## [2] Lemma Two: differentiating quantize $_k(r_{i_\ell})$ yields 1 under condition of Expectation of a Straight-Through Estimator.

Chromium OSX

https://github.com/ppwwyyxx/tensorpack/issues/31#issuecomment-254919972

- (1) Given quantize<sub>k</sub>( $r_{i_l}$ ) = (1 / (2<sup>k</sup>-1)) \* round((2<sup>k</sup> 1) $r_{i_l}$ ).
- (2) Consider ~quantize<sub>k</sub> $(r_{i_r}) = (1/(2^k-1)) * ((2^k-1)r_{i_r}) = r_{i_r}$ .
- (3)  $\sim$ quantize $'_k(r_{i_i}) = 1$ .
- (4) Observation: in the absence of a *round()* function the two scale factors cancel and the derivative is 1. Can we make the *round()* function "disappear" in some justified fashion?
- (5) Note that the  $round(r_{i_\ell})$  function adds some number  $n \in [-0.5, 0.5]$  to  $r_{i_\ell}$  to round  $r_{i_\ell}$  to the nearest integer
- (6) If n = 0, then quantize  $k(r_{i_\ell}) = quantize k(r_{i_\ell}) = 1$ .
- (7) if  $n \neq 0$ , then our outer scale factor of  $1/(2^k-1)$  is technically multiplying the result of  $(2^k-1)(r_{i_\ell}+n)$ , and thus the scale factors do not cancel.
- (8) Note that the probability of  $n \neq 0$  is low, and so any individual call to quantize<sub>k</sub>() is unlikely to result in a case where we can ignore the round() function.
- (8) However, under assumption that n is drawn uniformly and at random from [-0.5, 0.5], the expectation E(n) = 0.
- (9) \*:. under expectation E(n) = 0, quantize  $k'(r_i) = -quantize k'(r_i) = 1.**$

## [2] Lemma Two: differentiating quantize $_k(r_{i_\ell})$ yields 1 under condition of Expectation of a Straight-Through Estimator. Firefox 49.0.2 OSX

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- (1) Given quantize<sub>k</sub>( $r_{i}$ ) = (1 / (2<sup>k</sup>-1)) \* round((2<sup>k</sup> 1) $r_{i}$ ).
- (2) Consider ~quantize<sub>k</sub> $(r_{i_r}) = (1/(2^k-1)) * ((2^k-1)r_{i_r}) = r_{i_r}$ .
- (3)  $\sim$ quantize $'_k(r_{i,}) = 1$ .
- (4) Observation: in the absence of a *round()* function the two scale factors cancel and the derivative is 1. Can we make the *round()* function "disappear" in some justified fashion?
- (5) Note that the  $round(r_{i_\ell})$  function adds some number  $n \in [-0.5, 0.5]$  to  $r_{i_\ell}$  to round  $r_{i_\ell}$  to the nearest integer.
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- (8) Note that the probability of  $n \ne 0$  is low, and so any individual call to quantize<sub>k</sub>() is unlikely to result in a case where we can ignore the round() function.
- (8) However, under assumption that n is drawn uniformly and at random from [-0.5, 0.5], the expectation (n) = 0.
- (9) \*:. under expectation (n) = 0, quantize  $(r_i) = \text{-quantize}(r_i) = 1.**$