

# 10. Dynamic networks driven by human mobility

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NETWORKS STRUCTURES AND DYNAMICS

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# Plan

## 1 Mobile Networks

- Mobile Networks

- Capacity

- Different Protocols

- Some empirical results on mobility

## 2 Empirical study

- Markovian models

- Dataset

- Methodology

- Analyzing real traces

- Impact of the markovian model

# *Mobile Networks*

# Dynamical aspect of networks

## Motivation

- Development of wireless devices
- A lot of new open dataset
- Dynamics ON and **OF** the network
- New structural properties
- Redefining usual metrics (graphs)

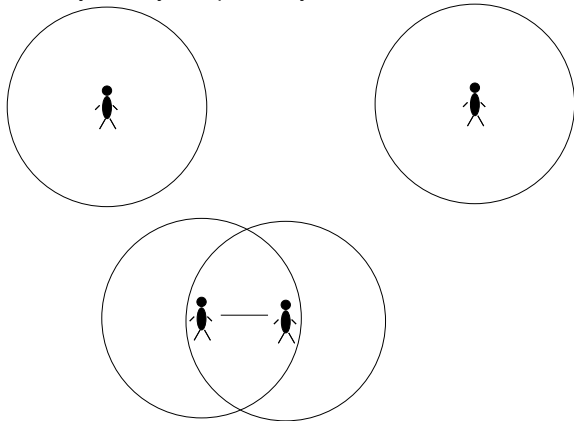
## Issues

- How acquire knowledge from this object ? (**measure**)
- Which notable properties ? (**analyze**)
- *Which models best capture those properties ? (modelling)*

# Object under study

Human-contact networks

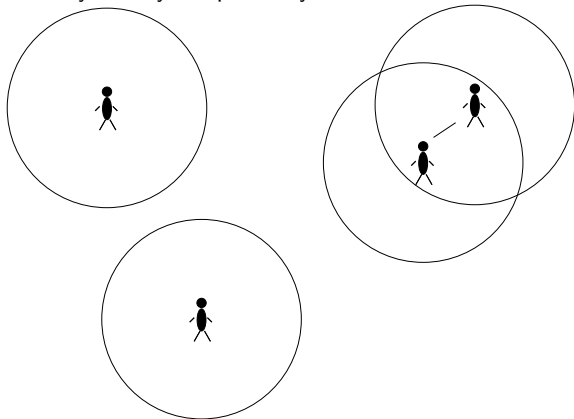
Mobility modify the proximity between users, hence wireless communications



# Object under study

## Human-contact networks

Mobility modify the proximity between users, hence wireless communications



# Motivations

Ad-hoc communications : transmission hop-by-hop

- Reduce the cost (eg. broadcast)
- Extreme events (eg. earth quake)
- Military applications

Virus propagation

Radio proximity  $\leftrightarrow$  physical proximity

# Efficiency ?

## Capacity :

- for a pair source/destination : the amount of data (bits) that can be transmitted (per sec.)
- of the network : average capacity for a random pair source/destination

## Need to model :

- who communicates with whom ?
  - when
  - how many times (frequency)
- which protocol of communication ?



# Point-to-point

For each packet, the source waits until it meets the target.

Advantage :

Drawbacks :

# Point-to-point

For each packet, the source waits until it meets the target.

Advantage :

simple

Drawbacks :

Time to send the paquet ?

# Flooding protocol

Each node send all its packets to all the nodes it meets

## Avantages

## Drawbacks

# Flooding protocol

Each node send all its packets to all the nodes it meets

## Avantages

- time to reach every one : proxy for a lower bound in terms of times required for the transmission

## Drawbacks

- Waste of memory
- Interference

# Two-hop relay

Each source transmits its packets to the first node it meets :

- either directly to the target
- either to a relay

Each relay waits until it meets the target

## Avantages/drawbacks

Protocol used in an article. Detailed later

# Static nodes

[Gupta, Kumar, 2000]

Settings :

- $n$  nodes are randomly placed on a disc whose surface is 1.
- the nodes don't move
- for each source : one destination is randomly chosen  
one sends an infinity of packets

## Results

- Capacity in  $c_{te}/\sqrt{n \log n}$  possible
- Capacity in  $c_{te}/\sqrt{n}$  impossible

# Discussion

# Discussion

The capacity decreases while the number of nodes increases  
→ the more the number of nodes, **the less the efficiency**

## Discussion

Important theoretical result

What happens if :

- nodes moves ?
- pattern of communication changes ?  
(who wants to communicate with whom)



# With mobile nodes

[Grossglauser, Tse, 2002]

Settings :

- The nodes move in a disc whose surface is 1.
- $X_i(t)$  : position of  $i$  at time  $t$ .
- Uniform distribution over the disc
- One node  $\longrightarrow$  one destination
- One sends an infinity of packets

# First idea

Each pair source/destination is infinitely often close  
→ direct communications when *distance* < *threshold*

## Problem

Better compromise : impossible to reach  $1/\sqrt{n}$

# First idea

Each pair source/destination is infinitely often close  
→ direct communications when *distance* < *threshold*

## Problem

- high threshold → lot of interferences  
few communication at the same time
- short threshold : short distances → needs to wait for longer

Total capacity **low** in both cases

Better compromise : impossible to reach  $1/\sqrt{n}$

# Second idea : relay

At each time step : one chooses randomly  $\theta n$  sources  
( $\theta < 1$ , parameter)  
the other nodes are receptors

## 2 modes

- if  $t$  odd : each source sends its packet to the closest receptor
  - either the destination
  - either a relay (**unique**)
- if  $t$  even : each source sends a relayed packet, if possible.
  - transmission **only to the destination**

## Results

The capacity of each pair is constant

# Discussion

Important theoretical result :



# Discussion

Important theoretical result : the mobility **plays a great impact**

Only one relay : surprising ?

# Discussion

Important theoretical result : the mobility **plays a great impact**

Only one relay : surprising ?

The modelling of the mobility assumes a trajectory :

- stationary
- uniformly distributed on the disc
- independant in regards to the nodes

→ each node has the **same probability** to meet the destination

Is it a reallistic model ?

# Let's find out

## Contact and inter-contact duration times

For radio badges networks :

### Contacts duration times

How long two nodes stay in contact

### Inter-contact duration times

How long before two given nodes meets again

→ Distribution



# One example : rollerblade tour

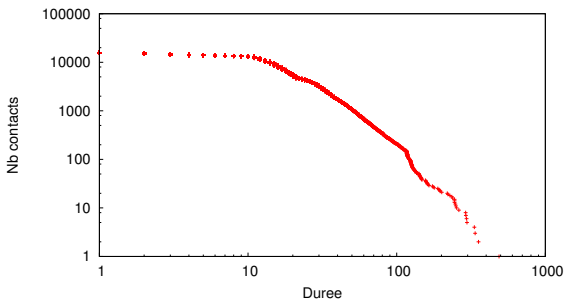
[Tournoux, Leguay, Benbadis, Conan, Dias de Amorim, Whitbeck, 2009]

## Rollernet

- Rollerblade tour in Paris
- 62 nodes
- 3 hours

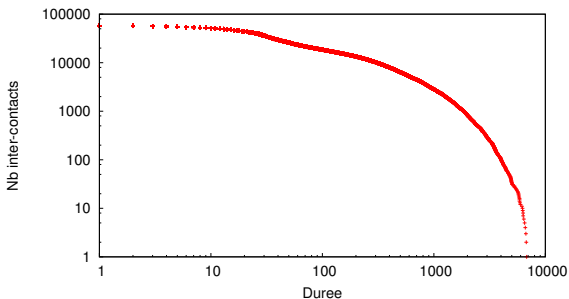
# Contacts duration times

Inverse CDF (cumulative distribution frequency)



# Inter-contacts duration times

Inverse CDF



# Discussion

Distributions **not homogeneous**

(more or less heterogeneous depending on the dataset)

Mobility

Consequences

[Chaintreau, Hui, Crowcroft, Diot, Gass, Scott, 2006]

Inter-contacts duration times following a powerlaw



# Discussion

Distributions **not homogeneous**

(more or less heterogeneous depending on the dataset)

## Mobility

Observations incompatible with hypothesis made in the previous article :

It is **not realistic** to model a regular and uniform mobility

## Consequences

[Chaintreau, Hui, Crowcroft, Diot, Gass, Scott, 2006]

Inter-contacts duration times following a powerlaw

⇒ **no efficient communications possible**

*Empirical study*

# Goal

## The existing :

- Studies analyzing mobile networks [CHA07, TOU09, ...]
- Few models but recently : [CLE08, CLE09]

## Used to study diffusion protocols :

- *flooding* protocol [BAU09, CLE10]
- *push* protocol [CLE13]

# Goal

## The existing :

- Studies analyzing mobile networks [CHA07, TOU09, ...]
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## Used to study diffusion protocols :

- *flooding* protocol [BAU09, CLE10]
- *push* protocol [CLE13]

*In this course : is the model realistic ?*



# Models for evolving graphs

## Background :

- **Evolving graph** model : recent [FER02]
- Evolving graph = Succession of distinct graphs  $G_0, G_1, \dots$  with  $V$  given
- Capture all types of dynamics

# Models for evolving graphs

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- Capture all types of dynamics

## Variant of edge-markovian evolving graph :

- Temporal dependency in the evolution of the graph
- $G_{t+1}$  determined by  $G_t$  and 2 parameters :
  - $p$  : probability of creation of a *non-existing* link
  - $d$  : probability of deletion of an *existing* link

# Example

Example with 4 nodes,  $p = 0.3$ ,  $d = 0.2$  and 5 time steps.

1	3	2	3
1	4	1	3
2	3	1	2
2	3	4	4
2	4	1	2
2	4	4	4
3	4	1	3

- 1st and 2nd column : identifiers of nodes involved in the contact
- 3rd column : starting time of contact
- 4th column : ending time of contact

# Advantages / drawbacks

Interest is twofold :

- $\forall G_0, p, d$  : converge towards an Erdős Rényi graph with  $\hat{p} = \frac{p}{p+d}$
- Few parameters  $\implies$  theoretical results

But it is also its weakness :

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But it is also its weakness :

- 2 parameters to rule **all** creations/deletions
- Suppose that those 2 values are representative for the l'**entire** evolution of the de network

# Methodology

## Goal of the course :

Conduct a study to see if it is true.

- Analyze properties of the dynamics as observed in several dataset
- Comparison with the markovian model

### *Elements of response*

- Yes for [WHI11] (and [VOJ11]) but ...
- ... study over 1 dataset
- ... the criteria is weak : time needed to flood the network

# Rollernet

- Rollerblade tour in Paris
- Date : August 2006.
- Duration : 3h with a break (30 min) covering approx. 30km,
- Location : street of Paris
- Technology : *iMotes* (bluetooth)
- Size : 62 participants
- Frequency : every 15s.

# Infocom06

- Experiment made during Infocom conference at Barcelona.
- Date : April 2006
- Duration : 3 days
- Technology : *iMote*
- Size : 98 iMotes (78 participants, 17 static, and 3 in elevators)
- Frequency : every 120s.



# Sociopattern

- Exhibition in at a gallery (diseases propagations).
- Date : 2009
- Duration : 3 months
- Technology : *radio badges*
- Size : 88 to 410 (depends on the day)
- Frequency : every 20s.

## 6 case studies

Dataset	RollerNet	Infocom05	Infocom06	HT09	Socio	PMTR
Duration	3 hours	4 days	4 days	2,5 days	1 day	10 days
Participants	62	41	98	113	151	44
Contacts	60 146	17 682	148 784	9 865	2 051	11 895
Frequency (sec.)	15	120	120	20	20	1

*For each :*

- "Physical" contact network among individuals
- Each individual is equipped with a sensing device
- Detection between devices if proximity between individuals (2 to 10 m.)
- Frequency of detection varies, as well as duration of the experiments

*In the rest of the presentation, 3 dataset only :*

- RollerNet
- Infocom06 : similar to Infocom05
- SocioPattern : similar to HT09 and PMTR

# Methodology

*For each dataset and for each time step*

- Fraction of created links (over possible new links)
- Fraction of deleted links (over existing links)

Corresponds to the parameters  $p$  and  $d$  of the model

*Analyze :*

- Evolution over time
- Distribution of the values
- Generation of artificial graphs according to the markovian model
- Comparison between real/artificial graph

# Created links

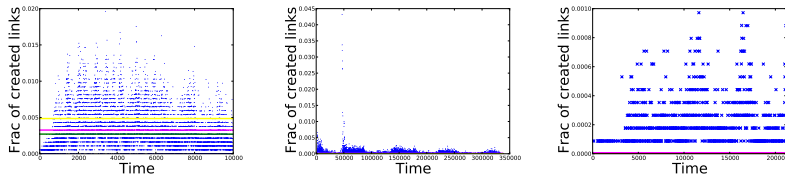


FIGURE : Evolution of the proportion de created links over time

## Results

# Created links

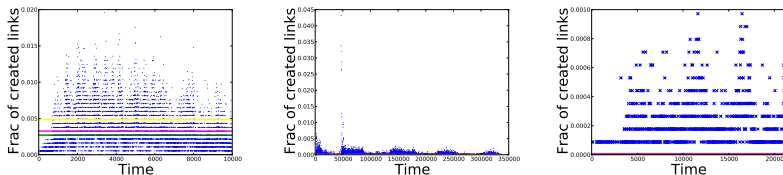


FIGURE : Evolution of the proportion de created links over time

## Results

- RollerNet : notion of average is relevant
- Infocom06, SocioPattern : wide range of values
- Infocom06, SocioPattern : average, median and 75th percentile overcome by weak values
- $\implies$  Infocom06, SocioPattern : non realistic

# Deleted links

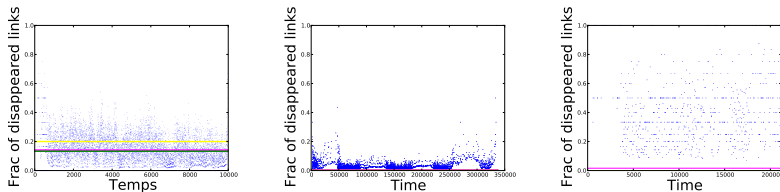


FIGURE : Evolution of the proportion of deleted links over time

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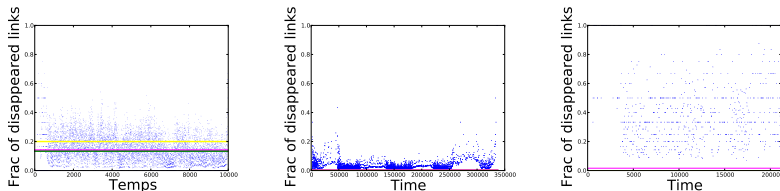


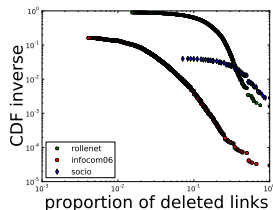
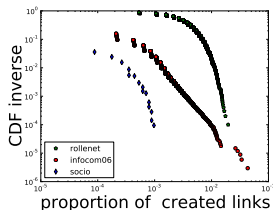
FIGURE : Evolution of the proportion of deleted links over time

## Results

- Same observation but amplified
- Range of values is covered ( $[0 : 1]$ )
- Particular case for  $d = 1$

# Distribution of $p$ and $d$ values

Dataset	RollerNet	Infocom06	Socio
Fractions of created links (average)	$3.2 (10^{-3})$	$9.5 (10^{-5})$	$9 (10^{-6})$
Fractions of deleted links (average)	$1.4 (10^{-1})$	$4.5 (10^{-3})$	$1.6 (10^{-2})$

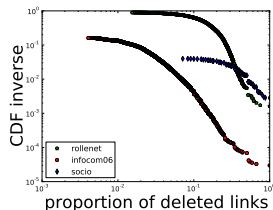
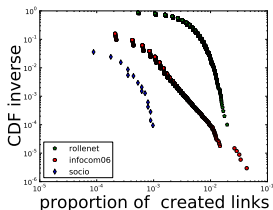


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## Results

- Clearly heterogeneous for Infocom06
- and on several order of magnitudes
- RollerNet : sudden slope around the average value

# Methodology

*So far :*

- Studied the dynamics related to creation and delation of links
- Provided evidences that the models *is probably not suited* to particular dataset

*How to demonstrate that the model is not pertinent ?*

# Methodology

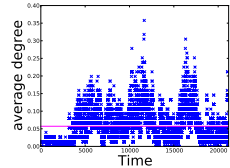
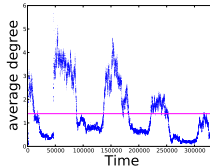
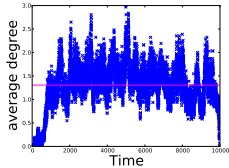
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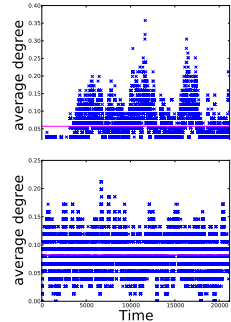
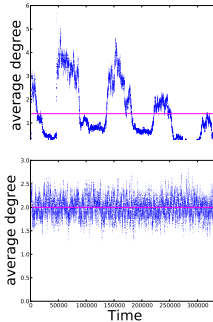
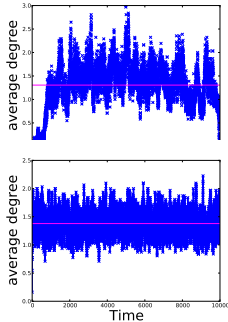
- Choose an external criteria (ie not the fraction of created and deleted links) ...
- ... but close enough the meaning of  $p$  and  $d$  (for fairness)
- Compute the value of the criteria for the real and the artificial graphs.
- Comparison between real/artificial graph.

# Evolution of mean degree



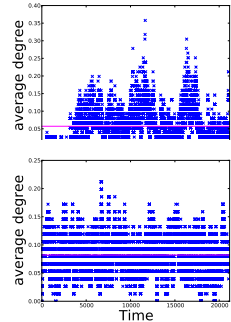
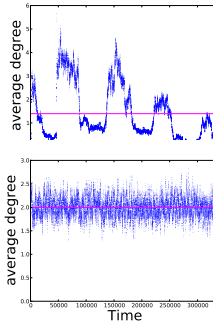
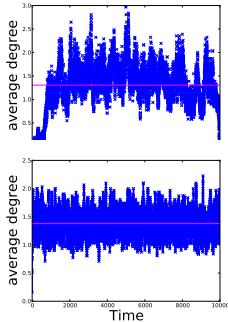
## Results

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## Results

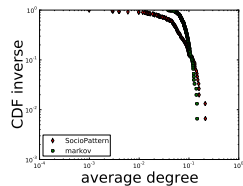
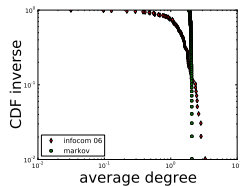
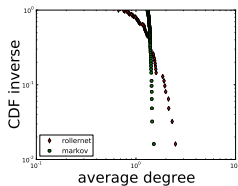
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## Results

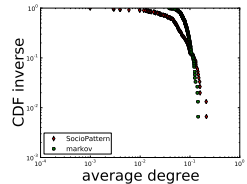
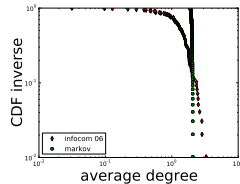
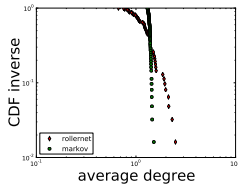
- "Uniformization" for Infocom06 and SocioPattern (not the same range of values!)
- Seems to have little impact on RollerNet
- Except at the beginning (expected)

# Average degree distribution



## Results

# Average degree distribution

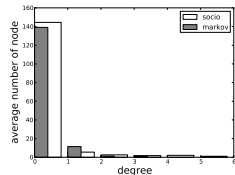
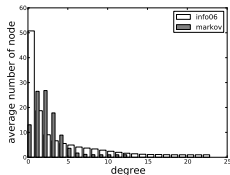
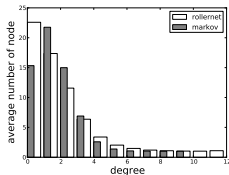


## Results

- **Infocom06** : clear differences between model and real data (expected)
- **RollerNet** and **SocioPattern** : also different, although less obvious

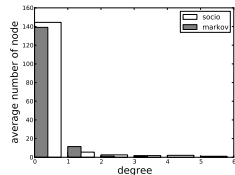
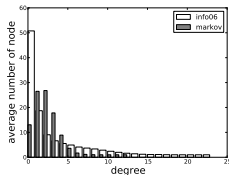
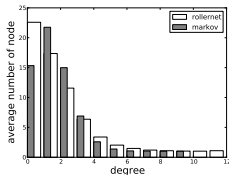


# Degree distribution



## Results

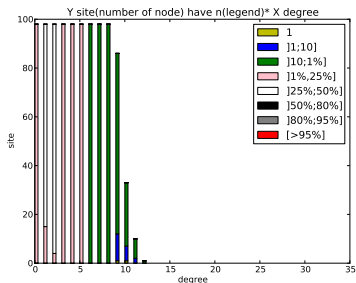
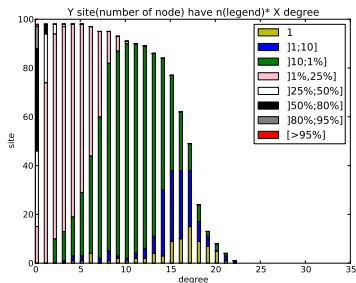
# Degree distribution



## Results

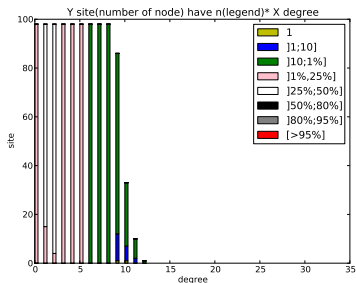
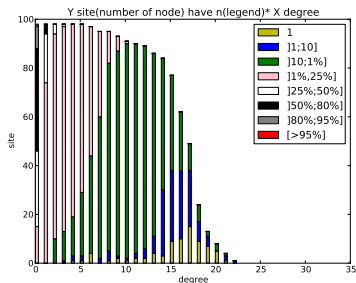
average value relevant  $\nRightarrow$  the model reproduces well the **global** properties of the networks

# Distribution and frequency of the degrees (Infocom06)



## Results

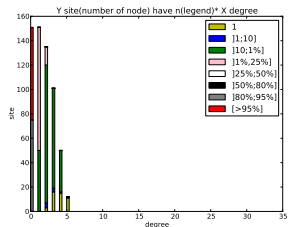
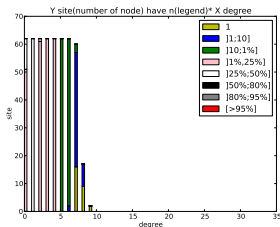
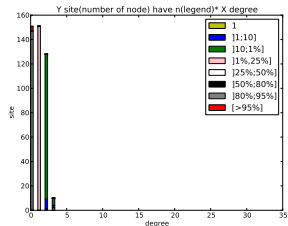
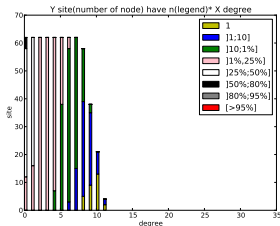
# Distribution and frequency of the degrees (Infocom06)



## Results

- Nodes are more degree-stable in real networks
- Small degrees are over-represented
- *No node with the same degree more than 50 % of the time in the model*

# Distribution and frequency of the degrees (RollerNet, SocioPattern)



# Conclusions and perspectives

## Conclusions

- Confrontation markovian model vs. real data
- Hypothesis of homogeneity does not stand in most of the cases
- Even in favourable case, it **does not reproduce the dynamics**
- *Still remain useful* : cf [WH11, VOJ11]

## Perspectives

- Consider other way to define  $p$  and  $d$  (following an heterogeneous distribution ? different for each nodes ? depending on the graph state ? ...)
- Study refined properties (repartition of connexions)
- Analyze correlation between creations and deletions
- Take into account the local density
- Study *gossip* protocols of diffusion on **real data**