

# Overview on unpolarized and polarized baryon fragmentation functions

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# Outline

- Definitions of FF
- What is known about the polarized baryon FF?
- Earlier attempts to understand some  $\Lambda$ ,  $\bar{\Lambda}$  data
- Basic procedure to construct the statistical **unpolarized** octet baryon FF
- Conclusions

# Definitions of FF

$D_f^h(z, Q^2)$  is the probability to find, at scale  $Q$ , a hadron  $h$  with fraction  $z$  of the parton  $f$  momentum. Note that  $Q^2 > 0$  and FF is the counterpart of the PDF  $f_h(x, Q^2)$  defined for  $Q^2 < 0$ . QCD predicts their  $Q^2$  evolution and like the PDF, they should be **universal**, i.e. processes independent. If  $h$  has spin-1/2 can define similarly to  $\Delta f$  for PDF the polarized FF

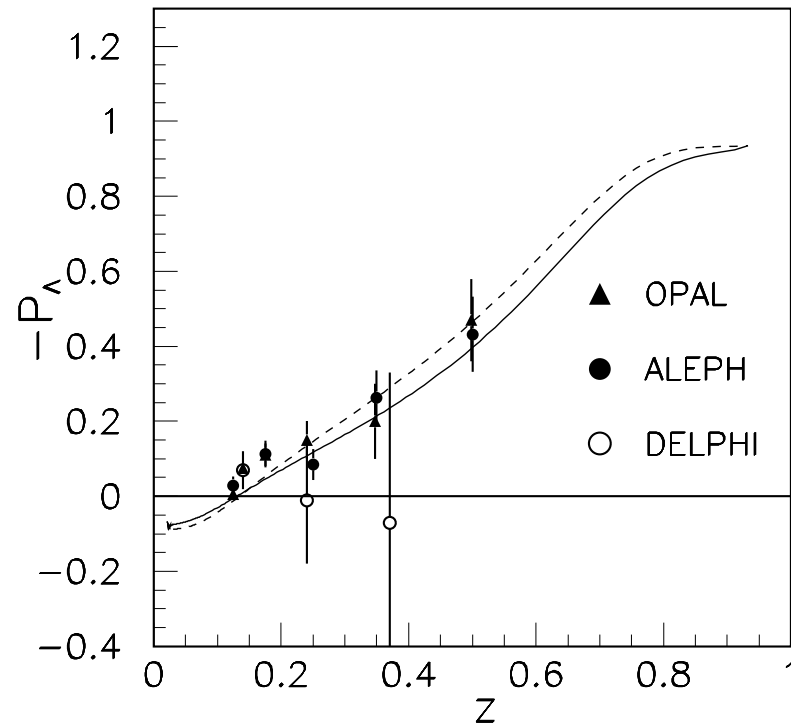
$$\Delta D_f^h = D_{f(+)}^{h(+)} - D_{f(+)}^{h(-)}$$

$D_f^h$  is the sum

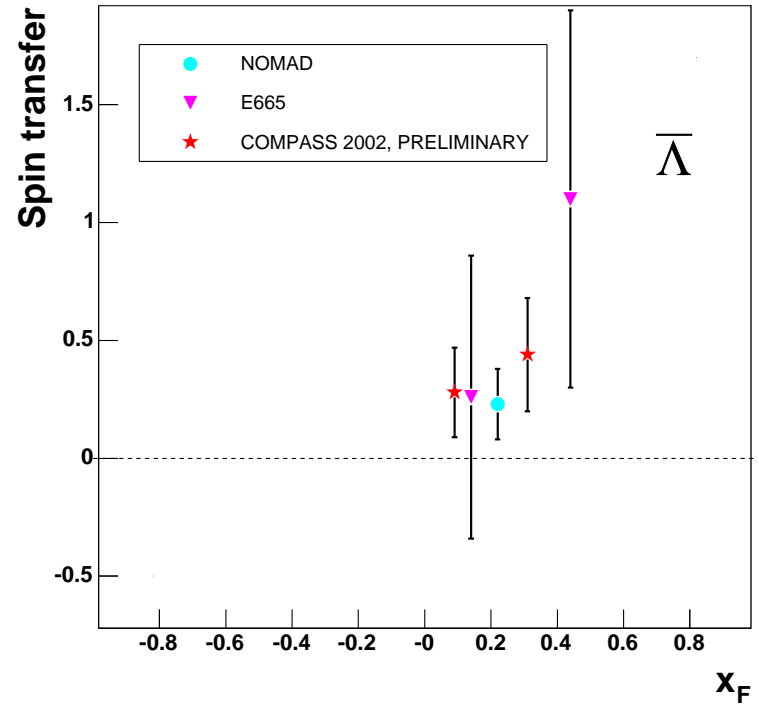
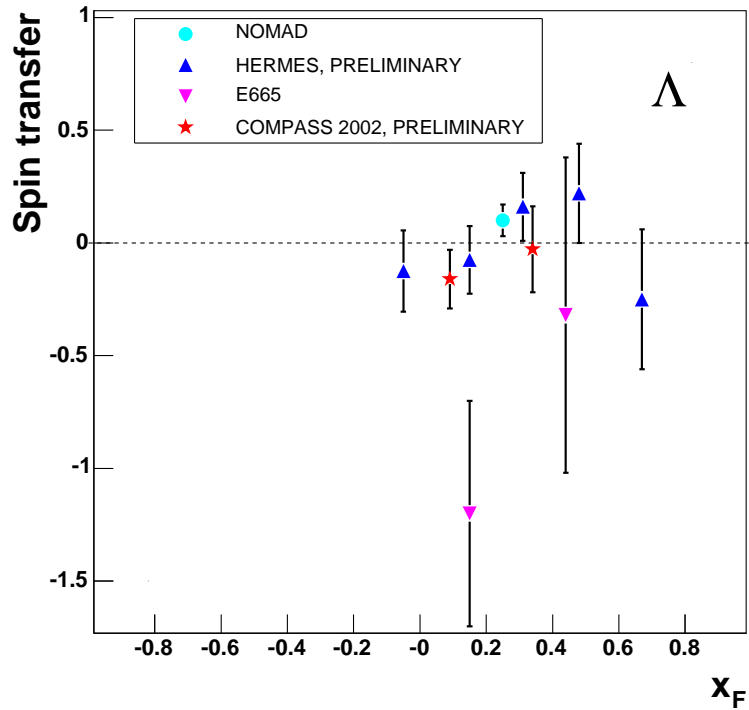
# What is known on the polarized baryon FF?

Very little and only for  $\Lambda$  and  $\bar{\Lambda}$

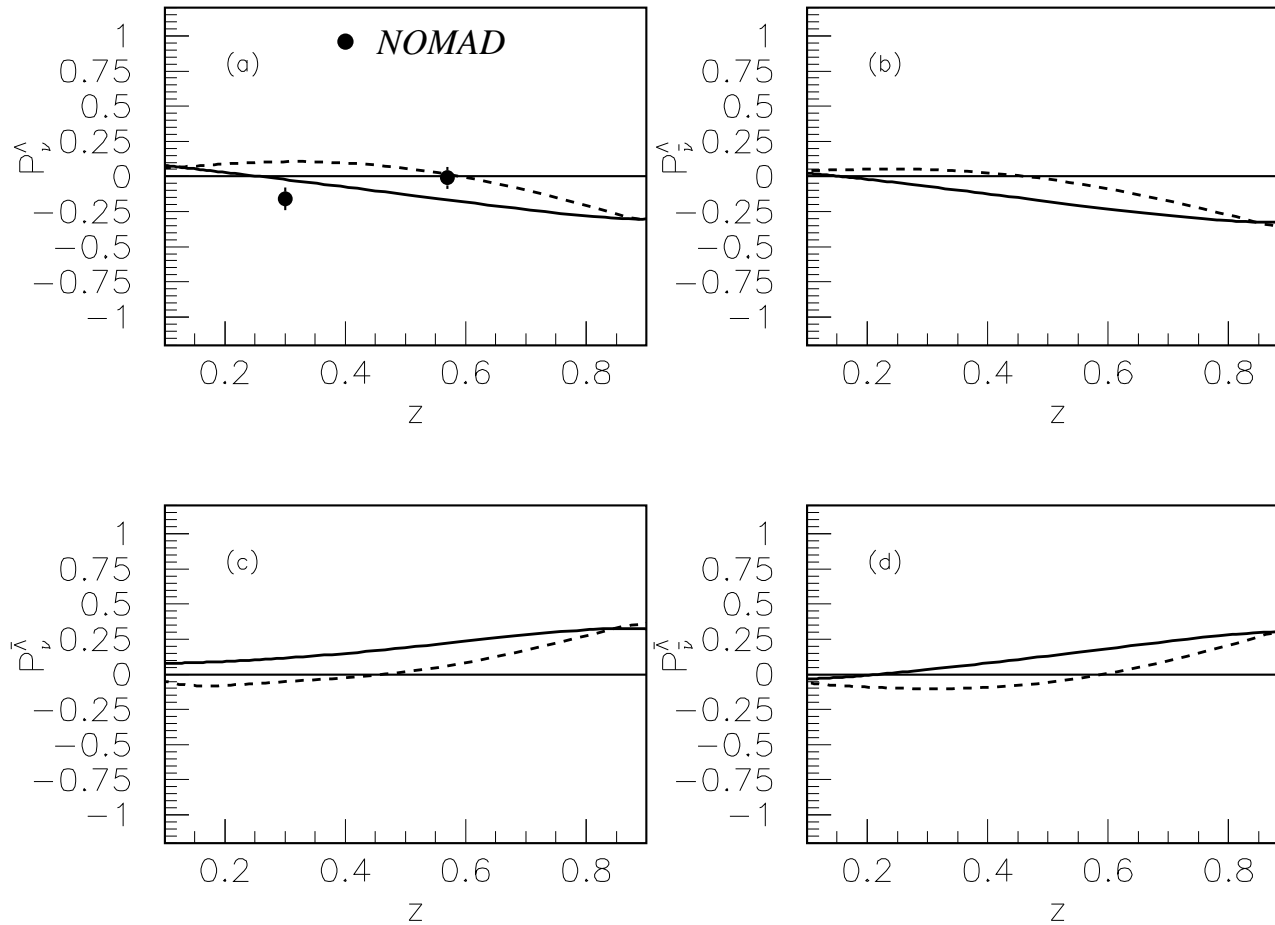
# $P_L(\Lambda + \bar{\Lambda})$ at the $Z$ pole in $e^+e^-$ collisions at LEP



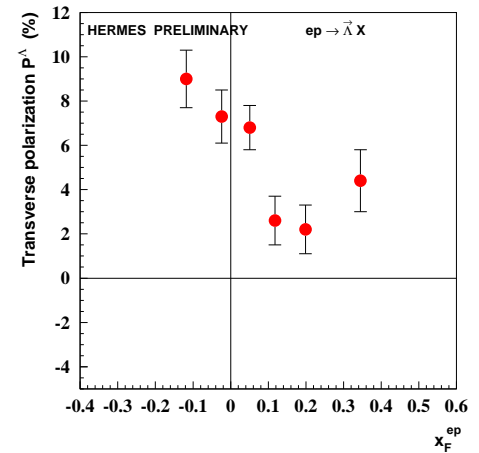
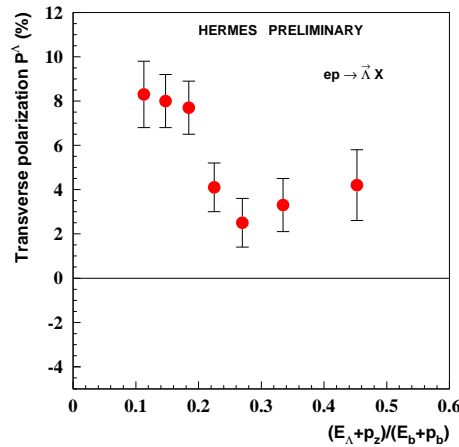
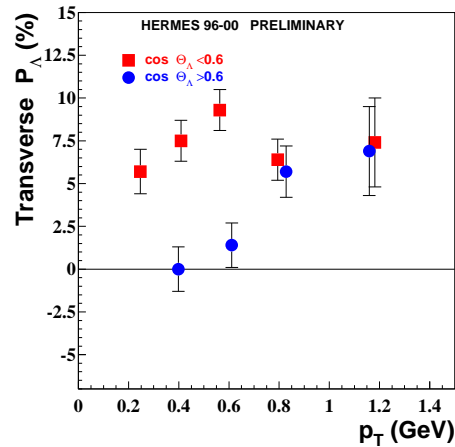
# Spin transfer for $\Lambda$ and $\bar{\Lambda}$



# Spin transfer for $\Lambda$ from NOMAD



# Transverse $\Lambda$ polarization from Hermes



(+ some NOMAD results large  $< 0$  for  $x_F < 0$ )  
 This is a transverse SSA hard to interpret



# Definitions

For a longitudinally polarized charged lepton beam and an unpolarized target, the  $\Lambda$  polarization along its own momentum axis is given in the quark parton model by

$$P_{\Lambda}(x, y, z) = P_B D(y) A^{\Lambda}(x, z) ,$$

where  $P_B$  is the polarization of the charged lepton beam, which is of the order of 0.7 or so.

$$\nu = E - E', \quad x = Q^2 / 2M\nu, \quad y = \nu / E, \quad z = E_{\Lambda} / \nu$$

$D(y)$ , whose explicit expression is

$$D(y) = \frac{1 - (1 - y)^2}{1 + (1 - y)^2},$$

is the longitudinal depolarization factor of the virtual photon with respect to the parent lepton, and

$$A^\Lambda(x, z) = \frac{\sum_q e_q^2 [q^N(x, Q^2) \Delta D_q^\Lambda(z, Q^2) + (q \rightarrow \bar{q})]}{\sum_q e_q^2 [q^N(x, Q^2) D_q^\Lambda(z, Q^2) + (q \rightarrow \bar{q})]},$$

is the longitudinal spin transfer to  $\Lambda$ .

# Earlier attempts to understand some $\Lambda$ , $\bar{\Lambda}$ data

D. De Florian et al., Phys. Rev. D57 (1998) 5811

C. Boros et al., Phys. Rev. D62 (2000) 014021

Use only data from  $e^+e^-$  collisions

$$D_q^{\Lambda+\bar{\Lambda}}(z) = N z^\alpha (1-z)^\beta$$

which implies no flavor separation and no  $q, \bar{q}$  separation. Use simple scenarios to construct

$$\Delta D_q(z) = N_q z^\delta D_q(z) \text{ with } N_s = 1 \text{ and } N_u = N_d = 1, -0.2, 0.$$

## Earlier attempts..(cont.)

Another approach based on the use of our knowledge of the PDF and the use of the reciprocity relation (Gribov-Lipatov)(see next slide).

B.-Q. Ma, I. Schmidt, J.S. and J.J. Yang, EPJ C16, 657 (2000)

B.-Q. Ma, I. Schmidt, J.S. and J.J. Yang, Phys. Rev. D62, 114009 (2000)

It works reasonably well but E665 remains puzzling. We generalize to all baryons with a SU(6) spectator quark-diquark model

**Gribov and Lipatov** have pointed out that the FF  $D_q^h(z)$ , for a quark  $q$  splitting into a hadron  $h$  with longitudinal momentum fraction  $z$ , can be related to the quark distribution  $q_h(x)$ , for finding the quark  $q$  inside the hadron  $h$  carrying a momentum fraction  $x$ , by the **reciprocity relation**

$$D_q^h(z) \sim q_h(x) .$$

This relation holds, in principle, in a certain  $Q^2$  range and in leading order approximation. It is only valid at  $x \rightarrow 1$  and  $z \rightarrow 1$ , but it provides a reasonable guidance for a phenomenological parametrization of the various FF.

For the  $\Lambda$ , we have explicit spin distributions for each valence quark,

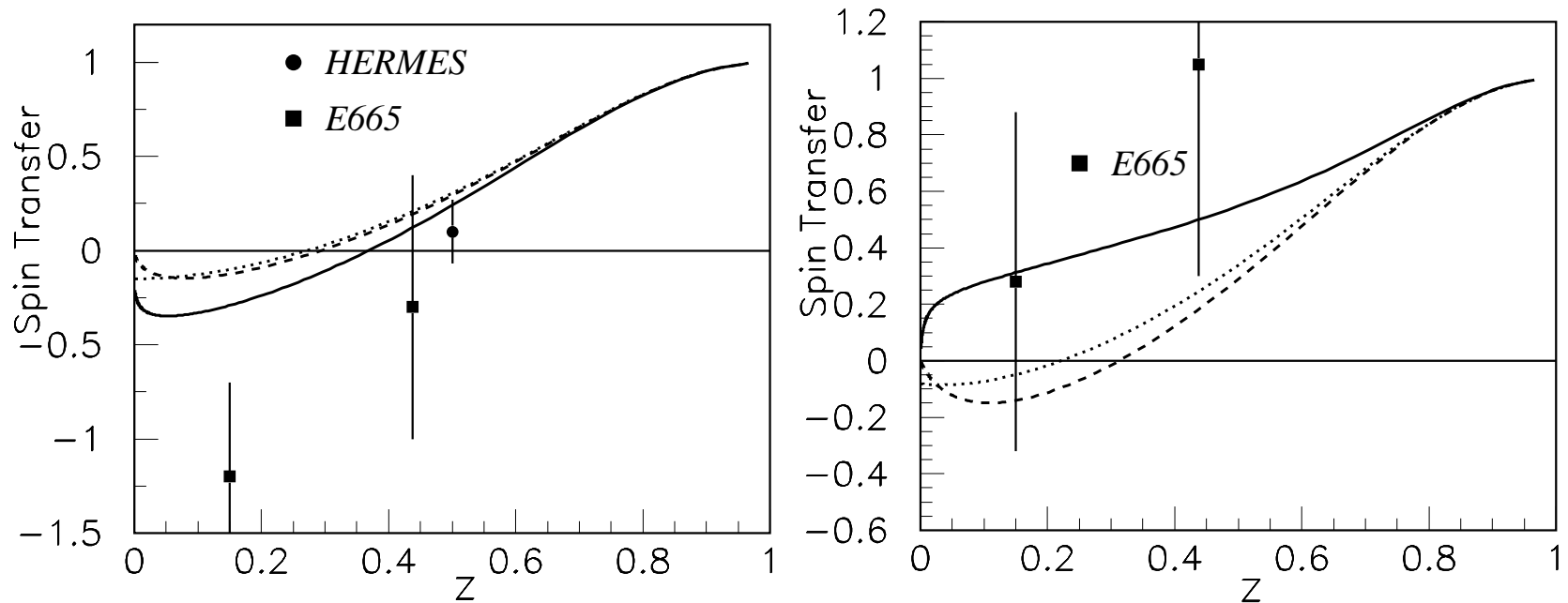
$$u_v^\uparrow(x) = d_v^\uparrow(x) = \frac{1}{x^{\alpha_v}} [A_{u_v} (1-x)^3 + B_{u_v} (1-x)^4],$$

$$u_v^\downarrow(x) = d_v^\downarrow(x) = \frac{1}{x^{\alpha_v}} [C_{u_v} (1-x)^5 + D_{u_v} (1-x)^6],$$

$$s_v^\uparrow(x) = \frac{1}{x^{\alpha_v}} [A_{s_v} (1-x)^3 + B_{s_v} (1-x)^4],$$

$$s_v^\downarrow(x) = \frac{1}{x^{\alpha_v}} [C_{s_v} (1-x)^5 + D_{s_v} (1-x)^6].$$

# Spin transfer for $\Lambda$ (right) and $\bar{\Lambda}$ (left)



dotted line (pure valence), solid line (asymmetric sea), dashed line (symmetric sea)

# Importance of neutrino DIS

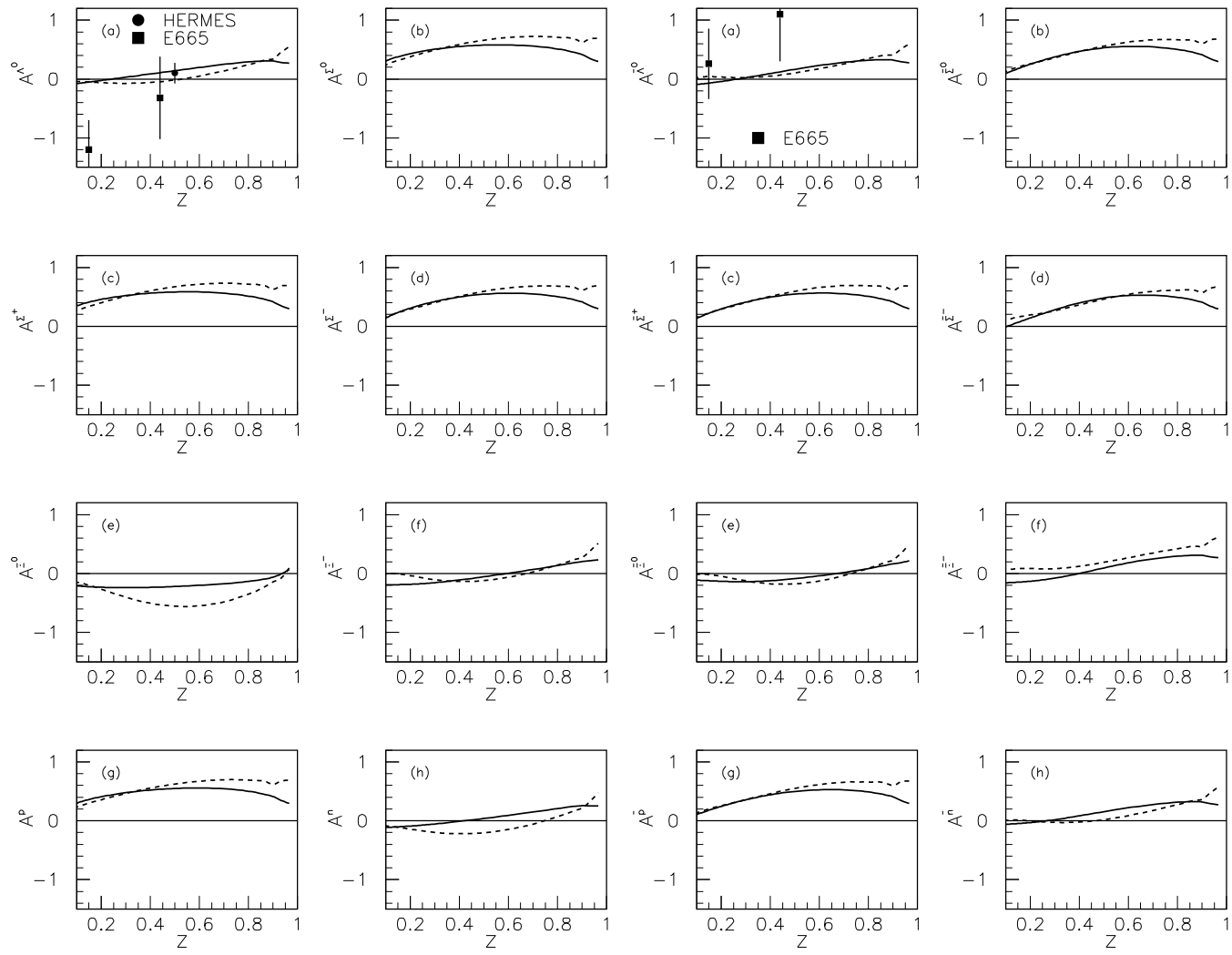
$\nu$  and  $\bar{\nu}$  DIS allow a quark flavor separation  
B.-Q. Ma and J.S., Phys. Rev. Lett. 82,2250  
(1999)

With four reactions  $\nu p \rightarrow \mu \Lambda X$ ,  $\bar{\nu} p \rightarrow \mu \Lambda X$ ,  
 $\nu p \rightarrow \mu \bar{\Lambda} X$  and  $\bar{\nu} p \rightarrow \mu \bar{\Lambda} X$  can extract four  
independent FF,  $D_u^\Lambda$ ,  $D_{\bar{u}}^\Lambda$ ,  $\Delta D_u^\Lambda$  and  $\Delta D_{\bar{u}}^\Lambda$ .

**A very powerful tool!**



# Spin transfer for $B(\text{right})$ and $\bar{B}(\text{left})$



# The PDF statistical model of C. Bourrely, F. Buccella and J.S.

- A Statistical Approach for Polarized Parton Distributions  
Euro. Phys. J. **C23**, 487 (2002)
- Recent Tests for the Statistical Parton Distributions  
Mod. Phys. Letters A **18**, 771 (2003)
- The Statistical Parton Distributions: status and prospects  
Euro. Phys. J. **C41**, 327, (2005)

# Basic procedure for the PDF

Use a simple description of the PDF, at input scale  $Q_0^2$ , proportional to  $[\exp[(x - X_{0p})/\bar{x}] \pm 1]^{-1}$ , *plus* sign for quarks and antiquarks, corresponds to a **Fermi-Dirac** distribution and *minus* sign for gluons, corresponds to a **Bose-Einstein** distribution.  $X_{0p}$  is a constant which plays the role of the *thermodynamical potential* of the parton  $p$  and  $\bar{x}$  is the *universal temperature*, which is the same for all partons.

# Explicit construction

(C.Bourely and J. S., Phys. Rev. D 68, 014003 (2003))

For the quarks  $q = u, s, d$  the FF  $D_q^B(x, Q_0^2)$  are expressed as

$$D_q^B(x, Q_0^2) = \frac{A_q^B X_q^B x^b}{\exp[(x - X_q^B)/\bar{x}] + 1},$$

where  $X_q^B$  is the potential corresponding to the fragmentation  $q \rightarrow B$  and  $Q_0^2$  is an initial scale.

The heavy quark FF  $D_Q^B(x, Q_0^2)$  for  $Q = c, b, t$ , which are expected to be large only in the small  $x$  region ( $x \leq 0.1$  or so), are parametrized by a **diffractive** term with a vanishing potential

$$D_Q^B(x, Q_0^2) = \frac{\tilde{A}_Q^B x^{\tilde{b}}}{\exp(x/\bar{x}) + 1}.$$

First we have the obvious constraints, namely,  
 $D_u^B = D_d^B$  for  $B = p, \Lambda$ . Moreover we assume that  
we need only **four** potentials, two for the proton  
 $X_u^p = X_d^p$  and  $X_s^p$  and two for the hyperons  
 $X_u^Y = X_d^Y$  and  $X_s^Y$  where  $Y = \Lambda, \Sigma^\pm, \Xi^-$ .

Finally for the gluon to baryon FF  $D_g^B(x, Q^2)$ , which is hard to determine precisely, we take a **Bose-Einstein** expression with a vanishing potential

$$D_g^B(x, Q_0^2) = \frac{A_g^B x^{\tilde{b}+1}}{\exp(x/\bar{x}) - 1}.$$

We assume it has the same small  $x$  behavior as the heavy quarks and it is the same for all baryons.

Table 1: Values of the normalization constants of the FF for the octet baryons

Baryon	$q_1$	$q_2$	$A_{q_1}^B$	$A_{q_2}^B$	$\tilde{A}_Q^B$
$p( uud )$	$u = d$	$s$	0.264	1.168	2.943
$\Lambda( uds )$	$u = d$	$s$	0.428	1.094	0.720
$\Sigma^+( uus )$	$u$	$s$	0.033	0.462	0.180
$\Sigma^-( dds )$	$d$	$s$	0.030	0.319	0.180
$\Xi^-( dss )$	$d$	$s$	0.023	0.082	0.072

We took  $\bar{x} = 0.099$  as determined earlier for the nucleon PDF

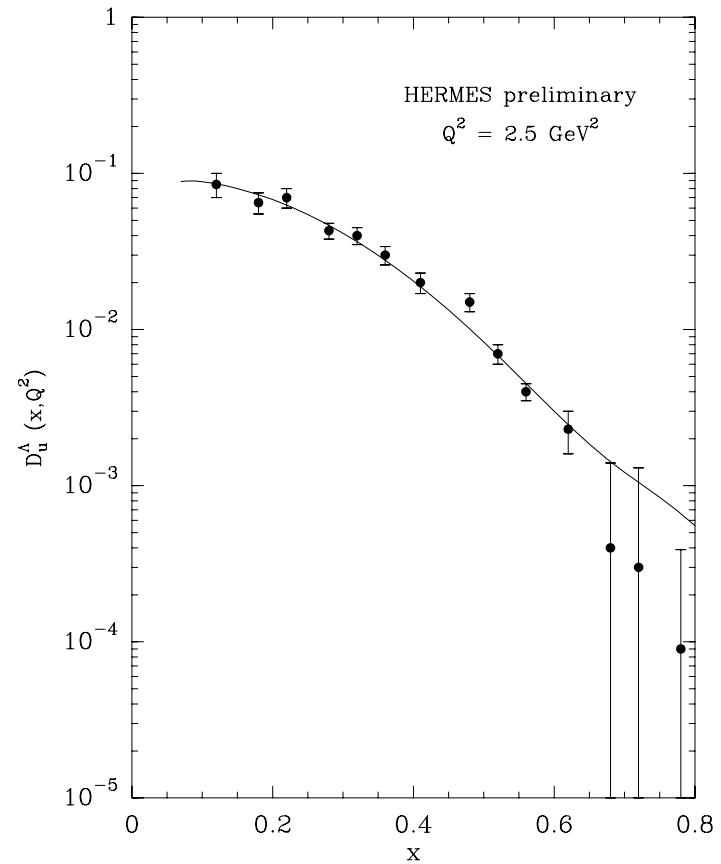
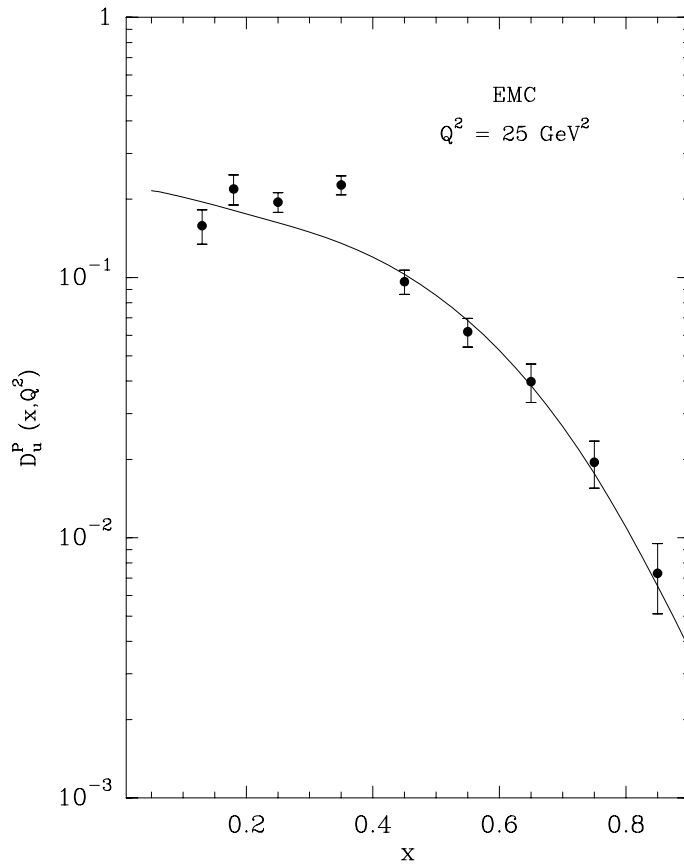


The values of the free parameters obtained from the NLO fit are

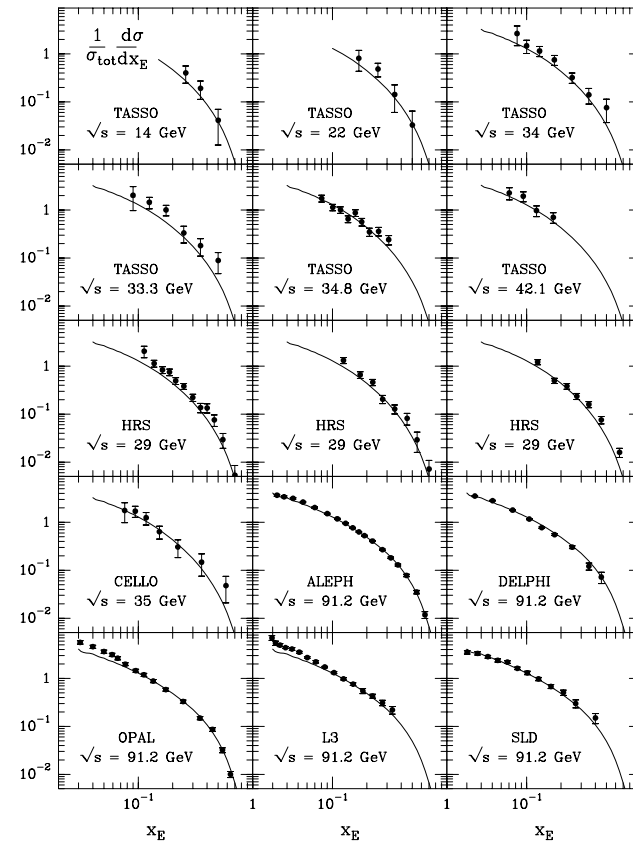
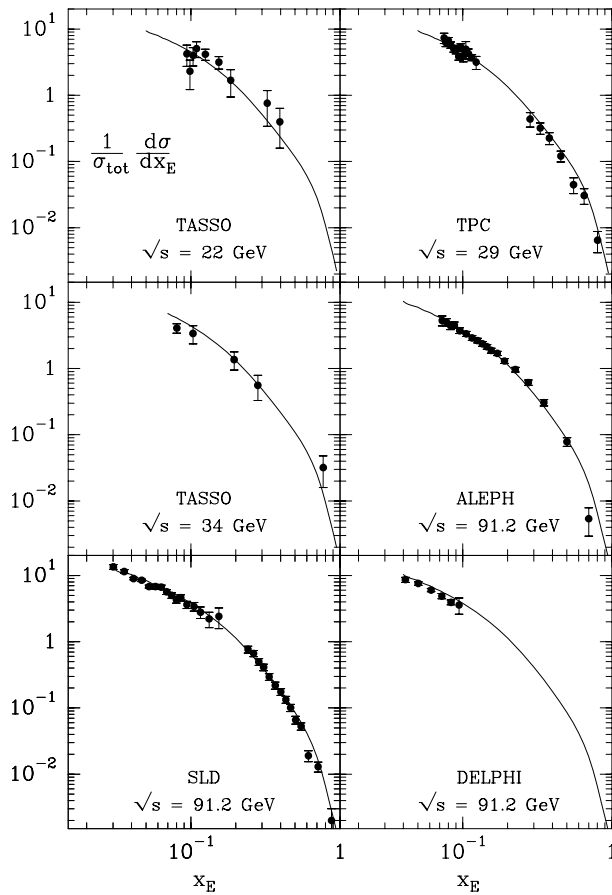
$$X_u^p = 0.648, \quad X_s^p = 0.247, \quad X_u^\Lambda = 0.296, \quad X_s^\Lambda = 0.476$$
$$b = 0.200, \quad \tilde{b} = -0.472, \quad A_g^B = 0.051.$$

Notice that in the nucleon PDF the  $u$  quark which is dominant has the larger potential and here we have analogously,  $X_u^p > X_s^p$  and  $X_s^\Lambda > X_u^\Lambda$ , a situation which is natural to expect. So the intrinsic properties of the quarks when observed in DIS or in fragmentation processes seem to be preserved.

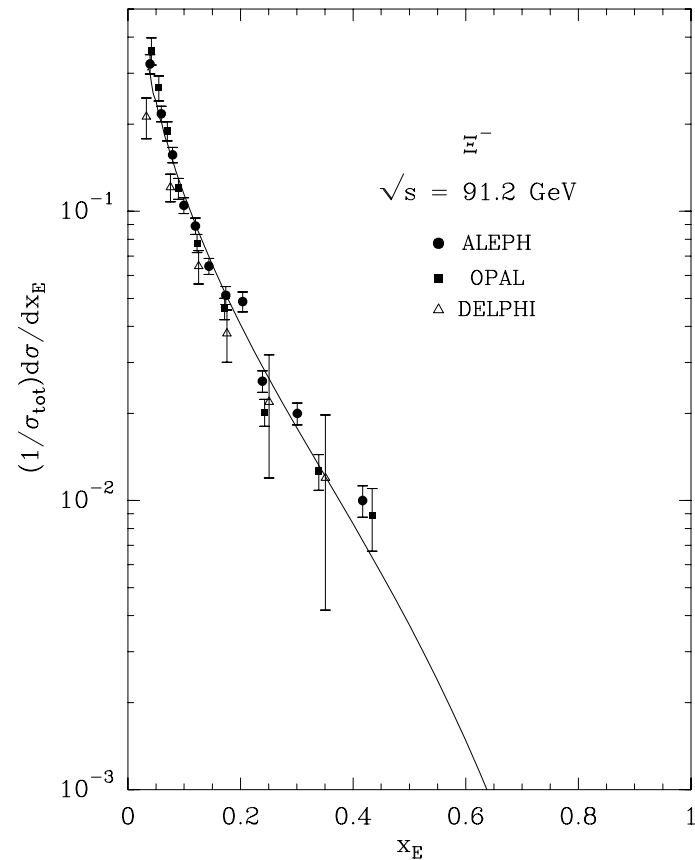
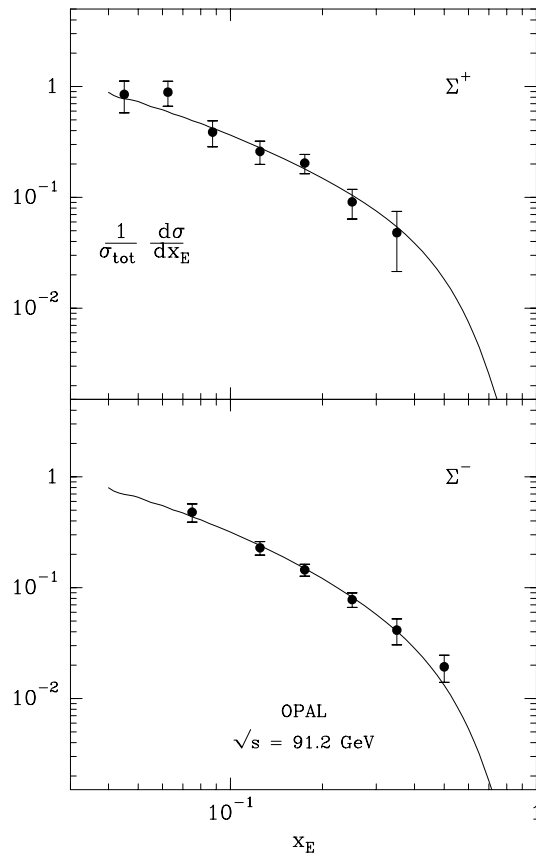
# The FF for $u \rightarrow p$ and for $u \rightarrow \Lambda$ (versus $x$ )



# Cross sections for $p$ and $\Lambda$ production in $e^+e^-$ annihilation

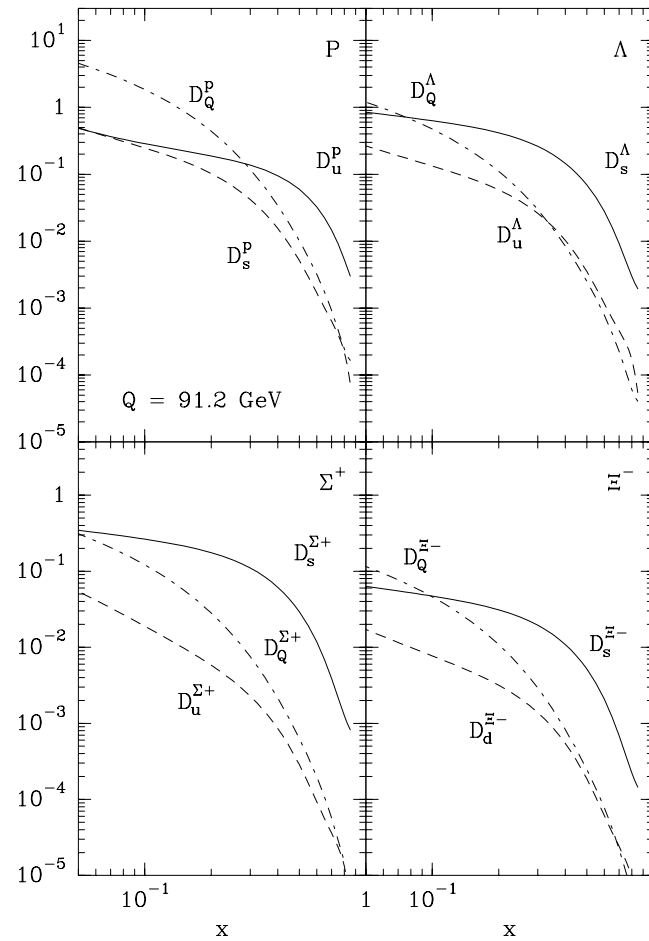


# Cross sections for $\Sigma^\pm$ and $\Xi^-$ production in $e^+e^-$ annihilation



# The quark to baryons FF

$D_q^B(x, Q^2)$  and  $D_Q^B(x, Q^2)$



# Some comments

For all hyperons the strange quark FF dominates over the  $u, d$  quarks. For  $\Lambda$ , we agree with a model for SU(3) symmetry breaking (Indumathi et al.) which gives  $D_u^\Lambda \sim 0.07 D_s^\Lambda$ . In Boros et al. one also finds  $D_u^\Lambda \ll D_s^\Lambda$  and  $D_{\bar{q}}^\Lambda$  is strongly suppressed. This contrasts with De Florian et al. where  $u, d$  and  $s$  are assumed to be equal. However the heavy quarks have a pattern similar to De Florian et al., with a sizeable contribution only for  $x \leq 0.1$  and a fast dropping off for large  $x$ .

## Comments ( cont.)

This is also at variance with **J.J. Yang**, where  $D_u^\Lambda / D_s^\Lambda$  decreases from 1 to 0.2 when  $x$  goes from 0 to 1. For the proton it is surprising to see that the  $u$ -quark FF dominates **only** at large  $x$ , whereas the strange and heavy quarks contribute substantially for  $x \leq 0.3$  or so.

# Conclusions

- FF are very relevant for better understanding of baryon structure
- Importance of semi-inclusive DIS to improve quark flavor separation
- Present situation:  $\Lambda$  unpolarized FF is known but need more data. Polarized FF poorly known
- Future prospects from Hermes, HERA, Compass and RHIC-BNL.