# **Algebra Cheat Sheet**

## **Basic Properties & Facts**

#### **Arithmetic Operations**

# abacabea ( ) bab — cc a b a a a b a aaac cbcb

$$\frac{abacad}{abc} = b\frac{da}{dc}, 0$$

$$\frac{a}{b}$$

$$\frac{b}{c}$$

#### **Exponent Properties**

cddcccc

$$a\ddot{a}\ddot{a}\ddot{a}^{nm} = \frac{1}{a\ddot{a}^{mn}} \qquad \frac{1}{a\ddot{a}^{mn}}$$

$$(a\ddot{a}\ddot{b}\ddot{a}) = \pm \qquad \qquad 0 \quad 1, \quad 0$$

$$(ab)\ddot{b} = nn \qquad \qquad \boxed{aa}^{n} \qquad \frac{n}{n}$$

$$a\bar{a}^{nn} = \frac{11}{a\ddot{a}^{n}} \qquad \qquad =$$

$$ab\bar{b}^{nn} = \frac{n}{a\ddot{a}^{n}} \qquad \qquad \frac{n}{n}$$

$$a\ddot{a}\ddot{a}\ddot{a} \qquad \qquad \frac{n}{n} \qquad \qquad \frac{n}{n}$$

# **Properties of Radicals**

$$\sqrt[n]{aab}ab \qquad \sqrt{\qquad} \sqrt{\qquad} \sqrt{\qquad}$$

$$\sqrt[n]{naa} = \sqrt{\qquad} \sqrt[n]{aa} \frac{n\sqrt{\qquad}}{\sqrt[n]{b}}$$

$$\sqrt[n]{aa} = \sqrt[n]{b} \text{ is odd}$$

$$\sqrt[n]{aa} = \sqrt[n]{b} \text{ is even}$$

# **Properties of Inequalities**

If abachood  $\frac{ab}{cc}$ If abachood and  $\frac{ab}{cc}$ If abachood and  $\frac{ab}{cc}$ 

#### **Properties of Absolute Value**

$$|a| = \begin{bmatrix} aa & \text{if } 0 \ge \\ & & \text{if } 0 \end{bmatrix}$$

$$|a|a \Rightarrow 0 = \qquad | \qquad | \qquad |$$

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#### **Distance Formula**

If  $P_{YY}$  (), and  $P_{YY}$  (), are two points the distance between them is

$$dP(P_{122}(y)) = \sqrt{(- )^{22} ()}$$

## **Complex Numbers**

#### **Logarithms and Log Properties**

Definition

*yxx***b**og<sub>b</sub> is equivalent to

Example

 $log 1253 = because 5125^3$ 

Special Logarithms Inlognatural log

loglogcommon log

where  $e = 2.718281828 \oplus$ 

Logarithm Properties

 $\log 1 \log 10$ 

 $\log_b b \dot{x} b x = \log_b x$ 

 $\log \log (x/x) =$ 

logloghog=+

 $\log \log \log x = xy$ 

The domain of  $\log_b x$  is x > 0

# **Factoring and Solving**

#### **Factoring Formulas**

 $x \overrightarrow{a} x \overrightarrow{a} x \overrightarrow{a} x \overrightarrow{a} = ($  )(

 $x^{22}$ xaxa+  $\left( \right)^2$ 

 $x \frac{\partial^2 x}{\partial x} \frac{\partial^2 x}{\partial x} \qquad \qquad \left( \qquad \right)^2$ 

 $x^{2}bx^{2}abxux^{2}b \qquad ( )( x^{2}x^{2}a^{2}x^{2}ux^{2}u \qquad ( )^{3}$ 

 $x^{\frac{3223}{3}} \partial xa$  ( )

 $x \frac{3322}{3} \frac{1}{3} \frac{1}{3}$ 

 $x \stackrel{3322}{ax} = x \stackrel{322}{ax} = x \stackrel$ 

 $x \frac{\partial x}{\partial x} \frac{\partial x}{\partial x} \frac{\partial x}{\partial x} + ($  )(

If *n* is odd then,  $xaxaxa(+)( -121 \otimes )$ 

 $x_a^{nn}+$ 

 $= (xaxa)(axa^{n+12231}$ 

## Quadratic Formula

Solve axbx = 0,  $a \neq 0$  $-bba\sqrt{\frac{2}{3}}$ 

2*a* 

If bac 40 - Two real unequal solns.

If bac-40 - Repeated real solution.

If bac 40 - Two complex solutions.

## **Square Root Property**

If 
$$xp^2 = then xp = \pm \sqrt{ }$$

# **Absolute Value Equations/Inequalities**

If *b* is a positive number

pbpbpb = or

| pbb<del>pb</del> <<

pbpbpb > or

# **Completing the Square**

Solve  $26 \div 90 =$ 

- (1) Divide by the coefficient of the  $x^2$  $x^2x-350$
- (2) Move the constant to the other side.  $x_x^2 \frac{2}{3}5$
- (3) Take half the coefficient of x, square it and add it to both sides

$$x^{2}x^{2}-355=1339^{2}29$$

(4) Factor the left side



(5) Use Square Root Property

$$x - \frac{32929}{242} \sqrt{\frac{1}{242}} \sqrt{\frac{1}{242}$$

(6) Solve for x

## **Functions and Graphs**

#### **Constant Function**

yaf<del>x</del>a or ()

Graph is a horizontal line passing through the point (0, a).

#### **Line/Linear Function**

ymxbfxmxb or ( )

Graph is a line with point (0,b) and slope m.

Slope

Slope of the line containing the two points  $(xy_i)$  and  $(xy_i)$  is

$$m = \frac{yy_1^-}{xx_1^-} \quad \frac{\text{rise}}{\text{run}}$$

Slope – intercept form

The equation of the line with slope m and y-intercept (0,b) is

yını Point – Slope form

The equation of the line with slope m and passing through the point  $(x_k \mid s)$ 

#### Parabola/Quadratic Function

yaxhhfxaxhh $^{22}$ 

()

The graph is a parabola that opens up if a > 0 or down if a < 0 and has a vertex at (hk].

## Parabola/Quadratic Function

yaxbxefxaxbxc ()

The graph is a parabola that opens up if a > 0 or down if a < 0 and has a vertex

at 
$$\frac{bb}{2aa}$$
,  $f = 0$ .

#### Parabola/Ouadratic Function

 $xaybye^{22}yaybyc$  ( )

The graph is a parabola that opens right if a > 0 or left if a < 0 and has a vertex

at 
$$g = bb$$
 \_  $22a$ , —

#### Circle

 $(xhykh)^{22} = ($ 

Graph is a circle with radius r and center  $(h \not k)$ 

#### **Ellipse**

$$\frac{\left(xhyk\right)^{22}}{ak^2} + \frac{\left(\begin{array}{c} \\ \end{array}\right)}{1}$$

Graph is an ellipse with center (hk) with vertices a units right/left from the center and vertices b units up/down from the center.

#### Hyperbola

$$\frac{\left(xhyk\right)^{22}}{ak^2} - \stackrel{(}{=} )$$

Graph is a hyperbola that opens left and right, has a center at (hk) vertices a units left/right of center and asymptotes that pass through center with slope  $\pm \frac{b}{a}$ .

## Hyperbola

$$\frac{\left(ykxh\right)^{22}}{b\ddot{a}^{22}} - \frac{\left(\phantom{ykxh}\right)^{22}}{\phantom{a}} \quad 1$$

Graph is a hyperbola that opens up and down, has a center at (hk,) vertices b units up/down from the center and asymptotes that pass through center with slope  $\pm \frac{b}{a}$ .

# **Common Algebraic Errors**

Error	Reason/Correct/Justification/Example
$\frac{2}{0} \neq 0$ and $\frac{2}{0} \neq 2$	Division by zero is undefined!
<del>0</del>	$-3^{\circ}$ , $(-3)^{\circ}$ Watch parenthesis!
$(x\hat{x}^3)^3 \neq$	(xx)xx=
	$ \frac{1111}{-=\neq +=} 2 $ $ 2111 #$
	2111  A more complex version of the previous
$\frac{1}{xx^3+} \neq x\bar{x}^{23}$	error.
$\frac{\cancel{a} + bx}{\cancel{a}} \neq 1  bx$	$ \frac{abxabxbx}{aaaa} = += + - 1 1 $
Á	Beware of incorrect canceling!
-a(axa1)	-a(axa1) Make sure you distribute the "-"!
$\left(x \frac{\partial x}{\partial t}\right)^2$ 22	$(xava)^2 axava$ )( ) $^{22}$ 2
$\sqrt{x^{22}xa}$	52 <del>53</del> 4 <del>3</del> 434 2222 \( \sqrt{1}
$\sqrt{x}$ dixta+ $\sqrt{-}$	See previous error.
$(xax \frac{\pi}{4})^n$ and $\sqrt[n]{xax \frac{\pi}{4}} + \sqrt{}$	More general versions of previous three errors.
	2(3)21212=+( 22 )
$2(22 + 2)^{2}$ ( )	(2 <b>2</b> 484) <sup>2</sup> + 2
	Square first then distribute!
$(232H \neq)^{22}$ ( )	See the previous example. You can not factor out a constant if there is a power on the parethesis!
$\sqrt{-\frac{2222}{3}}$	$\sqrt{-x^{\frac{2222}{44444}}}$ ( ) <sup>1</sup> / <sub>2</sub> Now see the previous error.
$\frac{aab}{c} \neq \frac{b}{c}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
$\frac{a}{cb} \neq ac$	