Models and Algorithms for Genome Rearrangement with Positional Constraints

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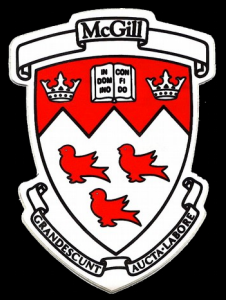
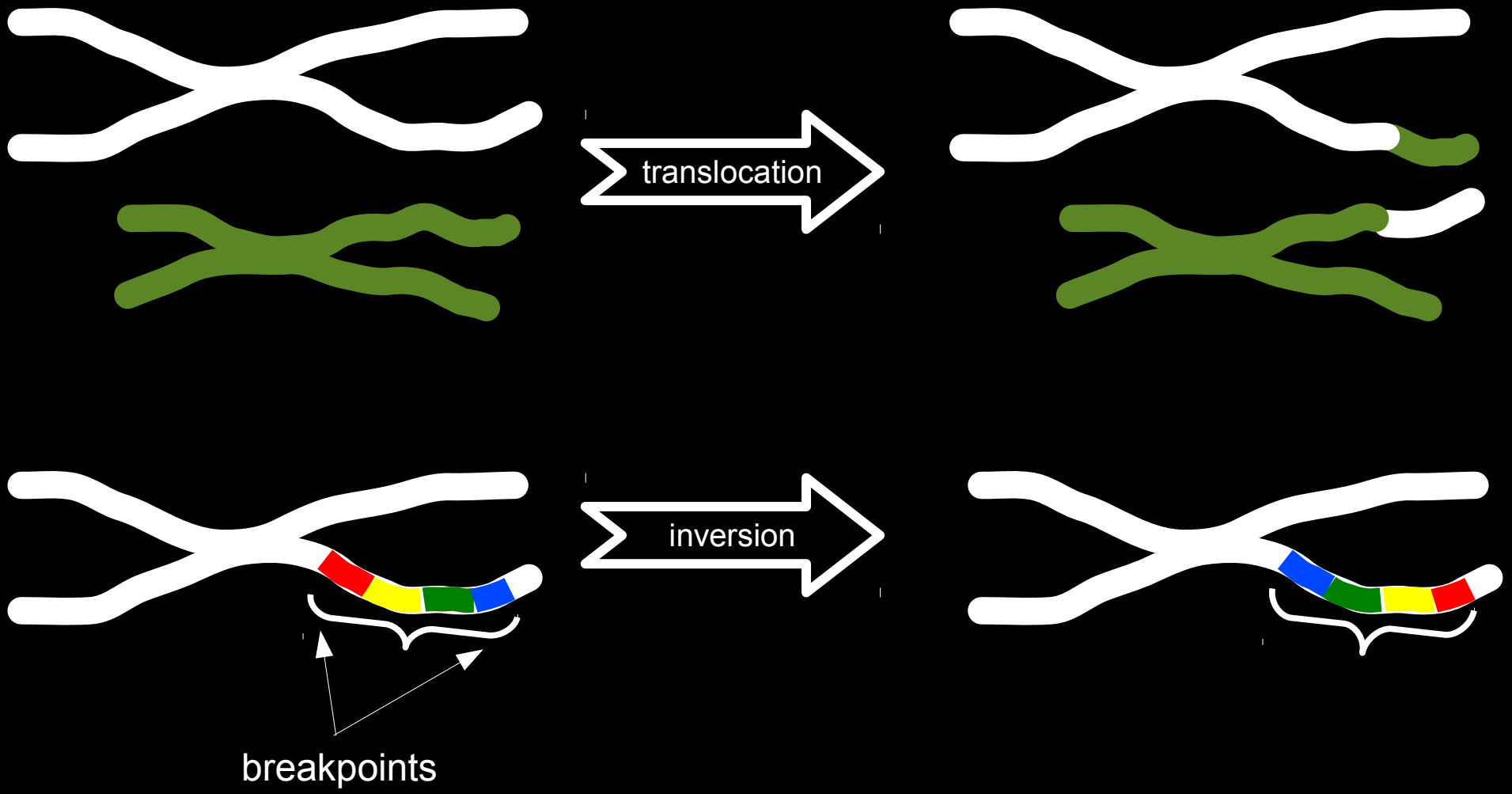
Montreal, Canada

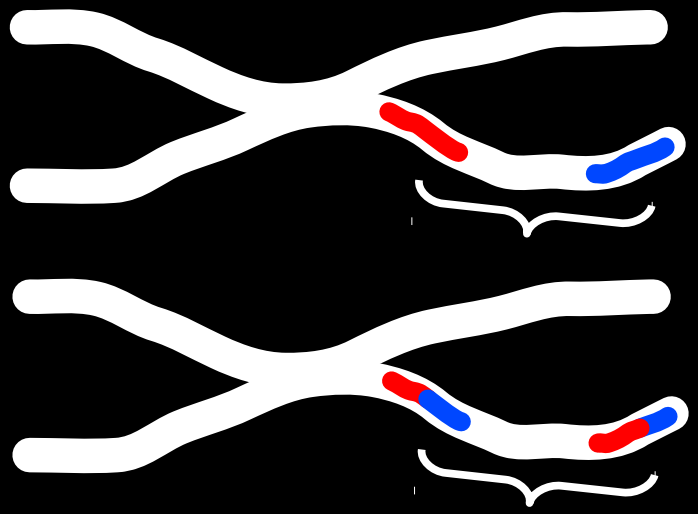


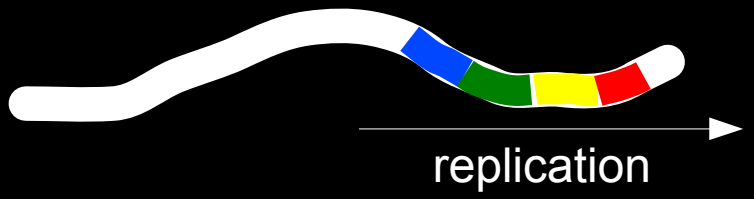
Genome Rearrangements



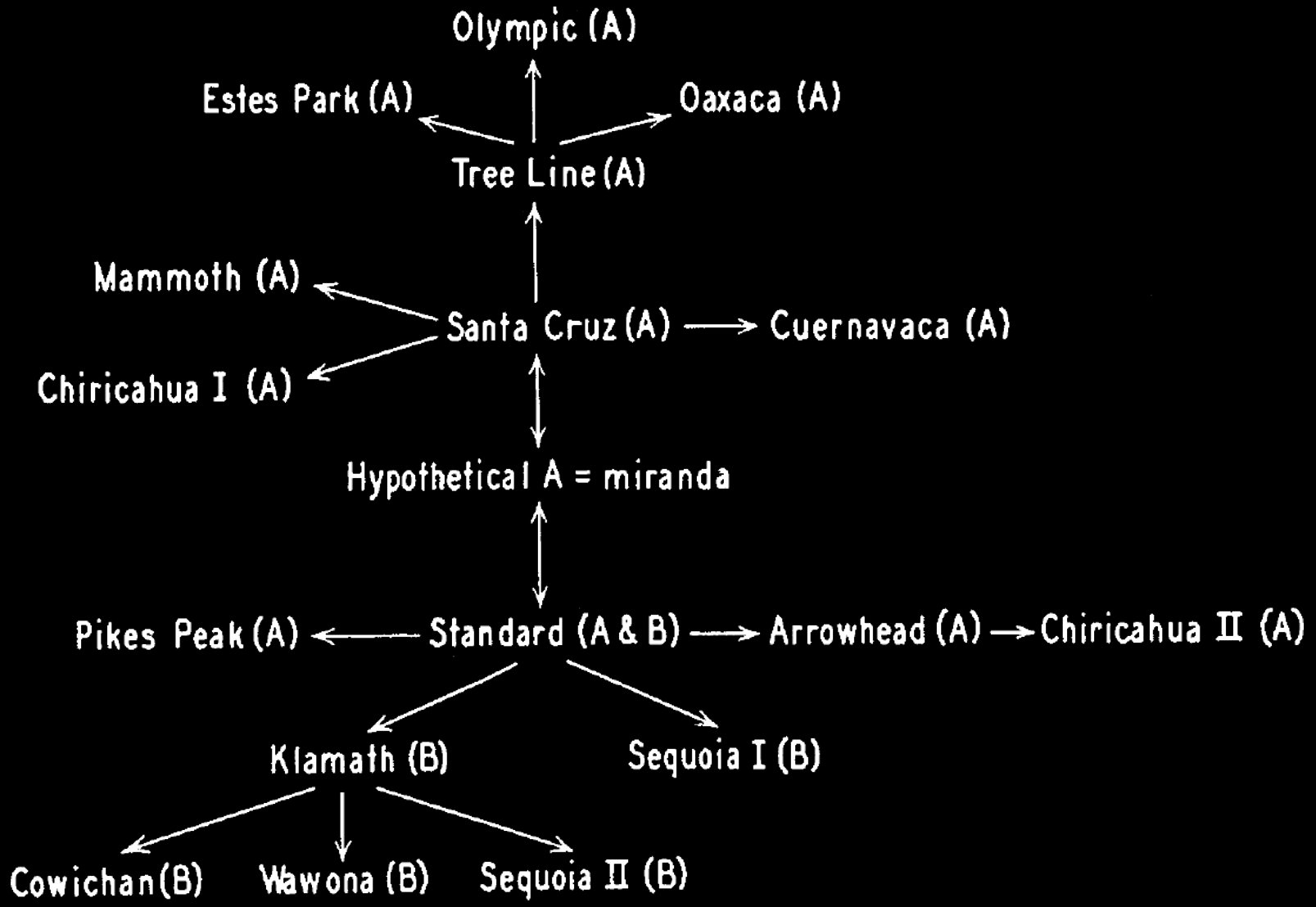
Consequences of Rearrangements

- Role in speciation
  - reproductive isolation
- Gene regulation
  - aberrant proteins
  - positional effects
- Disease
  - many cancers
  - hemophilia A
  - etc.

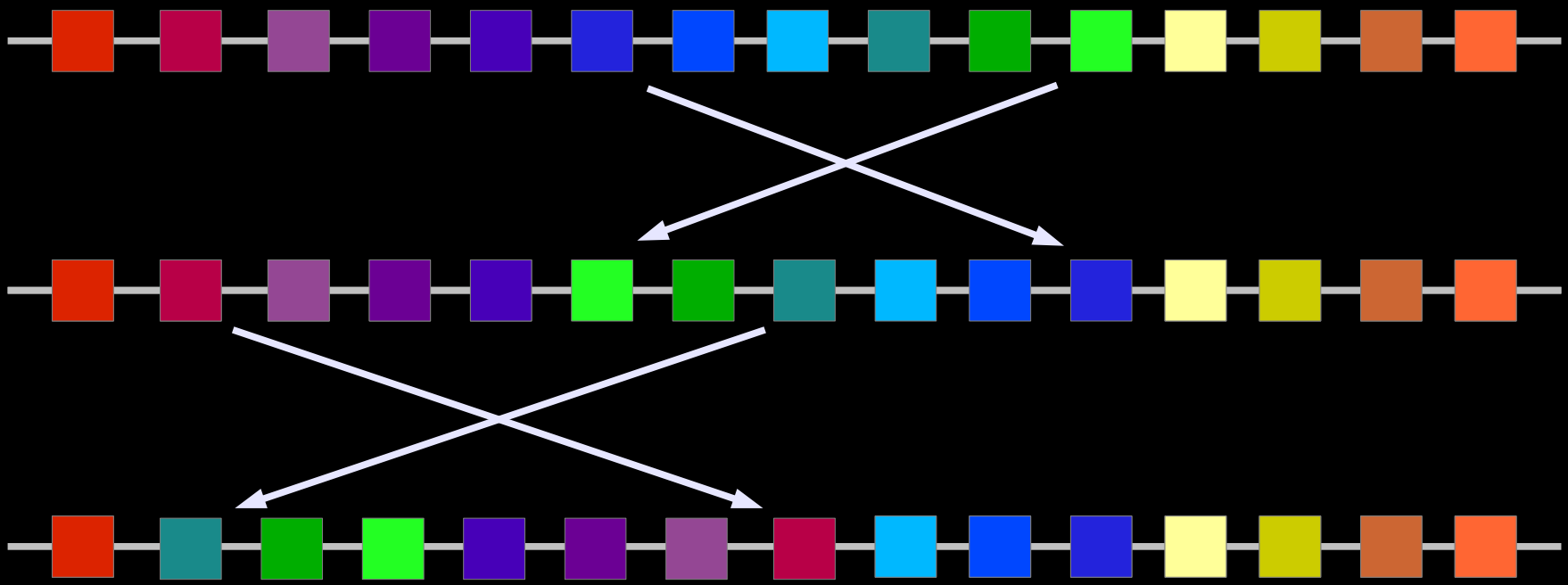




Phylogeny Reconstruction (~1930)

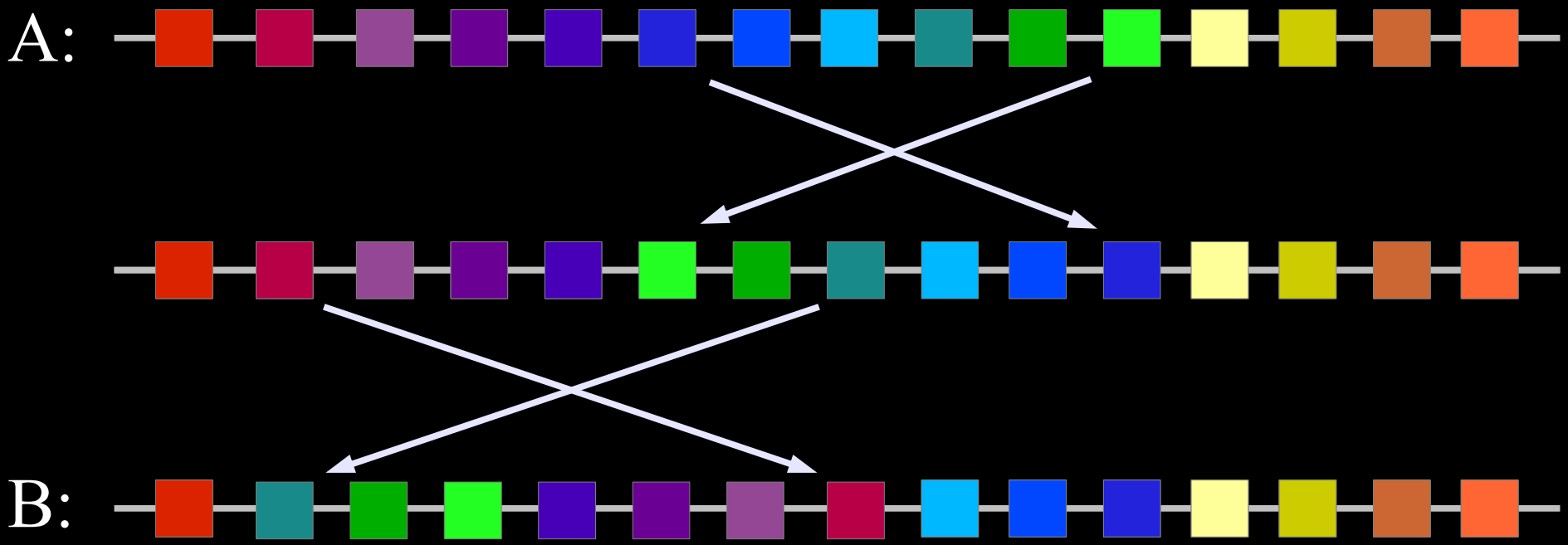


Rearrangement Scenario



Rearrangement Scenario

What is the distance between genome A and genome B?



Whole Genome Analysis

- Pair-wise rearrangement distances
  - species tree reconstruction
  - gene homology inference

- Ancestral Reconstruction

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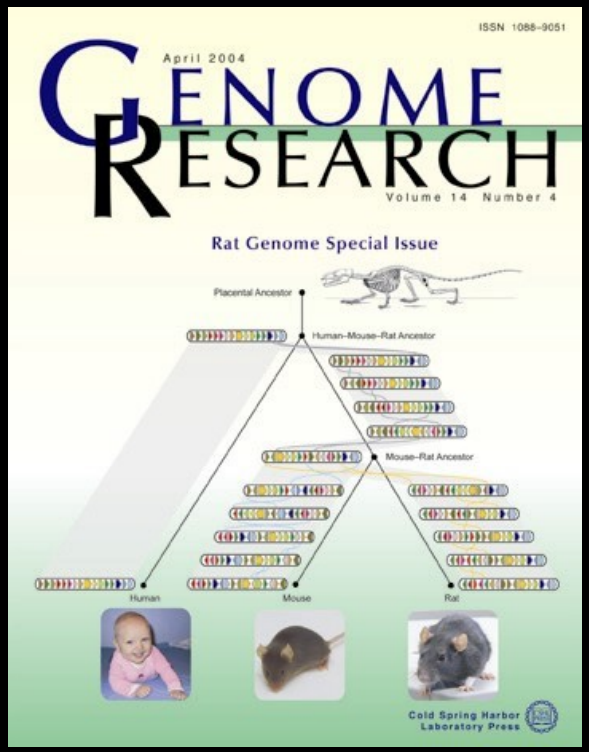

Article

Reconstructing the Genomic Architecture of Ancestral Mammals: Lessons From Human, Mouse, and Rat Genomes

Guillaume Bourque,[1] Pavel A. Pevzner,[2] and Glenn Tesler[3,4]

[1]Centre de Recherches Mathématiques, Université de Montréal, Canada H3C 3J7; [2]Department of Computer Science and Engineering and [3]Department of Mathematics, University of California–San Diego, La Jolla, California 92093, USA

Genome Research 2004

Chicken Special/Letter

Comparative architectures of mammalian and chicken genomes reveal highly variable rates of genomic rearrangements across different lineages

Guillaume Bourque,[1,5] Evgeny M. Zdobnov,[2] Peer Bork,[2] Pavel A. Pevzner,[3] and Glenn Tesler[4]

[1]Genome Institute of Singapore, Singapore 138672, Republic of Singapore; [2]European Molecular Biology Laboratory, 69117 Heidelberg, Germany; [3]Department of Computer Science and Engineering, [4]Department of Mathematics, University of California, San Diego, La Jolla, California 92093, USA

Genome Research 2007

Resource

Breakpoint graphs and ancestral genome reconstructions

Max A. Alekseyev and Pavel A. Pevzner[1]

Department of Computer Science and Engineering, University of California at San Diego, La Jolla, California 92093-0404, USA

Genome Research 2009

Whole Genome Analysis

"Initial sequencing and comparative analysis of the mouse genome"

- Nature 2002

"Genome sequence of the Brown Norway rat yields insights into mammalian evolution"

- Nature 2004

"Sequence and comparative analysis of the chicken genome provide unique perspectives on vertebrate evolution"

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Conclusions:

- X chromosomes are scrambled in rodents but not humans (since common ancestor)
  - human X is the ancestral order
- rodent gene orders evolve faster (3x) than human and chicken lineages
- breakpoint reuse
- few translocations between human and chicken

Whole Genome Analysis

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all based solely on parsimony

Conclusions:

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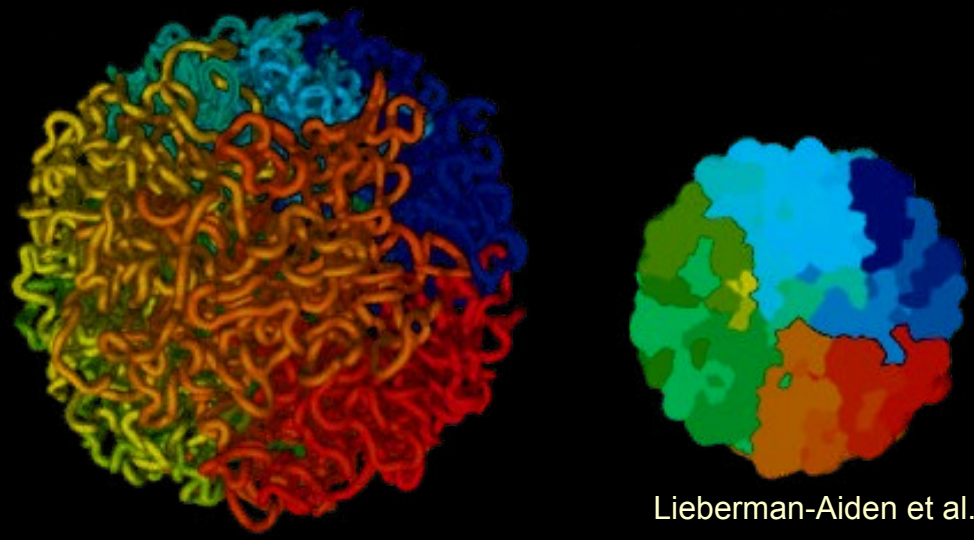
Addressing Limitations

- Limitation based on parsimony
  - uncertainty due to the LARGE search space

- Solution:

  introduce biological constraints



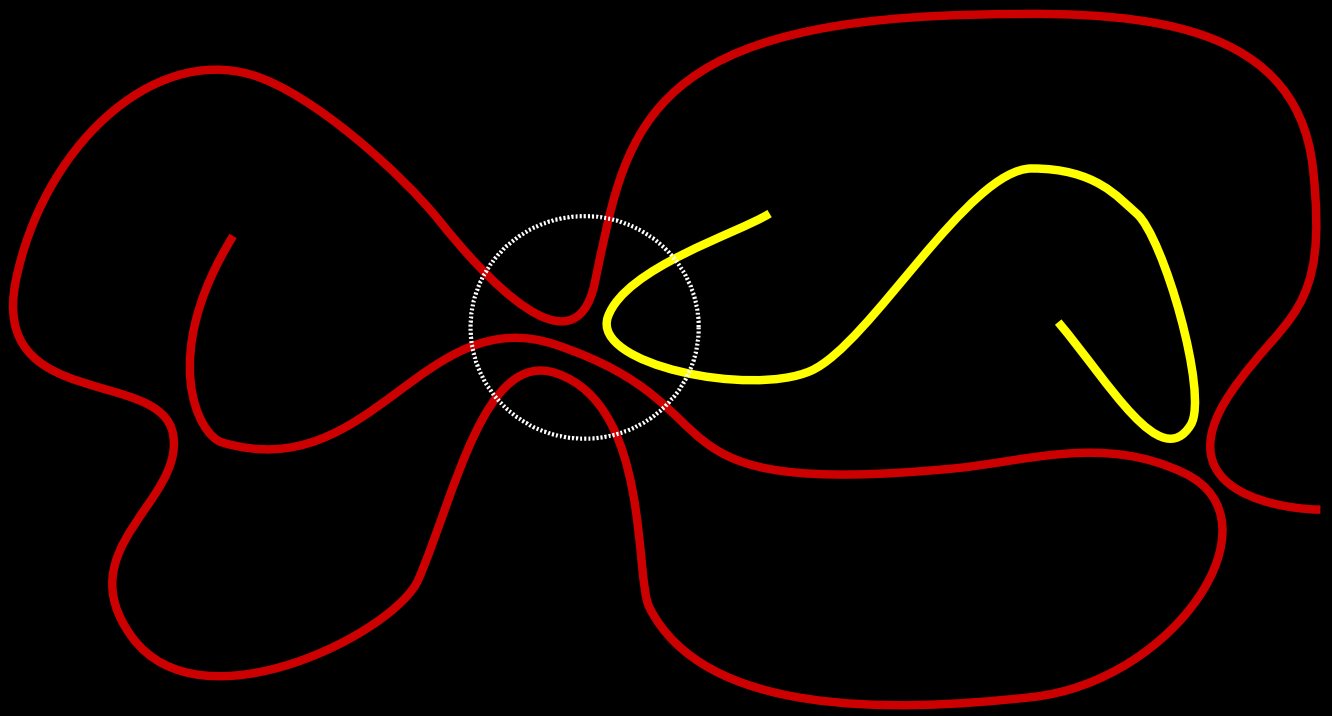
Lieberman-Aiden et al.

Hypothesis:

Rearrangement breakpoints are spatially close.

Véron, Lemaitre, Gautier, Lacroix and Sagot
"*Close 3D proximity of evolutionary breakpoints argues for the notion of spatial synteny*"

A “Local” Translocation



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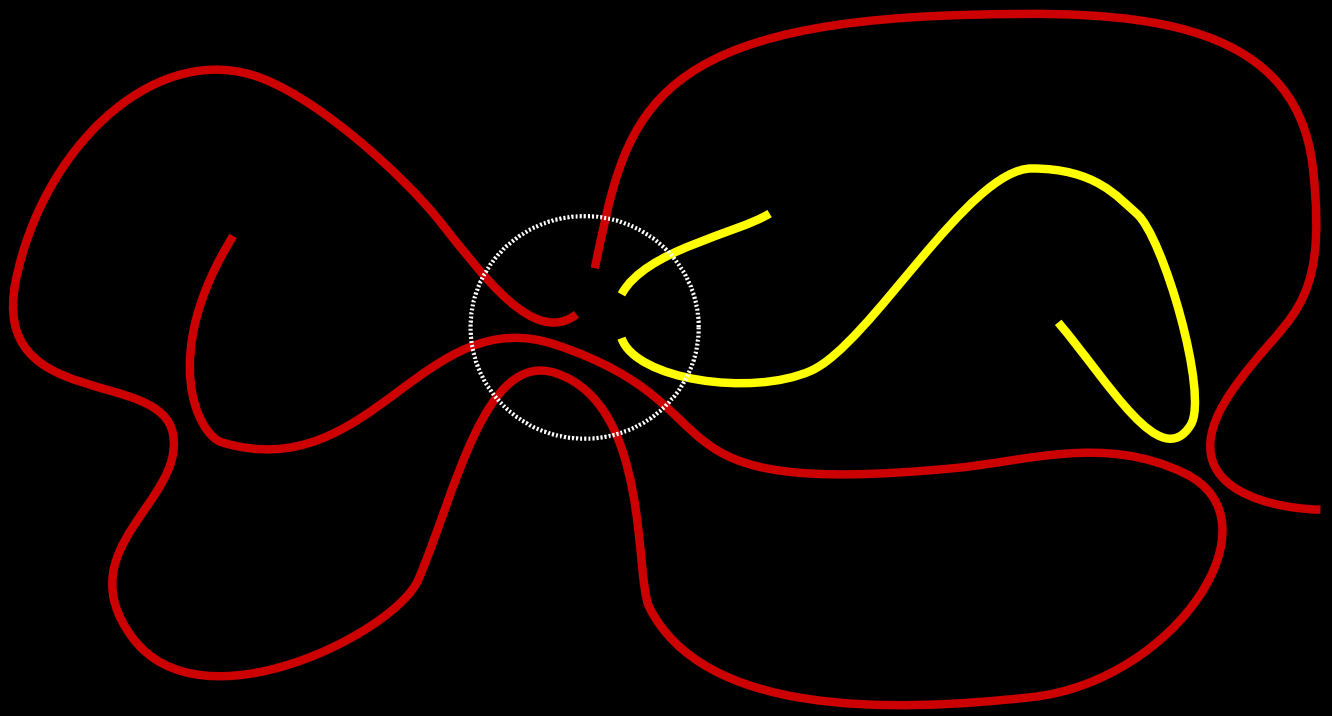

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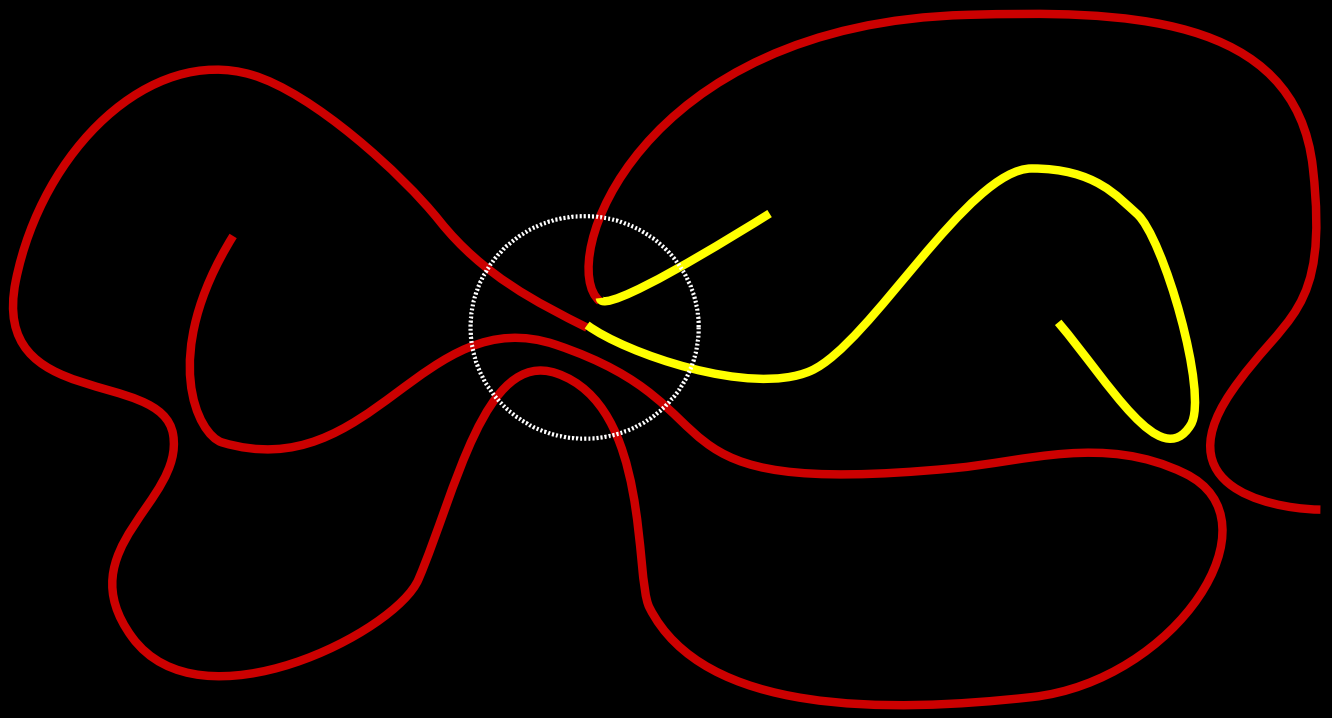
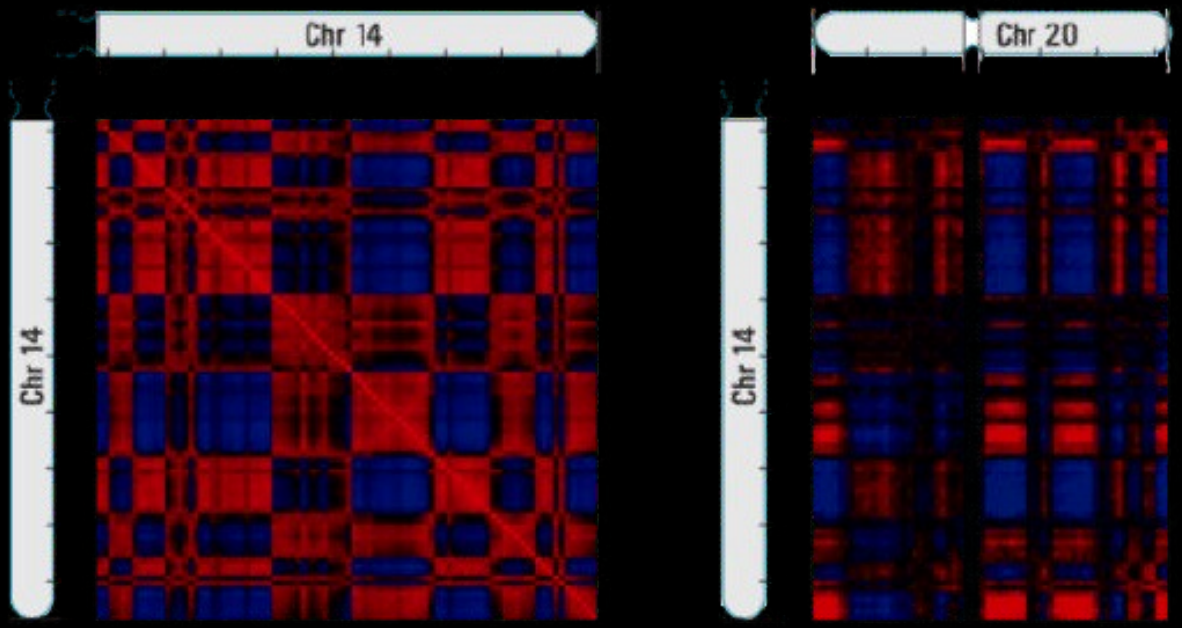
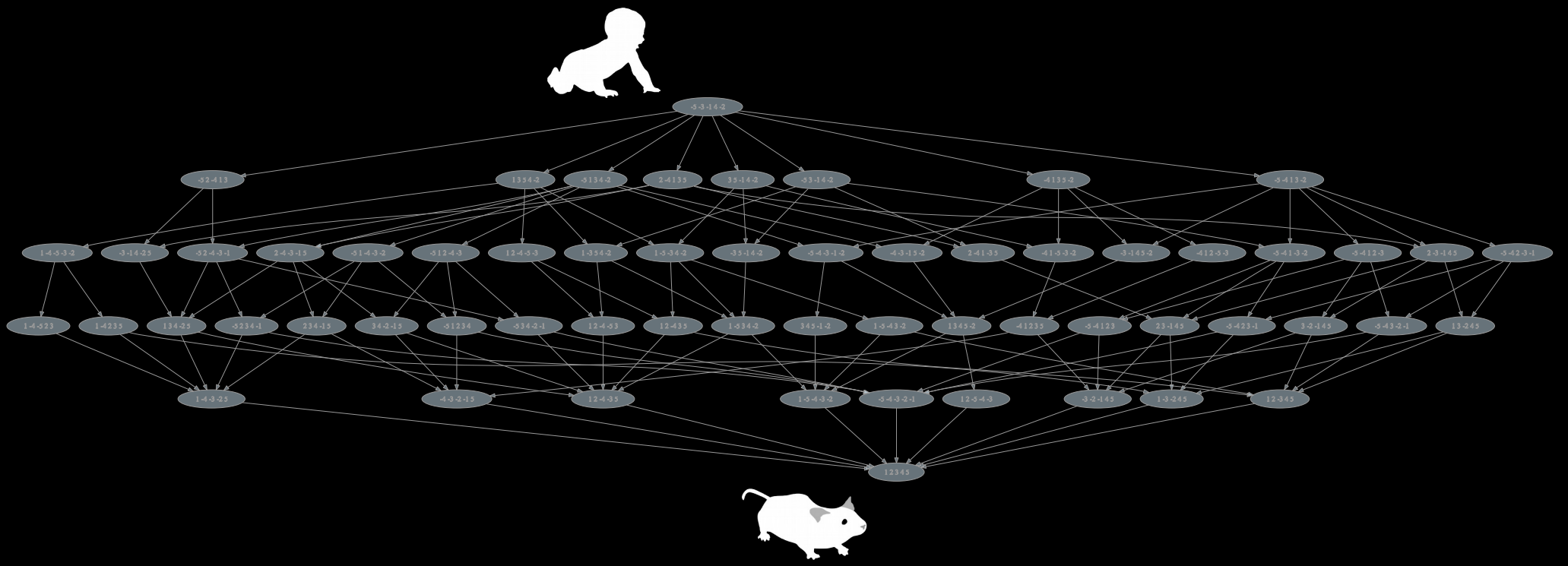


Hi-C Heatmaps

Each entry is proportional to spacial proximity.



Evolutionary Context



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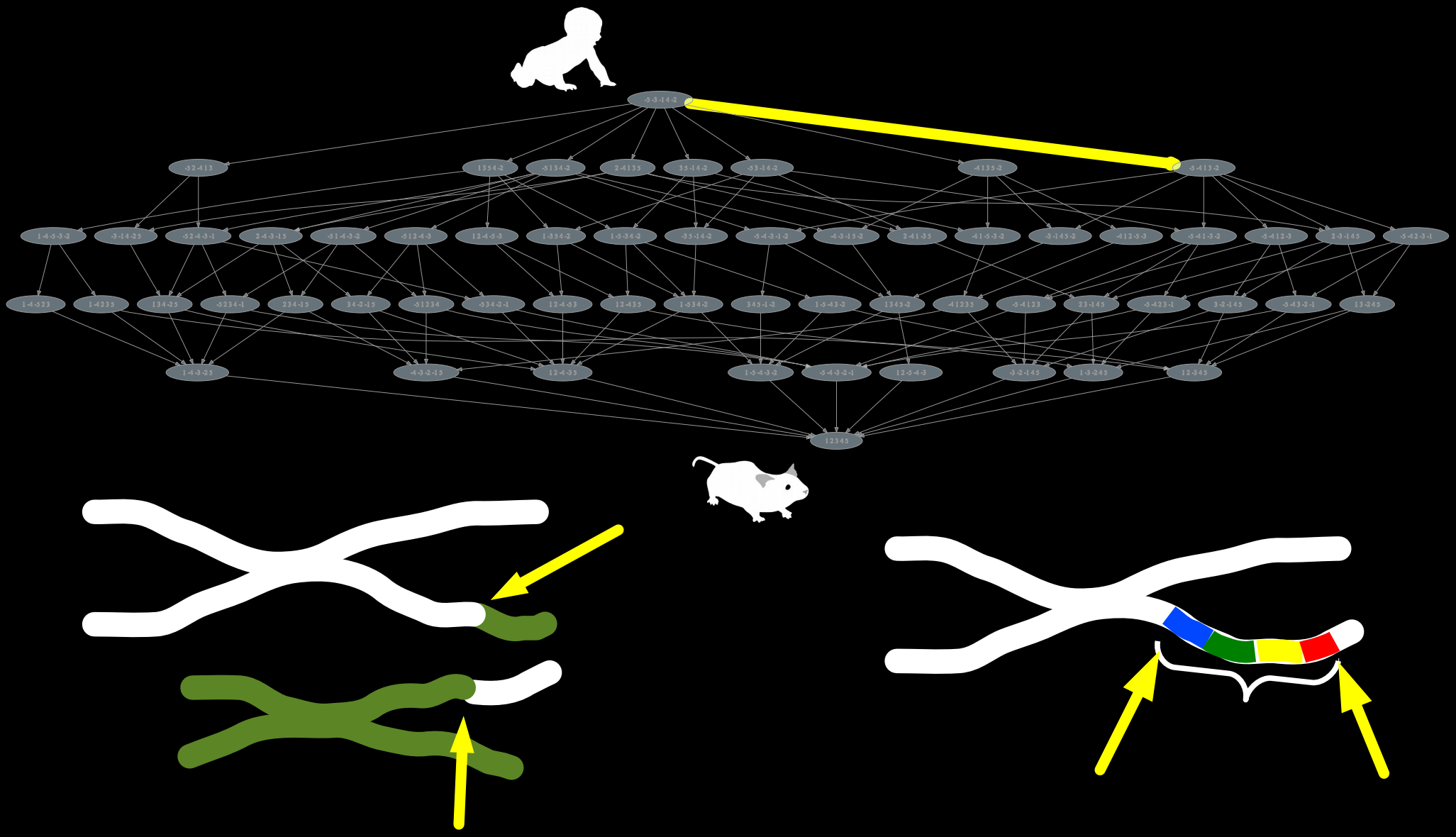

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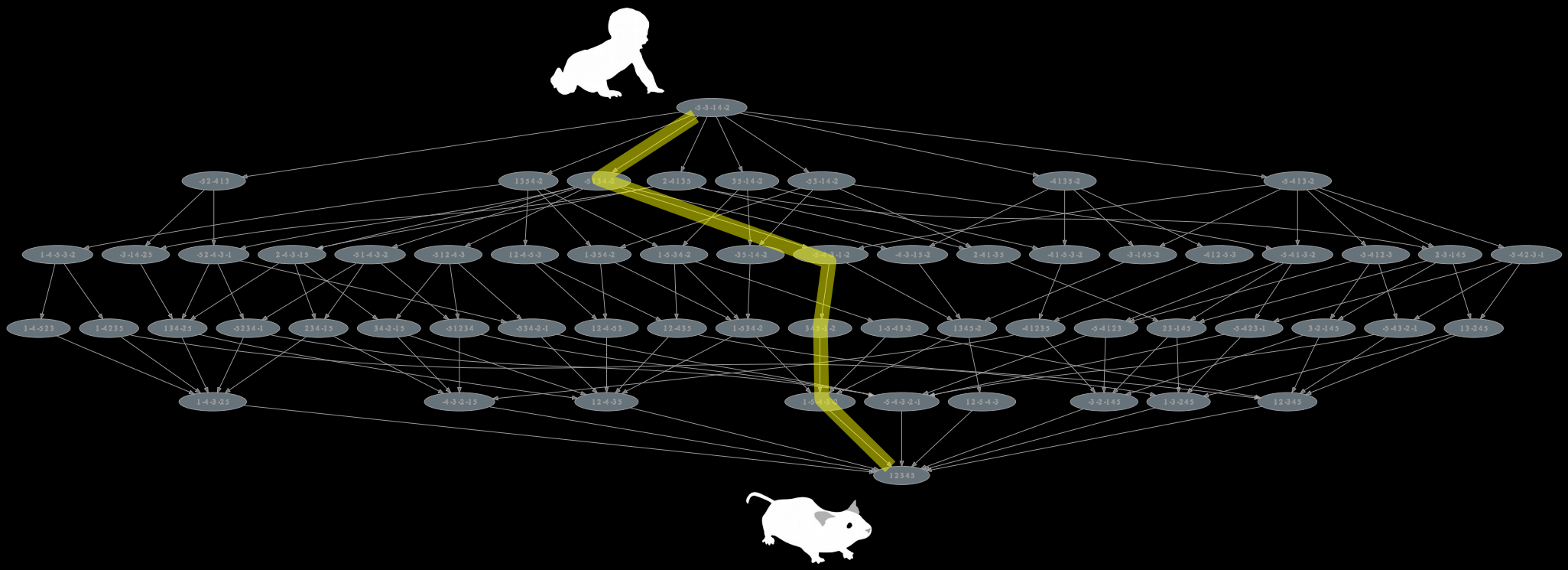

Numerous *scenarios* between two genomes

- parsimonious

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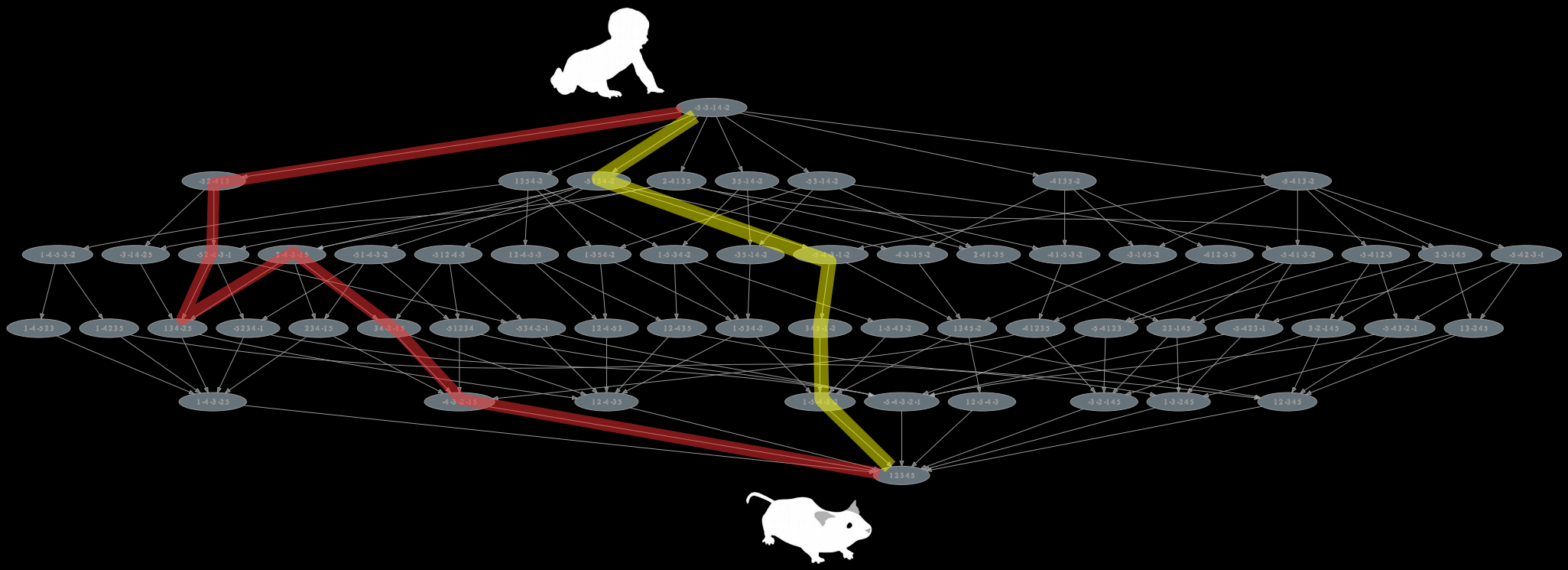

Numerous *scenarios* between two genomes

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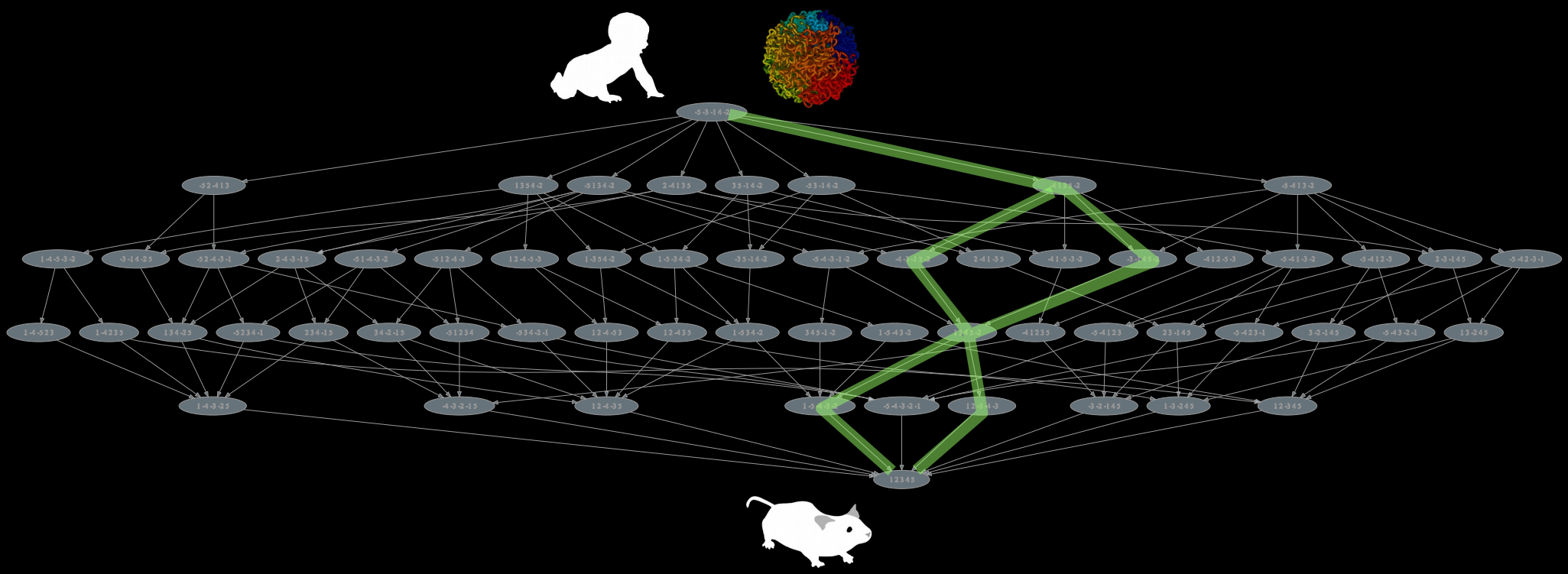
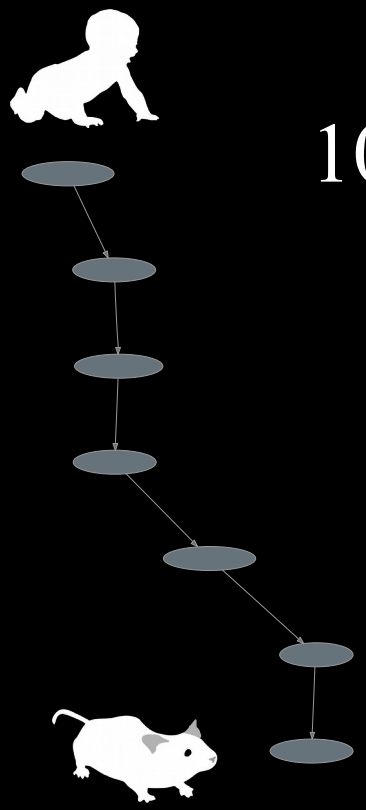


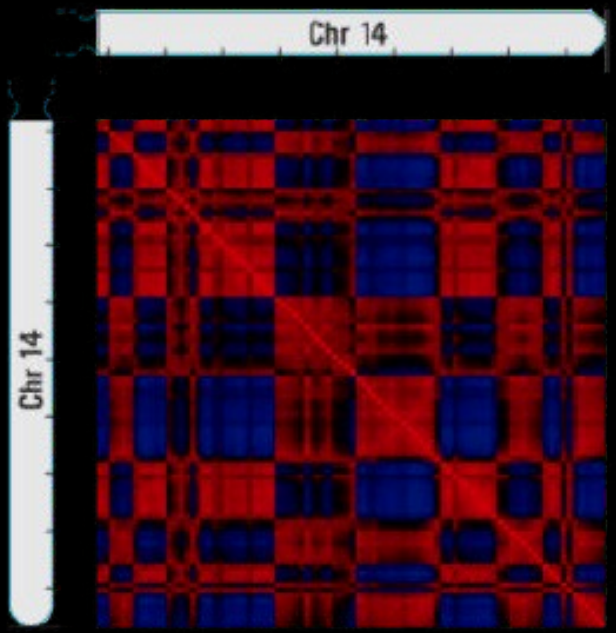
Numerous *scenarios* between two genomes

- parsimonious / non-parsimonious
- spatially local

Sampling Scenarios



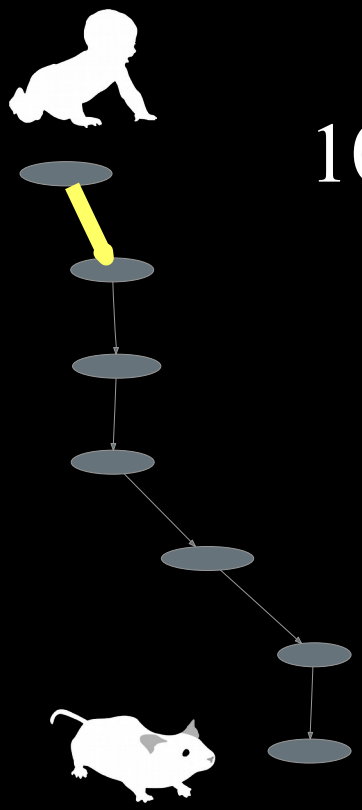
10,000 parsimonious scenario



Chr 14

Chr 15

Sampling Scenarios



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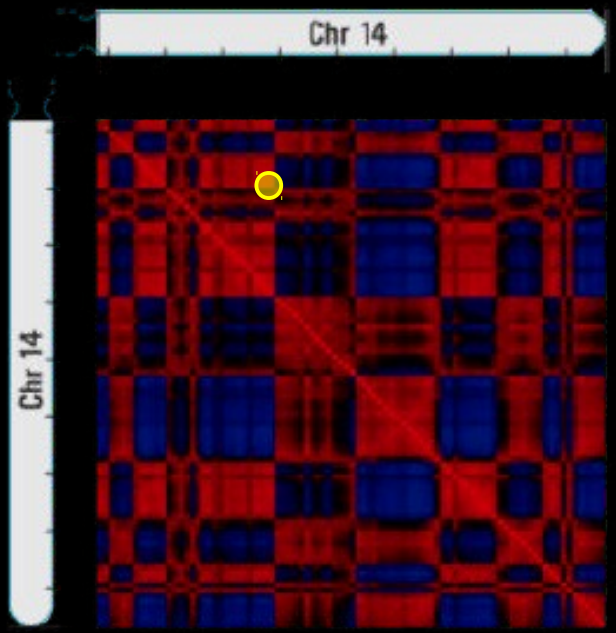

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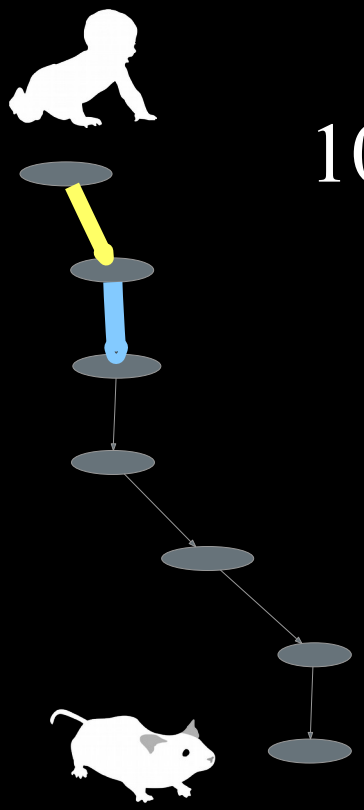

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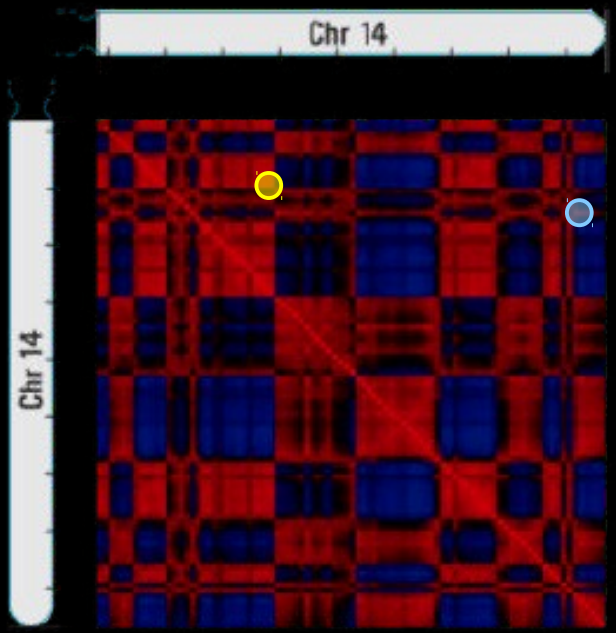

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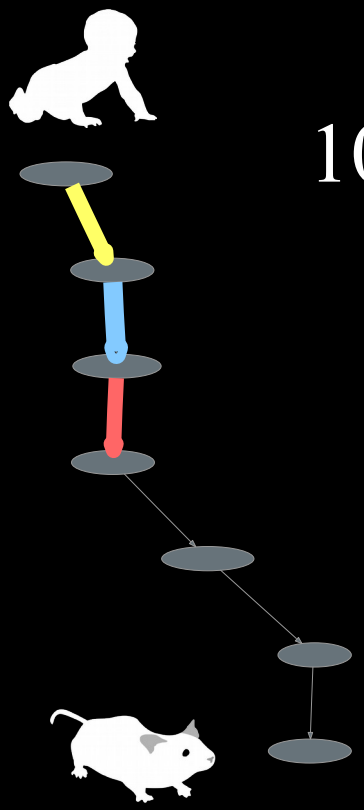

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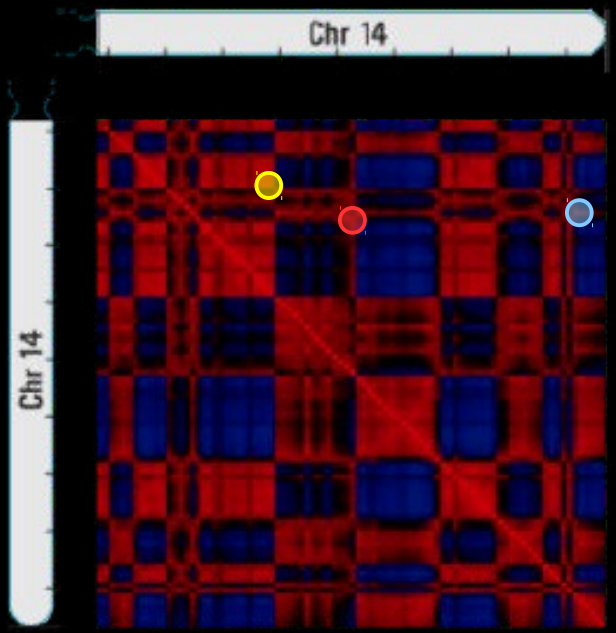

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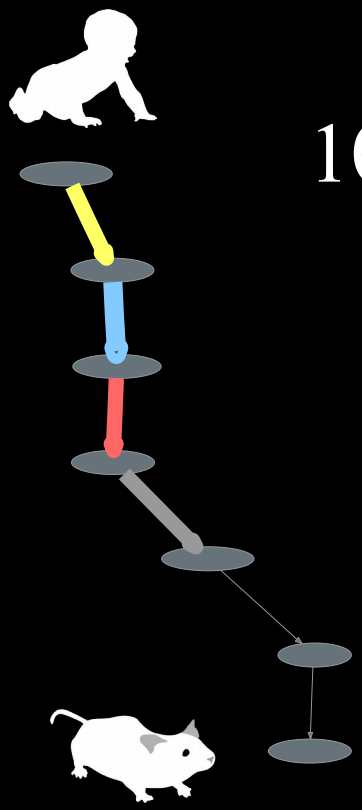

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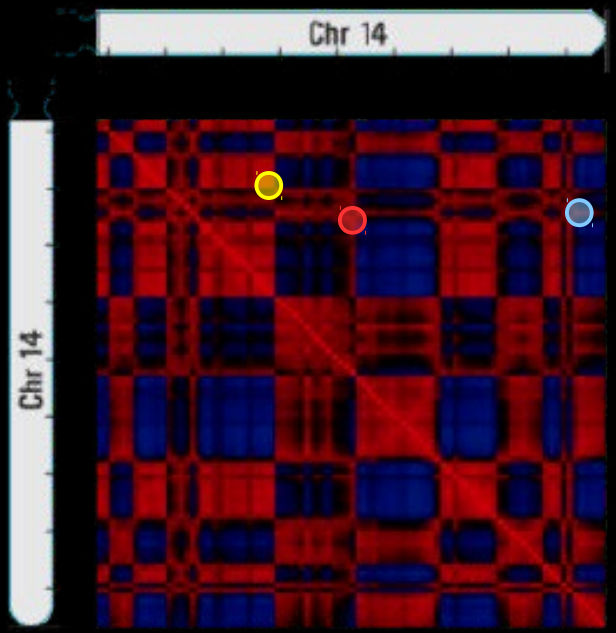

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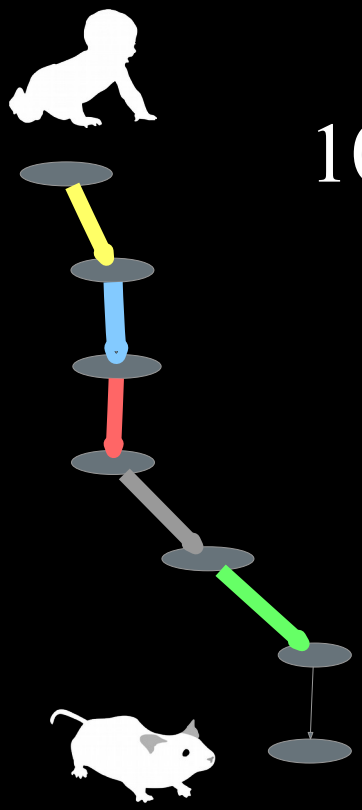

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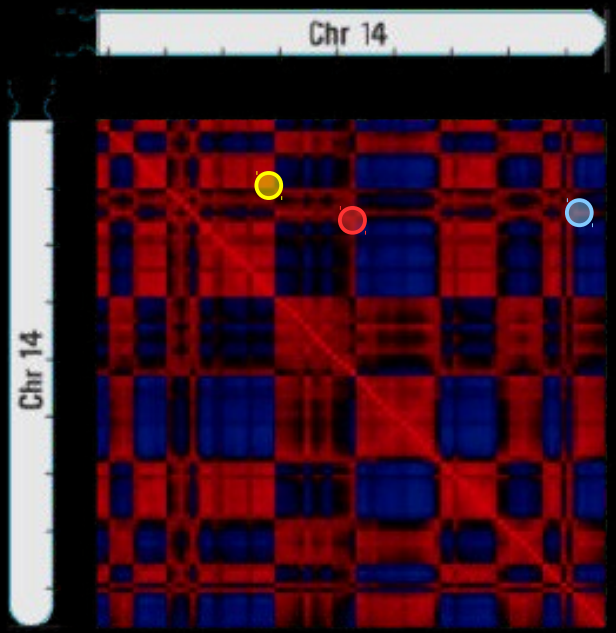

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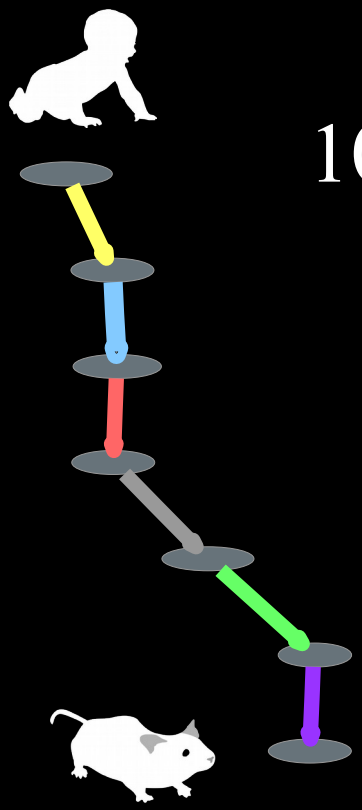

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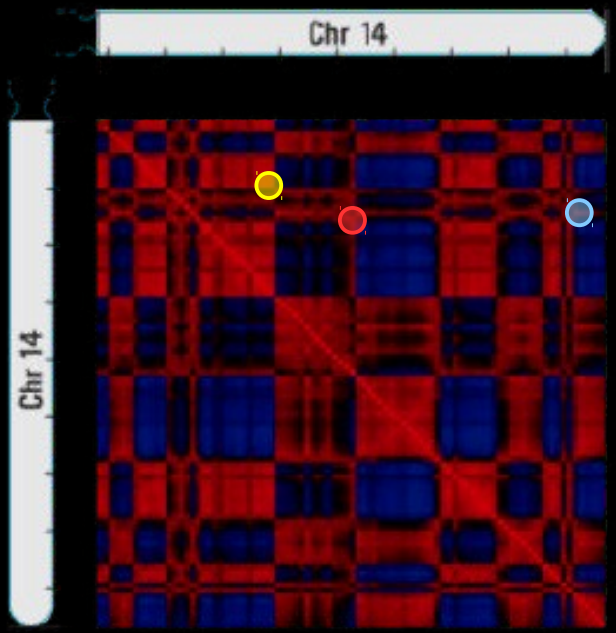
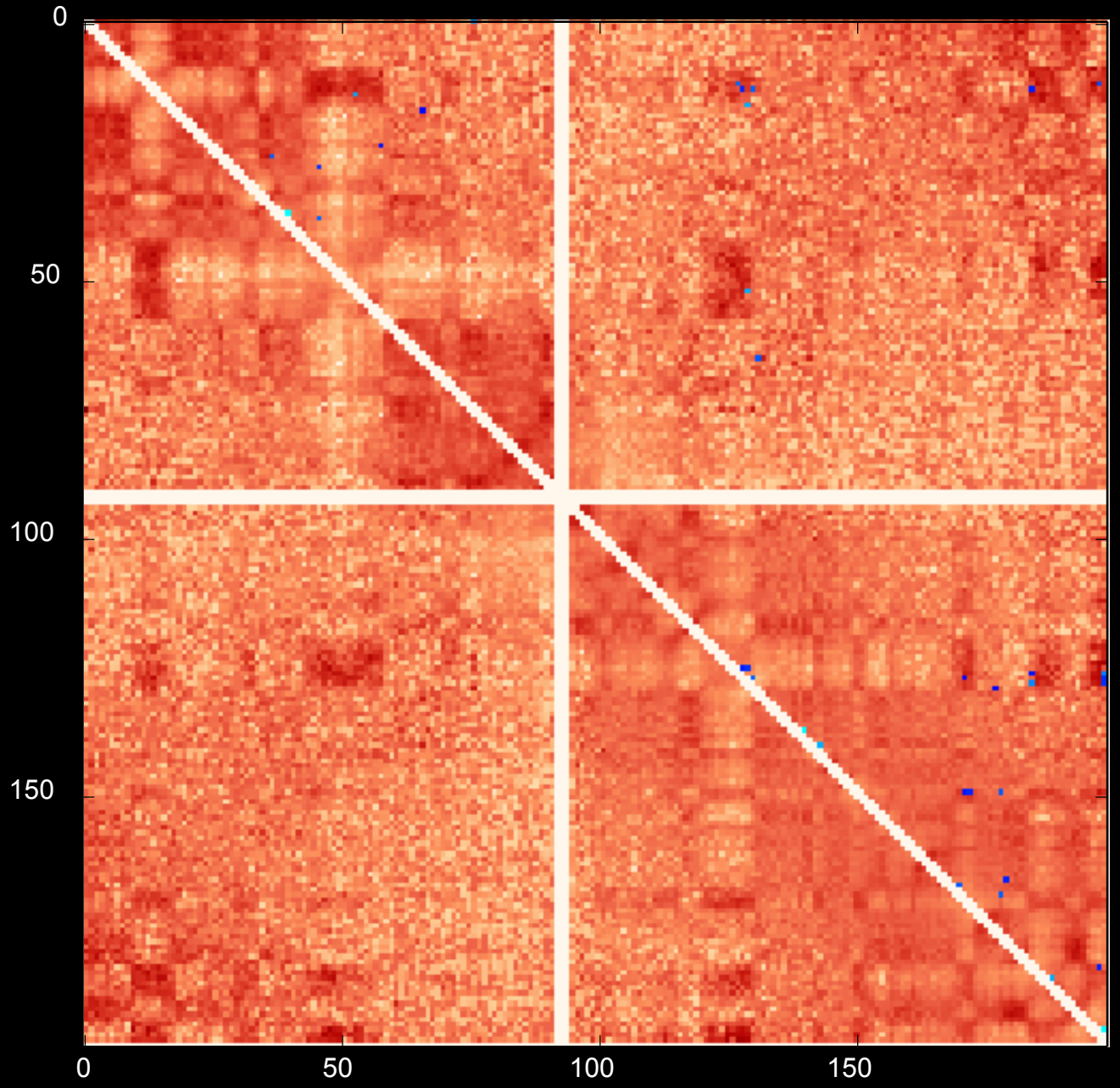


Sample from Chr 3



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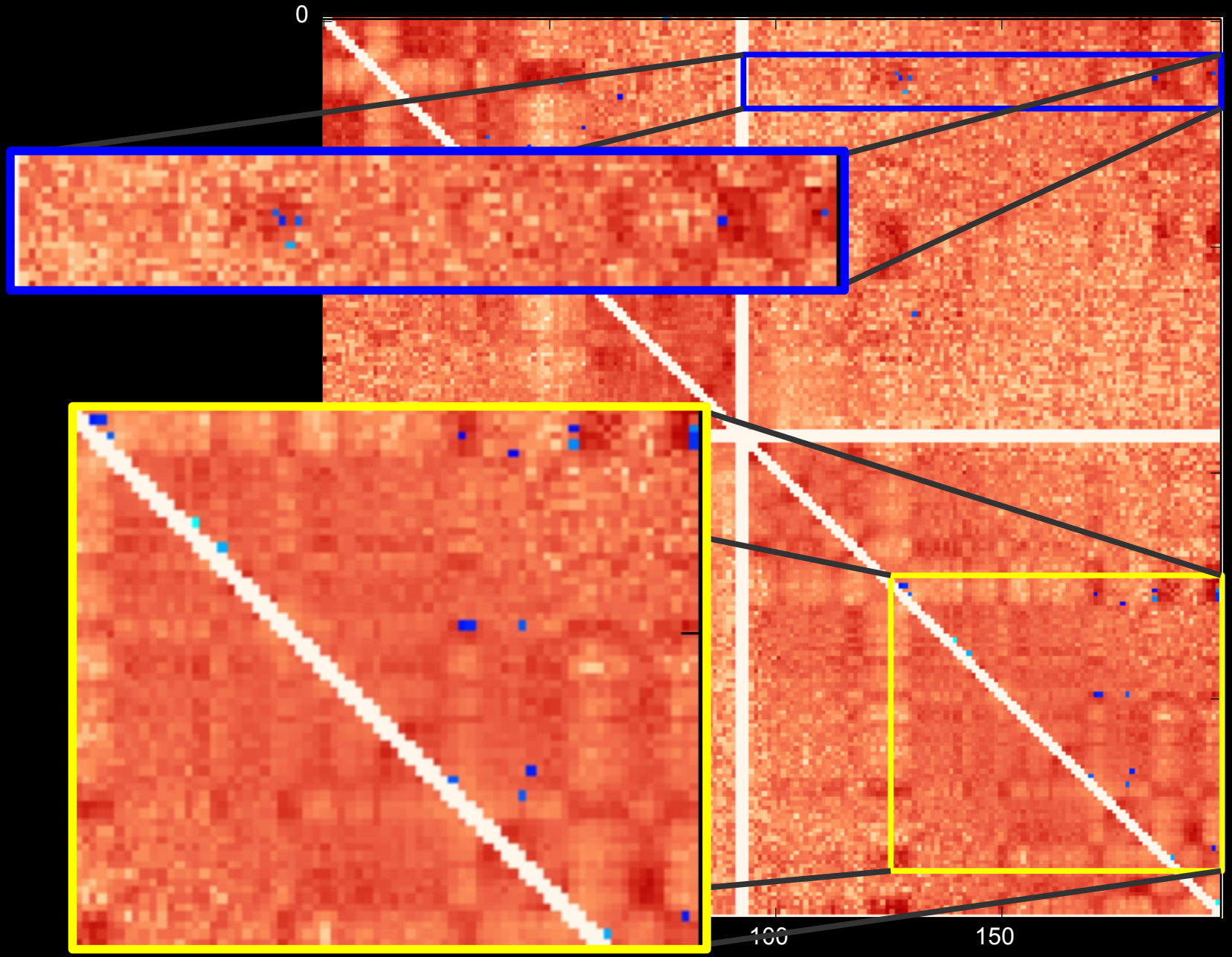
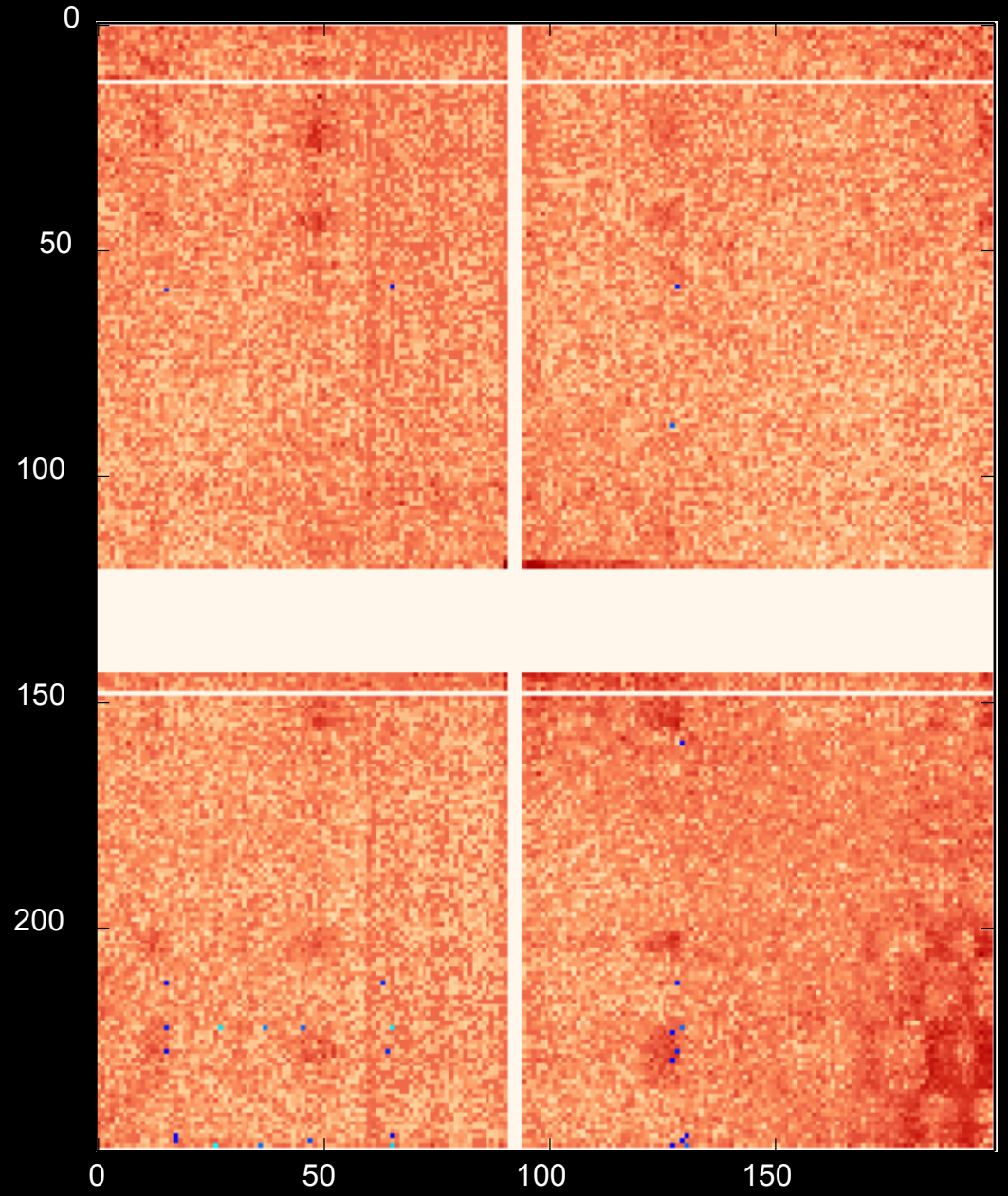


Sample from 1 vs. 3



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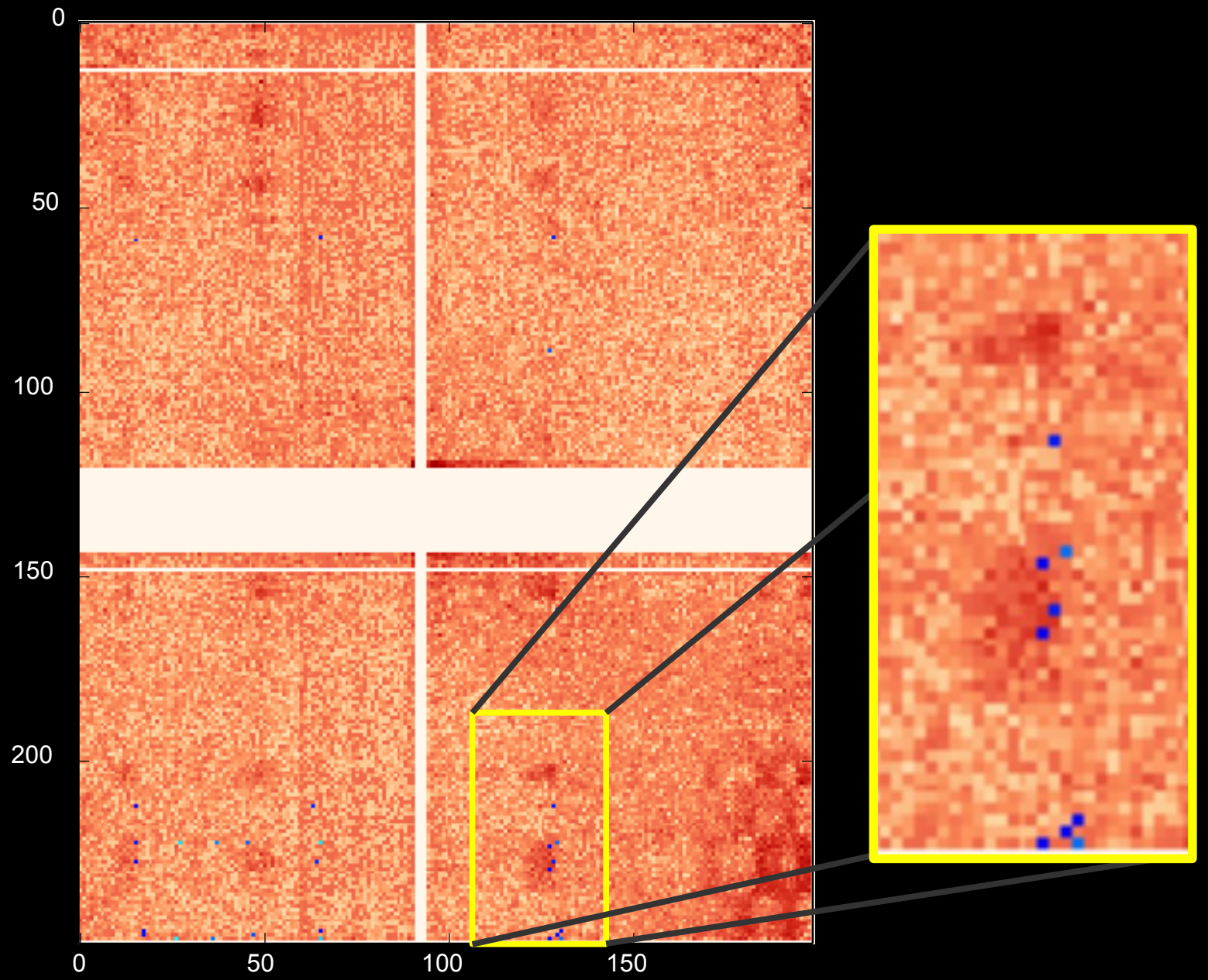

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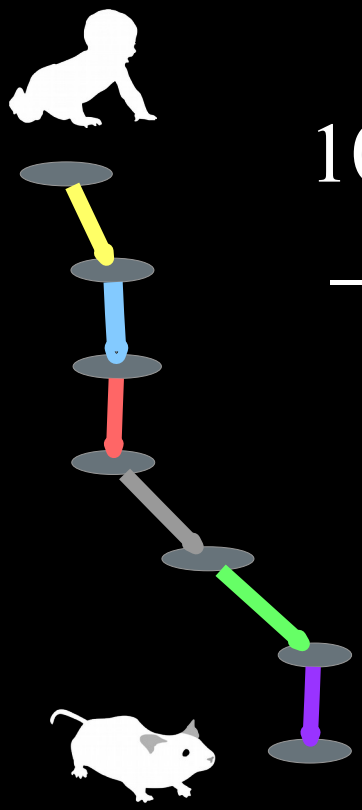
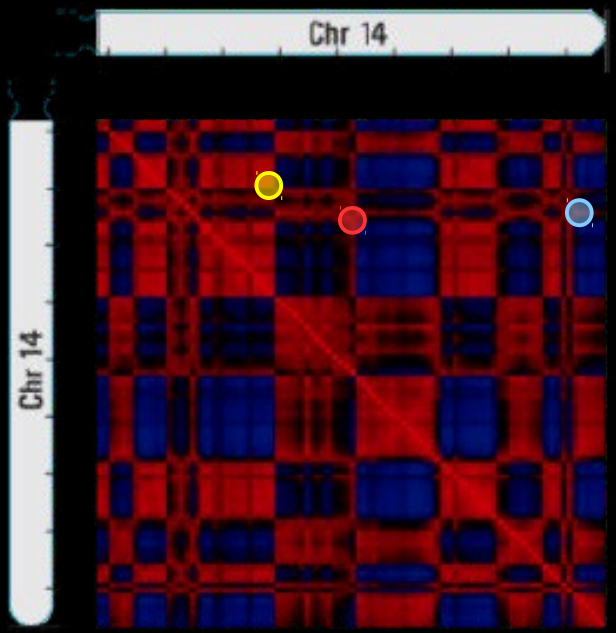
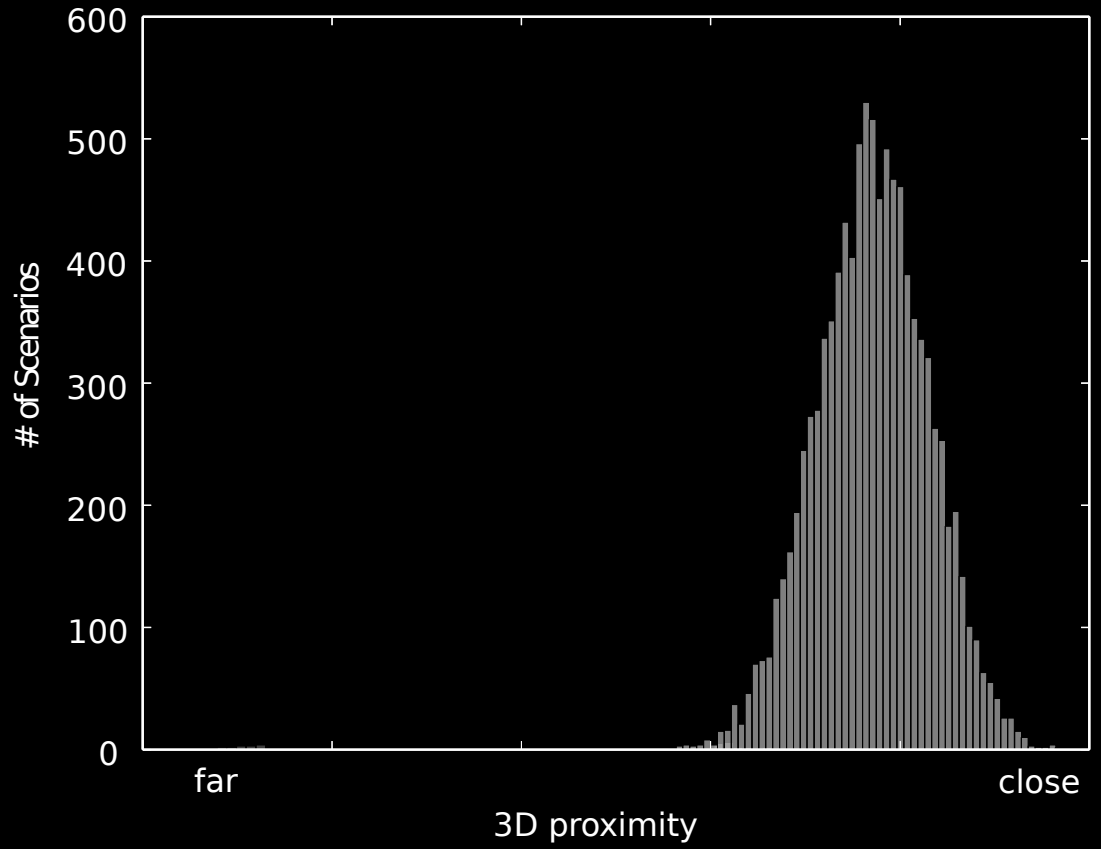


10,000 parsimonious scenario

- average over true breakpoints



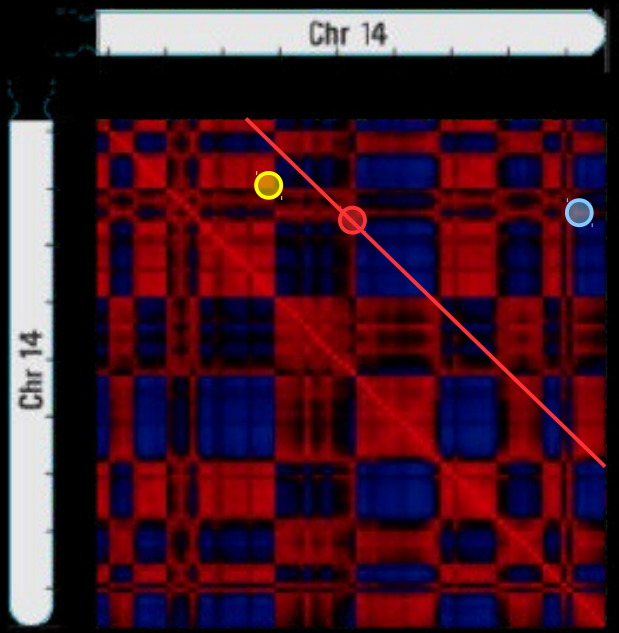
Human-Mouse Scenarios are Local



Sampling Scenarios

10,000 parsimonious scenario

- average over true breakpoints
- average over randomized breakpoints



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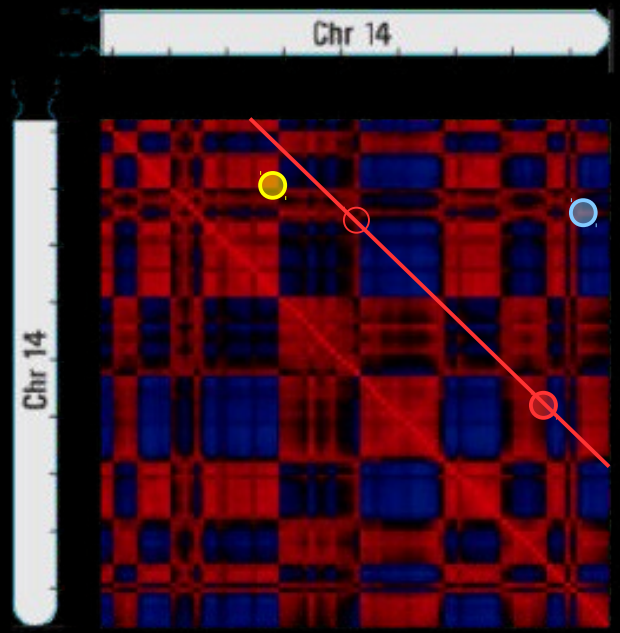

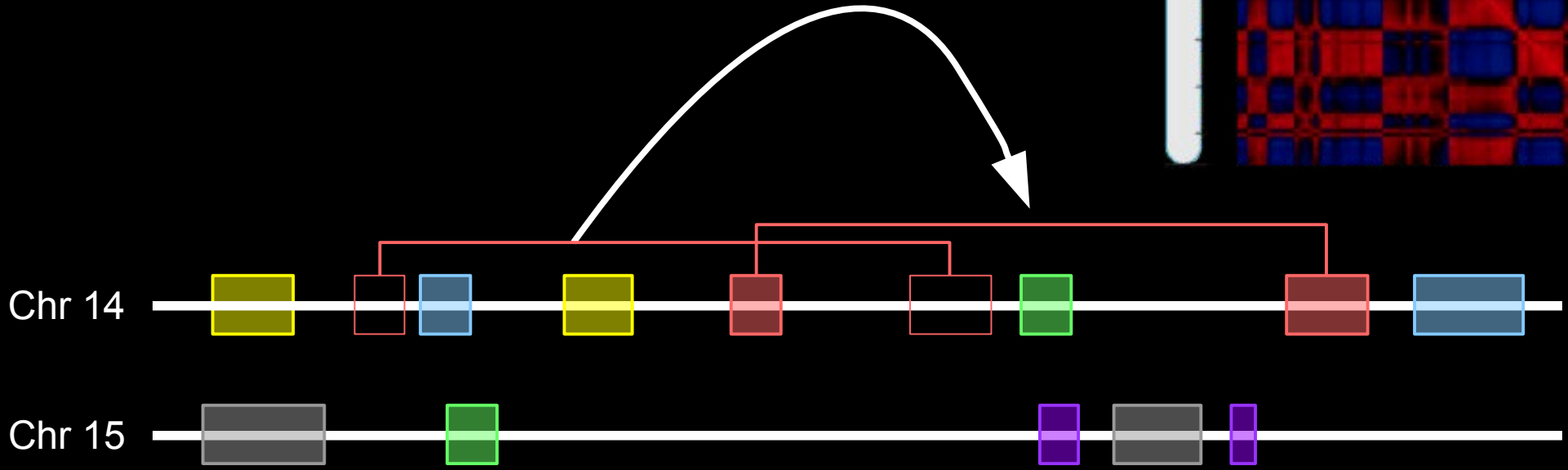

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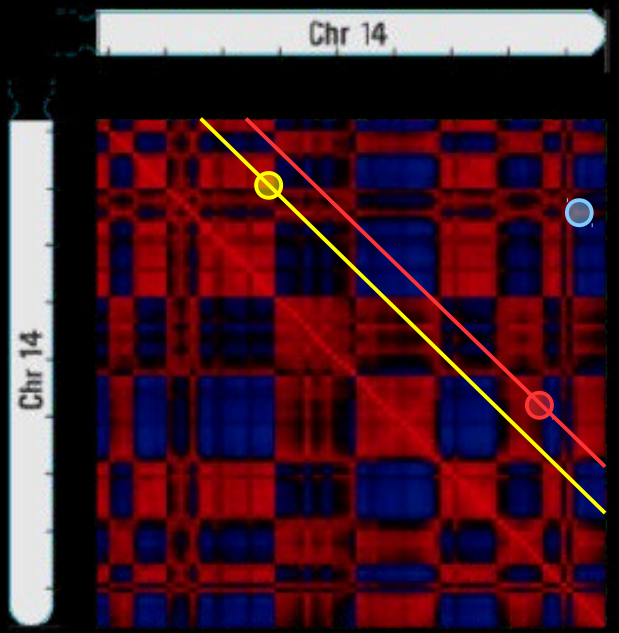

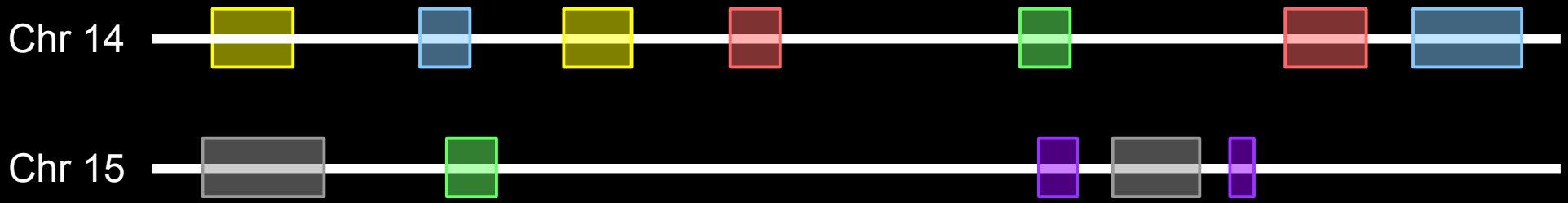

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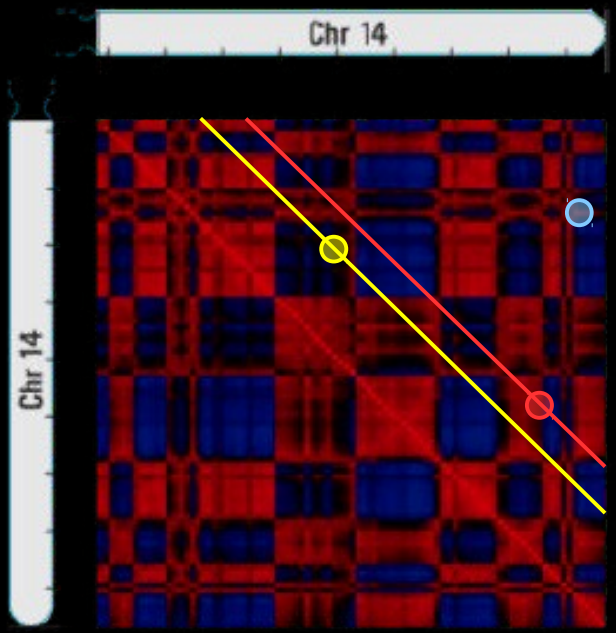

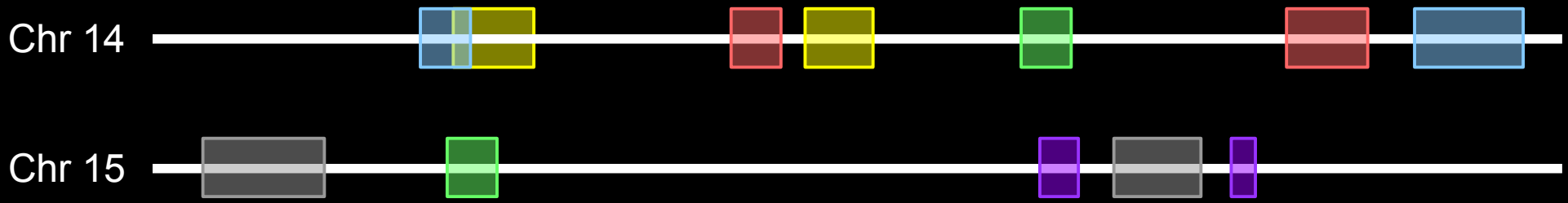

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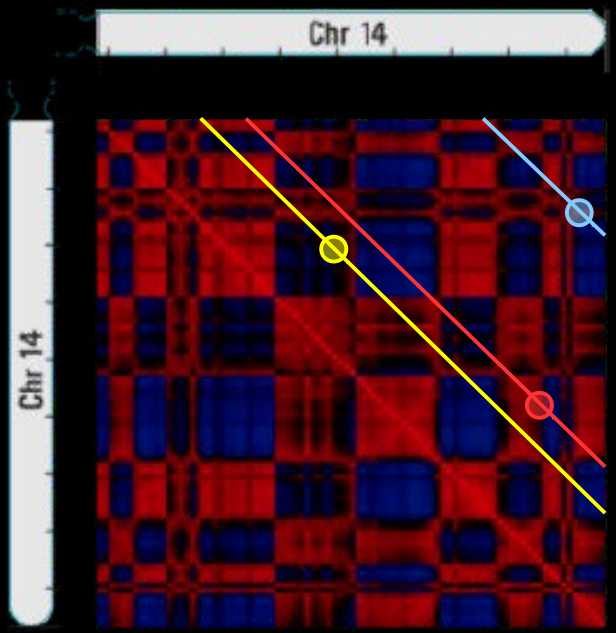

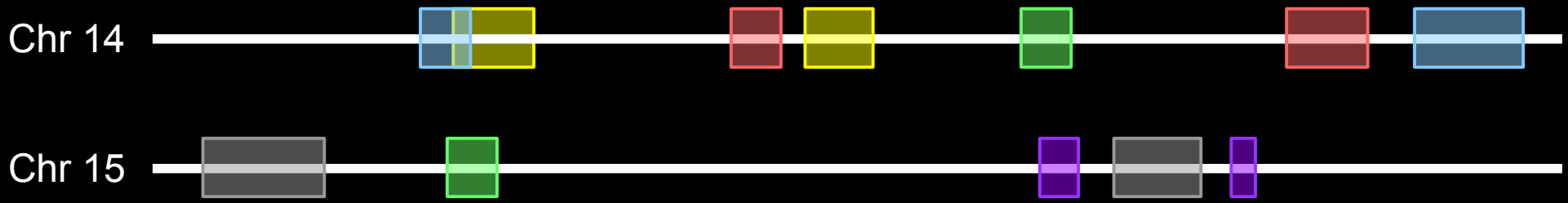

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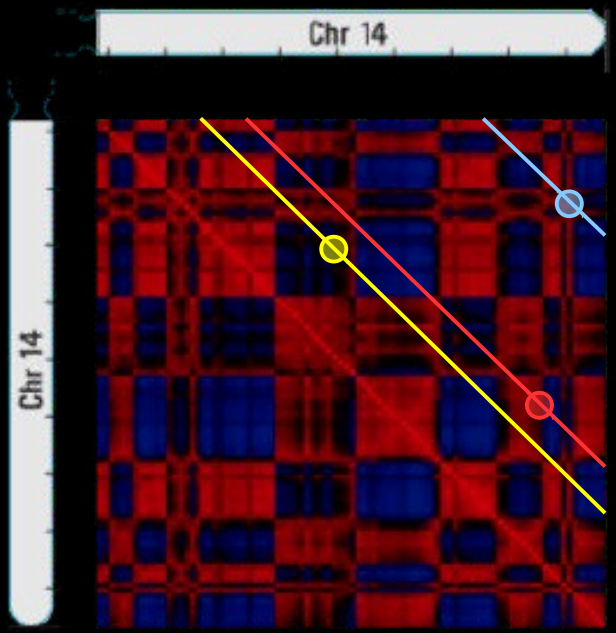

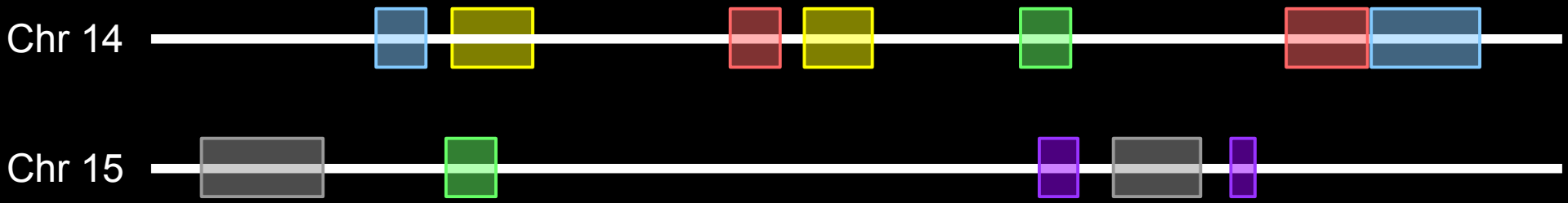

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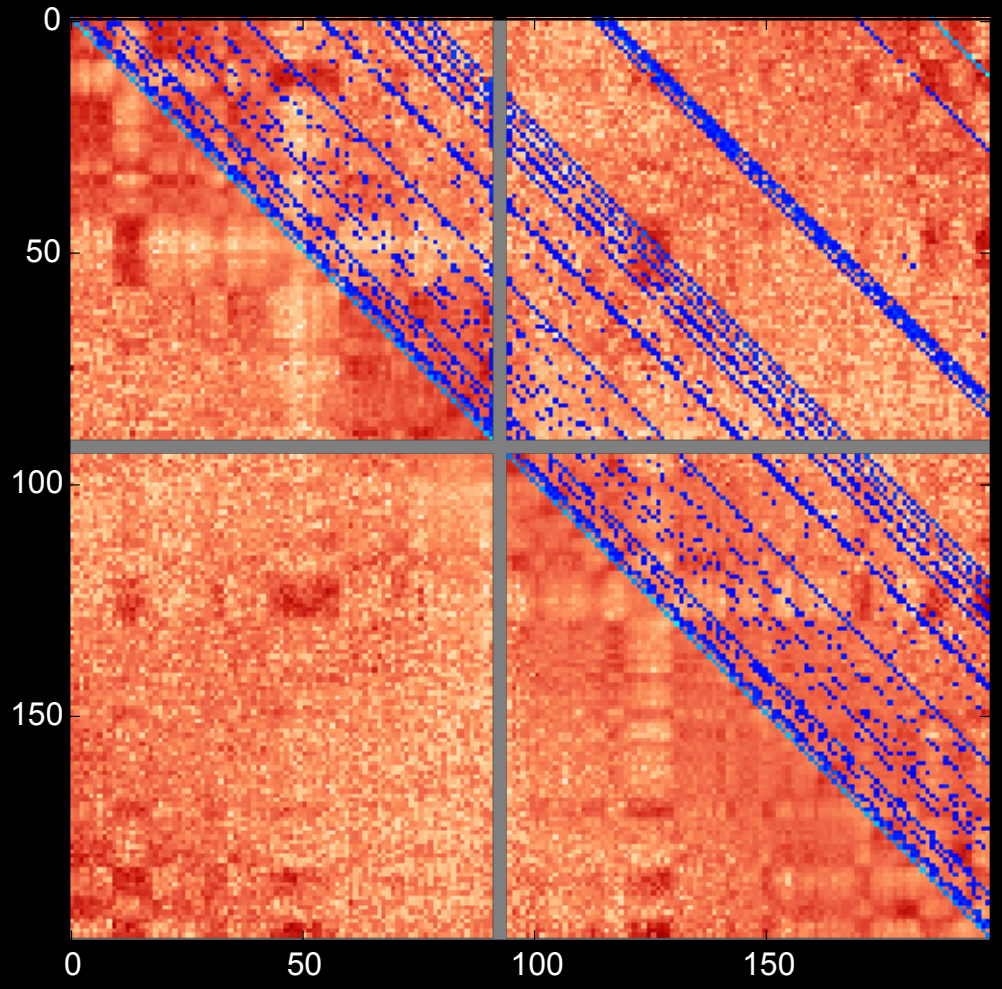
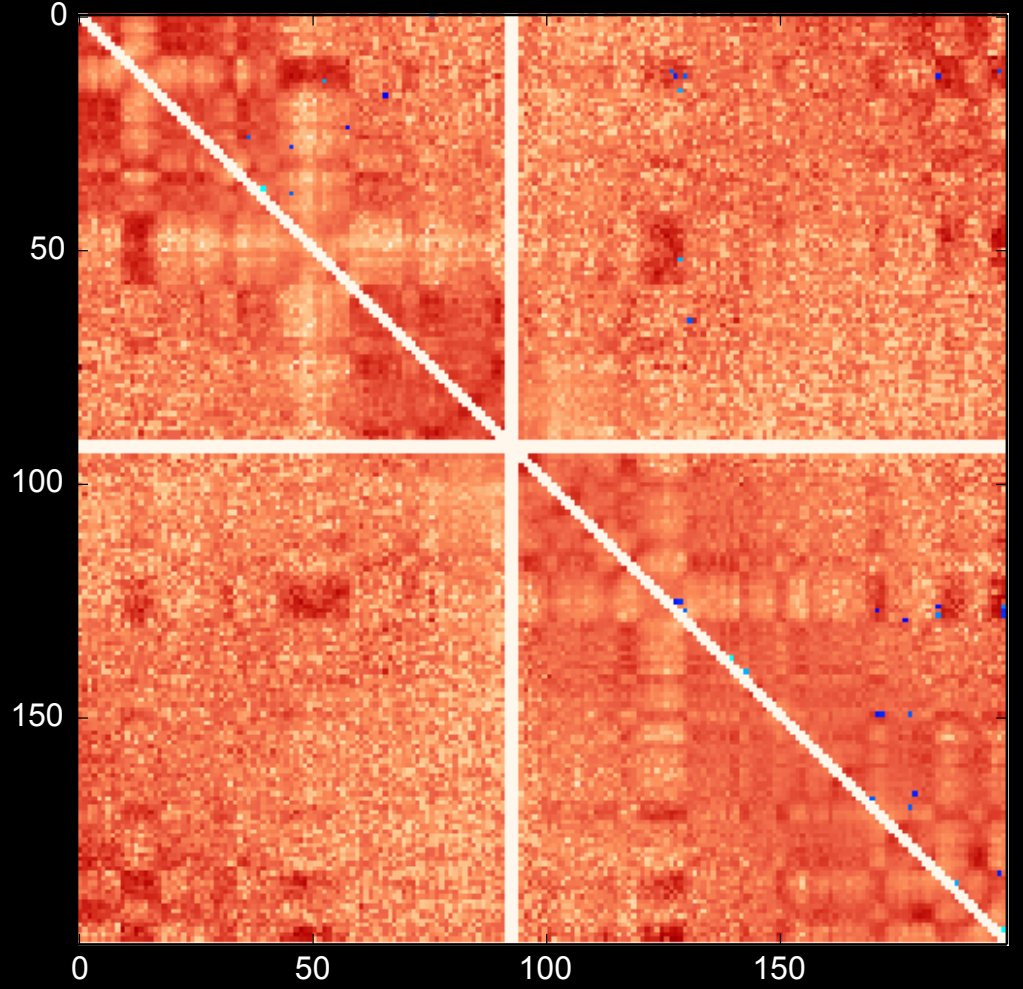
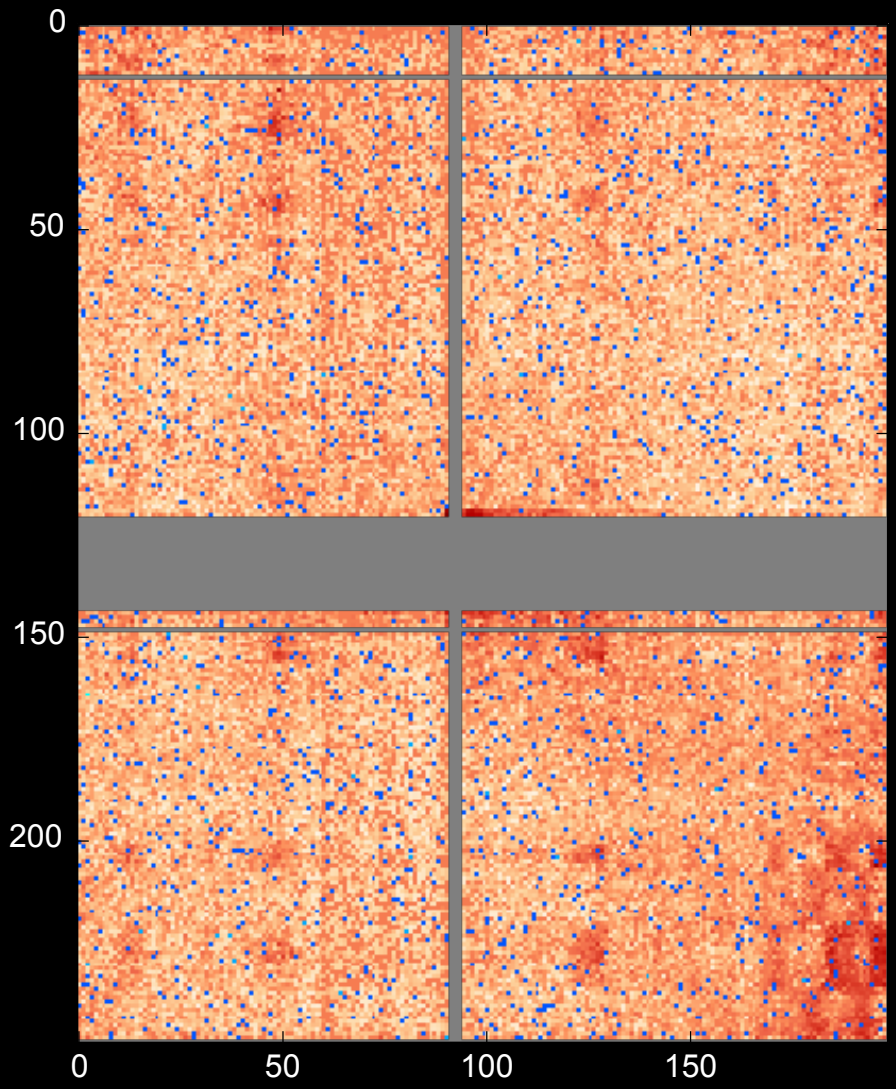
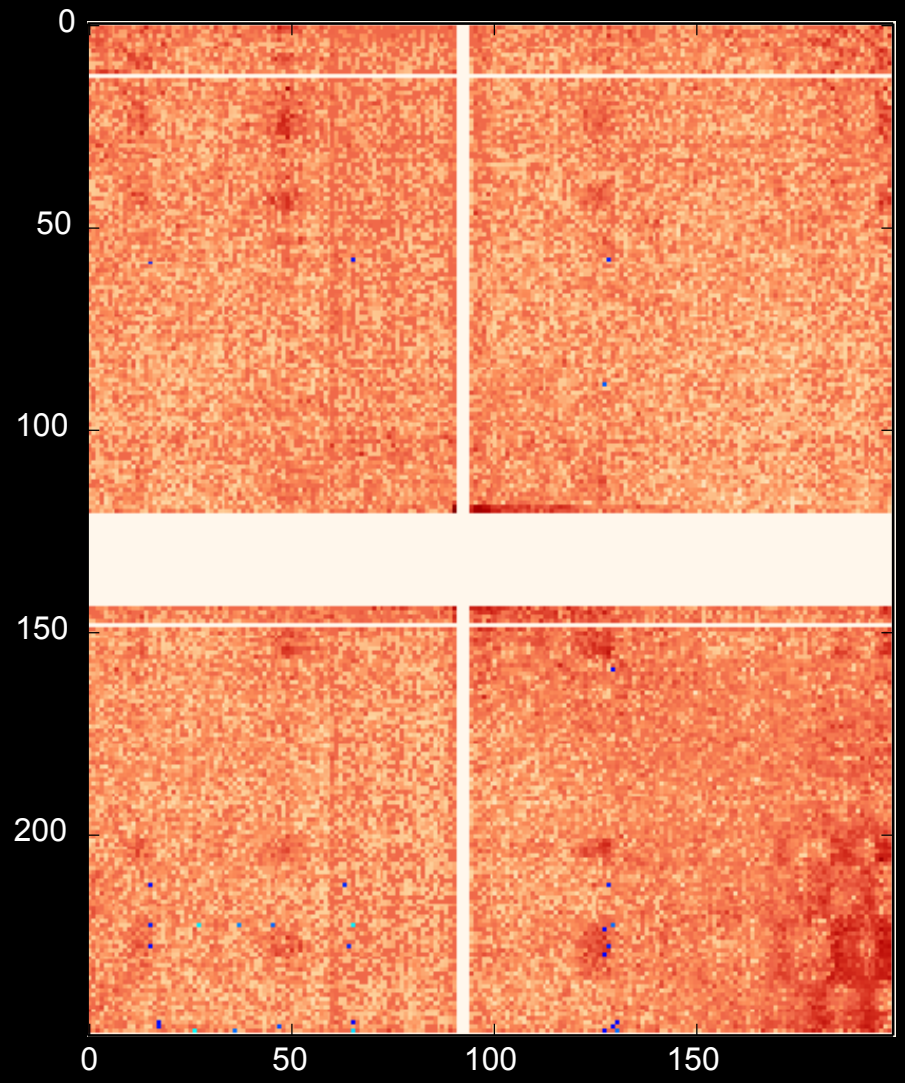


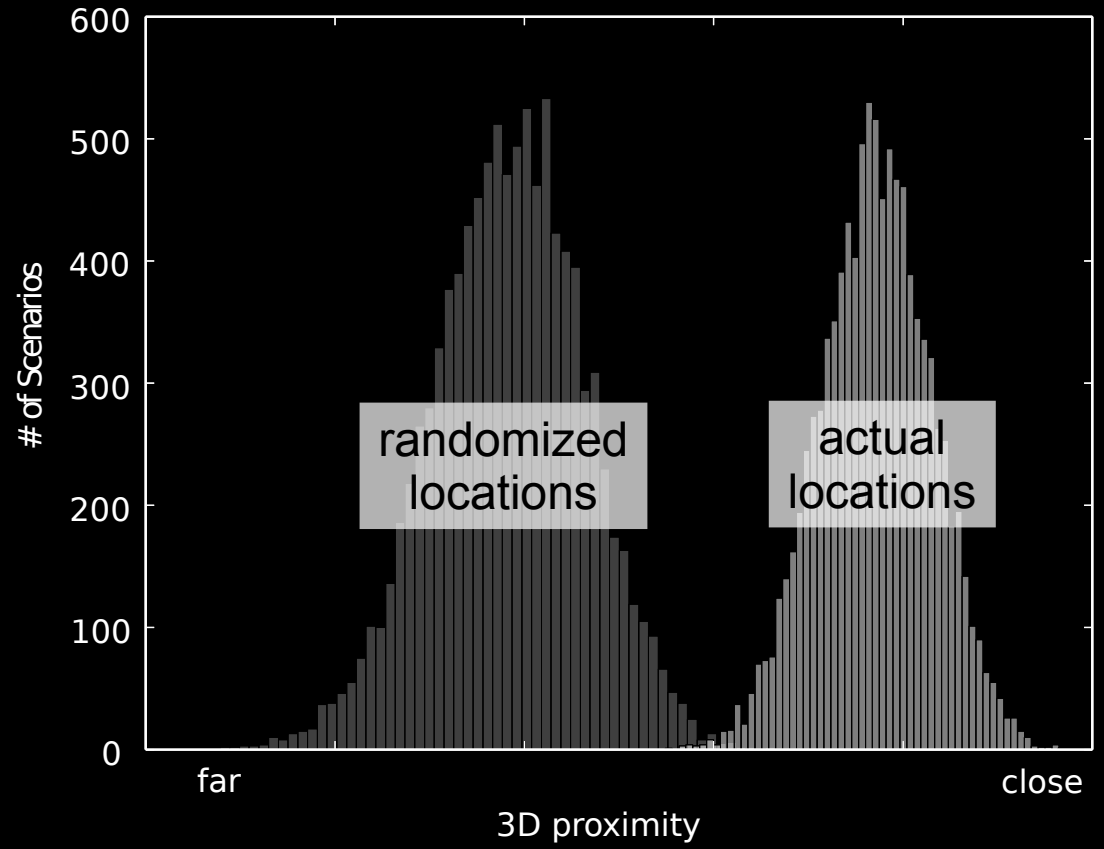


Sample from 1 vs. 3





Human-Mouse Scenarios are Local



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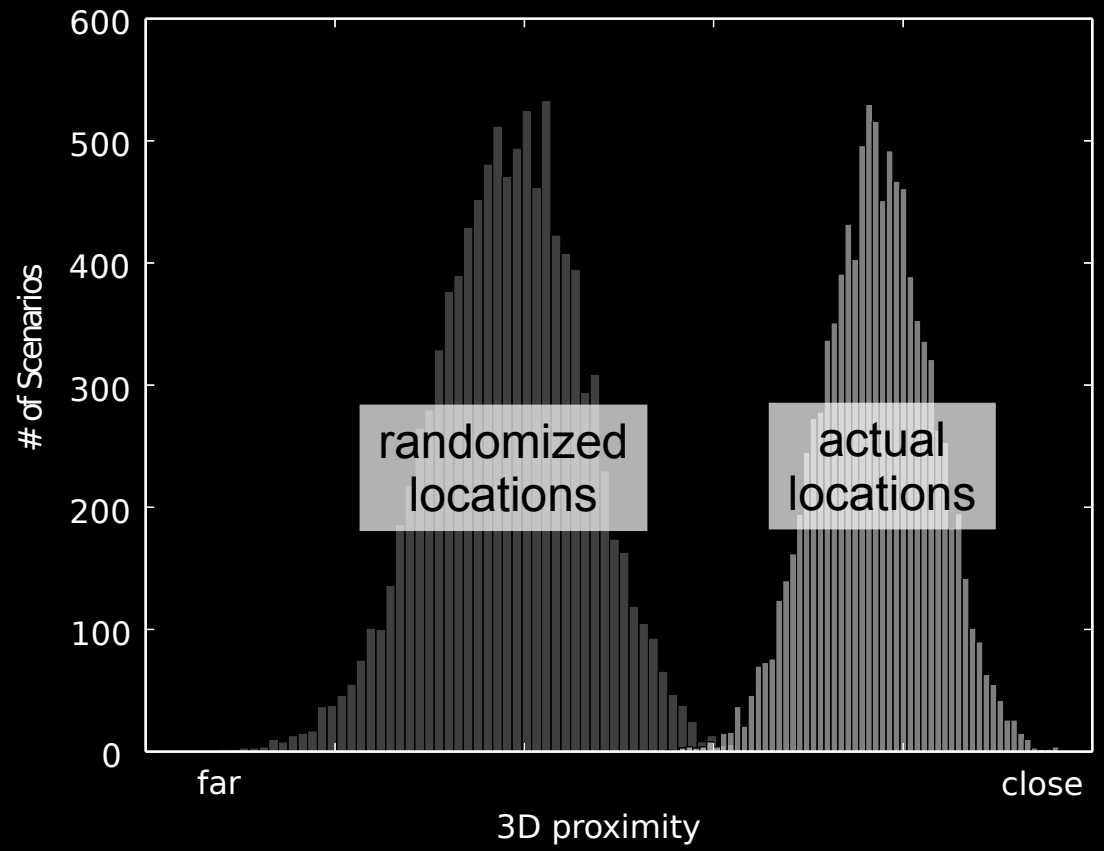
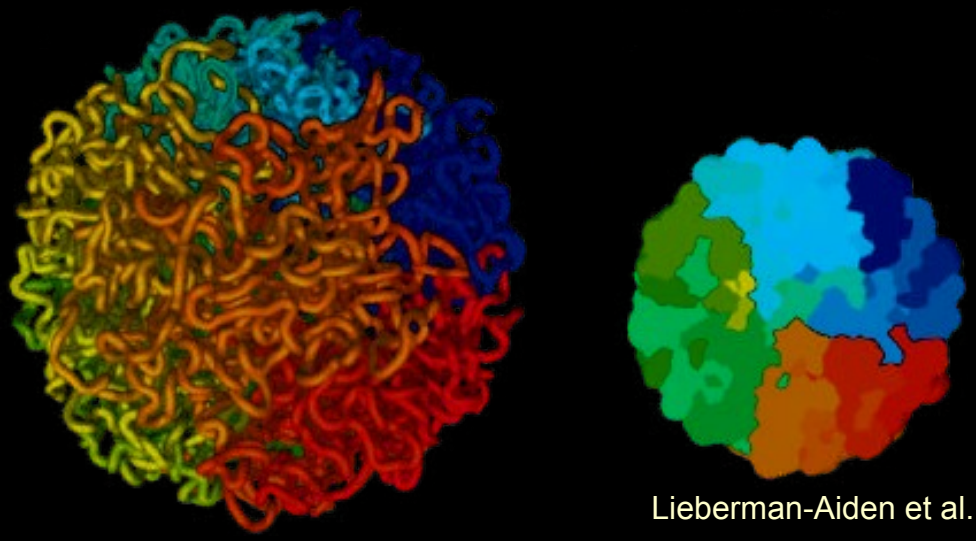


Intrachromosomal and interchromosomal breakpoint pairs

- Evolutionarily conserved rearrangements are local
- Pattern exists despite only using human Hi-C



Lieberman-Aiden et al.

Question:

How do we find scenarios that are spatially close?

Double Cut and Join

Cut 1 or 2 adjacencies

- IF 1 cut: create two telomeric adjacencies
- IF 2 cut: glue back 1 of 2 new ways

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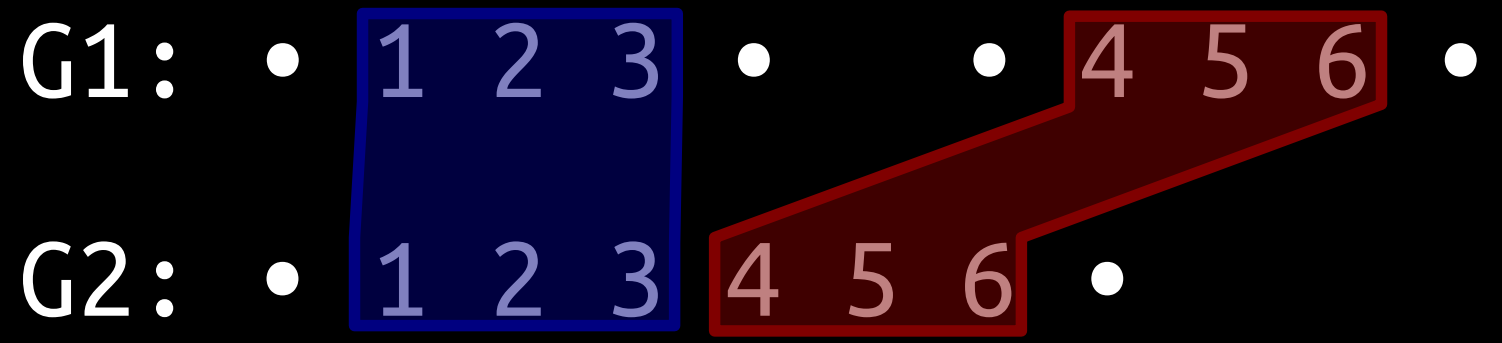

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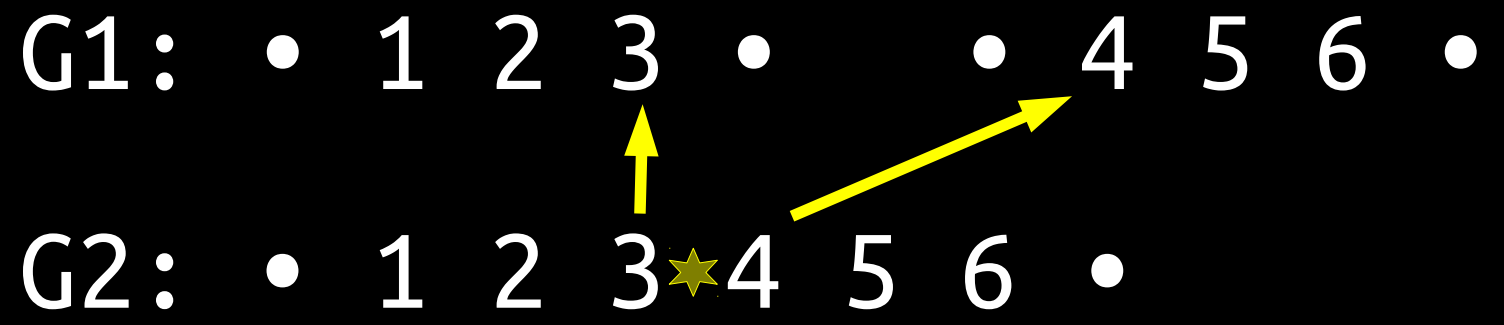

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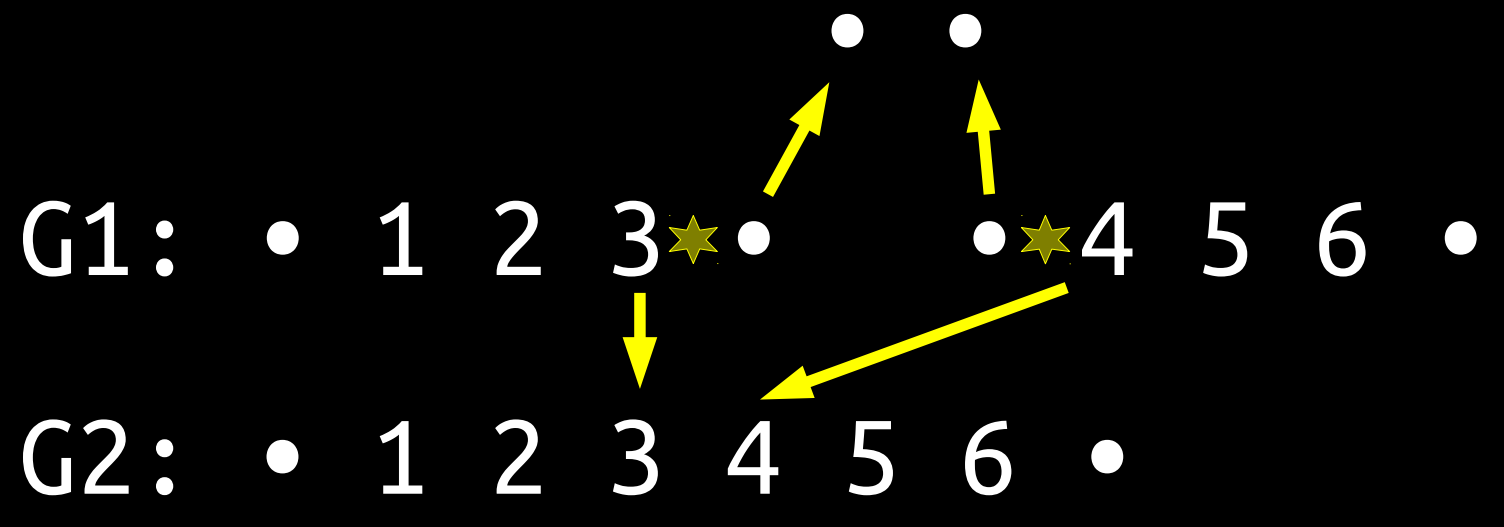

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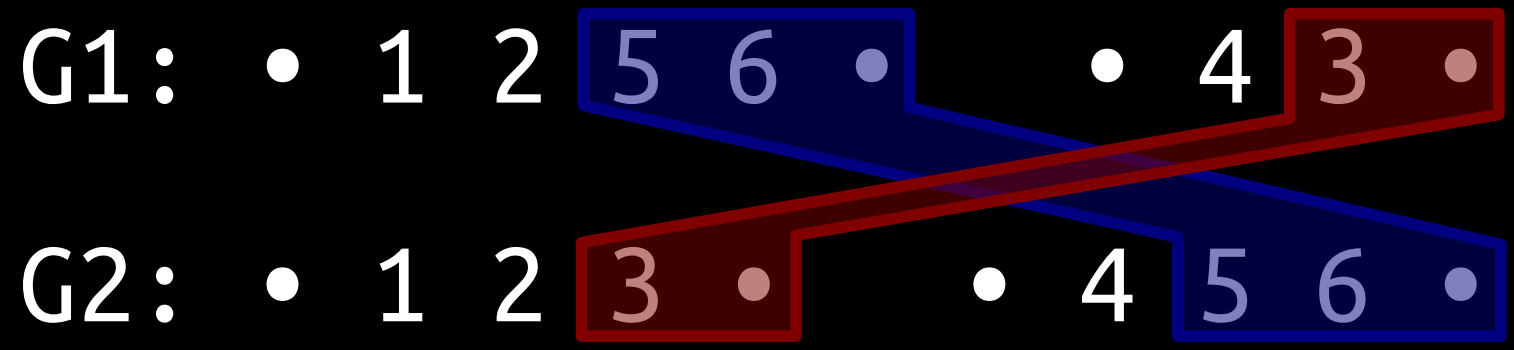

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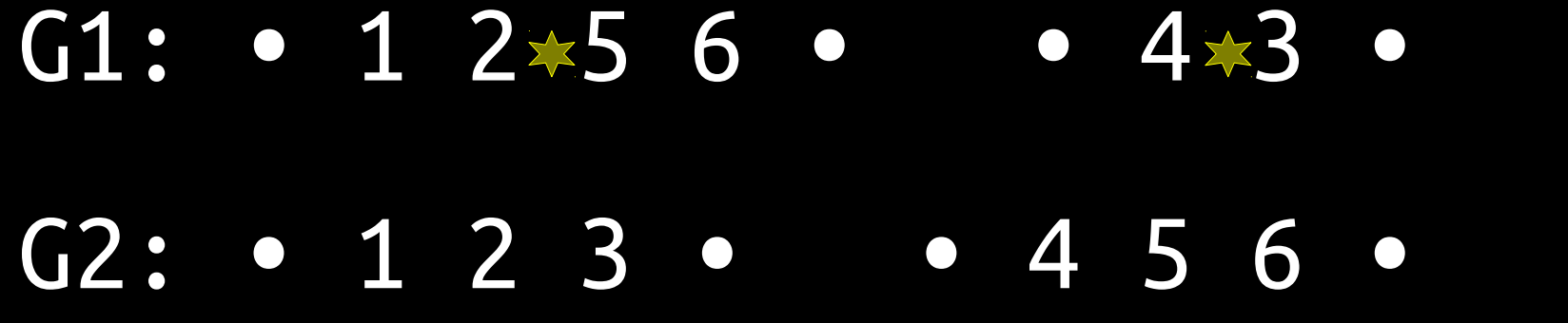

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G1: 1 ✶ 2 3 ✶

1 -3 ✶ -2 ✶

G2: 1 -3 2

DCJ Scenarios

How do we find rearrangements?

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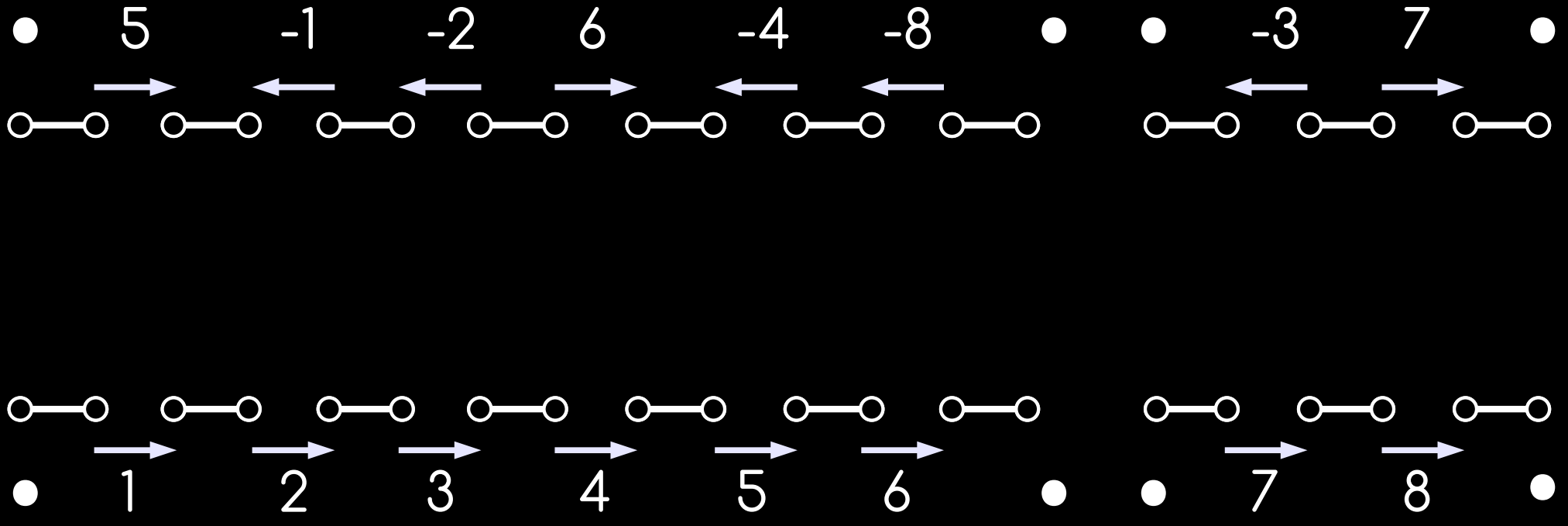

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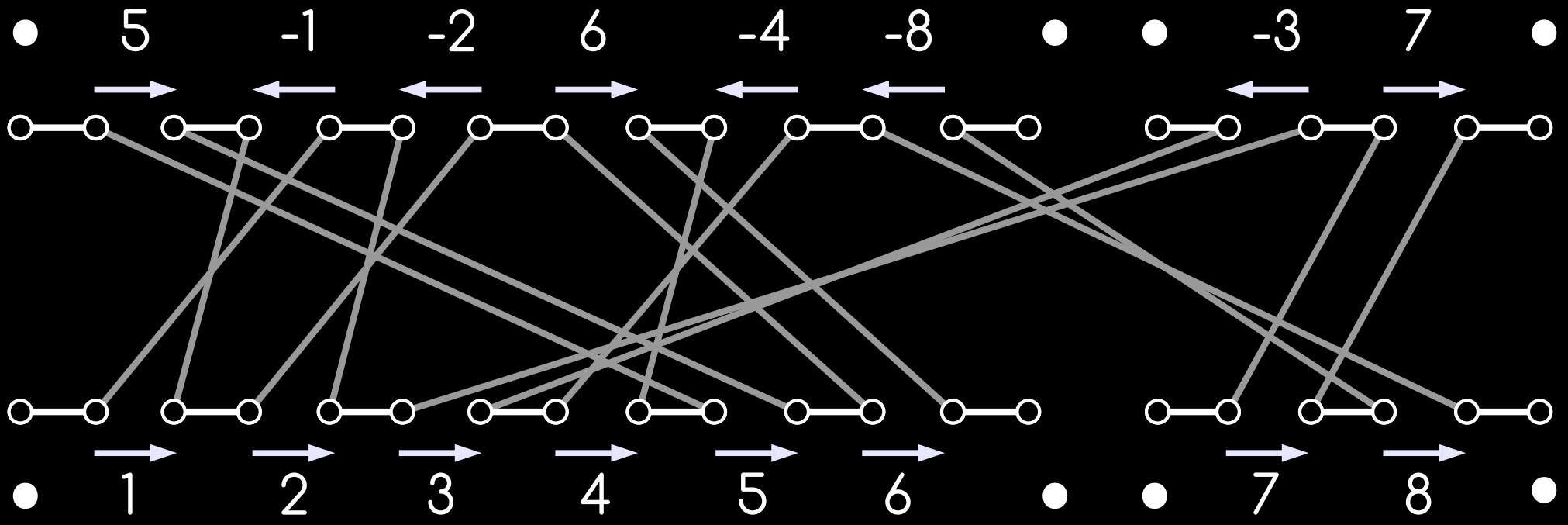
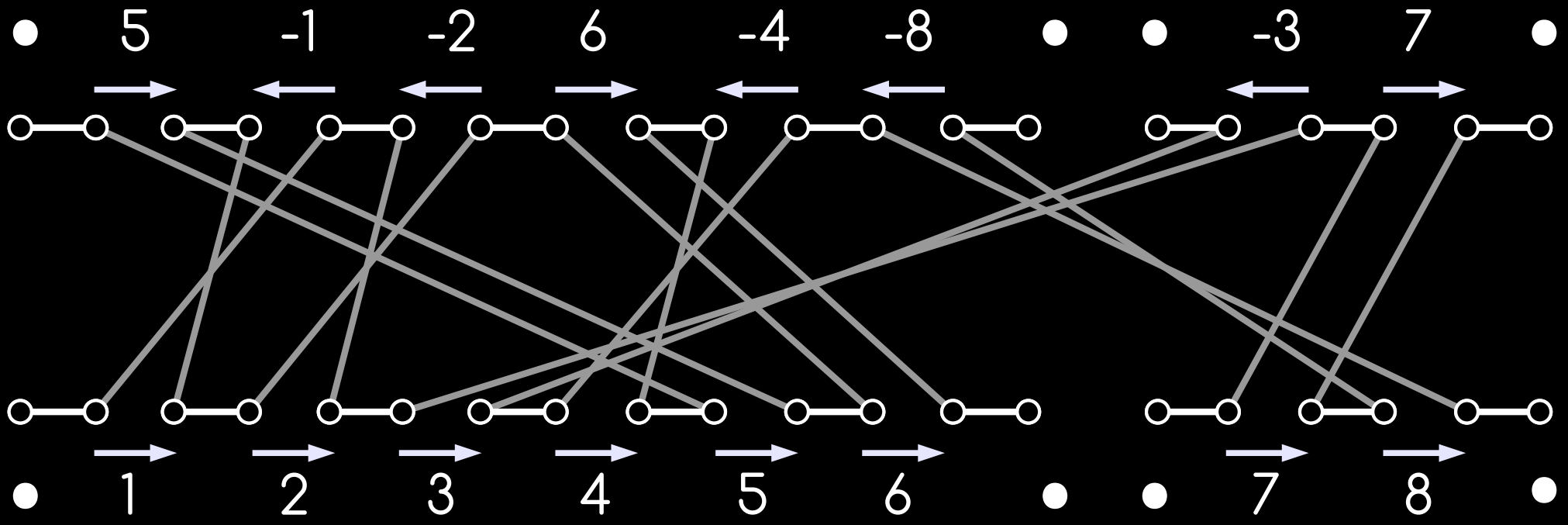


DCJ Scenarios

How do we find rearrangements?

- d_{DCJ} (G1, G2) = N – (C + I/2)



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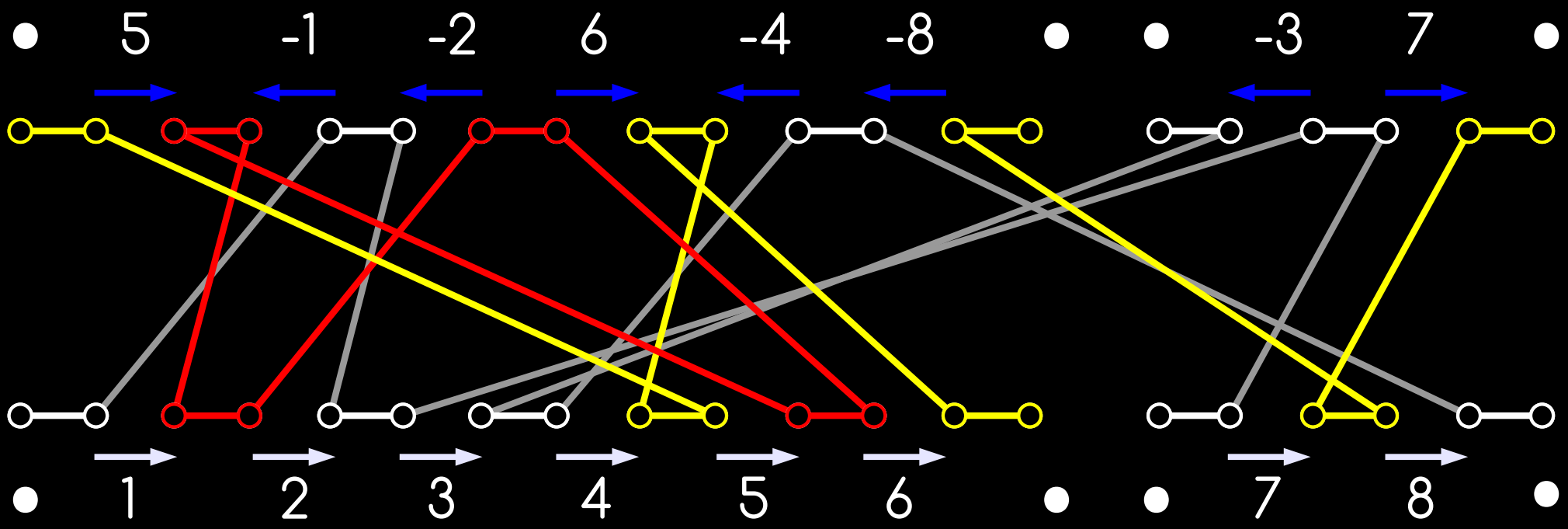
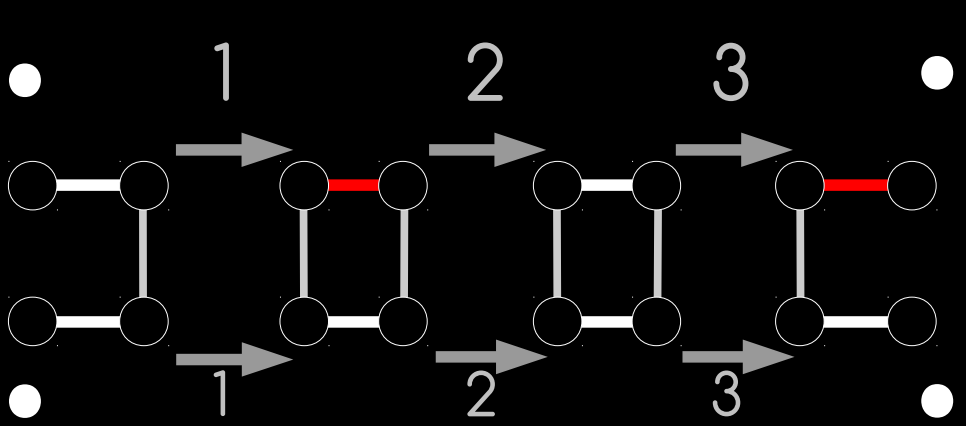
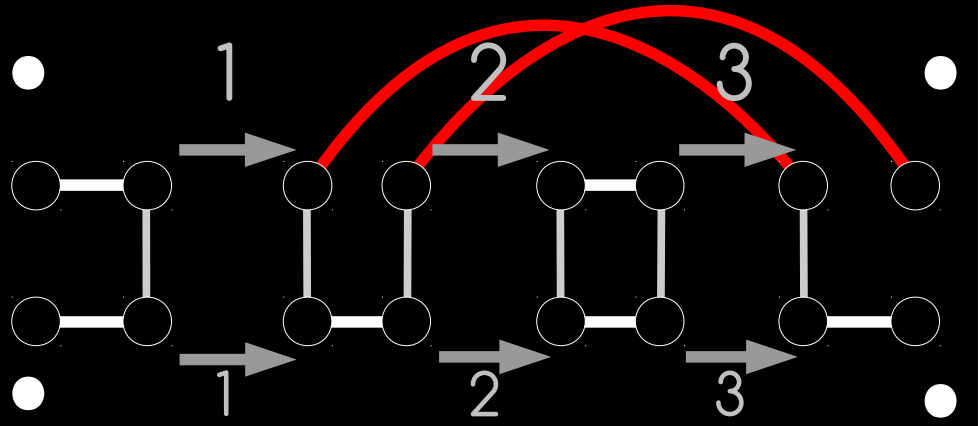
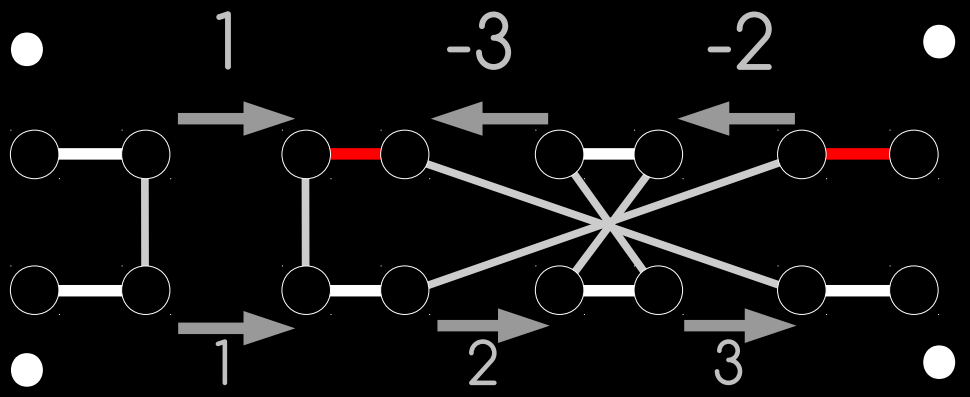


DCJ Moves

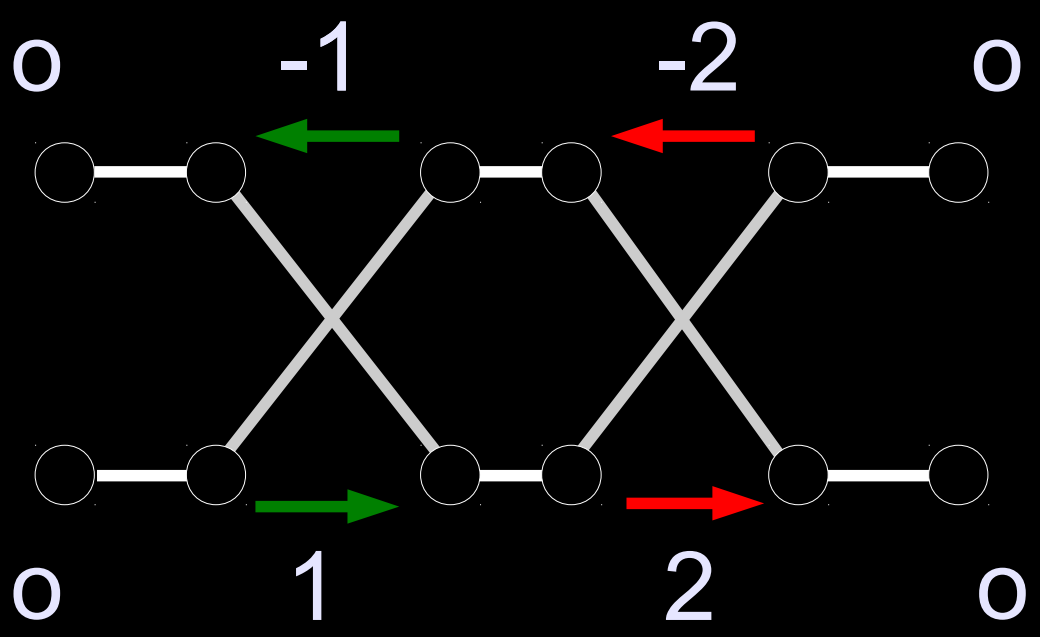


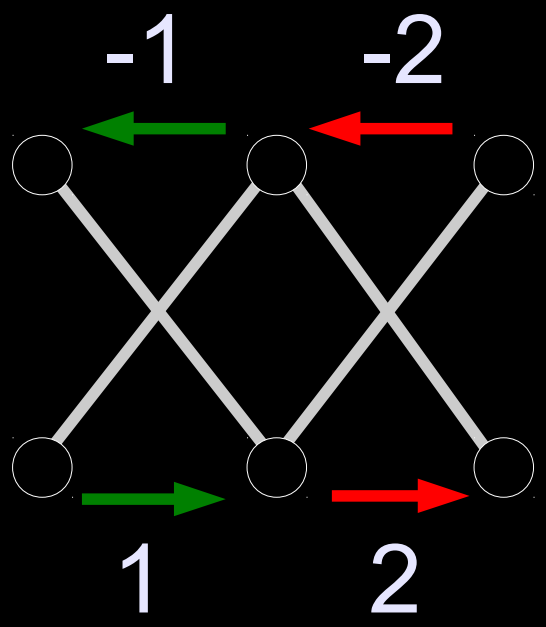




$$d_{DCJ}(G1, G2) = N - (C + I/2)$$

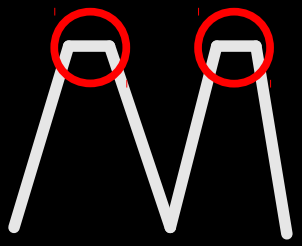
Shorthand

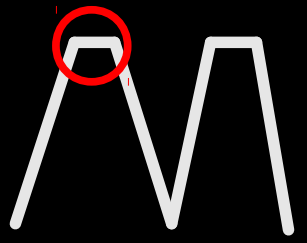




All DCJ Scenarios

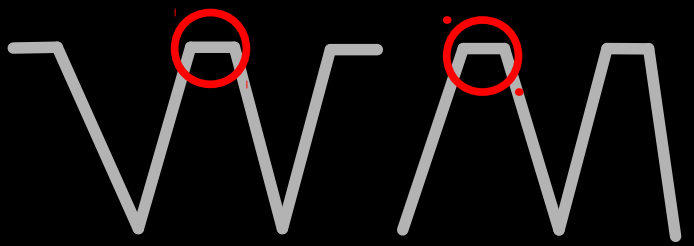
- even path
  - extract cycle
  - path fission



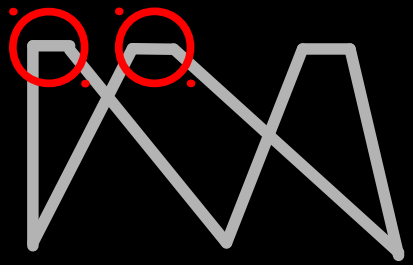


- odd path
  - extract cycle

- 2 even paths



- cycle
  - split cycle



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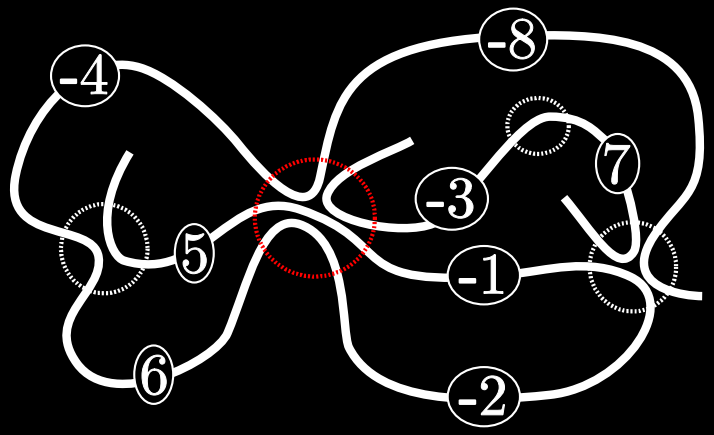
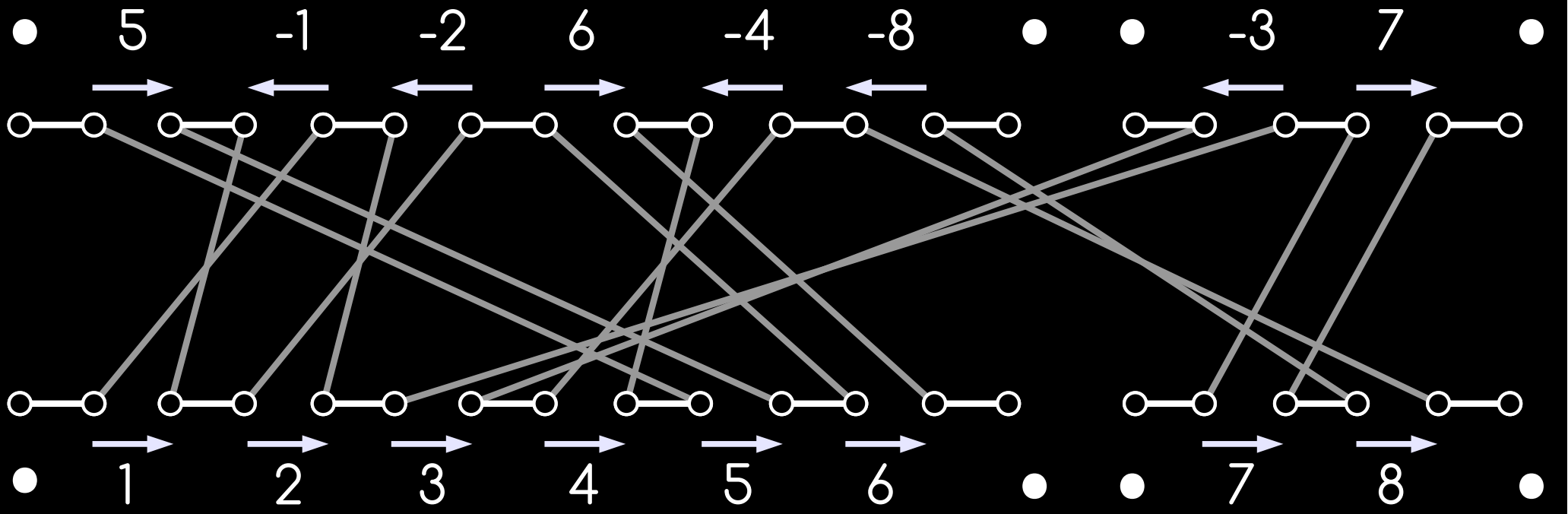
Local DCJ





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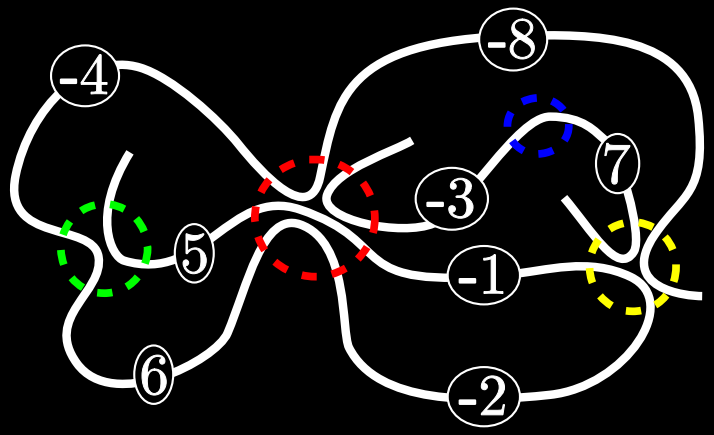
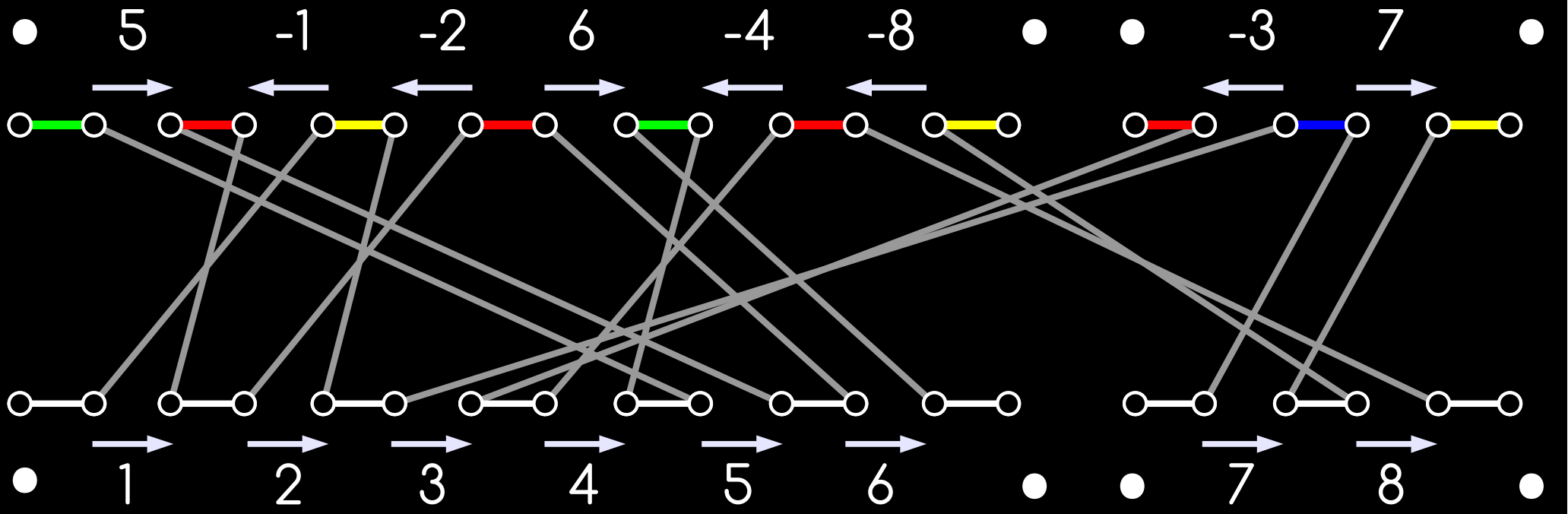
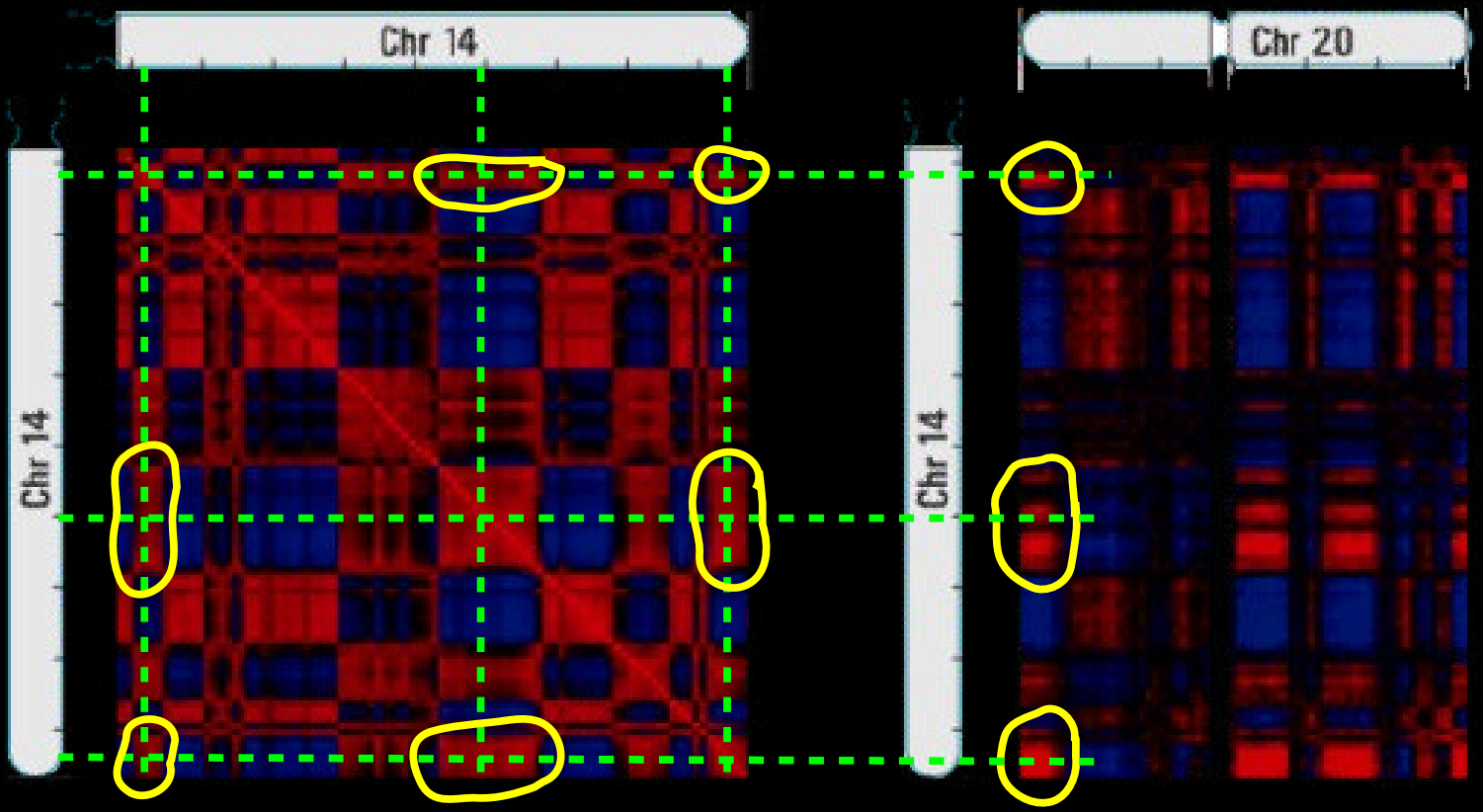




Hi-C Heatmaps

Heatmaps define a locality constraint.

- transitivity appears to hold



Non-locality

- Two problems...

  INPUT: two genomes with colored adjacencies

  - OUTPUT 1:
    scenario with minimum # of non-local moves

  - OUTPUT 2:
    a minimum length scenario, with a minimum # of non-local moves

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    NP-Hard

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    THIS PAPER

    Polynomial

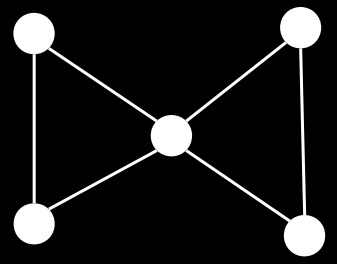
Minimize Distant Rearrangements

- NP-Hardness
  - Max Eulerian Cycle Decomposition

    INPUT: Eulerian graph G = (V, E)

    OUTPUT: partition of E into cycles

    MEASURE: |E|



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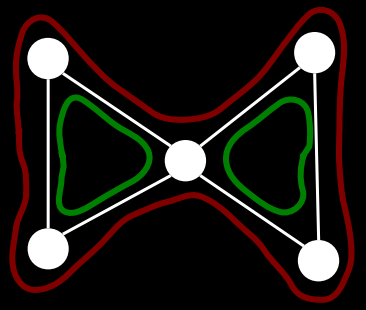

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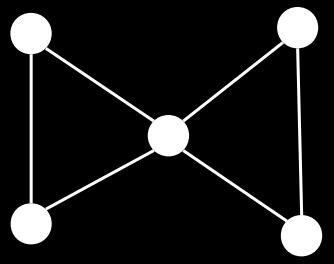

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  - Min Non-Crossing Colored Partition

    INPUT: ordered set of colored elements

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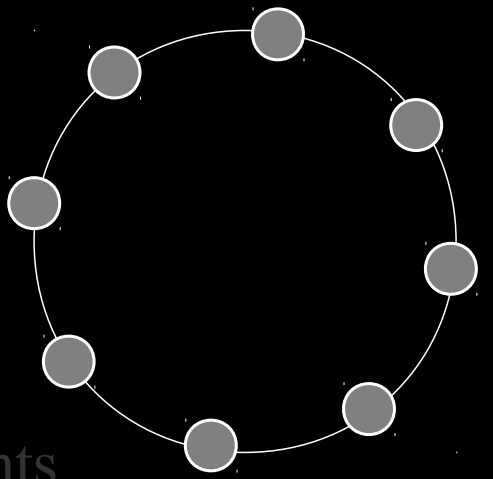

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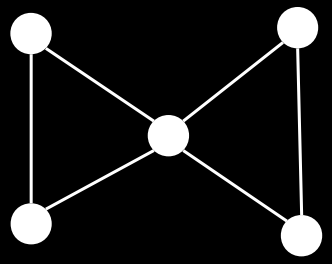

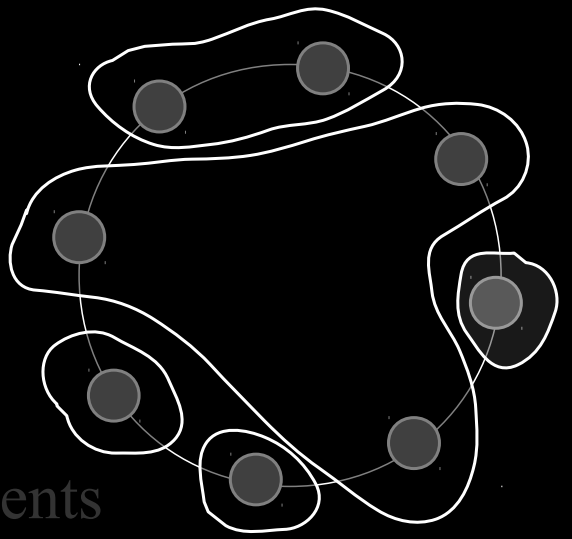

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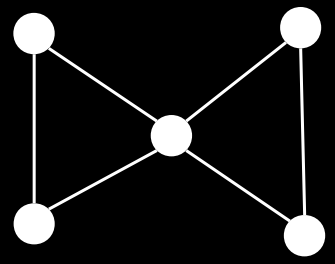

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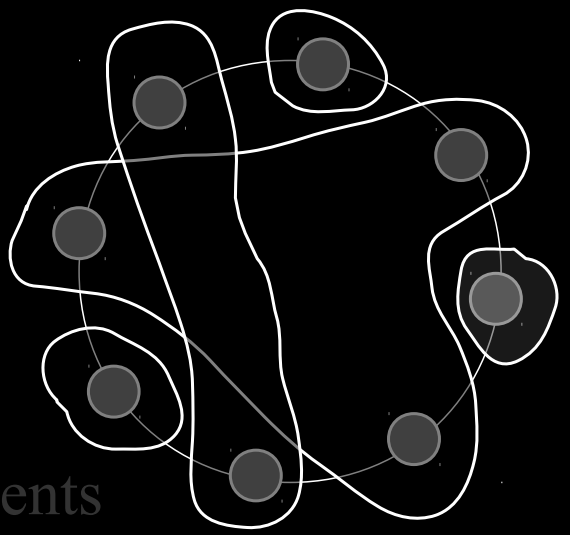

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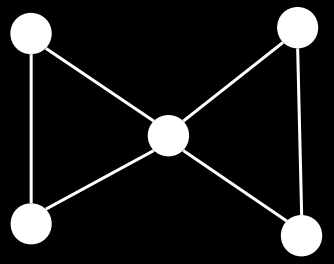

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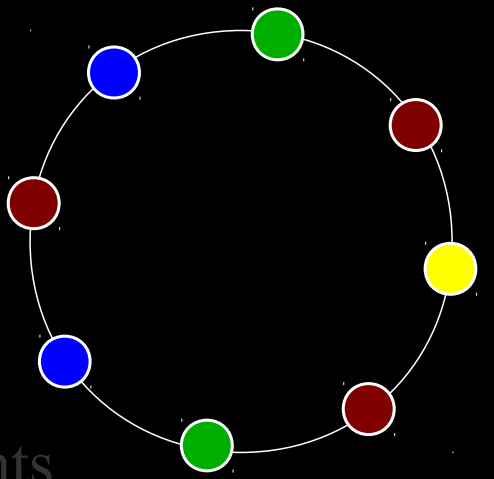

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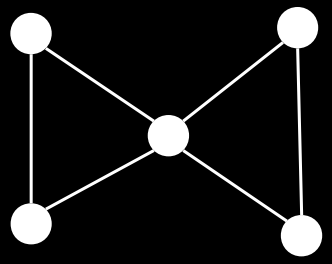

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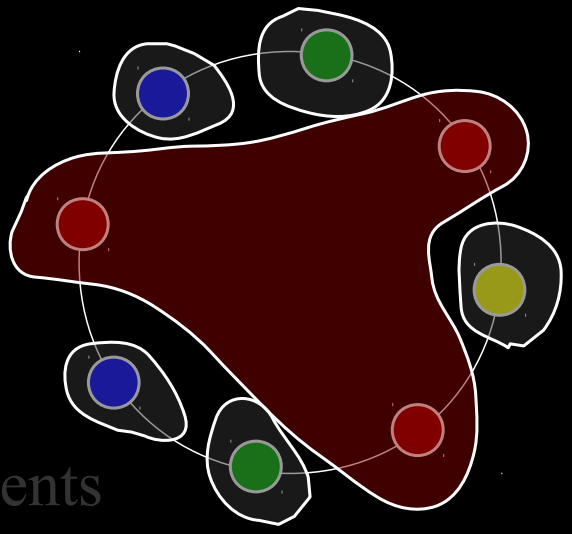

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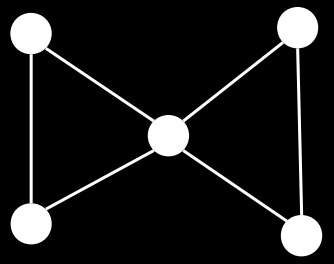

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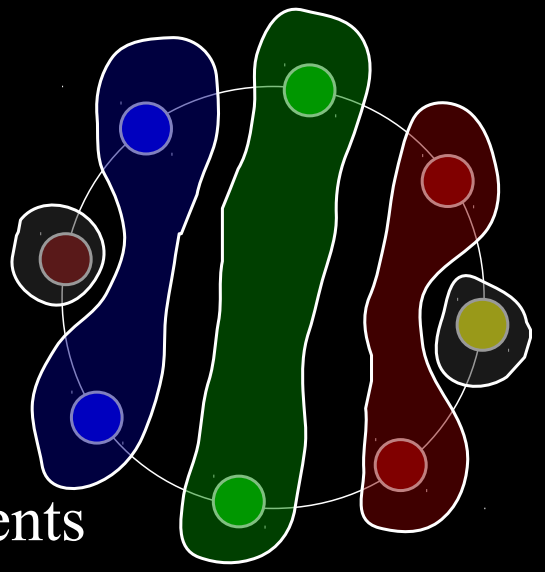
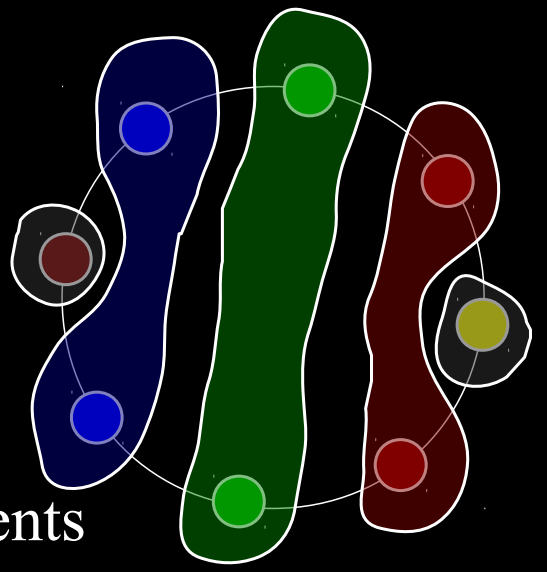


Minimize Distant Rearrangements

Generalization of Maximum
Independent Set on a Circle Graph

Solved by Dynamic Programming



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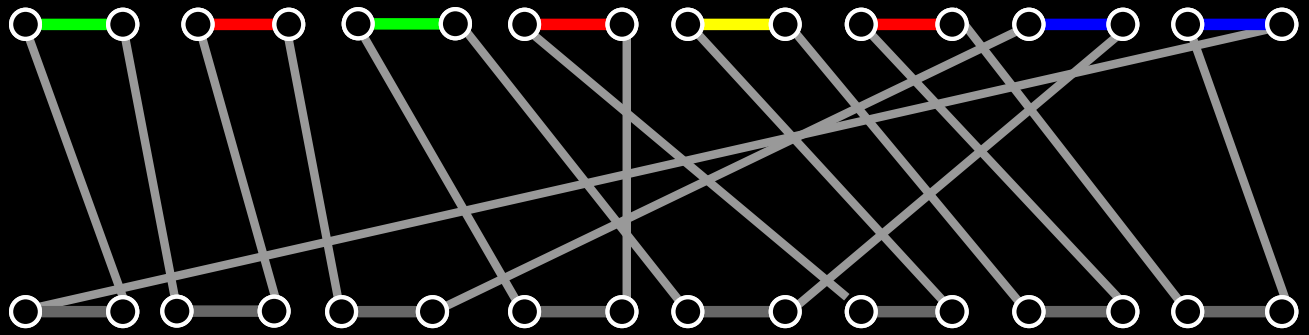

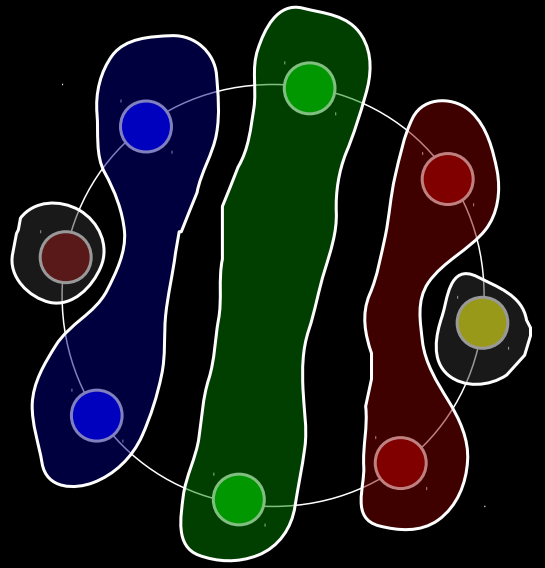

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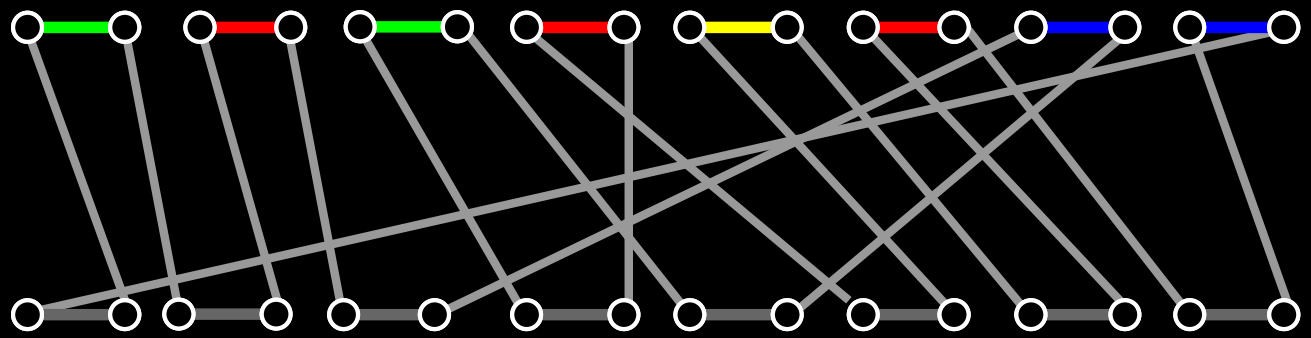
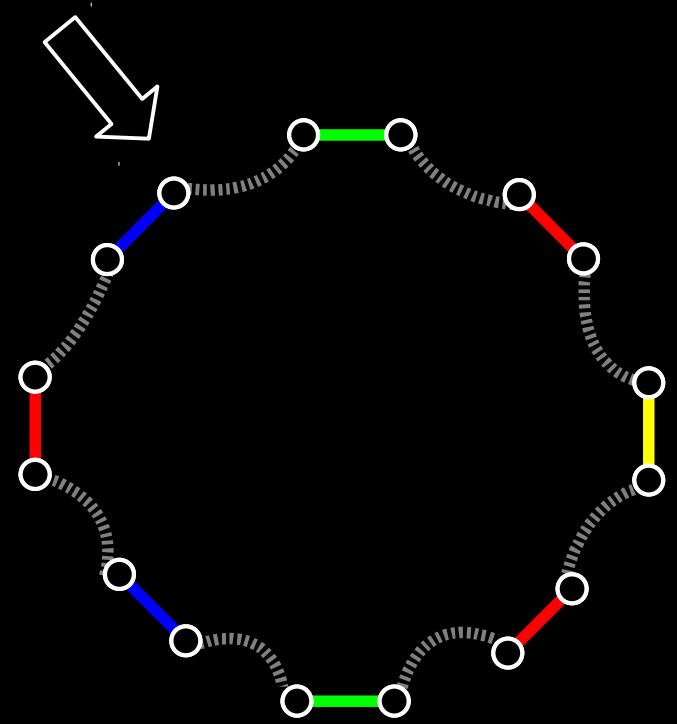
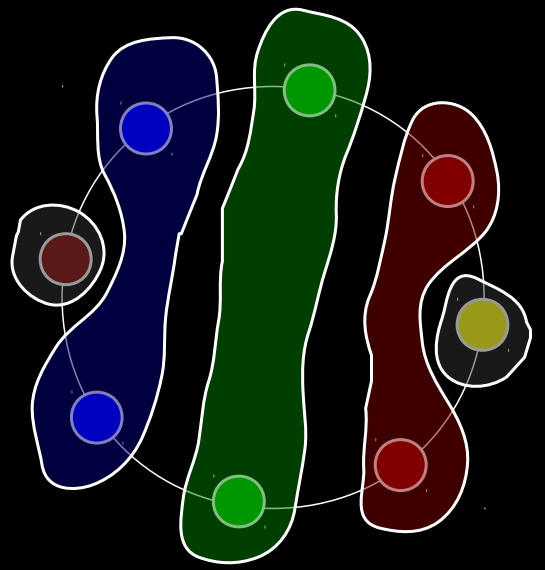
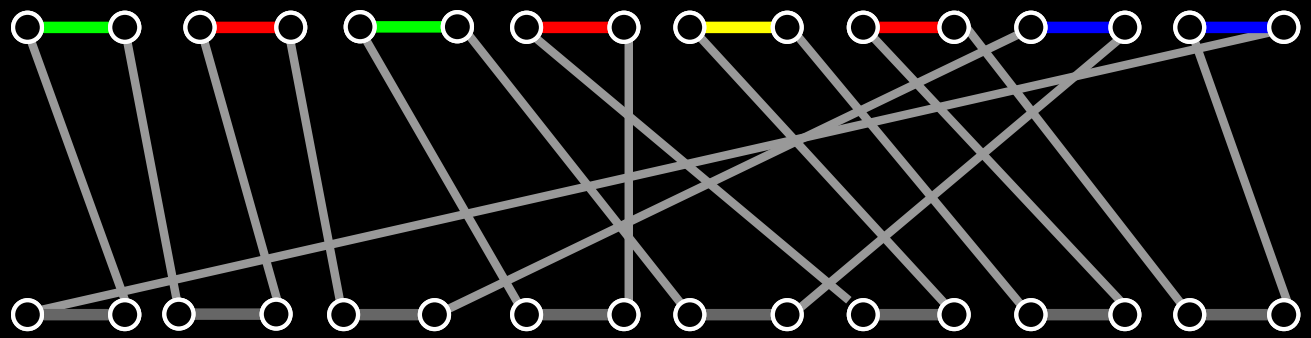
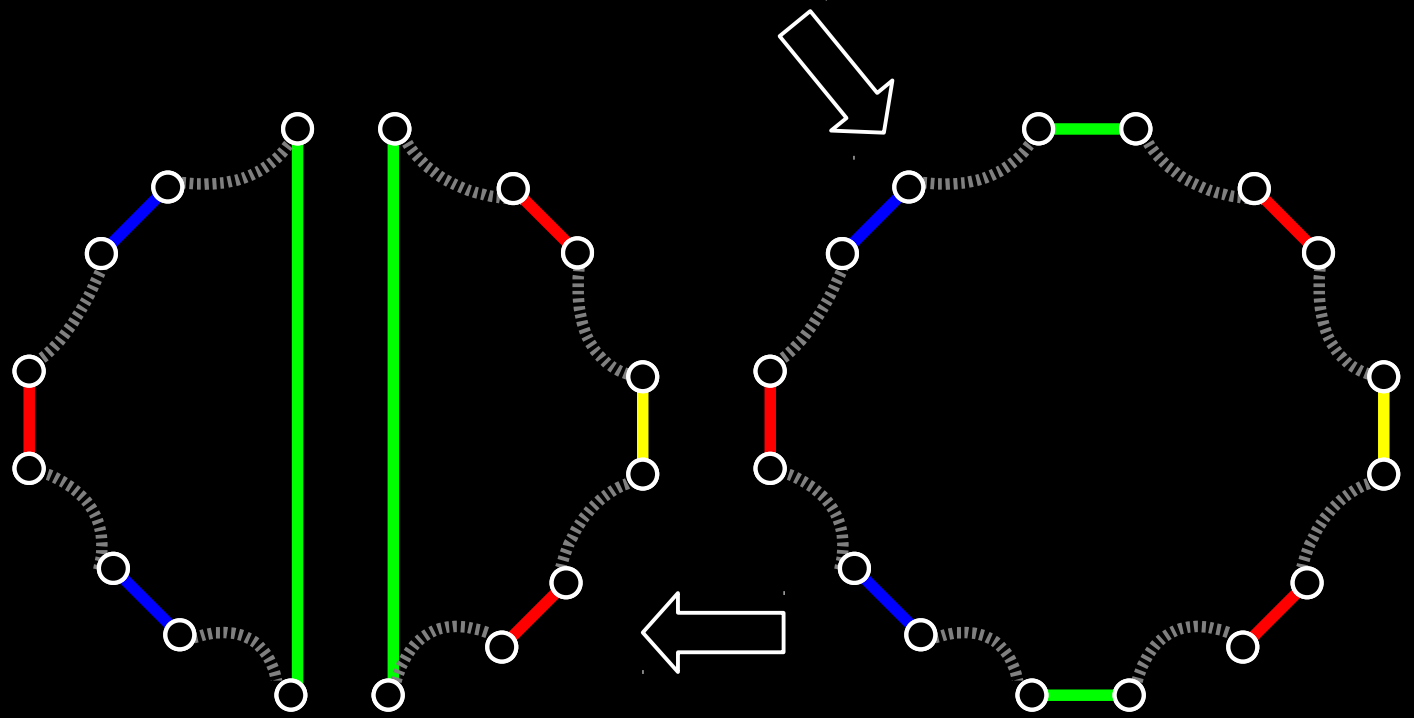


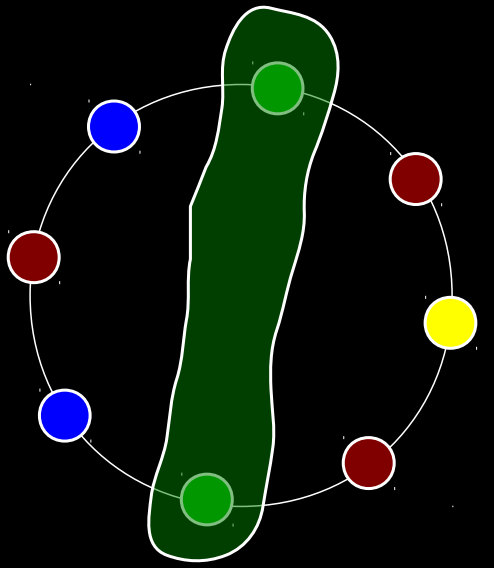




Sorting a Single Component

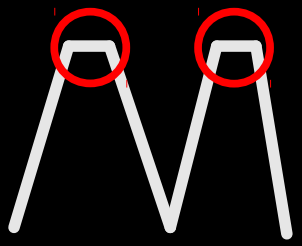


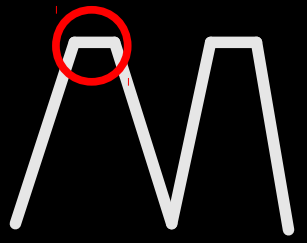




All DCJ Scenarios

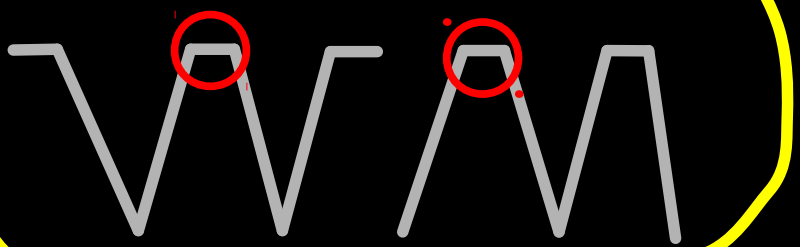
- even path
  - extract cycle
  - path fission



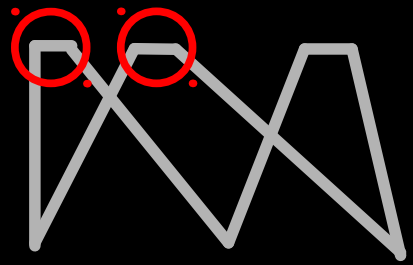


- odd path
  - extract cycle

- 2 even paths

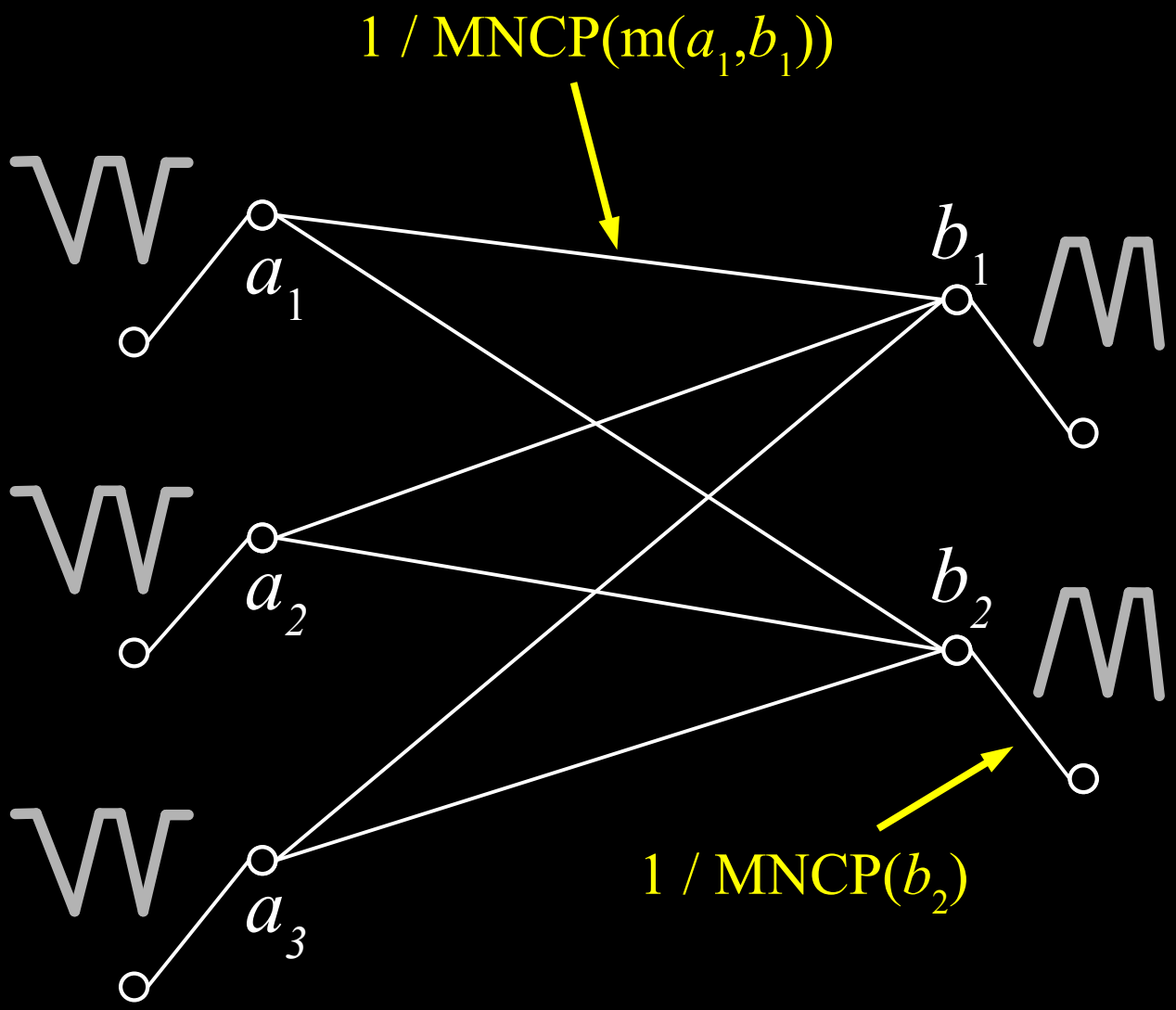


- cycle
  - split cycle



$$d_{DCJ}(G1, G2) = N - (C + I/2)$$

Multiple Even-Length Paths



Running Time

- $O(n^3)$
  - Min Non-Crossing Colored Partition
- $O(N(W)\ N(M)\ n^3) \in O(n^5)$
  - Labeling edges in the bipartite graph

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- $O(n^3)$
  - Min Non-Crossing Colored Partition
- $O(N(W)\ N(M)\ n^3) \in \cancel{O(n^5)}$ $O(n^4)$
  - Labeling edges in the bipartite graph
- In practice $N(W)\ N(M)$ is small!
  - 182 for human/mouse comparison

Future Work

- 3/2 approx to minimize # of non-local moves
- Other models of evolution
  - inversions
  - inversions/transpositions
- General weights
  - NP-Hard to minimize # of non-local
  - ?minimize # of non-local moves in *parsimonious*?
- 2-sided version of the problem
- Generalize to multiple species

Montpellier, France

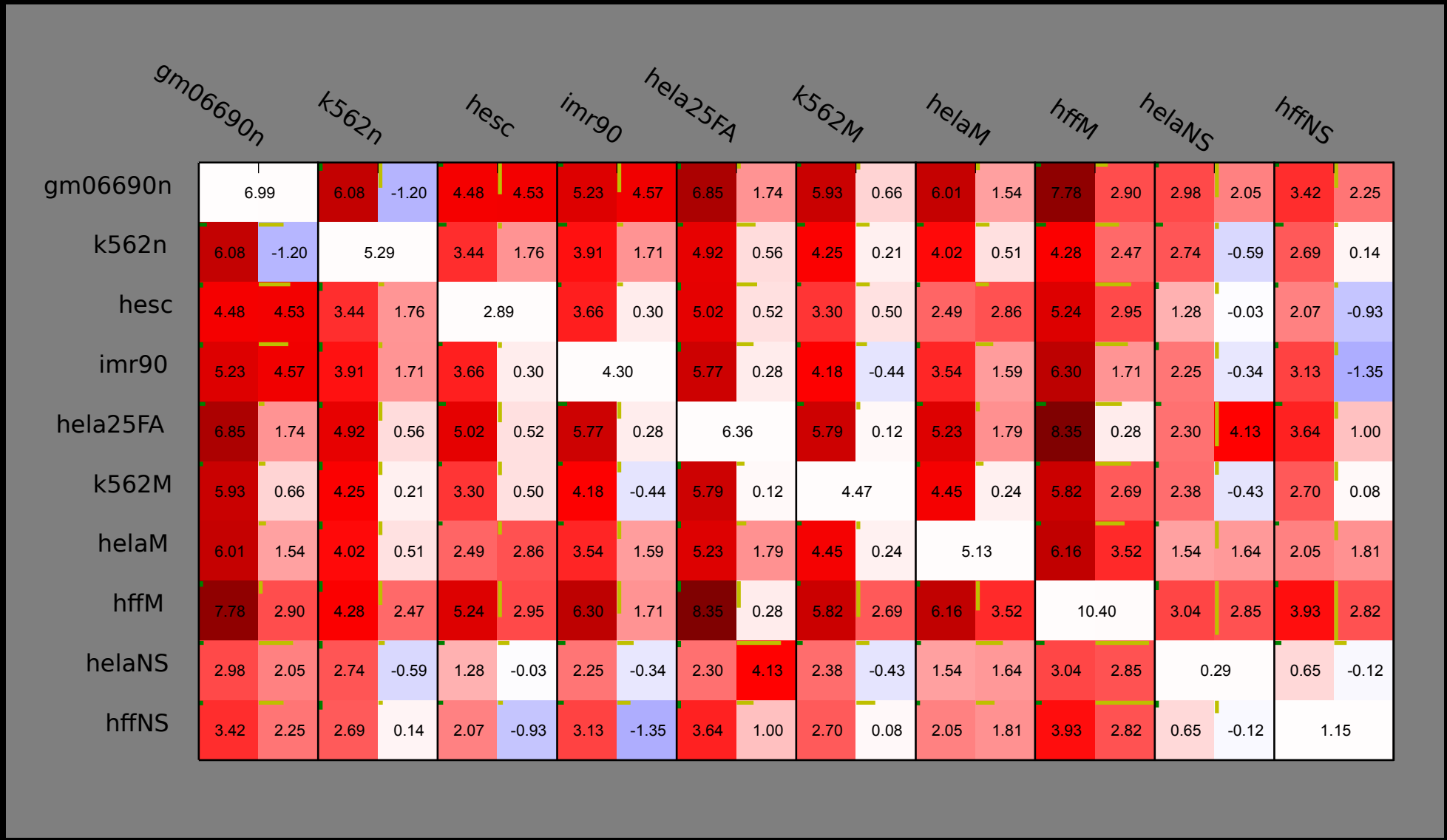
Come to the mediterranean!

Kirkpatrick

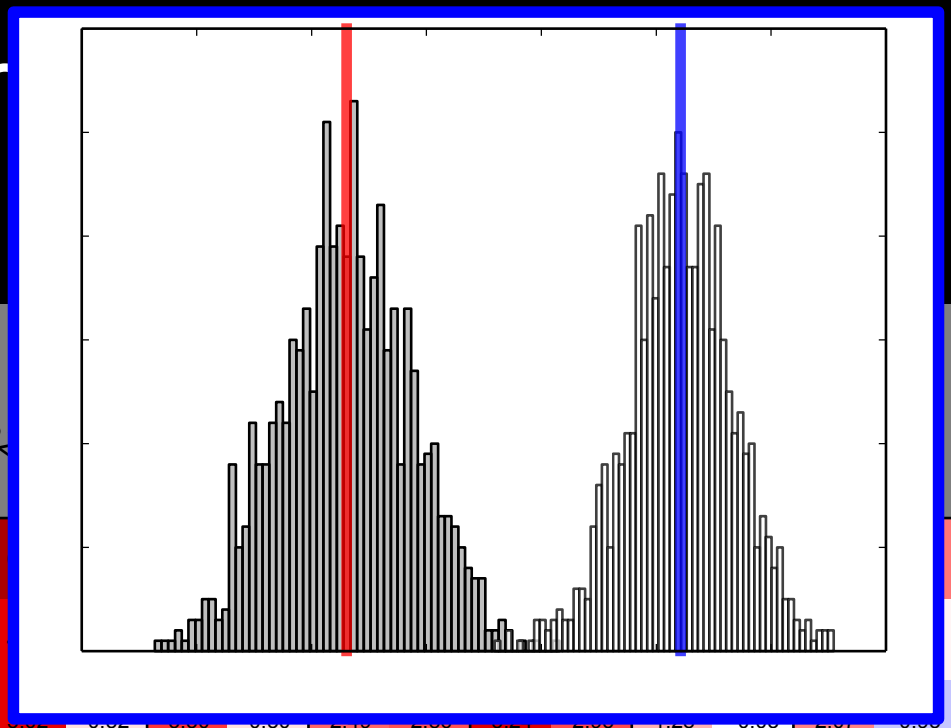
2 post-doc fellowships

THE END

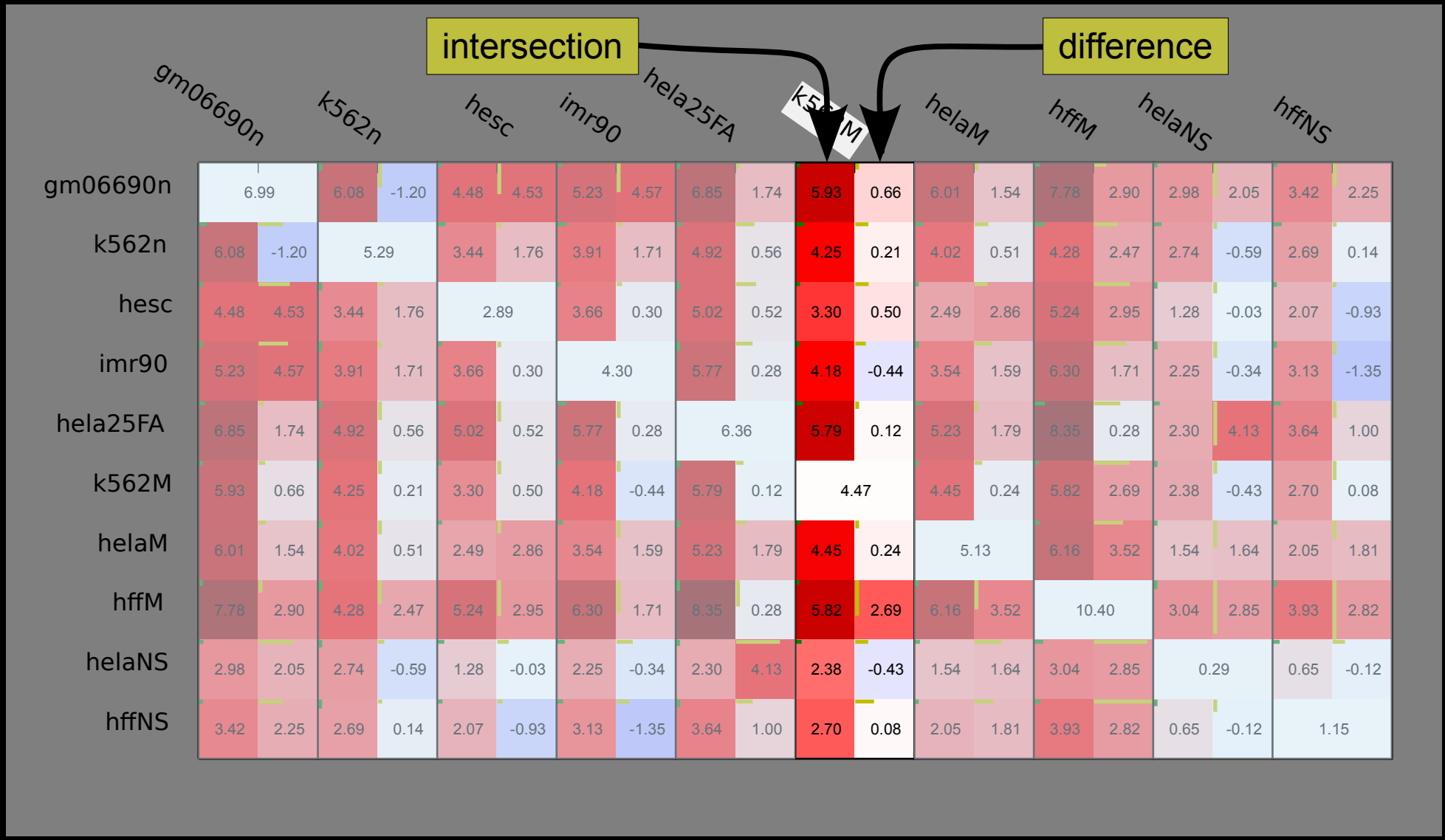
Cell Type Comparison - intra



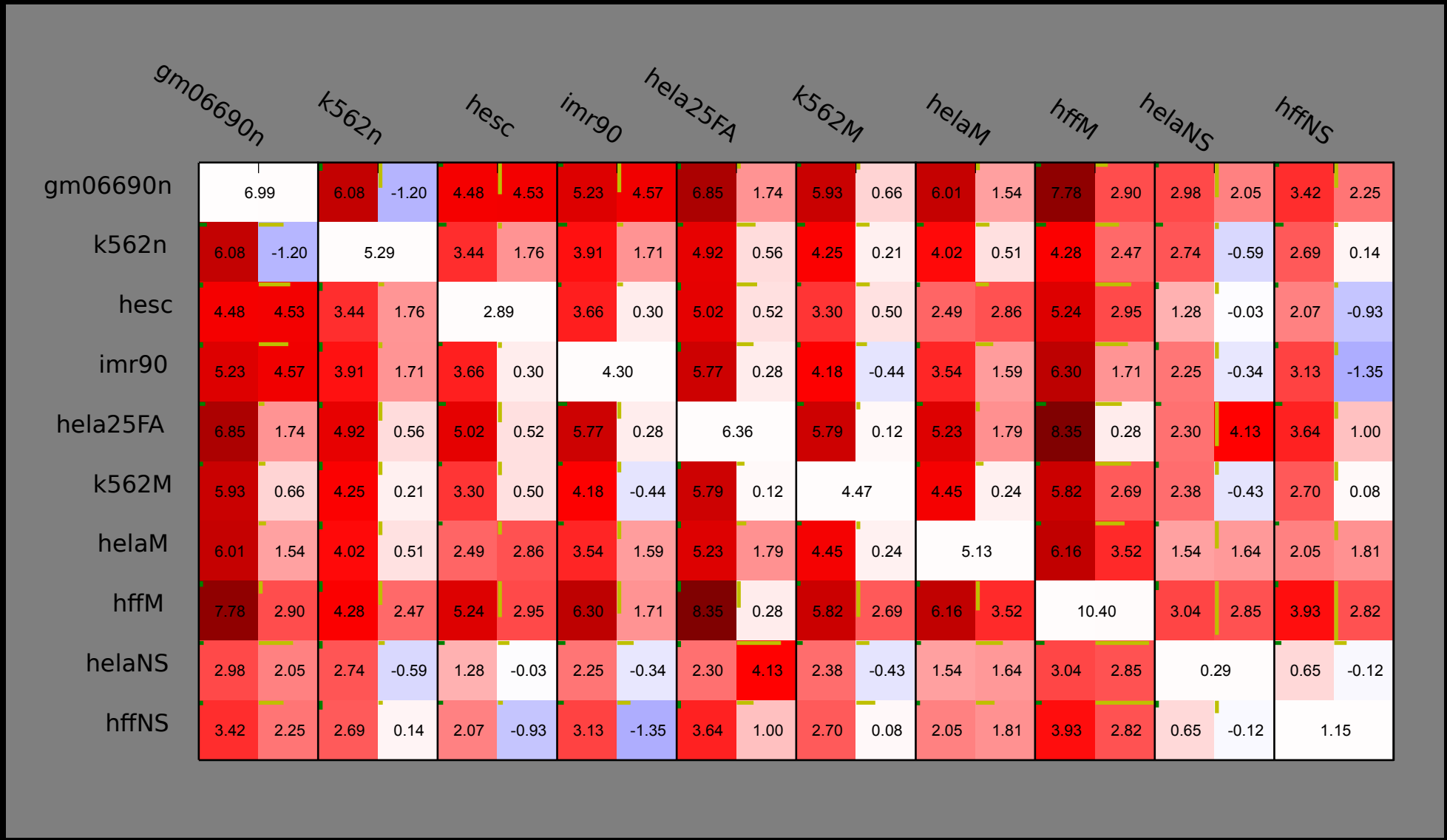
Cell Type Cor



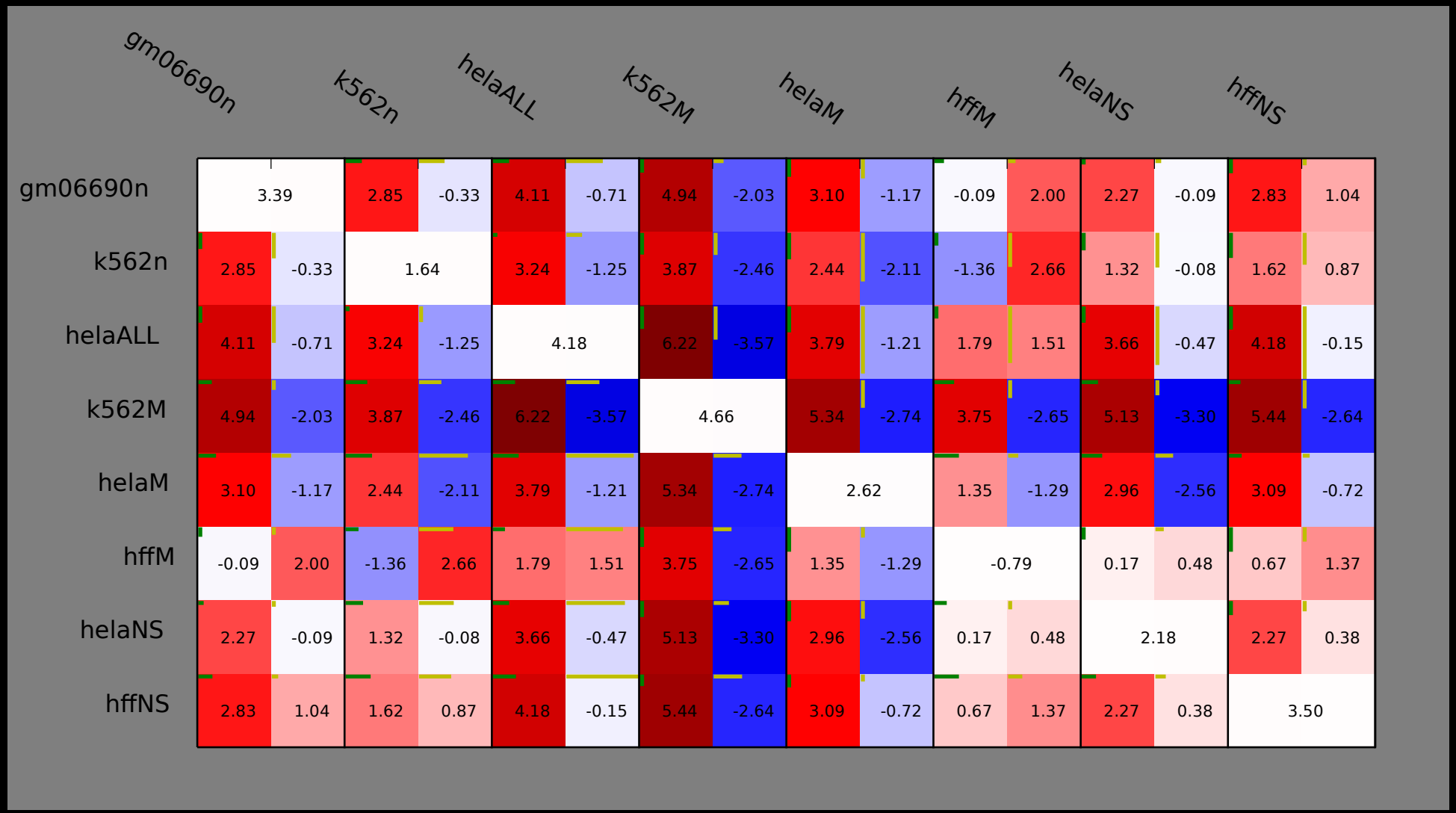
Cell Type Comparison - intra



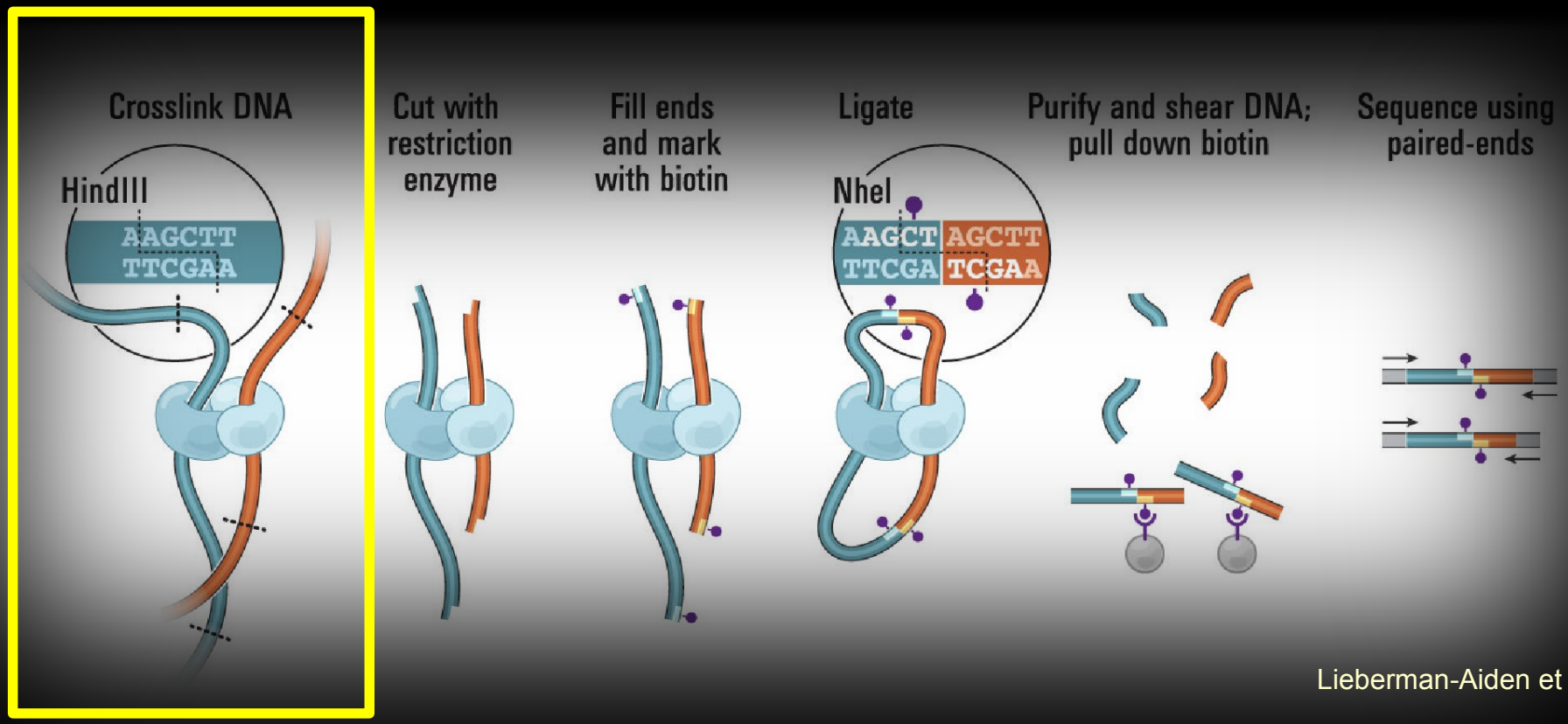
Cell Type Comparison - intra



Cell Type Comparison - inter



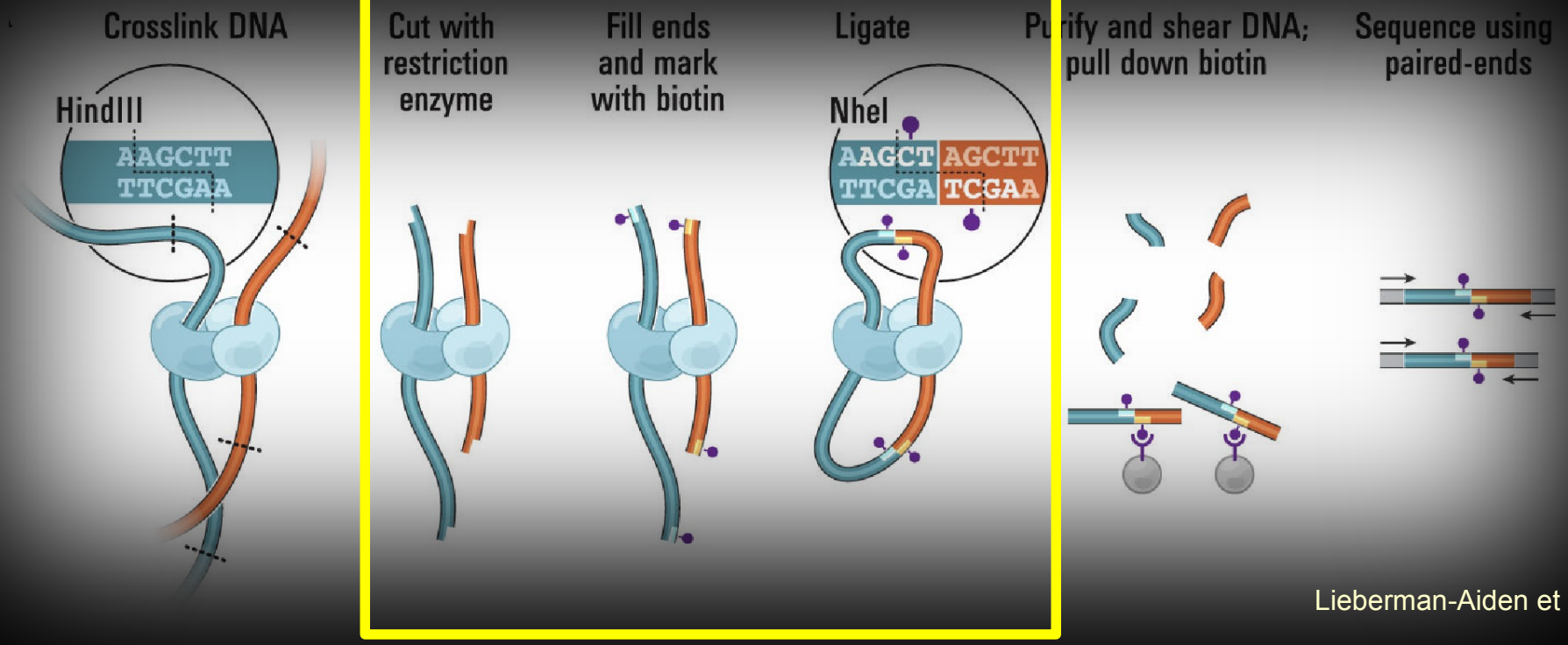
Data: Hi-C



Lieberman-Aiden et al.

1) crosslink

Data: Hi-C

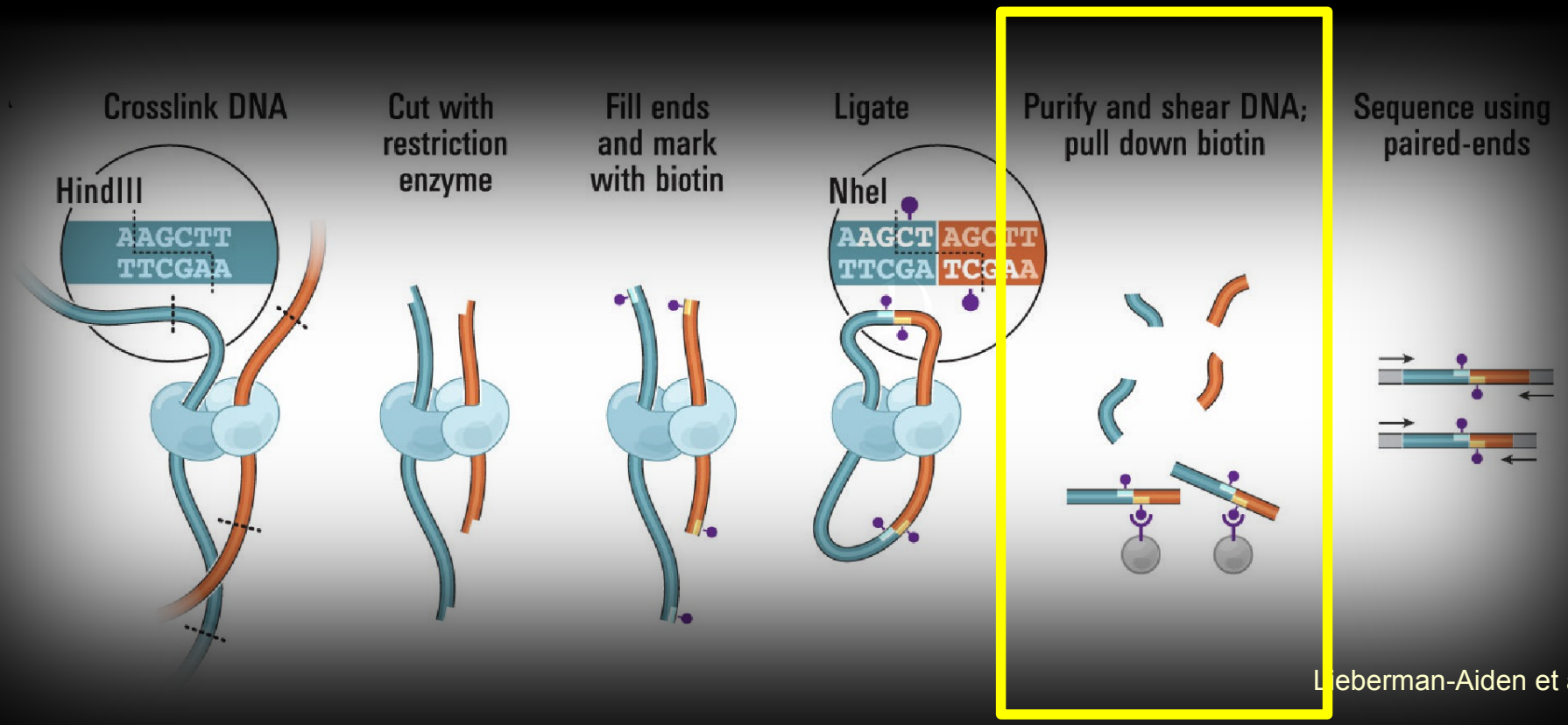


Lieberman-Aiden et al.

1) crosslink

2) ligate

Data: Hi-C

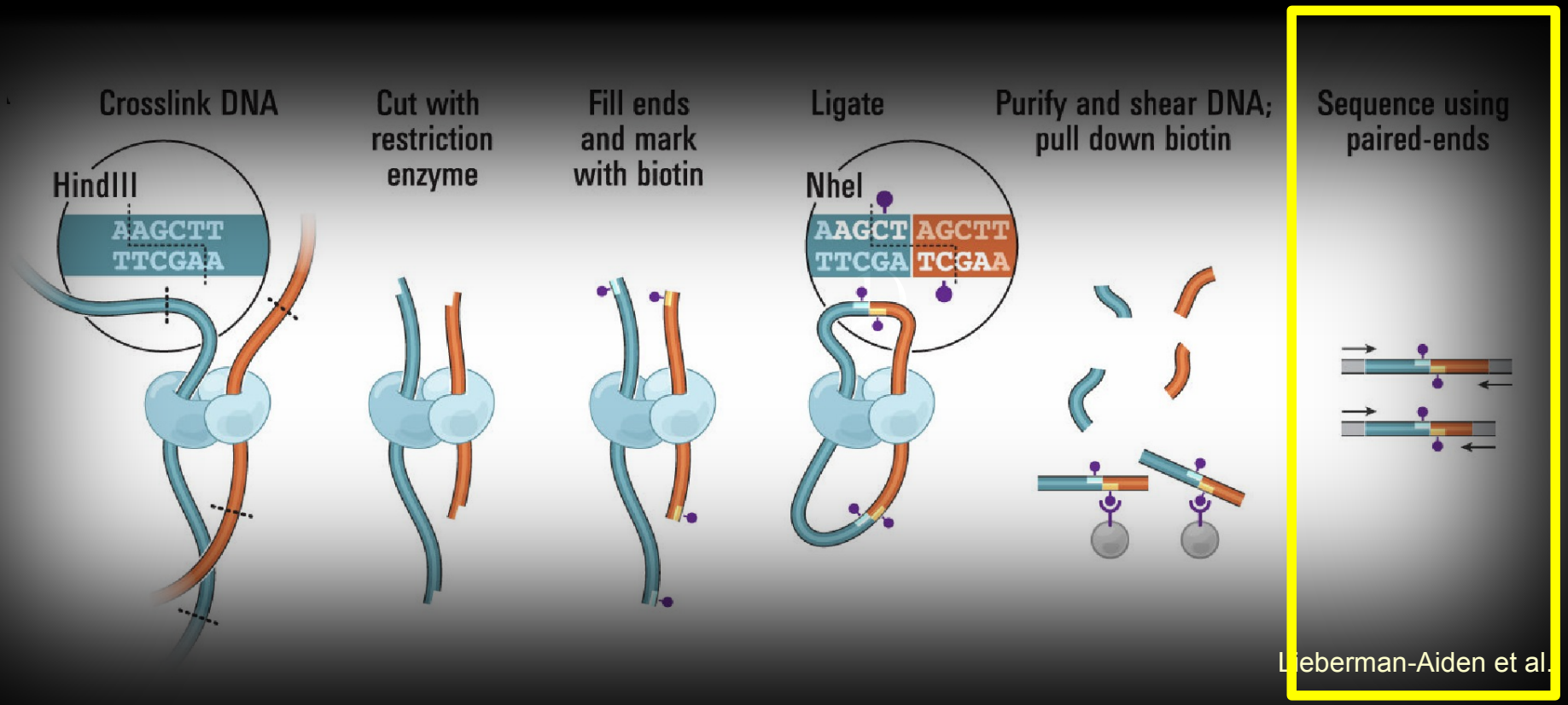


1) crosslink

2) ligate

3) shear

Data: Hi-C



1) crosslink

2) ligate

3) shear

4) sequence

Cell Lines

- 3 different labs
- 10 different experiments
  - 3 metaphase cell lines
  - 6 types of cells

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  - 3 metaphase cell lines
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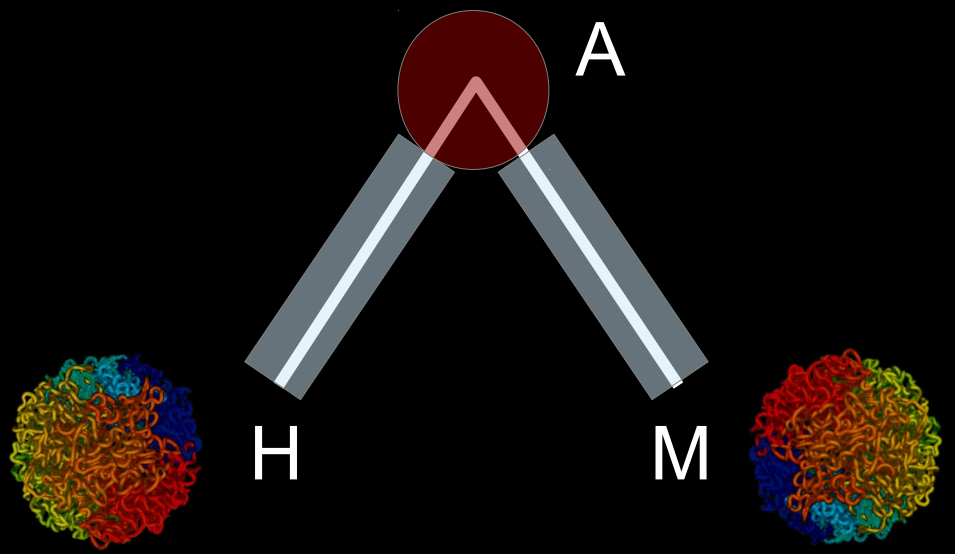
We see significant similarities between all of them!

→ selection on breakpoints?

Directions

- Search for “local” scenarios.
- Use Mouse AND Human data.
- Place rearrangements on path to ancestor.



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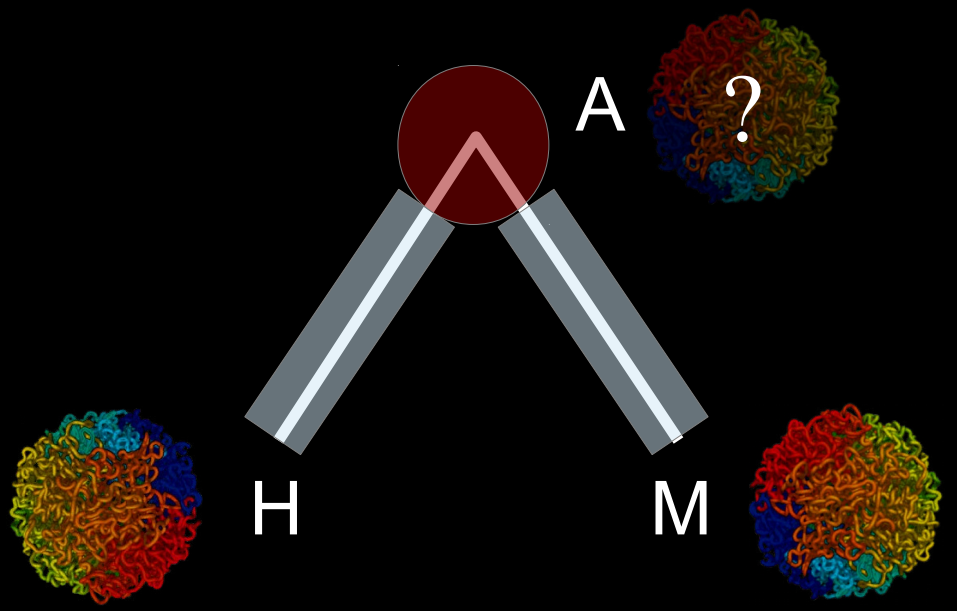
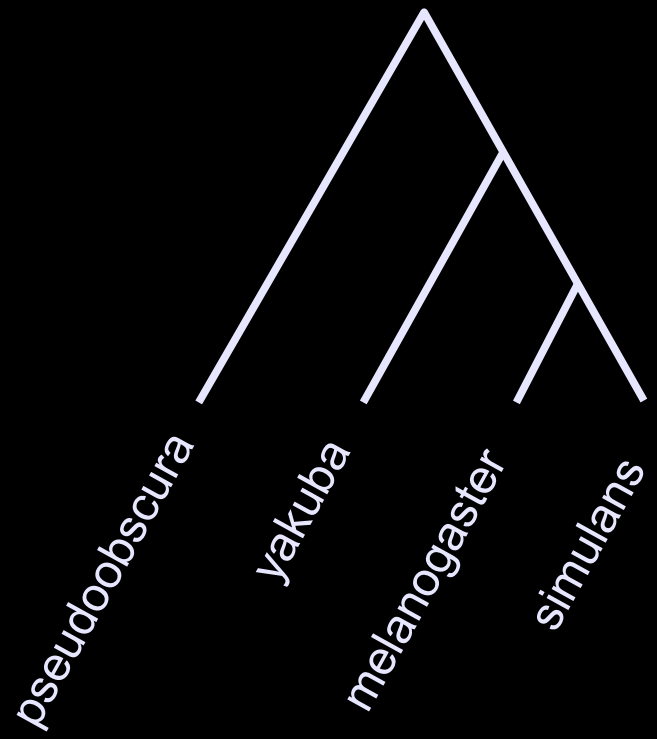


Directions



Drosophila!
(Giacomo Cavalli Lab)