

# Thermal-Structural Analysis of Sunshield Membranes

John Johnston Keith Parrish NASA Goddard Space Flight Center

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## **Future IR Space Telescopes**



- There are several large infrared (IR) space telescopes planned for the coming decades...
  - James Webb Space Telescope (JWST)
  - Single Aperture Far Infrared (SAFIR)
- The JWST consists of a cryogenic telescope and instruments, a room temperature spacecraft, and a deployable sunshield.
- The sunshield provides passive radiative cooling to cryogenic operating temperatures, stability at operating temperature, and stray light control.



#### **JWST Observatory**

#### **Sunshields for Large Space Telescopes**



- Typical deployable sunshield concepts consists of:
  - Multiple layers of thin-film membranes
  - Deployable booms to support the film layers
  - Membrane management hardware to position and tension the films:
    - Ladder structures
    - Constant force springs
  - Container for the stowed structure



#### **Sunshield Temperatures**



- Mean temperatures will vary widely from layer-to-layer:
  - Sun-side film layer ~ 400 K
  - Cold-side film layer ~ 100 K.
- In-plane temperature variations within the film layers are predicted to be large (up to 100 K) due to:
  - Greater view to deep space at the edges than at the center
  - Presence of the room temperature spacecraft at the center
- Membrane layers must be maintained in their nominal geometry (both spacing and flatness) when subject to thermal strain effects due to both layer-to-layer temperature differences and in-plane temperature gradients.



### **Accommodating Thermal Strains**



- Post-deployment structural performance of the sunshield is a concern since it may impact observatory thermal performance.
- A constant-force preloading scheme is typically implemented to accommodate thermal expansion/contraction of the membrane layers and is effective in compensating for uniform temperature changes and layer-to-layer bulk temperature differences.
- Even with constant-force preloading, large radial temperature gradients could lead to a loss of tensile preload within the film layers:
  - Results from over-contraction of the cold film perimeter relative to the warmer center of the film.
  - The formation of a slack region would result if the tensile preload drops to zero.
- Reduced preload or slackness in the films is a concern since any resulting sagging of the films could lead to "thermal shortcuting" if adjacent membrane layers come into contact.

# **Objective**



- The objective was to study the effects of temperature on the structural behavior of preloaded sunshield film layers utilizing recent developments in finite element modeling of partially wrinkled thin-film membranes.
- The problem of a single film layer from the NASA reference concept JWST sunshield is used to demonstrate the analysis process and study sensitivities to:
  - In-plane temperature variations
  - Film preload level

#### **Thermal-Structural Analytical Process**



- Multi-step, sequentially coupled thermal-structural analysis:
- 1. Thermal analysis predicts temperatures
- 2. Temperature mapping used to interface thermal and structural models
- Structural analysis predicts displacements/stresses/etc. due to combination of mechanical preloads and prescribed temperatures

# **Thermal Analysis**



- Thermal analysis performed using:
  - Thermal Synthesis System (TSS) to calculate radiation interchange factors
  - SINDA85 to solve for model nodal temperatures
- Sunshield cold-side (layer 6) temperatures:
  - Tmean = 73.9 K
  - Tmax = 111.7 K
  - Tmin = 44.3 K
  - In-plane gradient = 67.4 K



#### **Temperature Mapping**



- Since thermal and structural models typically have dissimilar meshes, it is necessary to perform a "mapping" of the temperatures from the thermal model mesh to the structural model mesh.
- Temperature mapping approaches:
  - Pair corresponding thermal and structural model nodes, then prescribe these temperatures in a steady-state heat transfer analysis performed using the FEM.
  - Fit a function to the thermal results, then map this function to the structural model mesh (i.e. MATLAB "griddata" function)



#### **Structural Analysis**



- The structural analysis was performed using ABAQUS.
- The baseline analysis consisted of three nonlinear static analysis steps:
  - 1. Apply constant force spring preloads, Specify uniform temperature = 294 K (room temperature)
  - 2. Specify uniform temperature = 74 K (mean cold-side temperature)
  - 3. Specify mapped temperature distribution (mean temperature + gradient)

#### **Thin-Film Modeling**



- Thin-film membrane layer modeled using membrane elements (M3D3) in conjunction with a wrinkling material model:
  - Material model is a finite element implementation of Stein-Hedgepeth membrane wrinkling theory.
  - Approach developed by Miller-Hedgepeth (1982) and Adler-Mikulas (2000).
- Membrane element stiffness iteratively modified to account for the effects of wrinkling:
  - Element state determined using a mixed stress-strain criteria
  - Stiffness matrix formulation based on the element state
  - Approach predicts stress distributions corrected for wrinkling and slackness as well as wrinkled/slack regions, but not wrinkling details.
- Shell element overlay provides small artificial stiffness:
  - Allows slack regions to become taut when preload is increased despite zero in-plane stiffness in slack membrane elements
  - Studies showed minimal effect on the membrane stresses
- Additional numerical stabilization provided by ABAQUS \*STABILIZE

#### **Finite Element Model**



- Mesh:
  - 5146 Nodes
  - 19800 Elements
- Components:
  - Film (M3D3 membrane elements)
  - Corner reinforcements (STRI3 shell elements)
  - Spreader Bars (B31 beam elements)
  - Constant Force Springs (B31 beam elements)
- Central cut-out in film representative of attachment to spacecraft
- Assumed uniform, temperature independent CTE for all materials (2.0E-5 /K)



#### FEM – Load & Constraints



- Loads:
  - 2 CFS per corner
  - 14.25 N total per corner
  - Applied constant force preload using ABAQUS \*PRE-TENSION SECTION
- Constraints:
  - Fixed at spreader bars (interface with deployment booms)
  - Pinned around the perimeter of central cut-out



#### **Uniform Temperature = 294 K**





| Preload | Temper | ature (K) |             | Stress      | Area (%)    |             |       |          |      |
|---------|--------|-----------|-------------|-------------|-------------|-------------|-------|----------|------|
| (N)     | Tmean  | Tmax-Tmin | Major - Max | Major - Min | Minor - Max | Minor - Min | Slack | Wrinkled | Taut |
| 14.25   | 294    | 0         | 1.30E+06    | 7.07E+04    | 1.27E+05    | 0.00E+00    | 0.00  | 0.33     | 0.67 |
| 14.25   | 74     | 0         | 1.20E+07    | 7.59E+04    | 3.51E+05    | 0.00E+00    | 0.00  | 0.40     | 0.60 |
| 14.25   | 74     | 67        | 9.90E+06    | 0.00E+00    | 5.44E+05    | 0.00E+00    | 0.15  | 0.63     | 0.22 |

#### **Thermal Strains**





Uniform Temperature = 74 K

Mapped Temperature Distribution (Tmean = 74 K, Tmax-Tmin= 67 K)

Difference (i.e. thermal strain due to radial gradient)

#### **Uniform Temperature = 74 K**





| Preload | Temper | ature (K) |   | Stress   | Area (%) |          |      |      |      |
|---------|--------|-----------|---|----------|----------|----------|------|------|------|
| (N)     | Tmean  | Tmax-Tmin | Major - Max Major - Min Minor - Max Minor - Min |          | Slack    | Wrinkled | Taut |      |      |
| 14.25   | 294    | 0         | 1.30E+06  | 7.07E+04 | 1.27E+05 | 0.00E+00 | 0.00 | 0.33 | 0.67 |
| 14.25   | 74     | 0         | 1.20E+07  | 7.59E+04 | 3.51E+05 | 0.00E+00 | 0.00 | 0.40 | 0.60 |
| 14.25   | 74     | 67        | 9.90E+06  | 0.00E+00 | 5.44E+05 | 0.00E+00 | 0.15 | 0.63 | 0.22 |

#### Mapped Temperature Distribution (Tmean = 74 K, Tmax-Tmin= 67 K)





| Preload | Temper | ature (K) |             | Stress                    | Area (%) |             |       |          |      |  |
|---------|--------|-----------|-------------|---------------------------|----------|-------------|-------|----------|------|--|
| (N)     | Tmean  | Tmax-Tmin | Major - Max | K Major - Min Minor - Max |          | Minor - Min | Slack | Wrinkled | Taut |  |
| 14.25   | 294    | 0         | 1.30E+06    | 7.07E+04                  | 1.27E+05 | 0.00E+00    | 0.00  | 0.33     | 0.67 |  |
| 14.25   | 74     | 0         | 1.20E+07    | 7.59E+04                  | 3.51E+05 | 0.00E+00    | 0.00  | 0.40     | 0.60 |  |
| 14.25   | 74     | 67        | 9.90E+06    | 0.00E+00                  | 5.44E+05 | 0.00E+00    | 0.15  | 0.63     | 0.22 |  |

# **Effects of Varying Temperature Gradient**





**Temperature Gradient (K)** 

| Support | Preload (N) | Temper | ature (K) |             | Stress      | es (Pa)     |             | Area (%) |          |      |  |
|---------|-------------|--------|-----------|-------------|-------------|-------------|-------------|----------|----------|------|--|
| Case    |             | Tmean  | Tmax-Tmin | Major - Max | Major - Min | Minor - Max | Minor - Min | Slack    | Wrinkled | Taut |  |
| В       | 14.25       | 294    | 0         | 1.30E+06    | 7.07E+04    | 1.27E+05    | 0.00E+00    | 0.00     | 0.33     | 0.67 |  |
| В       | 14.25       | 74     | 0         | 1.20E+07    | 7.59E+04    | 3.51E+05    | 0.00E+00    | 0.00     | 0.40     | 0.60 |  |
| В       | 14.25       | 74     | 10        | 1.17E+07    | 1.05E+04    | 2.23E+05    | 0.00E+00    | 0.00     | 0.41     | 0.59 |  |
| В       | 14.25       | 74     | 20        | 1.14E+07    | 3.34E+01    | 2.58E+05    | 0.00E+00    | 0.01     | 0.53     | 0.46 |  |
| В       | 14.25       | 74     | 30        | 1.11E+07    | 0.00E+00    | 3.28E+05    | 0.00E+00    | 0.03     | 0.61     | 0.35 |  |
| В       | 14.25       | 74     | 40        | 1.04E+07    | 0.00E+00    | 4.51E+05    | 0.00E+00    | 0.06     | 0.64     | 0.30 |  |
| В       | 14.25       | 74     | 50        | 1.01E+07    | 0.00E+00    | 5.06E+05    | 0.00E+00    | 0.08     | 0.65     | 0.27 |  |
| В       | 14.25       | 74     | 60        | 9.82E+06    | 0.00E+00    | 5.57E+05    | 0.00E+00    | 0.11     | 0.65     | 0.24 |  |
| В       | 14.25       | 74     | 67        | 9.90E+06    | 0.00E+00    | 5.44E+05    | 0.00E+00    | 0.15     | 0.63     | 0.22 |  |
| В       | 14.25       | 74     | 70        | 9.53E+06    | 0.00E+00    | 6.04E+05    | 0.00E+00    | 0.17     | 0.62     | 0.21 |  |
| В       | 14.25       | 74     | 80        | 9.23E+06    | 0.00E+00    | 6.45E+05    | 0.00E+00    | 0.21     | 0.60     | 0.19 |  |
| В       | 14.25       | 74     | 90        | 9.23E+06    | 0.00E+00    | 6.45E+05    | 0.00E+00    | 0.25     | 0.57     | 0.18 |  |
| В       | 14.25       | 74     | 100       | 8.94E+06    | 0.00E+00    | 6.87E+05    | 0.00E+00    | 0.27     | 0.56     | 0.17 |  |



#### **Effects of Varying Preload**



Preload (N)

| Support | Preload (N) | Temper | ature (K) |             | Stress      | es (Pa)     | Area (%)    |       |          |      |
|---------|-------------|--------|-----------|-------------|-------------|-------------|-------------|-------|----------|------|
| Case    |             | Tmean  | Tmax-Tmin | Major - Max | Major - Min | Minor - Max | Minor - Min | Slack | Wrinkled | Taut |
| В       | 14.25       | 294    | 0         | 1.30E+06    | 7.07E+04    | 1.27E+05    | 0.00E+00    | 0.00  | 0.33     | 0.67 |
| В       | 14.25       | 74     | 0         | 1.20E+07    | 7.59E+04    | 3.51E+05    | 0.00E+00    | 0.00  | 0.40     | 0.60 |
| В       | 14.25       | 74     | 67        | 9.90E+06    | 0.00E+00    | 5.44E+05    | 0.00E+00    | 0.15  | 0.63     | 0.22 |
| В       | 28.5        | 74     | 67        | 1.01E+07    | 0.00E+00    | 6.90E+05    | 0.00E+00    | 0.06  | 0.69     | 0.25 |
| В       | 42.75       | 74     | 67        | 1.02E+07    | 0.00E+00    | 8.50E+05    | 0.00E+00    | 0.02  | 0.66     | 0.32 |
| В       | 57          | 74     | 67        | 1.03E+07    | 2.93E+04    | 9.96E+05    | 0.00E+00    | 0.00  | 0.58     | 0.42 |
| В       | 71.25       | 74     | 67        | 1.04E+07    | 1.05E+05    | 1.13E+06    | 0.00E+00    | 0.00  | 0.47     | 0.53 |
| В       | 85.5        | 74     | 67        | 1.05E+07    | 1.86E+05    | 1.24E+06    | 0.00E+00    | 0.00  | 0.39     | 0.61 |
| В       | 99.75       | 74     | 67        | 1.05E+07    | 2.06E+05    | 1.30E+06    | 0.00E+00    | 0.00  | 0.38     | 0.62 |
| В       | 114         | 74     | 67        | 1.13E+07    | 2.52E+05    | 1.39E+06    | 0.00E+00    | 0.00  | 0.37     | 0.63 |

#### **Summary**



- Results from an analysis of the cold-side film layer of the NASA reference concept JWST sunshield were used to demonstrate a thermal-structural analysis approach and provide insight into the response of the membrane to thermo-mechanical loading.
- For the problem considered, the film was shown to develop slack regions when subject to a large in-plane temperature gradient. Subsequent analyses showed that the slack region could be eliminated by increasing the magnitude of the mechanical preload by a factor of four.
- These studies demonstrate the importance of including thermal effects in thin-film membrane structural analyses when significant temperature variations are expected within the structure.
- Topics for future study include: thermal model refinement, temperaturedependent material properties, mismatches in coefficient of thermal expansion, and additional approaches to film tensioning.