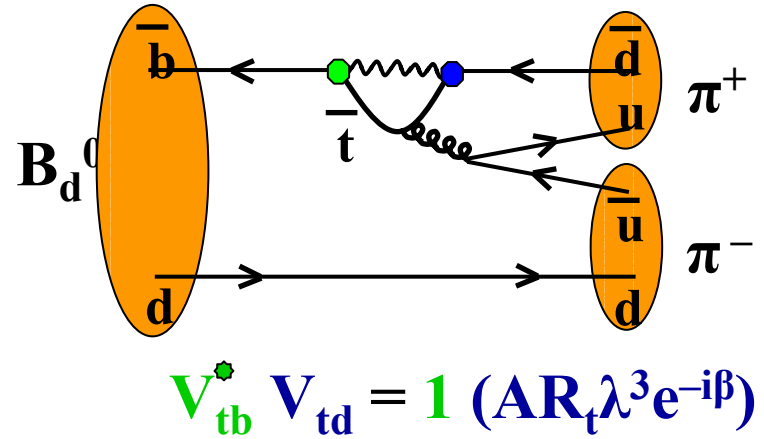
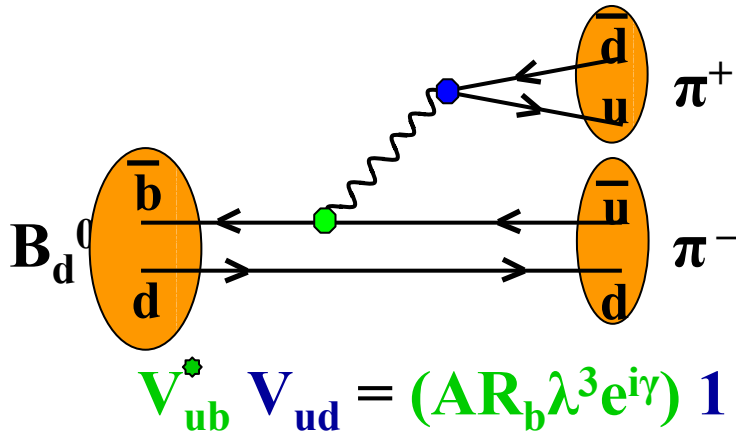
$$\sin 2\beta_{AKs} - \sin 2\beta_{VKs} = -0.05 \pm 0.26$$

Thanks to Hiller

Status of $B \rightarrow \Phi K_S$

- **Experimental central values are in a state of flux**
- **Current average for $\beta_{\Phi K_S}$ differs from $\beta_{\Psi K_S}$ by 2.7σ**
- **If the effect remains, comparison with other measurements of β could discriminate between different NP models**

$B \rightarrow \pi^+ \pi^-$ is affected by penguin pollution



$$\lambda_{\pi\pi} = \frac{q}{P} \frac{A(\bar{B} \rightarrow \pi^+ \pi^-)}{A(B \rightarrow \pi^+ \pi^-)} = e^{-2i\beta} \frac{e^{-i\gamma} \langle t \rangle + e^{+i\beta} \langle p \rangle}{e^{+i\gamma} \langle t \rangle + e^{-i\beta} \langle p \rangle}$$

$$= e^{-2i(\beta+\gamma)} \frac{1 + r e^{i\delta} e^{i(\beta+\gamma)}}{1 + r e^{i\delta} e^{-i(\beta+\gamma)}} \quad r e^{i\delta} = \frac{\langle p \rangle}{\langle t \rangle}$$

What can we learn from $B \rightarrow \pi^+ \pi^-$?

$$\lambda_{\pi\pi} = e^{-2i(\tilde{\beta}+\gamma)} \frac{1 + r e^{i\delta} e^{i(\beta+\gamma)}}{1 + r e^{i\delta} e^{-i(\beta+\gamma)}}$$

- **SM**

$\beta = \tilde{\beta}$ from ΨK_S ; δ γ r unknown

- **NP**

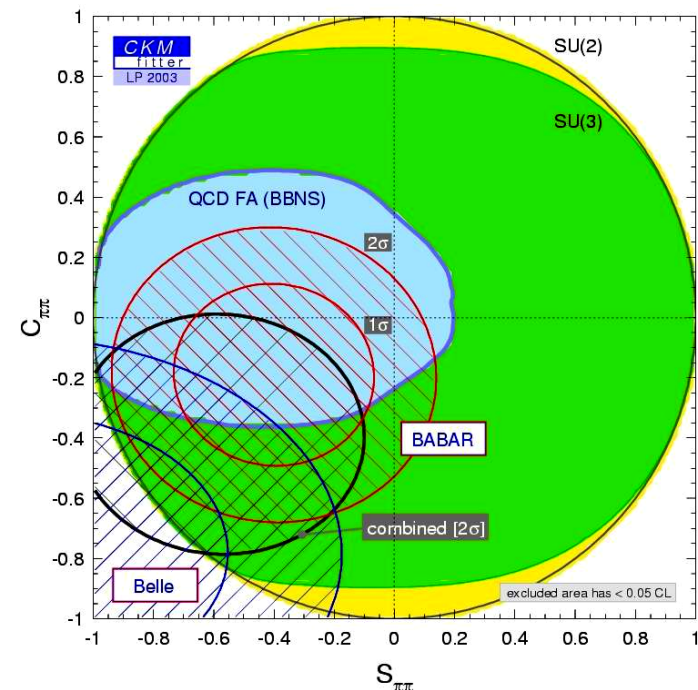
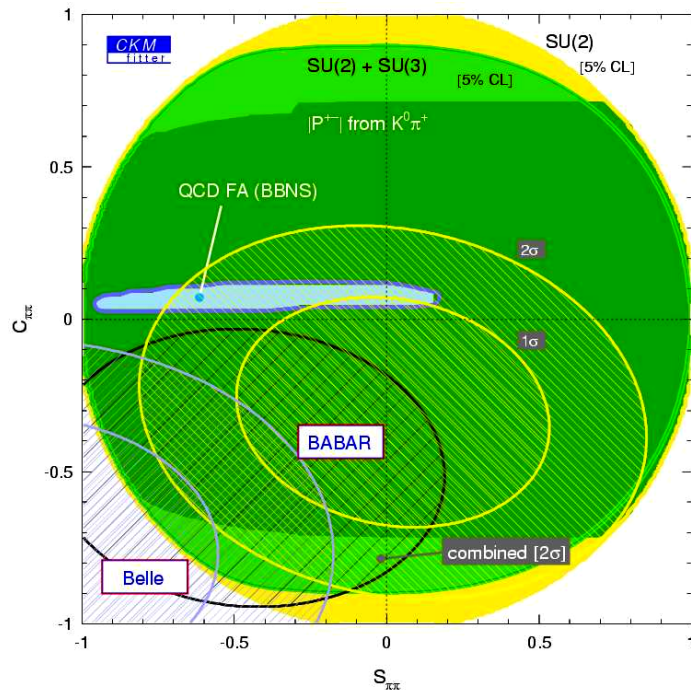
$\tilde{\beta}$ from ΨK_S ; δ γ r and β unknown

Note: $S_{\pi\pi} + [\sin(2\beta) = 0.736 \pm 0.049]$ also probes direct CPV

Measurements of $B \rightarrow \pi^+ \pi^-$

from HFAG

Obs.	Date	BaBar	Belle	Average
$S_{\pi\pi}$	previous	$-0.02 \pm 0.34 \pm 0.05$	$-1.23 \pm 0.41 \pm 0.08$	-0.47 ± 0.26
	2003	$-0.40 \pm 0.22 \pm 0.03$		-0.58 ± 0.20
$C_{\pi\pi}$	previous	$-0.30 \pm 0.25 \pm 0.04$	$-0.77 \pm 0.27 \pm 0.08$	-0.49 ± 0.19
	2003	$-0.19 \pm 0.19 \pm 0.05$		-0.38 ± 0.16



Trapping the penguin: r

- **Use isospin** Gronau & London PRL65, 3381 (1990)

measure $\text{BR}_{\text{av}}(\pi^+\pi^-)$, $C_{\pi^+\pi^-}$, $S_{\pi^+\pi^-}$, $\text{BR}_{\text{av}}(\pi^0\pi^0)$, $C_{\pi^0\pi^0}$, $\text{BR}_{\text{av}}(\pi^+\pi^0)$

\implies determine α with 16-fold ambiguity

(if one could) measure also $S_{\pi^0\pi^0}$

\implies determine α with usual 4-fold ambiguity

- **Use “partial isospin”** Grossman & Quinn PRD58, 017504 (1998)

measure $S_{\pi^+\pi^-}$, $C_{\pi^+\pi^-}$, $\text{BR}_{\text{av}}(\pi^0\pi^0)$, $\text{BR}_{\text{av}}(\pi^+\pi^0)$

$\implies \delta_\alpha \leq 48^\circ$ at 90% c.l. Jawahery LP03

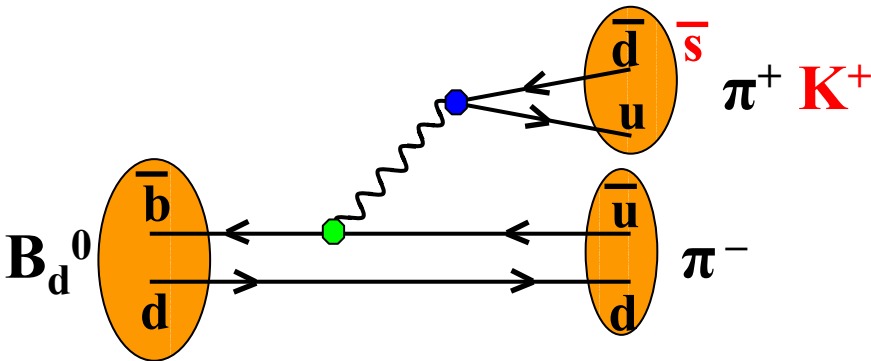
$$S_{\pi^+\pi^-} = \sqrt{1 - C_{\pi^+\pi^-}^2} \sin 2(\alpha + \delta_\alpha)$$

Trapping the penguin: r

- Use **SU(3)** [U-spin]

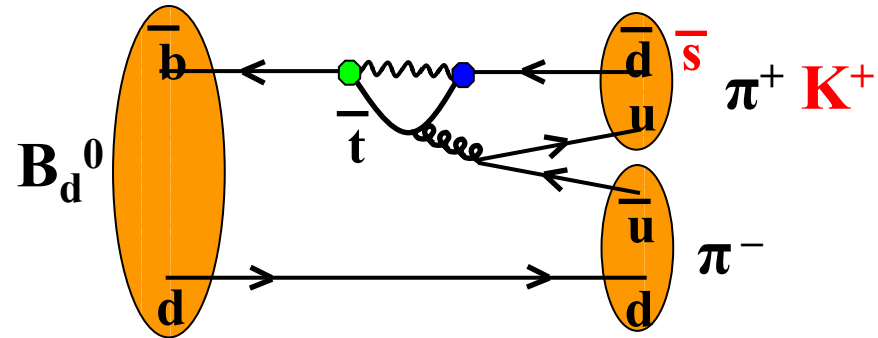
Silva & Wolfenstein PRD49, 1151 (1994)

measure $S_{\pi^+\pi^-}$, $BR_{av}(B \rightarrow K^+\pi^-)$



$$V_{ub}^* V_{ud} = (AR_b \lambda^3 e^{i\gamma}) 1$$

$$V_{ub}^* V_{us} = (AR_b \lambda^3 e^{i\gamma}) 1$$



$$V_{tb}^* V_{td} = 1 (AR_t \lambda^3 e^{-i\beta})$$

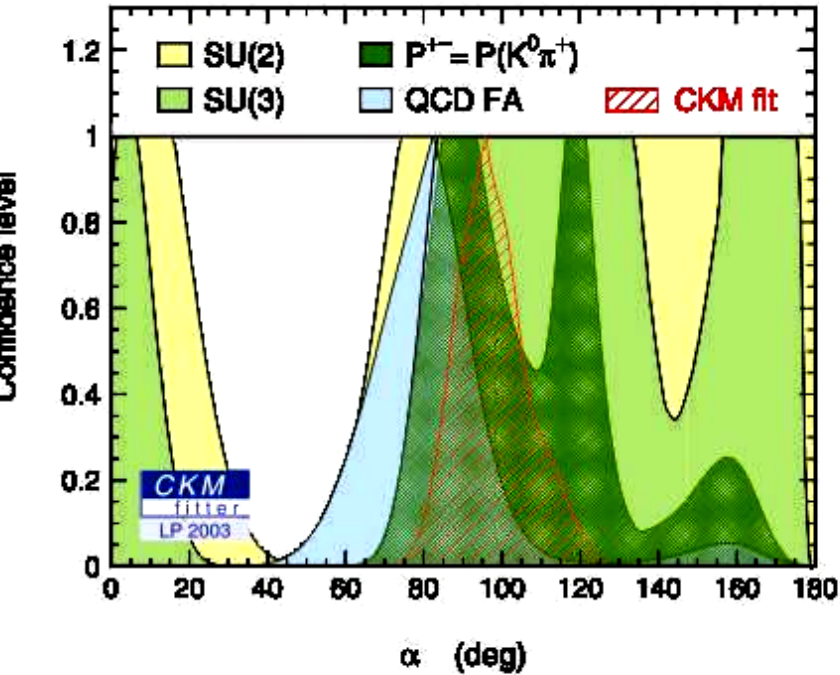
$$V_{tb}^* V_{ts} = 1 (-A\lambda^2 e^{i\chi})$$

Expect $B \rightarrow K\pi$ to be penguin dominated

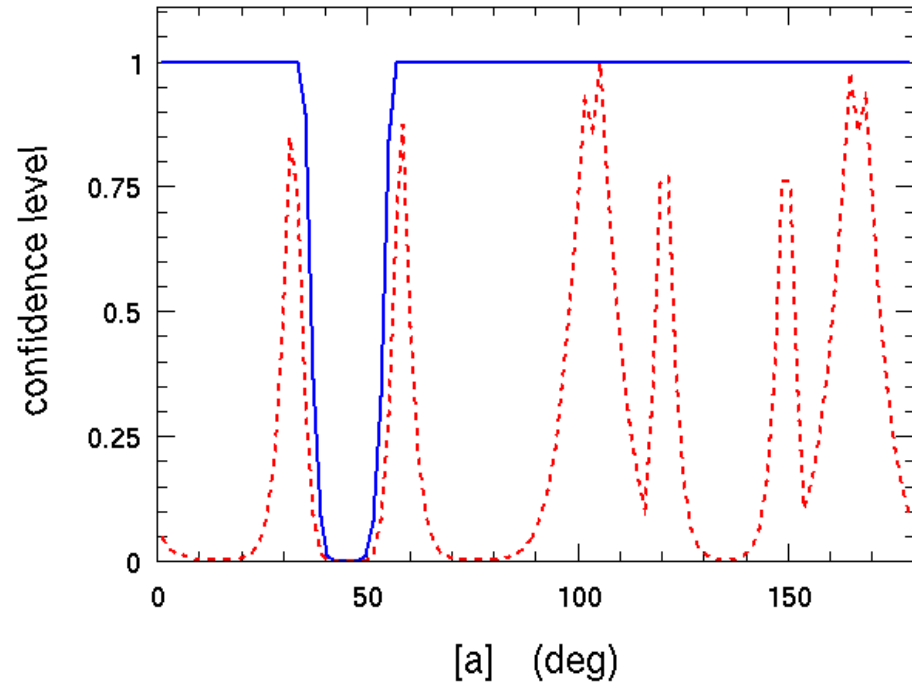
\implies good source of information on the penguin

- Trust calculations of hadronic matrix elements

Trapping the penguin: r



Current Situation



Futuristic

central: $BR_{av}(\pi^+\pi^0)$, $BR_{av}(\pi^+\pi^-)$, $BR_{av}(\pi^0\pi^0)$

central: $C_{\pi^+\pi^-}$, $S_{\pi^+\pi^-}$ from BaBar

errors: current/5

$$|\lambda_{\pi^0\pi^0}| = 1.00 \pm 0.08$$

Enormous courtesy of Höcker

The usefulness of $B \rightarrow \pi^0 \pi^0$

- Current measurement of $BR_{av}(\pi^0\pi^0)$ provides bound on α
- $C_{\pi^0\pi^0}$ is the next goal since it enables the isospin analysis
- Current measurement of $BR_{av}(\pi^0\pi^0)$ is at odds with QCD based calculations of the hadronic matrix elements

Some $B \rightarrow PP$ decays

The next table has been compiled from the following references:

- Fry LP'03
- Keum and Sanda [ph/0306004](#) pQCD
- Beneke & Neubert [ph/0308039](#) QCDF
- Chiang, Gronau & Rosner [ph/0306021](#) and
Gronau & Rosner [ph/0307095](#) SU(3)
- Fu, He & Hsiao [ph/0304242](#) U(3)

Mode	pQCD	QCDF	SU(3)	U(3)	BR _{exp}
$B^0 \rightarrow \pi^+ \pi^-$	6 – 11	8.9 +4.0 +3.6 +0.6 +1.2 -3.4 -3.0 -1.0 -0.8			
$B^0 \rightarrow \pi^0 \pi^0$	0.33 – 0.65	0.3 +0.2 +0.2 +0.3 +0.2 -0.2 -0.1 -0.1 -0.1	0.4 – 1.6	1.2 – 2.7	
$B^+ \rightarrow \pi^+ \pi^0$	2.7 – 4.8	6.0 +3.0 +2.1 +1.0 +0.4 -2.4 -1.8 -0.5 -0.4			
$B^0 \rightarrow K^+ \pi^-$	13 – 19	16.3 +2.6 +9.6 +1.4 +11.4 -2.3 -6.5 -1.4 -4.8			
$B^0 \rightarrow K^0 \pi^0$	8 – 14	7.0 +0.7 +4.7 +0.7 +5.4 -0.7 -3.2 -0.7 -2.3			
$B^+ \rightarrow K^0 \pi^+$	14 – 26	19.3 +1.9 +11.3 +1.9 +13.8 -1.9 -7.8 -2.1 -5.6			
$B^+ \rightarrow K^+ \pi^0$	8 – 14	11.1 +1.8 +5.8 +0.9 +6.9 -1.7 -4.0 -1.0 -3.0			
$B^0 \rightarrow K^0 \bar{K}^0$	1.4	1.35 +0.41 +0.71 +0.13 +1.09 -0.36 -0.48 -0.15 -0.45	0.6 – 0.8	0.5 – 1.1	
$B^+ \rightarrow K^+ \bar{K}^0$	1.4	1.36 +0.45 +0.72 +0.14 +0.91 -0.39 -0.49 -0.15 -0.40	0.6 – 0.9	0.6 – 1.2	

Note: $B^0 \rightarrow K^+ K^-$, not shown, is annihilation-dominated and expected to be $\sim 10^{-8}$

All BR x 10⁻⁶

Mode	pQCD	QCDF	SU(3)	U(3)	BR _{exp}
$B^0 \rightarrow \pi^+ \pi^-$	6 – 11	8.9 ^{+4.0 +3.6 +0.6 +1.2} _{-3.4 -3.0 -1.0 -0.8}			4.55±0.44
$B^0 \rightarrow \pi^0 \pi^0$	0.33 – 0.65	0.3 ^{+0.2 +0.2 +0.3 +0.2} _{-0.2 -0.1 -0.1 -0.1}	0.4 – 1.6	1.2 – 2.7	1.90±0.47
$B^+ \rightarrow \pi^+ \pi^0$	2.7 – 4.8	6.0 ^{+3.0 +2.1 +1.0 +0.4} _{-2.4 -1.8 -0.5 -0.4}			5.27±0.79
$B^0 \rightarrow K^+ \pi^-$	13 – 19	16.3 ^{+2.6 +9.6 +1.4 +11.4} _{-2.3 -6.5 -1.4 -4.8}			18.16 ± 0.79
$B^0 \rightarrow K^0 \pi^0$	8 – 14	7.0 ^{+0.7 +4.7 +0.7 +5.4} _{-0.7 -3.2 -0.7 -2.3}			11.21 ± 1.36
$B^+ \rightarrow K^0 \pi^+$	14 – 26	19.3 ^{+1.9 +11.3 +1.9 +13.8} _{-1.9 -7.8 -2.1 -5.6}			20.62 ± 1.35
$B^+ \rightarrow K^+ \pi^0$	8 – 14	11.1 ^{+1.8 +5.8 +0.9 +6.9} _{-1.7 -4.0 -1.0 -3.0}			12.82 ± 1.07
$B^0 \rightarrow K^0 \bar{K}^0$	1.4	1.35 ^{+0.41 +0.71 +0.13 +1.09} _{-0.36 -0.48 -0.15 -0.45}	0.6 – 0.8	0.5 – 1.1	<2.4
$B^+ \rightarrow K^+ \bar{K}^0$	1.4	1.36 ^{+0.45 +0.72 +0.14 +0.91} _{-0.39 -0.49 -0.15 -0.40}	0.6 – 0.9	0.6 – 1.2	<1.3

Note: $B^0 \rightarrow K^+ K^-$, not shown, is annihilation-dominated and expected to be $\sim 10^{-8}$

All BR x 10⁻⁶

B \rightarrow K π decays: diagrammatic decomposition

- Neglect annihilation and exchange diagrams
- Color-suppressed (tree and EW-penguin) are easily included: $C+P_{EW}$, $T+P_{EW}^c$, $P-1/3P_{EW}^c$

$$\begin{array}{ccc}
 A(B^0 \rightarrow K^+ \pi^-) = -(P + e^{i\gamma} T) & \xrightarrow{\mathbf{R} \text{ Fleischer-Mannel}} & A(B^+ \rightarrow K^0 \pi^+) = P \\
 \downarrow \mathbf{Buras-Fleischer R}_n & & \uparrow \mathbf{R}_c \text{ Neubert-Rosner} \\
 \sqrt{2} A(B^0 \rightarrow K^0 \pi^0) = P - P_{EW} & & \sqrt{2} A(B^+ \rightarrow K^+ \pi^0) = -(P + e^{i\gamma} T + P_{EW})
 \end{array}$$

Ratios of $B \rightarrow K \pi$ decays

- From Gronau & Rosner ph/0307095

Mode	Branching ratio _{av} (10^{-6})	Partial width _{av} (10^{-9}eV)	A_{CP}
$B^0 \rightarrow K^+ \pi^-$	18.16 ± 0.79	7.77 ± 0.35	-0.088 ± 0.040
$B^0 \rightarrow K^0 \pi^0$	11.21 ± 1.36	4.79 ± 0.58	
$B^+ \rightarrow K^0 \pi^+$	20.62 ± 1.35	8.19 ± 0.54	0.003 ± 0.059
$B^+ \rightarrow K^+ \pi^0$	12.82 ± 1.07	5.10 ± 0.43	0.035 ± 0.071

$$R = \frac{\Gamma(B^0 \rightarrow K^+ \pi^-)}{\Gamma(B^+ \rightarrow K^0 \pi^+)} = 0.948 \pm 0.074$$

$$R_c = \frac{2 \Gamma(B^+ \rightarrow K^+ \pi^0)}{\Gamma(B^+ \rightarrow K^0 \pi^+)} = 1.24 \pm 0.13$$

$$R_n = \frac{\Gamma(B^0 \rightarrow K^+ \pi^-)}{2 \Gamma(B^0 \rightarrow K^0 \pi^0)} = 0.81 \pm 0.10$$

- penguins have been measured and dominate the decays

- there are problems involving R_c and R_n

Fleischer-Mannels's insight

- $$R = \frac{\Gamma(B^0 \rightarrow K^+ \pi^-) + \Gamma(\bar{B}^0 \rightarrow K^- \pi^+)}{\Gamma(B^+ \rightarrow K^0 \pi^+) + \Gamma(B^- \rightarrow \bar{K}^0 \pi^-)} = 1 - 2 \frac{T}{P} \cos\gamma \cos\delta + \left(\frac{T}{P}\right)^2$$

- Imagine that $R < 1$; assume $\cos\delta > 0$

- $\implies \gamma$ cannot be $\pi/2$, regardless of the exact values of $\cos\delta > 0$ and T/P

- \implies can learn more about γ with knowledge of T/P and δ

Fleischer & Mannel PRD57, 2752 (1998)

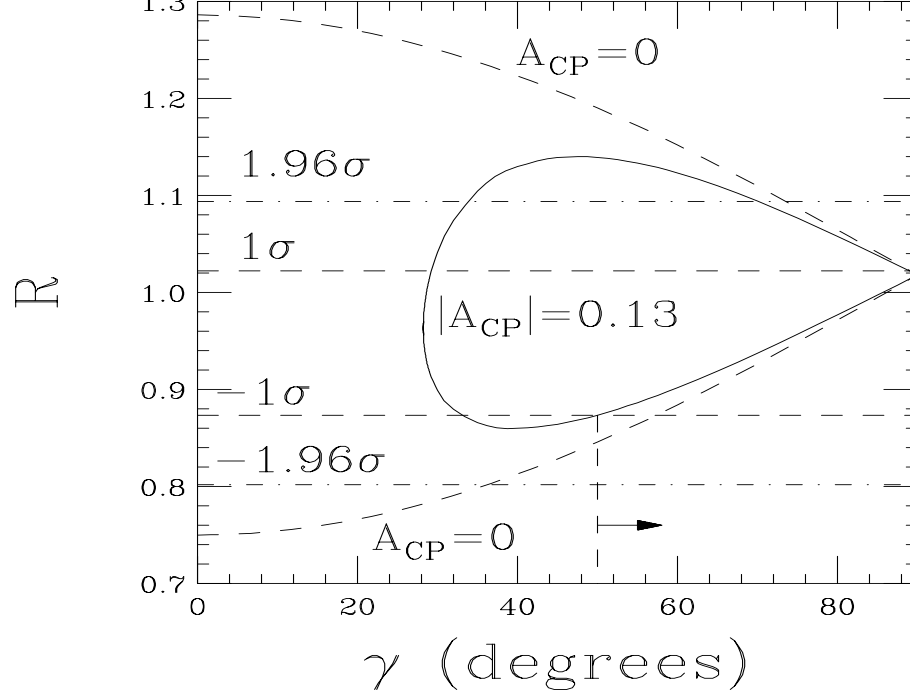
Gronau-Rosners's improvement

- Can cope with $R > 1$
- Eliminate δ using CP asymmetry

$$A_{CP} = \frac{\Gamma(\overline{B^0} \rightarrow K^- \pi^+) - \Gamma(B^0 \rightarrow K^+ \pi^-)}{\Gamma(\overline{B^0} \rightarrow K^- \pi^+) + \Gamma(B^0 \rightarrow K^+ \pi^-)} = -2 \frac{T}{P} \sin \gamma \sin \delta / R$$

==> Extract a value for γ , rather than a bound
(if you know T/P)

Gronau & Rosner PRD57, 6843 (1998)



Thanks to Gronau & Rosner

- Upper (lower) branch when $\cos\gamma \cos\delta < 0$ (> 0)
- Used $T/P_{\text{low}} = 0.17 - 0.04$ from $B^+ \rightarrow K^0 \pi^+$ and $B \rightarrow \pi \ell \nu$
- \implies Improvement on the **CP conserving R is much more important** for γ than the CP violating A_{CP} !!

Intriguing $B \rightarrow K\pi$ relation

So far:

- $R_{-1} = 0.052 \pm 0.074$ & asym \implies constraint on γ
- Can also use $R_c + R_n - 2 = 0.05 \pm 0.23$
- However, $R_c - R_n = 0.43 \pm 0.23$ is difficult to explain because

$$\Delta_{cn} \equiv R_c - R_n = \mathcal{O}\left(\frac{P_{EW}, T}{P}\right)^2 \rightarrow \text{In a } \Delta I=1 \text{ combination}$$

$\implies 2\sigma$ hints seen in $B \rightarrow K\pi$ decays

Look back at diagrammatic decomposition

$$A(B^0 \rightarrow K^+ \pi^-) = -(P + e^{i\gamma} T) \quad \text{R Fleischer-Mannel}$$

$$A(B^+ \rightarrow K^0 \pi^+) = P$$

Buras-Fleischer R_n

$$\sqrt{2} A(B^0 \rightarrow K^0 \pi^0) = P - P_{EW}$$

R_c Neubert-Rosner

$$\sqrt{2} A(B^+ \rightarrow K^+ \pi^0) = -(P + e^{i\gamma} T + P_{EW})$$

\implies Problems occur in the ratios involving P_{EW} and π^0

Possible explanations

- Possible problem with estimate of π^0 detection

Gronau & Rosner ph/0307095

- Study γ with $R_c R_n$ instead

- Enhanced $\Delta I=1$ pieces, electroweak penguins

Grossman, Neubert & Kagan JHEP9910, 029 (1999)

Yoshikawa ph/0306147, Gronau & Rosner ph/0307095, Buras et al. ph/0309012

- It is possible to fit simultaneously R_c and R_n with P_{EW}
- This requires $P_{EW} \approx i P/2$
- Such a large strong phase is at odds with QCD factoriz.

4 – Conclusions

- Progress in the field is finally dictated by experimentalists (Free at last! Free at last...)
- $\beta_{\Phi K_S}$ differs from $\beta_{\Psi K_S}$ by 2.7σ
- 2σ hint for isospin violating new physics seen in $B \rightarrow K\pi$ decays

4 – Conclusions

- $\text{BR}_{\text{av}}(\pi^0\pi^0)$ disagrees with QCD based calculations
- $C_{\pi^0\pi^0}$ is the next big thing
- Further information on γ will come from $\text{B} \rightarrow \text{D}$ decays
- B_s to get complete picture



Very Bright Future

**artist's
impression of
the very bright
future ahead of
us**