#### Models and Algorithms for Genome Rearrangement with Positional Constraints

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# Genome Rearrangements





# Consequences of Rearrangements

- Role in speciation
  - reproductive isolation
- Gene regulation
  - aberrant proteins
  - positional effects
- Disease
  - many cancers
  - hemophilia A
  - etc.





### Phylogeny Reconstruction (~1930)



#### Rearrangement Scenario



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What is the distance between genome A and genome B?



- Pair-wise rearrangement distances
  - species tree reconstruction
  - gene homology inference
- Ancestral Reconstruction

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#### Reconstructing the Genomic Architecture of Ancestral Mammals: Lessons From Human, Mouse, and Rat Genomes

Guillaume Bourque,<sup>1</sup> Pavel A. Pevzner,<sup>2</sup> and Glenn Tesler<sup>3,4</sup> <sup>1</sup>Centre de Recherches Mathématiques, Université de Montréal, Canada H3C 3/7; <sup>2</sup>Department of Computer Science and Engineering and <sup>3</sup>Department of Mathematics, University of California–San Diego, La Jolla, California 92093, USA

#### Genome Research 2004

#### Chicken Special/Letter

#### Comparative architectures of mammalian and chicken genomes reveal highly variable rates of genomic rearrangements across different lineages

Guillaume Bourque,<sup>1,5</sup> Evgeny M. Zdobnov,<sup>2</sup> Peer Bork,<sup>2</sup> Pavel A. Pevzner,<sup>3</sup> and Glenn Tesler<sup>4</sup>

<sup>1</sup>Genome Institute of Singapore, Singapore 138672, Republic of Singapore; <sup>2</sup>European Molecular Biology Laboratory, 69117



#### Resource-

#### Breakpoint graphs and ancestral genome reconstructions

Max A. Alekseyev and Pavel A. Pevzner<sup>1</sup>

Department of Computer Science and Engineering, University of California at San Diego, La Jolla, California 92093-0404, USA

Recently completed whole-genome sequencing projects marked the transition from gene-based phylogenetic studies to phylogenomics analysis of entire genomes. We developed an algorithm MCRA for reconstructing networking genomes and used it to study the reconstructing the rest of genome the rest of ge

Genome Research 2007

"Initial sequencing and comparative analysis of the mouse genome"

- Nature 2002

"Genome sequence of the Brown Norway rat yields insights into mammalian evolution"

- Nature 2004

"Sequence and comparative analysis of the chicken genome provide unique perspectives on vertebrate evolution"

- Nature 2004

#### Conclusions:

- X chromosomes are scrambled in rodents but not humans (since common ancestor)
  - human X is the ancestral order
- rodent gene orders evolve faster (3x) than human and chicken lineages
- breakpoint reuse
- few translocations between human and chicken



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all based solely on parsimony

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#### Addressing Limitations

- Limitation based on parsimony
  - uncertainty due to the LARGE search space
- Solution:

introduce biological constraints



#### Hypothesis:

# Rearrangement breakpoints are spatially close.

Véron, Lemaitre, Gautier, Lacroix and Sagot "Close 3D proximity of evolutionary breakpoints argues for the notion of spatial synteny"

#### A "Local" Translocation



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#### Hi-C Heatmaps

Each entry is proportional to spacial proximity.









#### Numerous scenarios between two genomes

#### - parsimonious



Numerous scenarios between two genomes

– parsimonious / non-parsimonious



Numerous scenarios between two genomes

- parsimonious / non-parsimonious
- spatially local















# Sample from Chr 3



# Sample from Chr 3



#### Sample from 1 vs. 3



#### Sample from 1 vs. 3





#### Human-Mouse Scenarios are Local



### Sampling Scenarios

10,000 parsimonious scenario

- average over true breakpoints
- average over randomized breakpoints





### Sampling Scenarios



- average over true breakpoints
- average over randomized breakpoints

Chr 14




- average over true breakpoints
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- average over true breakpoints
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# Sample from Chr 3



## Sample from 1 vs. 3





## Human-Mouse Scenarios are Local



## Human-Mouse Scenarios are Local



- Evolutionarily conserved rearrangements are local
- Pattern exists despite only using human Hi-C



#### Question:

How do we find scenarios that are spatially close?

- IF 1 cut: create two telomeric adjacencies
- IF 2 cut: glue back 1 of 2 new ways

#### Cut 1 or 2 adjacencies

- IF 1 cut: create two telomeric adjacencies
- IF 2 cut: glue back 1 of 2 new ways

# G1: • 1 2 3 • • 4 5 6 • G2: • 1 2 3 4 5 6 •

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How do we find rearrangements?



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 $- d_{DCJ} (G1, G2) = N - (C + I/2)$ 



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## DCJ Moves





$$d_{DCJ}(G1, G2) = N - (C + I/2)$$

## Shorthand



# All DCJ Scenarios

- even path
  - extract cycle
  - path fission
- odd path
  - extract cycle
- 2 even paths

- cycle
  - split cycle





 $\overline{\mathbf{d}}_{\mathrm{DCJ}}(\mathrm{G1},\mathrm{G2}) = \mathbf{N} - (\mathbf{C} + \mathbf{I}/2)$ 

## Local DCJ





## Local DCJ





## Hi-C Heatmaps

Heatmaps define a locality constraint.

- transitivity appears to hold



# Non-locality

- Two problems...
  - INPUT: two genomes with colored adjacencies
  - OUTPUT 1: scenario with minimum # of non-local moves
  - OUTPUT 2:

a minimum length scenario, with a minimum # of non-local moves

# Non-locality

• Two problems...

INPUT: two genomes with colored adjacencies

- OUTPUT 1: NP-Hard scenario with minimum # of non-local moves

OUTPUT 2: a minimum length scenario, with a minimum # of non-local moves THIS PAPER Polynomial

- NP-Hardness
  - Max Eulerian Cycle Decomposition
    - INPUT: Eulerian graph G = (V, E)
    - OUTPUT: partition of E into cycles
    - MEASURE: |E|



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- Max Eulerian Cycle Decomposition
  - INPUT:Eulerian graph G = (V, E)OUTPUT:partition of E into cyclesMEASURE:|E|
- O(n<sup>3</sup>) algorithm
  - Min Non-Crossing Colored Partition

INPUT:ordered set of colored elementsOUTPUT:non-crossing colored partitionMEASURE:cardinality of the partition





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crossing!

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### Minimize Distant Rearrangements

#### • NP-Hardness

- Max Eulerian Cycle Decomposition

INPUT:Eulerian graph G = (V, E)OUTPUT:partition of E into cyclesMEASURE:|E|

- O(n<sup>3</sup>) algorithm
  - Min Non-Crossing Colored Partition

INPUT: ordered set of colored elements

OUTPUT: non-crossing colored partition

MEASURE: cardinality of the partition

#### Minimize Distant Rearrangements

Generalization of Maximum Independent Set on a Circle Graph

Solved by Dynamic Programming

- O(n<sup>3</sup>) algorithm
  - Min Non-Crossing Colored Partition
    - INPUT: ordered set of colored elements
    - OUTPUT: non-crossing colored partition

MEASURE: cardinality of the partition



#### Sorting a Single Component





#### Sorting a Single Component



#### Sorting a Single Component



#### All DCJ Scenarios

• even path - extract cycle - path fission • odd path • cycle - extract cycle - split cycle 2 even paths  $\overline{\mathbf{d}}_{\mathrm{DCJ}}(\mathrm{G1},\mathrm{G2}) = \mathbf{N} - (\mathbf{C} + \mathbf{I}/2)$ 



## Running Time

- $O(n^3)$ 
  - Min Non-Crossing Colored Partition
- $O(N(W) N(M) n^3) \in O(n^5)$ 
  - Labeling edges in the bipartite graph

## Running Time

- $O(n^3)$ 
  - Min Non-Crossing Colored Partition
- $O(N(W) N(M) n^3) \in O(n^5)$



- Labeling edges in the bipartite graph
- In practice *N*(W) *N*(M) is small!
  - 182 for human/mouse comparison

#### Future Work

- 3/2 approx to minimize # of non-local moves
- Other models of evolution
  - inversions
  - inversions/transpositions
- General weights
  - NP-Hard to minimize # of non-local
  - ?minimize # of non-local moves in *parsimonious*?
- 2-sided version of the problem
- Generalize to multiple species



Kirkpatrick



#### Montpellier, France

#### Come to the mediterranean!



2 post-doc fellowships

## THE END



#### Cell Type Comparison - intra

<sup>g</sup> m <sub>O</sub>	gino6690n		ksezn hesc		کر	imrgo helazsi		a25FA	FA HSGZMA		1	helaM		hrm h		elaNS		hrens		
gm06690n	6.9	99	6.08	-1.20	4.48	4.53	5.23	4.57	6.85	1.74	5.93	0.66	6.01	1.54	7.78	2.90	2.98	2.05	3.42	2.25
k562n	6.08	-1.20	5.	29	3.44	1.76	3.91	1.71	4.92	0.56	4.25	0.21	4.02	0.51	4.28	2.47	2.74	-0.59	2.69	0.14
hesc	4.48	4.53	3.44	1.76	2.	89	3.66	0.30	5.02	0.52	3.30	0.50	2.49	2.86	5.24	2.95	1.28	-0.03	2.07	-0.93
imr90	5.23	4.57	3.91	1.71	3.66	0.30	4.30 5.77 0.		0.28	4.18	-0.44	3.54	1.59	6.30	1.71	2.25	-0.34	3.13	-1.35	
hela25FA	6.85	1.74	4.92	0.56	5.02	0.52	5.77	0.28	6.	36	5.79	0.12	5.23	1.79	8.35	0.28	2.30	4.13	3.64	1.00
k562M	5.93	0.66	4.25	0.21	3.30	0.50	4.18	-0.44	5.79	0.12	4.	47	4.45	0.24	5.82	2.69	2.38	-0.43	2.70	0.08
helaM	6.01	1.54	4.02	0.51	2.49	2.86	3.54	1.59	5.23	1.79	4.45	0.24	5.	13	6.16	3.52	1.54	1.64	2.05	1.81
hffM	7.78	2.90	4.28	2.47	5.24	2.95	6.30	1.71		0.28	5.82	2.69	6.16 3.52		10.40		3.04	2.85	3.93	2.82
helaNS	2.98	2.05	2.74	-0.59	1.28	-0.03	2.25	-0.34	2.30	4.13	2.38	-0.43	1.54	1.64	3.04	2.85	0.:	29	0.65	-0.12
hffNS	3.42	2.25	2.69	0.14	2.07	-0.93	3.13	-1.35	3.64	1.00	2.70	0.08	2.05	1.81	3.93	2.82	0.65	-0.12	1.	15



3.13

3.64

2.70

2.05

3.93

0.65

-1.35

1.00

0.08

1.81

2.82

-0.12

1.15

#### Cell Type Comparison - intra

0.					intersection											fere	nce			
SUUS	DEEgOr	)	4562r	,	hes	کر	imrgo	nel D	a25FA		fs. M		helal	4	hren	5	elaNs		MANS	
gm06690n	6.9	99	6.08	-1.20	4.48	4.53	5.23	4.57	6.85	1.74	5.93	0.66	6.01	1.54	7.78	2.90	2.98	2.05	3.42	2.25
k562n	6.08	-1.20	5.	29	3.44	1.76	3.91	1.71	4.92	0.56	4.25	0.21	4.02	0.51	4.28	2.47	2.74	-0.59	2.69	0.14
hesc	4.48	4.53	3.44	1.76	2.	89	3.66	0.30	5.02	0.52	3.30	0.50	2.49	2.86	5.24	2.95	1.28	-0.03	2.07	-0.93
imr90	5.23	4.57	3.91	1.71	3.66	0.30	4.30		5.77	0.28	4.18	-0.44	3.54	1.59		1.71	2.25	-0.34	3.13	-1.35
hela25FA	6.85	1.74	4.92	0.56	5.02	0.52	5.77	0.28	6.	36	5.79	0.12	5.23	1.79		0.28	2.30	4.13	3.64	1.00
k562M	5.93	0.66	4.25	0.21	3.30	0.50	4.18	-0.44		0.12	4.4	47	4.45	0.24		2.69	2.38	-0.43	2.70	0.08
helaM	6.01	1.54	4.02	0.51	2.49	2.86	3.54	1.59	5.23	1.79	4.45	0.24	5.	13		3.52	1.54	1.64	2.05	1.81
hffM	7.78	2.90	4.28	2.47	5.24	2.95		1.71		0.28	5.82	2.69		16 3.52 10.40		3.04	2.85	3.93	2.82	
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#### Cell Type Comparison - inter

9nnO66	<sup>9</sup> 0n	Å	562n	held	ALL	Ą	562M	1	helang		hitry	he	NaNS		hren's	
gm06690n	3.	39	2.85	-0.33	4.11	-0.71	4.94	-2.03	3.10	-1.17	-0.09	2.00	2.27	-0.09	2.83	1.04
k562n	2.85	-0.33	1.	1.64		-1.25	3.87	-2.46	2.44	-2.11	-1.36	2.66	1.32	-0.08	1.62	0.87
helaALL	4.11	-0.71	3.24	-1.25	4.	4.18		-3.57	3.79	-1.21	1.79	1.51	3.66	-0.47	4.18	-0.15
k562M	4.94	-2.03	3.87	-2.46	6.22	-3.57	4.	66	5.34	-2.74	3.75	-2.65	5.13	-3.30	5.44	-2.64
helaM	3.10	-1.17	2.44	-2.11	3.79	-1.21	5.34	-2.74	2.	62	1.35	-1.29	2.96	-2.56	3.09	-0.72
hffM	-0.09	2.00	-1.36	2.66	1.79	1.51	3.75	-2.65	1.35	-1.29	-0	.79	0.17	0.48	0.67	1.37
helaNS	2.27	-0.09	1.32	-0.08	3.66	-0.47	5.13	-3.30	2.96	-2.56	0.17	0.48	2.	18	2.27	0.38
hffNS	2.83	1.04	1.62	0.87	4.18	-0.15	5.44	-2.64	3.09	-0.72	0.67	1.37	2.27	0.38	3.	50



#### 1) crosslink



# crosslink ligate



crosslink
shear
ligate



crosslink
ligate

3) shear4) sequence

#### Cell Lines

- 3 different labs
- 10 different experiments
  - 3 metaphase cell lines
  - 6 types of cells

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We see significant similarities between all of them!

 $\rightarrow$  selection on breakpoints?

#### Directions

- Search for "local" scenarios.
- Use Mouse AND Human data.
- Place rearrangements on path to ancestor.



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