6) Find f'(x) where $f(x) = \sin(5x^2 - 3)$ g(x) will be sin(h(x)) and h(x) will be $(5x^2-3)$ $g'(h(x)) = \cos(5x^2-3)$ h'(x) = 10x $f'(x) = g'(h(x)) \bullet h'(x)$ $f(x) = 10 x \cos(5 x^2 - 3)$ <-- solution 7) find f'(x) where $f(x) = \sqrt{\cos 4x - 2x}$ $g(x) = \sqrt{x}$ $h(x) = \cos 4 x - 2x$ $g'(h(x)) = \frac{1}{2\sqrt{\cos 4x - 2x}}$ $h'(x) = -4 \sin 4x - 2$ $f'(x) = g'(h(x)) \bullet h'(x) = \frac{1}{2\sqrt{\cos 4x - 2x}} \times (-4\sin 4x - 2) = \frac{-4\sin 4x - 7}{7\sqrt{\cos 4x - 7x}} <--$ solution 8) $f(x) = \ln 2x$ $f'(x) = g'(h(x)) \bullet h'(x)$ $g(x) = \ln x$ h(x) = 2xg'(x) = 1/xh'(x) = 2g'(h(x)) = 1/(2x) $f'(x) = g'(h(x)) \bullet h'(x) = 1/(2x) \bullet 2 = 2/(2x) = 1/x$ <--- solution

13)
$$y = (\circ x^{r} - r x)^{e^{x}}$$

In both sides:

$$\ln y = e^x \ln (5 x^2 - 7 x)$$

breaking this down for product and chaining rules:

$$g(x) = e^{x}$$

$$h(x) = k(u(x))$$

$$k(x) = \ln (x)$$

$$u(x) = (5 x^{2} - 2 x)$$

so we differentiate both sides (product rule first):

$$\frac{1}{y}\frac{dy}{dx} = g'(x)h(x) + h'(x)g(x)$$

now the chain rule on h'(x):

$$\frac{1}{y}\frac{dy}{dx} = g'(x)h(x) + k'(u(x))u'(x)g(x)$$

multiply both sides by y:

$$\frac{dy}{dx} = (g'(x)h(x) + k'(u(x))u'(x)g(x)) \times y$$

Now we differentiate:

$$g(x) = e^{x}$$

 $g'(x) = e^{x}$ -- easy enough

$$k(x) = ln (x)$$

k'(x) = 1/x -- also easy

$$u(x) = (5x^{2} - 2x)$$

u'(x) = (10x-2) -- simple (the power rule is my friend)

now we plug it all in:

from above so I don't have to keep scrolling up:

$$y = (5x^{2} - 2x)^{e^{x}}$$

h(x) = k(u(x)) = ln (5x² - 2x)
$$\frac{dy}{dx} = (g'(x)h(x) + k'(u(x))u'(x)g(x)) \times y$$

$$\frac{dy}{dx} = (e^x \times \ln(5x^2 - 2x) + \frac{1}{5x^2 - 2x} \times (10x - 2) \times e^x) \times (5x^2 - 2x)^{e^x}$$

Which is the solution. To move it to look like the answer on the test, we rearrange to put y in front, flip the addition, and combine 1/u(x) and (u'(x) times g(x)):

$$\frac{dy}{dx} = (\circ x^{\tau} - \tau x)^{e^{x}} \times (\frac{e^{x}(\tau - \tau)}{\circ x^{\tau} - \tau_{X}} + e^{x} \times \ln(\circ x^{\tau} - \tau x))$$

finally (phew) we pull out e^x as a common factor and put it in front, getting the same solution as A on the quiz:

$$\frac{dy}{dx} = e^x (5x^2 - 2x)^{e^x} (\frac{10x - 2}{5x^2 - 2x} + \ln(5x^2 - 2x))$$