# Epistemology and Rosen's Modeling Relation 

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#### Abstract

Rosen's modeling relation is embedded in Popper's three worlds to provide an heuristic tool for model building and a guide for thinking about complex systems. The utility of this construct is demonstrated by suggesting a solution to the problem of pseudo science and a resolution of the famous Bohr-Einstein debates. A theory of bizarre systems is presented by an analogy with entangled particles of quantum mechanics. This theory underscores the poverty of present-day computational systems (e.g., computers) for creating complex and bizarre entities by distinguishing between mechanism and organism.


## INTRODUCTION

Rosen's modeling relation (MR) provides a powerful method of understanding and exploring the nature of the scientific method. Of course, the scientific method is itself epistemology in action. A decade ago Robert Rosen published an essay [1] on epistemology in honor of David Bohm. The explanation and use of the MR in that essay appeared as a revelation that evidently had great explanatory power and seemed to invite further development as an epistemological tool. The scientific method currently receives lip service but little practical understanding in the day-to-day lives of scientists. The method seems to exist more as a topic of intellectual discourse than a guide to pragmatic behavior even though it has been discussed at length by many philosophers, including Karl Popper [2]. A clear and simple model of the scientific method contributes a clarity that volumes of philosophy cannot provide.

To provide an appropriate conceptual setting for the extended MR developed here, the necessary background and vocabulary are first presented. Popper's 3 worlds are then suggested as a "container" for the MR. The ensuing framework allows one to analyze the MR itself, seeing how its parts fit onto the world of organisms, objects, brains, and theories-that is, the exceedingly complex, natural world comprised of all those atoms in their remarkable manifestations "of ships and shoes and sealing wax and cabbages and kings."

As examples of embedding the MR in the 3 worlds, Popper's problem of demarcation between science and pseudo science is revisited. The famous Einstein-Podolsky-Rosen paper serves to introduce the use of the MR as a tool for thinking. Finally, a mathematical definition of "bizarre" systems, based on a real-world bizarre object, is suggested. The definition meets our intuitive requirements of what such concepts as "bizarre" and "complex" should mean.

## EPISTEMOLOGY OF THE MODELING RELATION

While the 3 -worlds' embedding of the MR presented in this section is hardly a necessary undertaking, it certainly provides a useful and convenient means of concept bookkeeping, allowing one to maintain clear thought processes and keep ideas disentangled.

## Rosen's modeling relation

For those not familiar with Rosen's modeling relation [3], the following words are borrowed in a modified form from a previous publication [4] and summarize. For a canonical and detailed explanation of the MR, one can do no better than read Rosen's original works.

Without worrying about the niceties of meaning and existence, terms which a physicist or engineer takes for granted anyway, consider a natural system denoted by $N$ and a corresponding formal system denoted by $\boldsymbol{F}$. The natural system consists of components where any identification, language, or discourse leads us immediately into some formal system. $\boldsymbol{N}$ not only exists, but exhibits behaviors that can be observed by the process of measurement [5]. The temporal evolution taking place in such an $\boldsymbol{N}$ is an internal entailment termed 'causality.' $\boldsymbol{F}$ likewise has components in the form of elements, perhaps axioms or theorems, or maybe just embryonic concepts bearing quasilogical relationships to one another. The entailment structure possessed by $\boldsymbol{F}$ often takes the form of production rules that may be identified with inference of a logical, mathematical, or algorithmic nature. This entailment process is an internal operation within $\boldsymbol{F}$ that mirrors the autonomous, causal, and dynamic processes in $N$.

The measurement process is subsumed by the concept of encoding behaviors of $N$ into elements or sets in $\boldsymbol{F}$. Inferences are then be made in $\boldsymbol{F}$ by 'turning' the mathematical 'crank.' The results of the inferences must then be compared to the future behavior of $N$, which process is called 'prediction' in science. Decoding is a dual process to encoding-one that the scientist uses to verify predictions by another measurement procedure on the future behavior of $N$. The intimate relationship between the MR and the scientific method alluded to above should now be clear.

The possibility of making predictions and their subsequent verification lead to the idea of connectives or a relation between $\boldsymbol{N}$ and $\boldsymbol{F}$ that allow comparison of the two systems. The result, when all the pieces are placed in relationship to each other, is Rosen's modeling relation, shown in Figure 1.


Figure 1. Block diagram of an abstract modeling relation wherein a natural system is modeled by a formal system. Each system has its own internal entailment structures and the two systems are connected by the encoding and decoding processes.

Of course, natural systems can model other natural systems and formal systems other formal systems. That is the power of the MR as a conceptual tool and the basis for talking about a mathematics of thought and, perhaps, consciousness.

## Connection to Popper's 3 worlds

Popper himself gave the clearest expression of his 3-worlds' concept in the following passage:
" $[W]$ ithout taking the words 'world' or 'universe' too seriously, we may distinguish the following three worlds or universes: first, the world of physical objects or physical states; secondly, the world of states or consciousness, or of mental states, or perhaps of behavioral dispositions to act; and thirdly, the world of objective contents of thought, especially of scientific and poetic thoughts and works of art."-Karl Popper, [6, p. 59]
This concept of three worlds provides a convenient framework for the modeling-relation triad of natural system, encoding and decoding, and formal system. $N$ and its components clearly belong to world 1 and the encodings and decodings as processes belong to world 2 while being conceptualized, and thence to world 3, as formal procedures. $\boldsymbol{F}$ is clearly a world 3 construct, while the inferences are world-2 activities or world-3 implications depending on who or what is performing them. Implications in the world- 1 system-that is, causality-remain strictly a world- 1 activity or relation.

Just as one would claim objective existence in world 1 for any particular $N$, Popper would say that $\boldsymbol{F}$ likewise has objective existence-in world 3. Holding this distinction in mind can materially aid one's thought process when wrestling with new or complex ideas; confusing the worlds 1 and 3 leads to all sorts of nonsense and philosophical errors, primarily the so-called category error. Note that Popper does not suggest that any particular formal system must be correct or complete to be a candidate for world- 3 existence-it inhabits world 3 merely by its being conceived and discussed. It takes a mind to bring a any world- 1 object into world- 3 existence; this observation contains a lovely circularity in that such an act of creation can only be accomplished by a world- 1 organism. Popper argues convincingly [7] for the existence of world 3 and its creation by the human mind.

## The modeling relation as epistemology

Given Rosen's concept of the modeling relation and its embedding in Popper's three worlds, the role of the MR in constructing a rational epistemology becomes clear. The canonical example of this marriage is the scientific method. Here, all three elements of the MR (the two systems, natural and formal, the entailment processes within each, and the encoding and decoding connectives) are identified with each of the three worlds. The only piece that is not a direct mapping is the act of encoding and decoding; while obviously world-2 activities, these connectives of the MR have referents in both world 1 and 3 and consequences in world 3 . This "foot in both camps" nature of the connec-

## BRAINS, MACHINES, AND A MATHEMATICS OF CONSCIOUSNESS

It is well known that the first complex organism (beyond yeast) to have its genome completely mapped is C. Elegans, the nematode. Well before this genome work was completed, others had mapped out the nematode's central nervous system. In particular, a recent special report in Science [9] notes that there are a mere 302 cells in the worm's nervous system and that many, if not most, of the neurotransmitters, receptors, and transmitter channels are already known. The complete "wiring diagram" of the neural connections has been worked out, as a mechanism, and it is not too difficult to imagine that electrical and chemical signals can be assigned to particular paths and activities. In short, it is almost certain that the entire "brain" of C. Elegans can and will be simulated in great detail on a super computer. The simulation can then "run" and be made to exhibit behavior arbitrarily close to that an actual creature. Since the model of the nematode's brain-a model extracted from the physiology and biochemistry-will then be a simulation, the result can be nothing more than a simulation of a mechanism no matter how complicated and detailed it is made. Can the computer then be said to contain or generate or be an artificially live nematode? Only by greatly stretching any possible metaphorical interpretation the researchers will choose to give to the bit patterns that emerge, would such an assertion make sense. The point is that the simulation imagined here is just a "model" of an abstracted formal model and, as Rosen has shown [10], the entailment relations between the original model and the natural system are completely lost when passing to a simulation.

## On analyzing the modeling relation

Above, it was suggested that natural systems can serve as models of both formal and natural systems. Likewise, formal systems can model other formal systems. If one analyzes (deconstructs) the modeling relation, it is possible to speak about models themselves, recognizing the danger in losing track of the referent. Suppose, for a moment, that the formal system $\boldsymbol{F}$ is disconnected from the natural system $N$, leaving the encoding and decoding relations dangling. One might think of a molecule with a dangling orbital in search of another molecule with which to bond. To continue this metaphor, suppose there is a soup or solution containing many different types of $\boldsymbol{F}$ s, each with a different "affinity" for the target system. As the solution is cooled, a "bond" will form with some other $\boldsymbol{F}$. Repeating this operation many times, many different bonds will form. The set of formal systems $\{\boldsymbol{F}\}$ that bond to the original $\boldsymbol{F}$ form an equivalence class with "temperature" as a granularity parameter, perhaps.

## Partial ordering on the set $\{\boldsymbol{F}\}$

Not pushing this metaphor too far, suppose that $\{\boldsymbol{F}\}$ in a given equivalence class can now be analyzed by an ordering relation. Conceptually construct a sequence of formal models, each one more "distant" from the original natural system by some measure of similarity or correspondence.

Since one theory or explanation can often said to be better than another by some established set of criteria, ordering of some sort does seem useful while 'distance' may be too strong a term at this stage-it may be that a metric space is too restrictive. Ordering does make sense as the notion of equivalence class is involved and one can certainly imagine equivalence classes of models. A paradigm for these ideas is to be found in the practice of science-returning again to the scientific method, some theories or models are better than others, the criteria being Occam's razor, explanatory power, and correspondence of predicted behaviors with the natural system.

An essential step in a formal development of these ideas is to construct a space of formal systems. A partitioning into equivalence classes generated by a suitable relation on this space create conceptual objects each of which is either "bonded" to a particular $N$ or not. Perhaps adding a "null"
natural system, so that all equivalence classes are bonded, makes sense. The study of such augmented modeling relations then requires the full formalism of category theory.

## The "floating" formal system

Suppose no member of $\{\boldsymbol{F}\}$ ever "bonds" strongly to any $\boldsymbol{N}$-the $\{\boldsymbol{F}\}$ can said to be "floating." What are the properties of such floating formal systems? In one view, they seem to refer to pseudo science in the sense that any $\boldsymbol{F}$ in $\{\boldsymbol{F}\}$ not only does not refer to or closely correspond with any known $\boldsymbol{N}$, but the pseudo- $\boldsymbol{N}$ it is presumably bound to also "floats" in that no expenditure of effort can clearly identify it. The sought-for $\boldsymbol{N}$ becomes a moving target; the set $\{\boldsymbol{F}\}$ is a set in search of a referent. Such a floating set cannot be dismissed outright as it may be an essential step in the creative process and an aid to speculations and brain-storming. This situation is not necessarily an error; just because a particular instance of the set is floating does not mean that future representations or some evolution of the set can't find a suitable $N$.

## RESOLVING CONFLICTS AND PUZZLES

In this section, the above ideas are made more concrete by discussing some particular examples. These illustrations address primarily the use of MR3 as a framework for thinking. However, the examples should also hint at the direction that a formal theory of MR3 might take.

## Demarcation and the problem of pseudo science

The problem Popper originally set for himself was to establish a demarcation between science and pseudo science (PS). Any good philosopher categorically rejects appeals to authority such as, "that is science, this is not (period)." Popper sought a natural and consistent way to classify methods and belief systems; the result was the criterion of falsification. Given today's wide-spread cultural interest in such things as angels, astrology, aliens, creationism, The X Files, Men in Black, and so on and on and on, it seems that we have much the same problem nearly three-quarters of a century later. To compound matters, many pseudo sciences, or activities that we feel should be classified as such, make use of a modeling relation in much the same way as does actual science. Thus, PS can even be said to follow the scientific method in some perverse way. However, the 'natural systems' of PS do not necessarily exist in world 1-that is, they are imaginary constructs mostly in world 3. As such, the formal systems of PS are usually, but not entirely, incomplete systems in the sense of having only certain paths (implication chains) explored or publicized, or comprising inconsistent axioms or assumptions as well as having axioms or assumptions that are clearly at odds with the larger body of formal systems (e.g., science) that have been developed, amended, tested, and explored over the decades.

A method of demarcation suggested here is to identify precisely what the PS is talking about-not only what the object of the decoding process is claimed to be, but precisely how and from which natural system, if any, the encodings are said to have arisen. If there is a chain of formal systems, as is usually the case in intellectual constructs, simply chase along the chain in an attempt to locate some natural system that is the ultimate referent. In this view, France's N-rays, Russia's poly water, and Utah's cold fusion are not examples of pseudo science since the chain of quasiformal systems in all these cases could be followed and no ultimate natural system was found at the end. These models were simply in error. The claims of homeopathy, creationism, astrology, and many other systems have likewise been chased down the formal-system chain. The end result usually uncovers an appeal to authority, a circular sequence of formal systems, or simply an infinite regression of formal systems. Each of these endpoints indicates a PS.

## Quantum mechanics and the EPR paradox

Recent activity in the rapidly expanding field of quantum optics and quantum measurement has led to questions concerning the locality of phenomena and the concept of causality as interpreted in quantum mechanics. Asking whether certain behaviors are possible and whether they can be used for practical applications in communications and sensing, one is led to revisit the famous BohrEinstein debates concerning the nature of quantum mechanics and what quantum mechanics can and cannot say ("Speakables and unspeakables" in Bell's terminology [11]). In 1935, Einstein, Podolsky, and Rosen (EPR) published a paper [12] that was to affect the way future generations of physicists thought about reality.

## Einstein's viewpoint

Consider the opening paragraph of the famous EPR paper:
"Any serious consideration of a physical theory must take into account the distinction between the objective reality, which is independent of any theory, and the physical concepts with which the theory operates. These concepts are intended to correspond with the objective reality, and by means of these concepts we picture this reality to ourselves."-Einstein, Podolsky, Rosen [12]

This is an expression of clarity that few have achieved so surely and succinctly; it evokes an image much like that of Fig 1. The statement clearly expresses the relationship between epistemology and ontology and, incidentally, suggests that Einstein's concern was with the ontological. Theory, for him, was a means to know reality, with the emphasis on 'reality.'

The paper then goes on to suggest a thought experiment where two particles are made to share their properties jointly. A measurement on one of the particles simultaneously provides knowledge of the shared state of the other. It wasn't until some thirty years later that such experiments became feasible, realizing Einstein's deepest concerns.

Bohr's viewpoint
Consider the following excerpt from Bohr's reply [13] to the EPR paper:
"Of course there is in a case like that just considered [referring to the measurement on one member of a correlated 'EPR' pair allowing an inference to be made concerning the other member] no question of a mechanical disturbance of $t$ he system under investigation during the last critical stage of the measuring procedure. But even at this stage there is essentially the question of an influence on the very conditions which define the possible types of predictions regarding the future behavior of the system."-Nils Bohr

Bell [11] thought this incomprehensible and it certainly seems so, even after much pondering. However, when viewed in context of Einstein's statement and taking a hint from Jaynes [14], who

## Resolution

Although the debate initiated by Einstein continues to this day, a resolution to this paradox can be constructed that closely follows Jaynes' ideas and makes explicit use of Rosen's modeling relation. Consider the following particular modeling relation between a natural system (quantum reality) and a formal system (quantum mechanics). The encodings (measurements) and decodings (predictions) are present as are the causal dynamics, which can only be inferred but never perceptually apprehended. The inference or entailment structure of proofs of theorems and calculations are also indicated. This situation is shown in Figure 2.


Figure 2. The Bohr-Einstein debates seen from the viewpoint of the modeling relation.
placed by a sum. Suppose and $|\psi\rangle \in \boldsymbol{H}$ and $\left\{\left|\phi_{n}\right\rangle\right\}$ is an orthonormal basis for $\boldsymbol{H}$. Then an expansion of $|\psi\rangle$ in the $\phi$-representation is given by

$$
\begin{equation*}
|\psi\rangle=\sum_{j} c_{j}\left|\phi_{j}\right\rangle \tag{1}
\end{equation*}
$$

for a particular set of complex numbers $\left\{c_{j}\right\}$. Take the inner product of $|\psi\rangle$ with $\left|\phi_{m}\right\rangle$ and observe that $c_{m}=\left\langle\phi_{m} \mid \psi\right\rangle$ since $\left\langle\phi_{i} \mid \phi_{j}\right\rangle=\delta_{i, j}$, which is the Kronecker symbol that is 1 for $i=j$ and zero otherwise. Assume that $|\psi\rangle$ is normalized, that is $\langle\psi \mid \psi\rangle=1$. In the $\phi$-representation, that normalization may be written, noting that a complex number becomes its complex conjugate in the adjoint space, as

$$
\begin{equation*}
\langle\psi \mid \psi\rangle=\sum_{j, i} c_{j}^{*} c_{i}\left\langle\phi_{j} \mid \phi_{i}\right\rangle=\sum_{j, i} c_{j}^{*} c_{i} \delta_{j, i}=\sum_{j}\left|c_{j}\right|^{2} \tag{2}
\end{equation*}
$$

but this expression is equal to 1 since the function is normalized. In addition, note that the absolute value of any number is 0 .

Define (Bayesian) probability as a mapping, $p$, from a denumerable set of statements $X$ to the interval $[0,1]$ such that $p(x) 0, \quad p(\varnothing)=0$, and $p(X)=1$ where $x \in X . p(x)$, read "the probability that statement $x$ is true" or , simply, "the probability of $x$," is always assumed to be conditioned on some set of circumstances such as an experimental arrangement. This conditioning may be explicitly given by the notation $x \mid y$ which is read " $x$ given that the statement $y$ is true." The mapping $p$ obeys the product and sum rules [16], which state that $\mathrm{p}(x y)=\mathrm{p}(x) \mathrm{p}(y \mid x)$ and $p(x+y)=p(x)+p(y)-p(x y)$, where $x, y \in X$, " $x+y$ " is the disjunction of the two statements and " $x y$ " or " $x, y$ " is their conjunction. Note that both conjunction and disjunction are associative and commutative and that conjunction distributes over disjunction as in ordinary arithmetic. Since the spaces of interest are finite dimensional, as they must be for any real-world example of interest, the full machinery of (Kolmogorov) probability theory is not required.

A central postulate of quantum mechanics, which we require to talk about bizarre quantum systems, is that any physical observable of a quantum system is represented by a linear, self-adjoint operator on the corresponding Hilbert space. An operator $A$ is self-adjoint if $\langle u \mid A v\rangle=\langle A u \mid v\rangle$ for any two non-zero vectors belonging to $\boldsymbol{H}$. The other postulate needed identifies a probability distribution with amplitudes of normalized vectors expanded in an eigenbasis of any self-adjoint operator on the Hilbert space in question; "amplitude" refers to the coefficient in such an eigenexpansion, which are the $c_{j}$ in (1). The postulate states that the square of the absolute value of an amplitude of a normalized vector in a Hilbert space is the probability of obtaining the eigenvalue belonging to that eigenvector in a measurement of the corresponding operator.

## Magic coins and dice

With these definitions, consider a two-sided die (coin) on a real vector space. This object can be represented by the column vectors $\mid$ heads $\rangle=(1,0)^{\mathrm{T}}$ and $\mid$ tails $\rangle=(0,1)^{\mathrm{T}}$ where T means transpose. The "which-side" operator is the diagonal matrix with the number of spots (say 1 and 2 where 1 means "heads" and 2 "tails") along the diagonal. The state describing the coin during a toss is $(a, b)^{\mathrm{T}}$ where $a^{2}+b^{2}=1$ and both amplitudes $a$ and $b$ are real. A fair coin has $|a|=|b|$ since negative numbers are allowed; and the probability of heads is $|a|^{2}$ and tails $|b|^{2}$. This simple example allows one to compute the probabilities in any coin toss by identifying the square of the amplitudes with the probabilities of obtaining either heads or tails. So far, no magic or bizarre behavior.

The next step is to consider two coins or dice, each represented on its own Hilbert space. How can these entities be combined? For linear spaces, there are only two ways of describing the
two coins that both make sense and are not unduly complicated: on a direct sum space and on a direct product space. Both combinations are defined using the notion of a Cartesian product. The direct (Cartesian) product of two vector spaces $\boldsymbol{V}_{\boldsymbol{I}}$ and $\boldsymbol{V}_{2}$ over the same field (written as $\boldsymbol{V}=\boldsymbol{V}_{\boldsymbol{I}} \otimes \boldsymbol{V}_{2}$ ) is the set of pairs $\left\{\left(x_{i}, y_{j}\right): x_{i} \in \boldsymbol{V}_{\boldsymbol{I}}, y_{j} \in \boldsymbol{V}_{2}\right\}$ such that $a(u, v)=(a u, a v)$ and $(x, y)+(u, v)=(x+u, y+v)$ where $a$ is an element of the scalar field. In the Dirac notation chosen, simply choose one from each space, as $|i\rangle|j\rangle$ where $|i\rangle \in V_{I}$ and $|j\rangle \in V_{2}$. The order in which the two vectors are written distinguishes equally well between the two spaces as does the (., .) notation, not to be confused with the alternate notation for an inner product; if we need to specify the particular factor space, then subscripts can be used as $|i\rangle_{1}|j\rangle_{2}$. If the spaces are finite-dimensional Hilbert spaces, it is easy to prove that their pro
lands first, showing heads. One can predict with certainty that the other will show tails when it lands, yet the coins are fair. Such coins are said to be "magic" [17].

## Real-world 'magic' coins

The same situation obtains for electrons or photons or any other two quantum entities that are properly prepared in a source that emits them together as pairs. Such pairs are said to be "entangled," which simply means that their description as a function on the product Hilbert space cannot be factored into a product of two functions, one belonging to each individual space. If each $c_{i, j}$ in (3) were equal to $1 / 2$, such a factorization would be possible and the joint probability matrix would be 2 by 2 with $1 / 4$ for each of the 4 entries. Entanglement is not possible on a sum space.

The point of this mathematical digression into quantum physics is to make clear the distinction between sum and product spaces; the former do not support bizarre behavior while the latter do. This observation leads to the meaningful and reasonable suggestion that the term "bizarre," when used in conjunction with complex systems and artificial organisms, might profitably refer to an analysis on direct product spaces. The motivation for the distinction is that such bizarre systems actually exist in the quantum world. There is no reason why they cannot exist in the macro-world referred to in the Introduction. The suggestion here is that they indeed exist and are called organisms.

## Speculation on the possibility of artificial organisms

That such a simple system as described above can exhibit truly bizarre behavior gives us hope that our quest for artificial organisms might not be in vain. I believe we can learn how to construct complex, intelligent, and perhaps even conscious artifacts by a careful and direct extrapolation of the binary behavior of entangled quasi coins such as electrons and photons.

Protein synthesis is a quantum-mechanical process taking place within cells, both eukaryote and prokaryote. Biological macromolecules involved in this process are in well-defined quantum states and, ignoring thermalization processes demanded by equilibrium thermodynamics [14], these states are shared during interactions between molecules. Upon separation, when the protein leaves the ribosome, the entanglement is maintained even though it will be gradually lost due to an envi-ronmental-interaction effect known as "decoherence." Suppose the protein can reach the cell wall before full decoherence; here, there may be several possibilities such as opening an ion channel, passing through the membrane, or other bio-functions involving the membrane or other cellular structures. Suppose, further, that one of the protein's entangled partners also has a range of possibilities of interaction in its own neighborhood, possibilities that have non-uniform probabilities. Then, by an argument based on the probabilistic behavior of functions on the product Hilbert space (of very large dimensions), a quantum-mechanical calculation forces one to conclude that, in probability, the interaction occurring in the cell's interior will determine, in the sense used above, the particular choice made by the protein as it interacts with the cell wall. The point is that "decisions" made at the cell center can influence actions at the periphery without a mechanism being present. A disrupted cell would be open to excessive decoherence, effectively putting an end to its normal functioning; the cell would experience death. Only if the disruption could be removed in such a way as to reestablish quantum entanglement could the cell live again.

Alternatively, only if we can construct artifacts that allow entanglement at the quantum level while maintaining the large-dimensional complexity required of living organisms, will we succeed in creating artificial organisms. It is only artificial organisms that will be able to exhibit-not simu-late-life, intelligence, and consciousness; their entailment processes must be causal, not formal. The hope that present day computers can be "alive" or "conscious" or "spiritual" is based on mere naïve analogy with certain behaviors observed in real, live organisms and a false imputation of intention-
ality. Until we produce complex constructs based on quantum entanglement, such hopes will remain unrealized dreams.

## EPILOGUE

The heuristic structure of MR3 (Rosen's modeling relation embedded in Popper's 3 worlds) has been proposed as a structure for clear thinking and a guide to building models of complex systems. Using such an aid, pseudo science becomes easier to identify. Additionally, the great quantum debate of the past 75 years is seen to be nothing more serious than the parable of the three blind men and the elephant-the resolution was to identify the elephant. Of course, there is much more involved than this glib abstraction, but each twist and turn in the conceptual windings of the arguments on both sides is amenable to an analysis via the modeling relation.

The bizarre behavior of quantum-mechanical "coins" or "dice" leads to an existential basis for understanding the "bizarre" behavior of complex system by analyzing such systems on product spaces instead of the sum spaces $[10,18]$ that commonly describe computers and algorithmic, formal processes. That there is such a thing as bizarre behavior gives us hope of constructing artificial organisms.

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