

Chapter 9

stability problems

**Equations given:**

$$\begin{aligned}
 v &= \frac{\Delta x}{\Delta t} & a &= \frac{\Delta v}{\Delta t} & x_f &= x_0 + v_0 t + \frac{1}{2} a t^2 & v_f &= v_0 + a t & v_f^2 - v_0^2 &= 2 a (x_f - x_0) & x_f - x_0 &= \frac{1}{2} (v_f + v_0) t & x_f &= x_0 + v_f t - \frac{1}{2} a t^2 \\
 \theta_f &= \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2 & \theta_f &= \theta_0 + \omega_f t - \frac{1}{2} \alpha t^2 & \omega_f &= \omega_0 + \alpha t & \omega_f^2 - \omega_0^2 &= 2 \alpha (\theta_f - \theta_0) & \theta_f - \theta_0 &= \frac{1}{2} (\omega_f + \omega_0) t & x &= x_{\tan} = \theta r \\
 v &= v_{\tan} = \omega r & a_{\tan} &= \alpha r & a_c &= \omega^2 r = \frac{v^2}{r} & \sum \mathbf{F} &= m \mathbf{a} & F_g &= G \frac{M m}{r^2} & G &= 6.673 \times 10^{-11} \frac{\text{N m}^2}{\text{kg}^2} & \tau &= I \alpha & \tau &= r F_{\perp} \\
 I_{\text{other}} &= I_{\text{CM}} + m d^2 & I_{\text{rod length } l \text{ with axis through end}} &= (1/3) m l^2 & I_{\text{rod length } l, \text{ axis through middle}} &= (1/12) m l^2 & I_{\text{rectangle thru center}} &= (1/12) m (a^2 + b^2) \\
 I_{\text{rectangle about edge b}} &= (1/3) m a^2 & I_{\text{disk or cylinder}} &= (1/2) m r^2 & I_{\text{ring or hoop}} &= m r^2 & I_{\text{thick-walled hoop or cylinder}} &= (1/2) m (r_1^2 + r_2^2)
 \end{aligned}$$